

ABV- Indian Institute of Information Technology & Management, Gwalior

Discrete Structures (IT201)

Mid-Semester Examination (Session 2023–24)

Maximum Time: 1.5 Hours Max Marks: 30

All questions are compulsory. Answer each part clearly.

- 1. (a) Write the contrapositive and converse of the following statement: "If it rains, then the ground becomes wet." (b) Show using truth tables whether $(p \lor q) \to r$ is equivalent to $(p \to r) \land (q \to r)$.
- 2. (a) Define subset, proper subset, and power set with examples. (b) If $A = \{1, 2, 3, 4\}$, $B = \{2, 4, 6, 8\}$, find: $A \cup B$, $A \cap B$, A B, $A \times B$. [6]
- 3. (a) Define injective, surjective, and bijective functions with suitable examples. (b) Let $f: Z \to Z$ be defined as f(x) = 3x + 2. Is f one-to-one? Is it onto? Justify your answer. [6]
- 4. (a) Draw all possible simple graphs with 3 vertices. (b) Determine the degree of each vertex in the graph with vertices $\{a, b, c, d\}$ and edges $\{ab, ac, bd, cd\}$. State whether this graph is connected. [6]
- 5. (a) How many 5-digit numbers can be formed using the digits 1, 2, 3, 4, 5, 6 without repetition? (b) In how many ways can 6 students be seated in a row of 6 chairs if two particular students must sit together? [6]