## Classical Cryptography

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# Example and definitions of a cryptosystem

#### Caesar Cipher - the oldest cryptosystem

A shift cipher – attributed to Julius Caesar (100-44 BC)

MEET ME AFTER THE TOGA PARTY

PHHW PH DIWHU WKH WRJD SDUWB

Shift the alphabet 3 places further down and substitute letters

abcdefghijklmnopqrstuvwxyz

DEFGHIJKLMNOPQRSTUVWXYZABC

#### Communication over an insecure medium

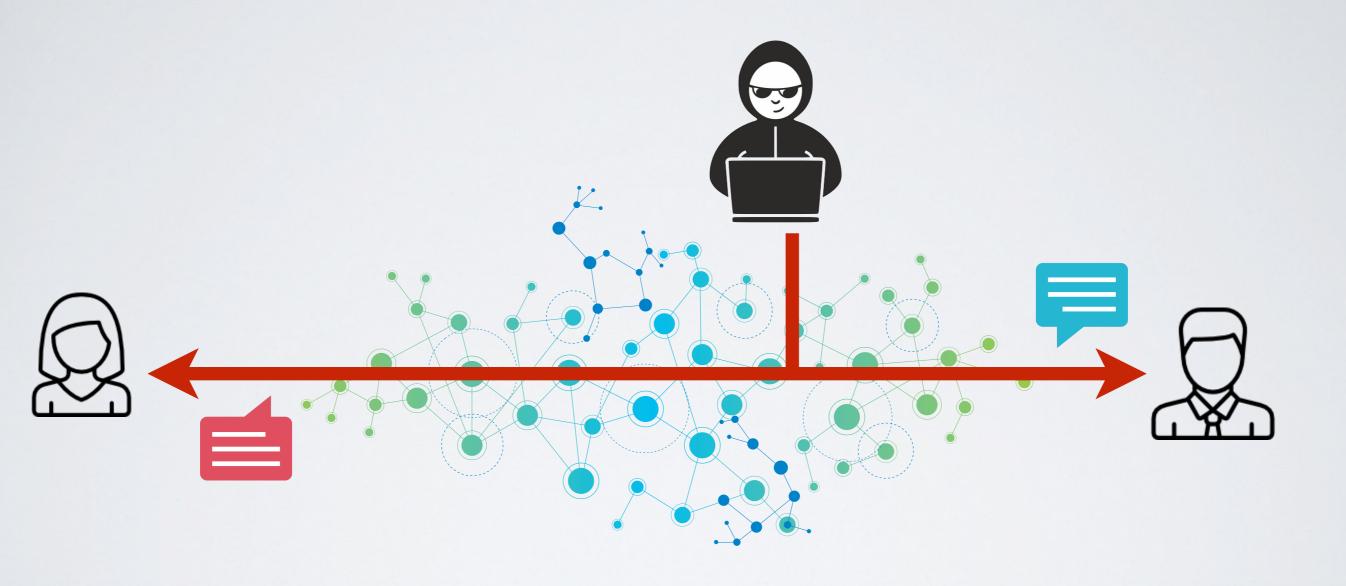


#### Threat | - Interception



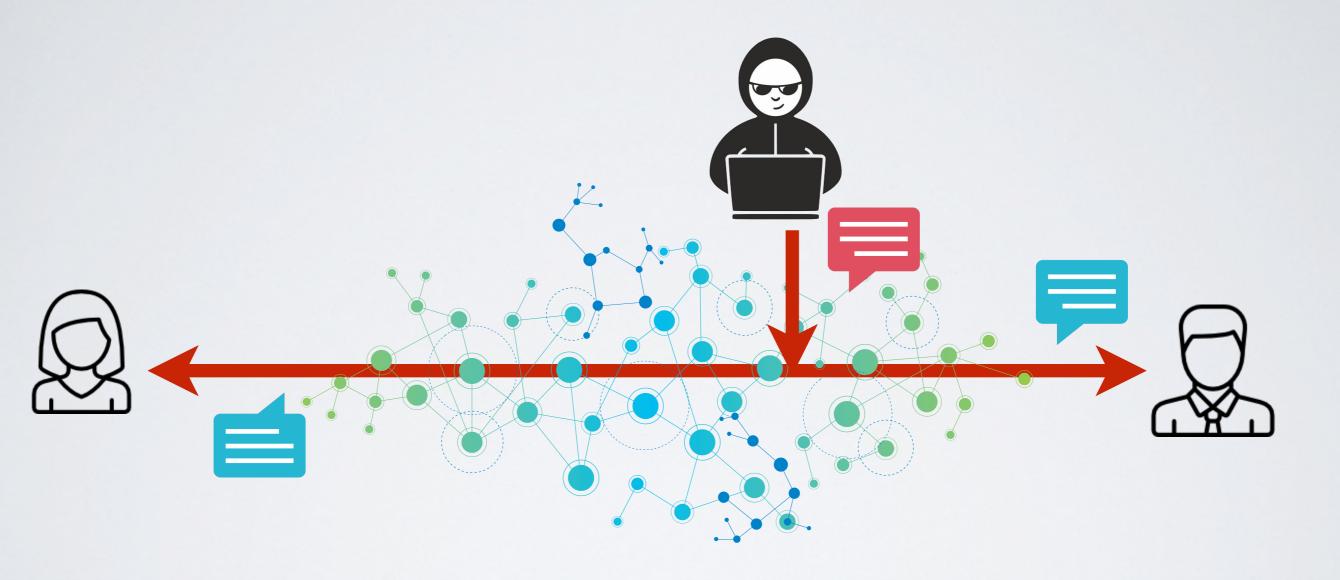
• Interception: an attacker can <u>read</u> messages

#### Threat 2 - Modification



Modification : an attacker can modify messages

#### Threat 3 - Fabrication



• Fabrication : an attacker can inject messages

## Threat 4 - Interruption



• Interruption : an attacker can block messages

#### Confidentiality and Integrity of communications



→ Implement a virtual trusted channel over an insecure medium

#### Definitions

#### **Plaintext**

The message in its clear form (the original message)

#### **Ciphertext**

The message in its ciphered form (the encrypted message)

#### **Encryption**

Transform a plaintext into ciphertext

#### **Decryption**

Transform a ciphertext into a plaintext

#### Definitions

#### Cryptographic algorithm

The method to do encryption and decryption

#### Cryptographic key

An input variable used by the algorithm for the transformation

N-bit security entropy (a.k.a. the key space)
The number of bits necessary to encode the number of possible keys (could be different than the key length)

#### Representing data as numbers

Cryptographic algorithms are mathematical operations

→ messages and keys must be represented as numbers for instance : ASCII encoding

## Back to Caesar Cipher

Algorithm: shift the alphabet of a certain number of positions

Key: the number of positions to shift

**Key space :** 25 possible rotations (~ 5 bits security)

#### **Encoding:**

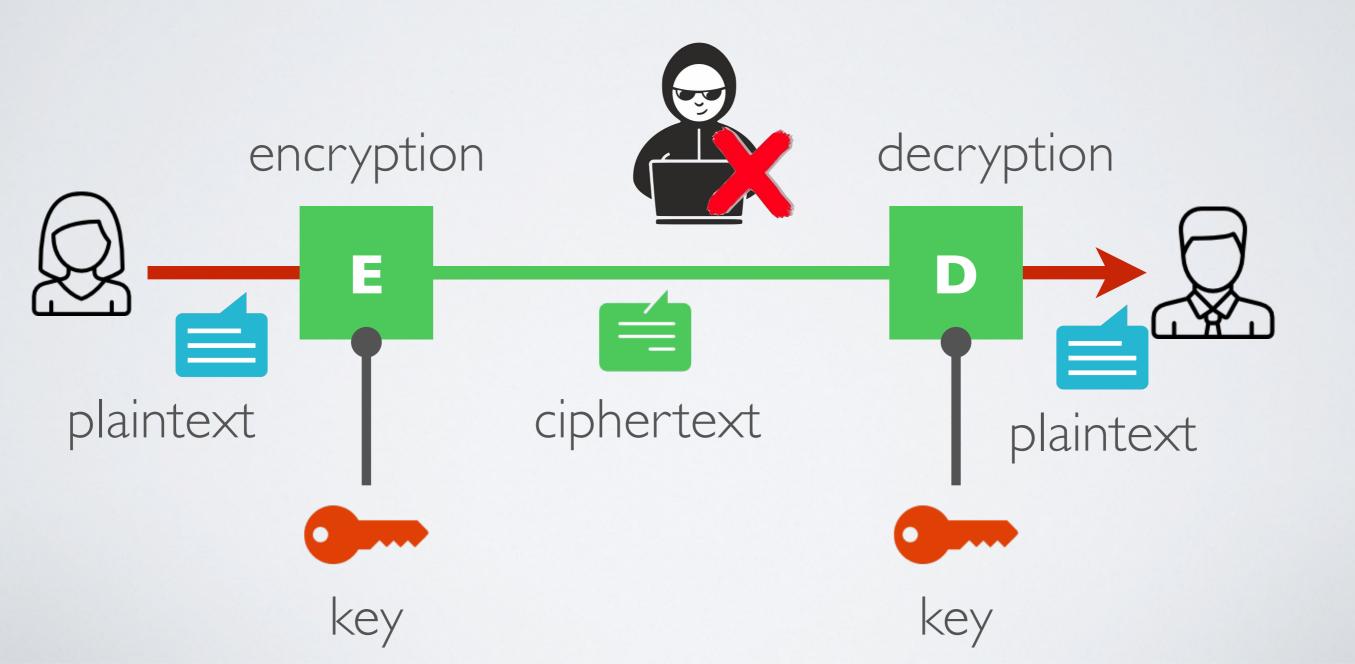
```
a b c d e f g h i j k l m n o p q r s t u v w x y z
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25
```

Encrypting and decrypting one character is obtained as follows:

$$c = E(k,p) = (p + k) \mod 26$$

$$p = D(k,c) = (c - k) \mod 26$$

## The big picture



## Breaking the cipher

#### The Kerckhoffs' principle (1883)

"The enemy knows the system" - the security of a communication should not rely on the fact that the algorithms are secrets

→ A cryptosystem should be secure even if everything about the system, except the key, is public knowledge

No security by obscurity

#### Breaking the cipher - the attacker's model

- Exhaustive Search (a.k.a brute force)
  Try all possible n keys (in average it takes n/2 tries)
- Ciphertext only
   You know one or several <u>random ciphertexts</u>
- Known plaintext
   You know one or several pairs of <u>random plaintext</u> and their corresponding ciphertexts
- Chosen plaintext
  You know one or several pairs of chosen plaintext and their corresponding ciphertexts
- Chosen ciphertext
  You know one or several pairs of plaintext and their corresponding chosen ciphertexts
- **→** A good crypto system resists all attacks

## Breaking Caesar cipher

Exhaustive search	Yes
ciphertext only	Statistical Analysis
known plaintext	Look at the first letter and get the shift
chosen plaintext	Choose "A" and get the shift
chosen ciphertext	Choose "A" and get the shift

## Statistical Cryptanalysis

→ Monoalphabetic ciphers do not change the relative frequency of letters in a message

## Evolution of cryptosystems

## A brief history of cryptography

~ 2000 years ago	Substitution ciphers  (a.k.a mono alphabetic ciphers)
few centuries later	Transposition ciphers
Renaissance	Polyalphabetic ciphers
1844	Mechanization
1976	Public key cryptography

## Substitution ciphers (a.k.a mono alphabetic ciphers)

→ Improvement over Caesar cipher

Algorithm: allow an arbitrary permutation of the alphabet

**Key:** set of substitutions

**Key space:** 26! possible substitutions ( $4 \times 10^{26} \sim 89$  bits)

```
abcdefghijklmnopqrstuvwxyz
DKVQFIBJWPESCXHTMYAUOLRGZN
```

if we wish to replace letters WI RF RWAJ UH YFTSDVF SFUUFYA

## Breaking substitution ciphers

Exhaustive search	Doable with a computer
ciphertext only	Statistical analysis
known plaintext	Match letters together
chosen plaintext	Choose ABCDE and match letters
chosen ciphertext	Choose ABCDE and match letters

## Polyalphabetic ciphers (a.k.a Renaissance Cipher)

→ Vigenere cipher

Algorithm: combine the message and the key

Key: a word

Key space: the length of the word

wearediscoveredsaveyourself
+ deceptivedeceptivedeceptive (mod 26)

ZICVTWQNGRZGVTWAVZHCQYGLMGJ

Advantage: Encryption of a letter is context dependent

## Breaking Polyalphabetic Ciphers

exhaustive search	Small key length only
ciphertext only	Statistical analysis for small key length and significant amount of ciphertext
known plaintext	Subtract plaintext from ciphertext
chosen plaintext	Choose AAAAA and match letters
chosen ciphertext	Choose AAAAA and match letters

#### OTP - One Time Pad

→ Improvement over Vigenere cipher

Algorithm: combine the message and the key

Key: an infinite random string

Key space: infinite

whatanicedaytoday

yksuftgoarfwpfwel

ZZZJUCLUDTUNNWGQS

Advantage: this is the perfect cipher!

Disadvantage: hard to use in practice, how to transmit the key?

## The impossibility of breaking OTP

The ciphertext bears no statistical relationship to the plaintext

→ No statistical analysis

For any plaintext and ciphertext, there exists a key mapping one to the other, and all keys are equally probable

→ A ciphertext can be decrypted to any plaintext of the same length

## Transposition Cipher

Algorithm: switch letters around a permutation

Key: a set of permutation

Key space: the set of permutations

helloworld LOLHERDLWO

## Breaking Transposition ciphers

brute force	Small key length only
ciphertext only	Hard
known plaintext	Match letters together
chosen plaintext	Choose ABCDE and match letters
chosen ciphertext	Choose ABCDE and match letters

## The seeds of modern cryptography

#### **Diffusion**

Mix-up symbols
Transposition Cipher

#### 2. Confusion

Replace a symbol with another Polyaphabetic Cipher

#### 3. Randomization

Repeated encryption of the same text are different OTP

## Mechanization

#### Mechanization



## The cryptography toolbox

## Cryptography is not just a about confidentiality

#### Integrity

digital signatures, hash functions

#### Non-repudiation

contract-signing

#### **Anonymity**

electronic cash, electronic voting

. . .

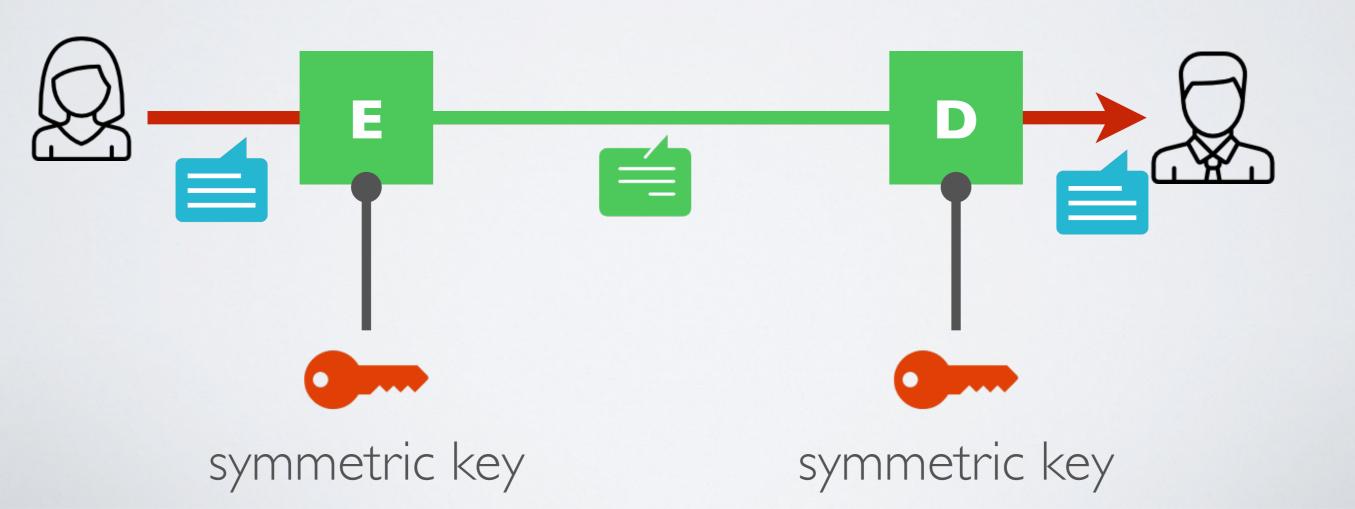
**Availability** 

## The crypto toolbox

- Symmetric cryptography schemes
- Asymmetric cryptography schemes
- Message digests
- Digital signatures
- Certificates

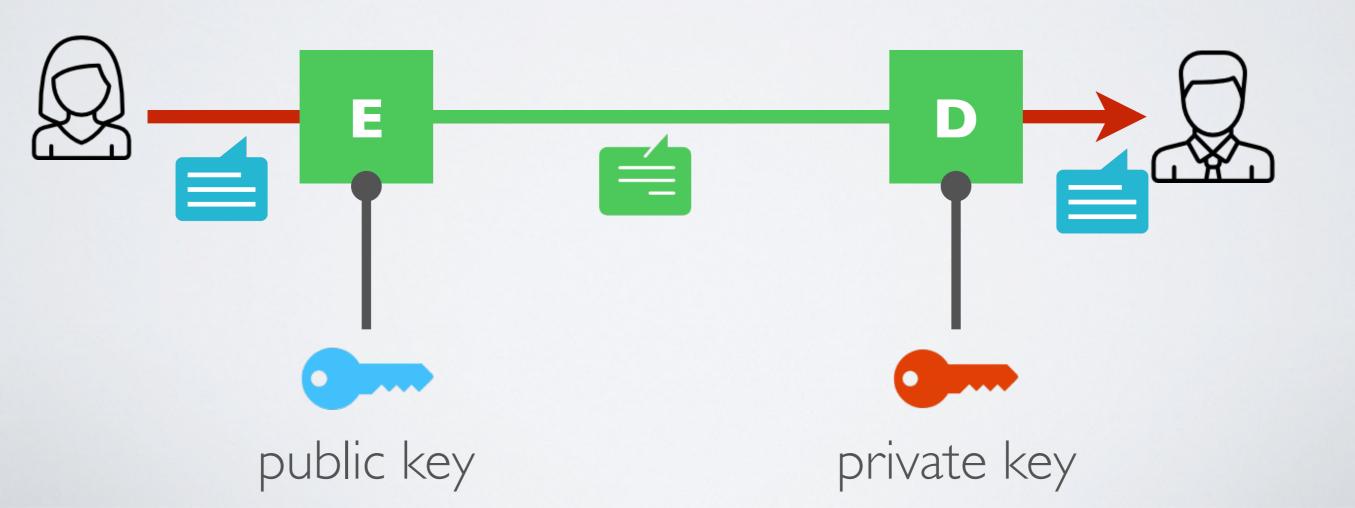
#### Symmetric encryption

The same key is used for encryption and decryption



## Asymmetric encryption a.k.a Public Key Cryptography

- → The public key for encryption
- → The private key for decryption



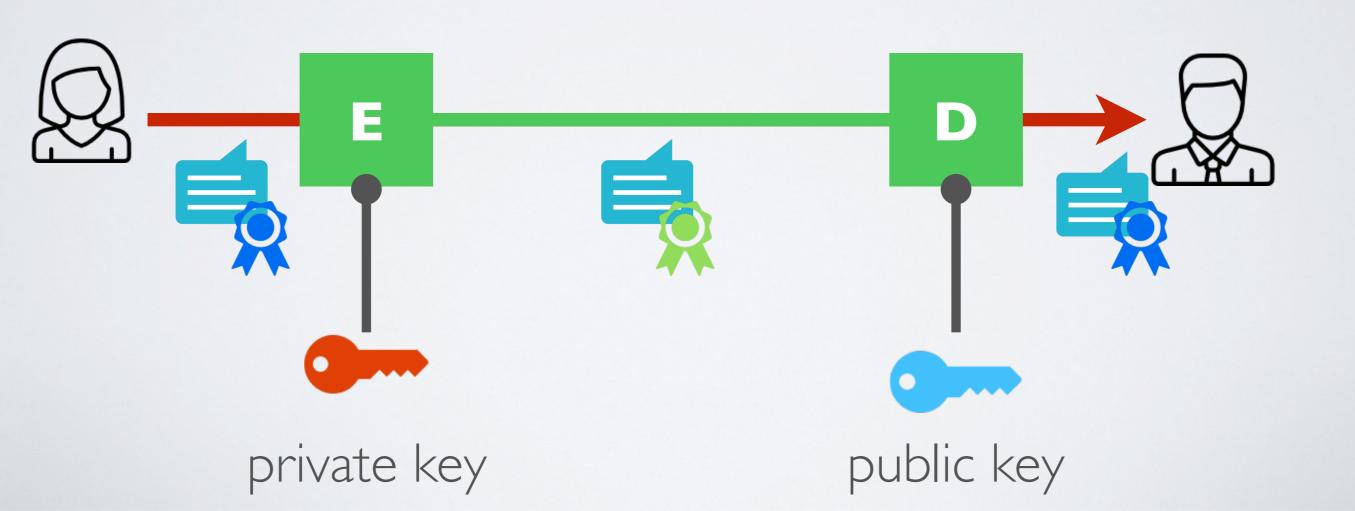
## Message digests

Message digests are meant for creating fingerprints of messages

- Un-keyed message digest: hashes, checksum
- <u>Keyed</u> message digests : MACs

#### Digital Signature

- → The private key for encryption
- → The public key for decryption



#### Certificates - Public Key Infrastructure

Certificates are meant for verifying someone's identity

- Binding between a public key and an owner
- Certified by a certification authority