Principal Component Analysis in R

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Reading the Wine dataset and checking

```
setwd("E:/College/CL7/Assignment12")
winedf <- read.csv("../Datasets/wine.csv")</pre>
head(winedf)
     Wine Alcohol Malic.acid Ash Acl Mg Phenols Flavanoids Nonflavanoid.phenols
## 1
            14.23
                         1.71 2.43 15.6 127
                                                2.80
                                                            3.06
                                                                                  0.28
## 2
            13.20
                         1.78 2.14 11.2 100
                                                2.65
                                                            2.76
                                                                                  0.26
        1
## 3
        1
            13.16
                         2.36 2.67 18.6 101
                                                2.80
                                                            3.24
                                                                                  0.30
## 4
            14.37
                         1.95 2.50 16.8 113
                                                3.85
                                                            3.49
                                                                                  0.24
## 5
            13.24
                         2.59 2.87 21.0 118
                                                2.80
                                                            2.69
                                                                                  0.39
## 6
            14.20
                         1.76 2.45 15.2 112
                                                3.27
                                                            3.39
                                                                                  0.34
##
     Proanth Color.int Hue
                               OD Proline
## 1
        2.29
                  5.64 1.04 3.92
## 2
        1.28
                  4.38 1.05 3.40
                                      1050
## 3
        2.81
                  5.68 1.03 3.17
                                      1185
## 4
        2.18
                  7.80 0.86 3.45
                                      1480
## 5
        1.82
                  4.32 1.04 2.93
                                      735
## 6
        1.97
                  6.75 1.05 2.85
                                      1450
```

Calculate Correlation of all attributes

```
cor_mat <- cor(winedf[, -1])</pre>
cor_mat
##
                            Alcohol Malic.acid
                                                         Ash
                                                                     Acl
## Alcohol
                         1.00000000 0.09439694
                                                 0.211544596 -0.31023514
## Malic.acid
                         0.09439694
                                    1.00000000
                                                 0.164045470
                                                             0.28850040
## Ash
                         0.21154460
                                    0.16404547
                                                 1.000000000
                                                             0.44336719
## Acl
                        -0.31023514 0.28850040
                                                 0.443367187
                                                             1.00000000
                         0.27079823 -0.05457510
                                                 0.286586691 -0.08333309
## Mg
                         0.28910112 -0.33516700
                                                 0.128979538 -0.32111332
## Phenols
## Flavanoids
                         0.23681493 -0.41100659
                                                 0.115077279 -0.35136986
## Nonflavanoid.phenols -0.15592947
                                    0.29297713
                                                 0.186230446 0.36192172
## Proanth
                         0.13669791 -0.22074619
                                                 0.009651935 -0.19732684
## Color.int
                         0.54636420 0.24898534
                                                 0.258887259
                                                             0.01873198
## Hue
                        -0.07174720 -0.56129569 -0.074666889 -0.27395522
## OD
                         0.07234319 -0.36871043 0.003911231 -0.27676855
                         0.64372004 -0.19201056 0.223626264 -0.44059693
## Proline
```

```
##
                                     Phenols Flavanoids Nonflavanoid.phenols
                               Mg
## Alcohol
                       0.27079823 0.28910112 0.2368149
                                                                -0.1559295
## Malic.acid
                      -0.05457510 -0.33516700 -0.4110066
                                                                 0.2929771
## Ash
                       0.28658669
                                  0.12897954
                                             0.1150773
                                                                 0.1862304
## Acl
                      -0.08333309 -0.32111332 -0.3513699
                                                                 0.3619217
## Mg
                       1.00000000 0.21440123
                                             0.1957838
                                                                -0.2562940
## Phenols
                       0.21440123
                                  1.00000000
                                             0.8645635
                                                                -0.4499353
## Flavanoids
                       0.19578377
                                  0.86456350
                                              1.0000000
                                                                -0.5378996
## Nonflavanoid.phenols -0.25629405 -0.44993530 -0.5378996
                                                                 1.0000000
## Proanth
                       0.23644061
                                  0.61241308
                                             0.6526918
                                                                -0.3658451
## Color.int
                       0.19995001 -0.05513642 -0.1723794
                                                                 0.1390570
## Hue
                       0.05539820
                                  0.43368134
                                              0.5434786
                                                                -0.2626396
## OD
                       0.06600394 0.69994936
                                              0.7871939
                                                                -0.5032696
## Proline
                       0.39335085 0.49811488
                                                                -0.3113852
##
                           Proanth
                                    Color.int
                                                                  OD
## Alcohol
                       0.136697912
                                   0.54636420 -0.07174720
                                                          0.072343187
                      ## Malic.acid
                       0.003911231
                      ## Acl
## Mg
                       0.236440610 0.19995001 0.05539820
                                                          0.066003936
## Phenols
                       0.612413084 -0.05513642 0.43368134
                                                         0.699949365
## Flavanoids
                       0.652691769 -0.17237940 0.54347857
                                                          0.787193902
## Nonflavanoid.phenols -0.365845099 0.13905701 -0.26263963 -0.503269596
## Proanth
                       1.000000000 -0.02524993 0.29554425
                                                          0.519067096
## Color.int
                      -0.025249931 1.00000000 -0.52181319 -0.428814942
## Hue
                       0.295544253 -0.52181319 1.00000000
                                                         0.565468293
                       0.519067096 -0.42881494 0.56546829
## OD
                                                          1.000000000
## Proline
                       0.330416700 0.31610011 0.23618345 0.312761075
##
                         Proline
## Alcohol
                       0.6437200
## Malic.acid
                      -0.1920106
## Ash
                       0.2236263
## Acl
                      -0.4405969
## Mg
                       0.3933508
## Phenols
                       0.4981149
## Flavanoids
                       0.4941931
## Nonflavanoid.phenols -0.3113852
                       0.3304167
## Proanth
## Color.int
                       0.3161001
## Hue
                       0.2361834
## OD
                       0.3127611
## Proline
                       1.0000000
```

We see that alcohol and Proline, alcohol and Color.int has fairly high correlation.

Similarly, Phenols with Proanth, and Flavanoids with Proanth has high correlation.

Flavanoids and nonflavanoids phenols has high negative correlation.

Checking the principal components of the dataset.

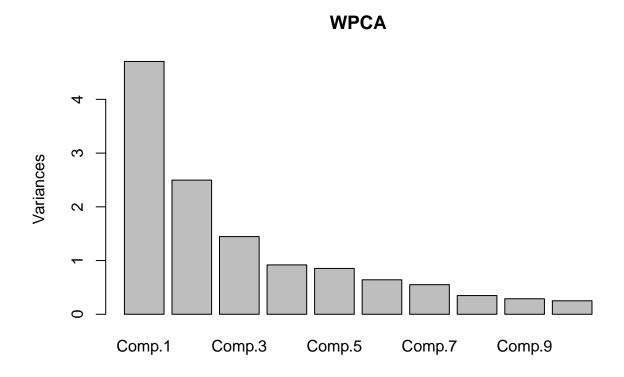
```
WPCA <- princomp(winedf[, -1], cor = T, scores = T, covmat = NULL)
summary(WPCA)</pre>
```

Importance of components:

```
##
                             Comp.1
                                       Comp.2
                                                 Comp.3
                                                           Comp.4
## Standard deviation
                          2.1692972 1.5801816 1.2025273 0.9586313 0.92370351
## Proportion of Variance 0.3619885 0.1920749 0.1112363 0.0706903 0.06563294
## Cumulative Proportion 0.3619885 0.5540634 0.6652997 0.7359900 0.80162293
                              Comp.6
                                         Comp.7
                                                    Comp.8
                                                                Comp.9
                                                                          Comp.10
## Standard deviation
                          0.80103498 0.74231281 0.59033665 0.53747553 0.50090167
## Proportion of Variance 0.04935823 0.04238679 0.02680749 0.02222153 0.01930019
## Cumulative Proportion 0.85098116 0.89336795 0.92017544 0.94239698 0.96169717
##
                             Comp.11
                                        Comp.12
                                                    Comp.13
## Standard deviation
                          0.47517222 0.41081655 0.321524394
## Proportion of Variance 0.01736836 0.01298233 0.007952149
## Cumulative Proportion 0.97906553 0.99204785 1.000000000
```

Plot the WPCA graph

```
plot(WPCA)
```



(component coefficients) correlation coefficients between variables (rows) and factors (columns) $\,$

```
loadings(WPCA)

##

## Loadings:

##

Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8
```

```
## Alcohol
                        0.144 0.484 0.207
                                                     0.266 0.214
## Malic.acid
                        -0.245
                               0.225
                                             -0.537
                                                            0.537 - 0.421
                                0.316 -0.626 0.214
                                                     0.143 0.154 0.149 -0.170
## Ash
                        -0.239
## Acl
                                      -0.612
                                                           -0.101 0.287 0.428
## Mg
                        0.142
                               0.300 -0.131 0.352 -0.727
                                                                  -0.323 -0.156
## Phenols
                        0.395
                                                                         -0.406
                                      -0.146 -0.198 0.149
## Flavanoids
                         0.423
                                      -0.151 -0.152 0.109
                                                                         -0.187
## Nonflavanoid.phenols -0.299
                                      -0.170 0.203 0.501 -0.259 -0.595 -0.233
                                      -0.149 -0.399 -0.137 -0.534 -0.372 0.368
## Proanth
                         0.313
## Color.int
                                0.530 0.137
                                                           -0.419 0.228
## Hue
                         0.297 - 0.279
                                              0.428
                                                    0.174 0.106 -0.232
                                                                         0.437
## OD
                         0.376 -0.164 -0.166 -0.184 0.101 0.266
## Proline
                         0.287   0.365   0.127   0.232   0.158   0.120
                                                                          0.120
##
                        Comp.9 Comp.10 Comp.11 Comp.12 Comp.13
## Alcohol
                         0.509 0.212
                                       0.226
                                                0.266
## Malic.acid
                               -0.309
                                               -0.122
## Ash
                        -0.308
                                       0.499
                                                       -0.141
                         0.200
## Acl
                                       -0.479
## Mg
                         0.271
## Phenols
                         0.286 - 0.320
                                      -0.304
                                                0.304 - 0.464
## Flavanoids
                               -0.163
                                                        0.832
## Nonflavanoid.phenols 0.196 0.216
                                      -0.117
                                                        0.114
## Proanth
                        -0.209 0.134
                                       0.237
                                                       -0.117
## Color.int
                               -0.291
                                               -0.604
## Hue
                                               -0.259
                               -0.522
## OD
                         0.137 0.524
                                               -0.601
                                                      -0.157
## Proline
                        -0.576 0.162
                                      -0.539
##
##
                 Comp.1 Comp.2 Comp.3 Comp.4 Comp.5 Comp.6 Comp.7 Comp.8 Comp.9
                   1.000 1.000 1.000 1.000 1.000 1.000 1.000
## SS loadings
                                                                   1.000 1.000
## Proportion Var 0.077 0.077 0.077 0.077
                                                     0.077
                                                            0.077
                                                                    0.077 0.077
## Cumulative Var 0.077 0.154 0.231 0.308 0.385 0.462 0.538 0.615 0.692
##
                 Comp.10 Comp.11 Comp.12 Comp.13
## SS loadings
                   1.000
                            1.000
                                    1.000
                                            1.000
## Proportion Var
                   0.077
                            0.077
                                    0.077
                                            0.077
## Cumulative Var
                   0.769
                            0.846
                                   0.923
                                            1.000
```

Checking the attributes of the Principal Component Analysis

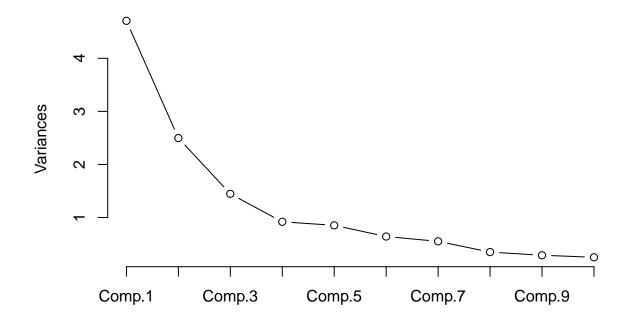
attributes(WPCA)

```
## $names
## [1] "sdev" "loadings" "center" "scale" "n.obs" "scores" "call"
##
## $class
## [1] "princomp"
```

Plotting various graphs and scree graph to check the variation of information in the variables/components.

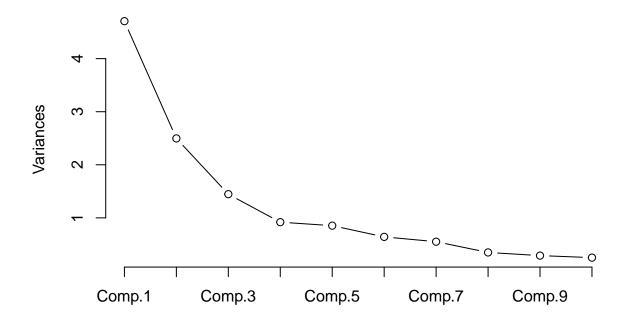
plot(WPCA, t='1')

WPCA

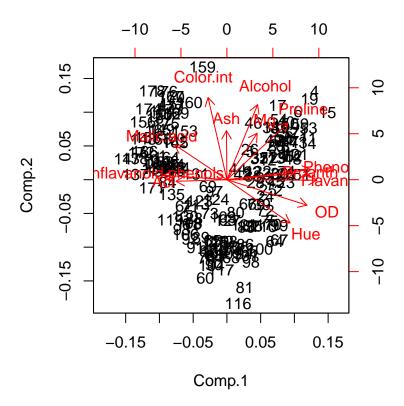


screeplot(WPCA, type="line", main="Scree plot")

Scree plot



biplot(WPCA)



Check the score of PCA

WPCA\$scores[1:10, 1]

[1] 3.316751 2.209465 2.516740 3.757066 1.008908 3.050254 2.449090 2.059437

[9] 2.510874 2.753628