

- (a) Discuss the various cases for insertion of key in red-black tree for given sequence of key in an empty red-black tree- {15,13,12,16,19,23,5,8}. Also show that a red-black tree with n internal nodes has height at most $2\lg(n+1)$.
- (b) Explain and write an algorithm for union of two binomial heaps and write its time complexity.

5. Attempt any *one* part of the following: 10*1 = 10

- (a) Explain “greedy algorithm” Write its pseudo code to prove that fractional Knapsack problem has a greedy-choice property.
- (b) What are single source shortest paths? Write down Dijkstra’s algorithm for it.

6. Attempt any *one* part of the following: 10*1 = 10

- (a) What is the sum of subsets problem? Let $w=\{5,7,10,12,15,18,20\}$ and $m=35$. Find all possible subsets of w that sum to m using recursive backtracking algorithm for it. Draw the portion of the state-space tree that is generated.
- (b) Illustrate n queen’s problem. Examine 4 queen’s problem using back tracking method.

7. Attempt any *one* part of the following: 10*1 = 10

- (a) What is string matching algorithm? Explain Rabin-Karp method with examples.
- (b) Explain approximation algorithm. Explore set cover problem using approximation algorithm.