

Kaplan

Ist semester

Please write your Roll. No. immediately

First term Examination(B. Tech)

September 2017

Max. Time :1hour 30min.

Max. Marks: 30

Sub. Code:ETMA-101

Sub. Name:Applied Mathematics-I

Note: Attempt Q. No. 1 and two more Questions

1.(a) State Leibnitz's test for convergence with an example. (3)

1.(b) Find n^{th} derivative of the following function : $y = x^4 / \{(x-1)(x-2)\}$ (3)

1.(c) Find the radius of curvature at the point $\left(\frac{1}{4}, \frac{1}{4}\right)$ of the curve : $y^2 = 4ax$ (2)

1.(d) Find Taylor series expansion of the function $f(x) = x^3 + 3x^2 + 15x - 10$ in power of $(x-1)$. (2)

2.(a) If $U_n = \frac{d^n}{dx^n} (x^n \log x)$, prove that $U_n = (n-1)! + n U_{n-1}$ ($n = 1, 2, \dots$).

Hence deduce that $U_n = n! \left[\log x + 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} \right]$ ($n = 1, 2, \dots$). (5)

2.(b) Test the nature of the series $\frac{1x^3}{2.3} + \frac{1.3x^5}{2.4.5} + \frac{1.3.5x^7}{2.4.6.7} + \dots$ (5)

3.(a) Using the expansion of $\tan(x+h)$, compute $\tan 46^\circ$ correct to 4 significant figures. (5)

3.(b) Find all the asymptotes of the curve : $x^3 + x^2y - xy^2 - y^3 + x^2 - y^2 = 2$. (5)

4.(a) Trace the curve $x^3 + y^3 = 3axy$, ($a > 0$) (5)

OR If $U_n = \int_0^{\pi/2} x^n \sin x \, dx$ and $n > 1$, show that $U_n + n(n-1) U_{n-2} = n \left(\frac{1}{2}\pi\right)^{n-1}$

4.(b) In the cycloid $x = a(\theta + \sin \theta)$, $y = a(1 - \cos \theta)$ prove that $\rho = 4a \cos \frac{1}{2} \theta$ (5)