

## ABV- Indian Institute of Information Technology & Management, Gwalior

## Theory of Computation (IT206)

Major Examination (Session 2024–25)

Maximum Time: 3 Hours Max Marks: 45

Note: Attempt all questions. Justify your steps clearly to secure full marks.

- 1. (a) Define and explain the equivalence of DFA and NFA with proof. (b) Minimize the DFA given by the state transition diagram below (diagram to be provided). (8 Marks)
- 2. (a) Prove using the Pumping Lemma that  $L = \{a^n b^n c^n \mid n \ge 1\}$  is not regular. (b) Show that every regular language can be accepted by a DFA with at most  $2^n$  states if the NFA has n states. (8 Marks)
- 3. (a) Construct a Pushdown Automaton (PDA) for the language  $L = \{a^n b^n \mid n \ge 0\}$ . (b) Convert the PDA into an equivalent CFG. (8 Marks)
- 4. (a) Design a Turing Machine that accepts the language  $L = \{a^n b^n \mid n \ge 1\}$ . (b) Explain how a Turing Machine can simulate a PDA. (7 Marks)
- 5. (a) Define NP-completeness. Prove that SAT (Boolean Satisfiability) is NP-complete. (b) Explain polynomial-time reductions with an example. (7 Marks)
- 6. Write short notes on any **two**: (i) Chomsky Hierarchy and its significance (ii) Applications of Automata in Compiler Design (iii) Undecidability of the Halting Problem (7 Marks)