

# Operating Systems

Semaphores

# Lecture Overview

- Semaphores

# Last Week

## Concurrency

- Locks
- Lock Implementation
  - Data Structures
- Condition Variables
- Pipes

# Concurrency Objectives

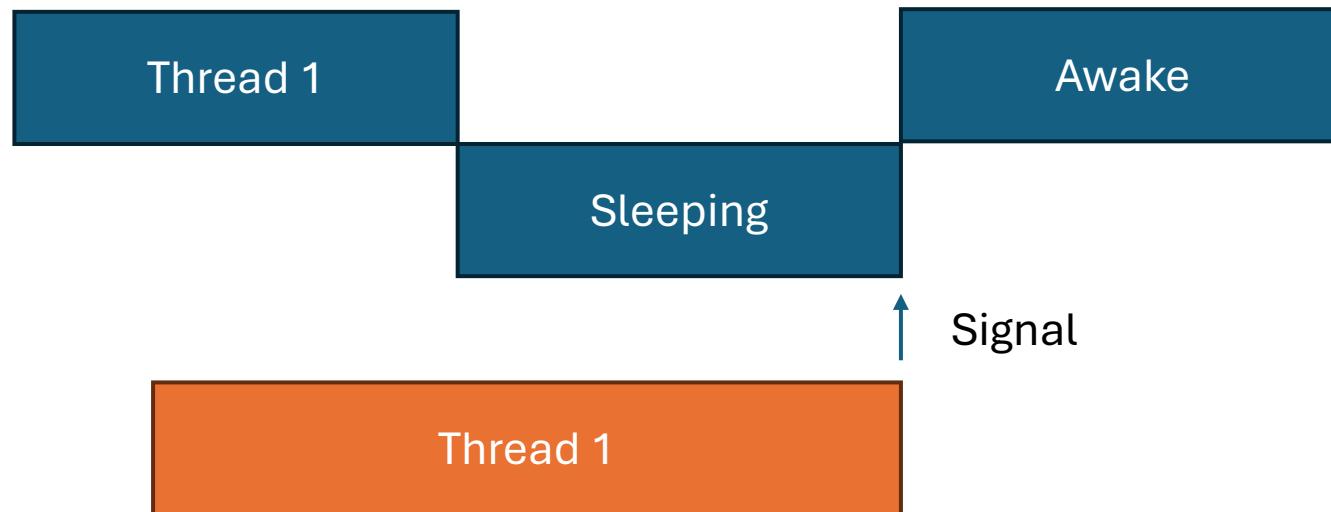
## Main Objectives

- Mutual Exclusion (atomic logic)
  - Mutexes
- Ordering (A waits for B)
  - Condition Variables

# Semaphores

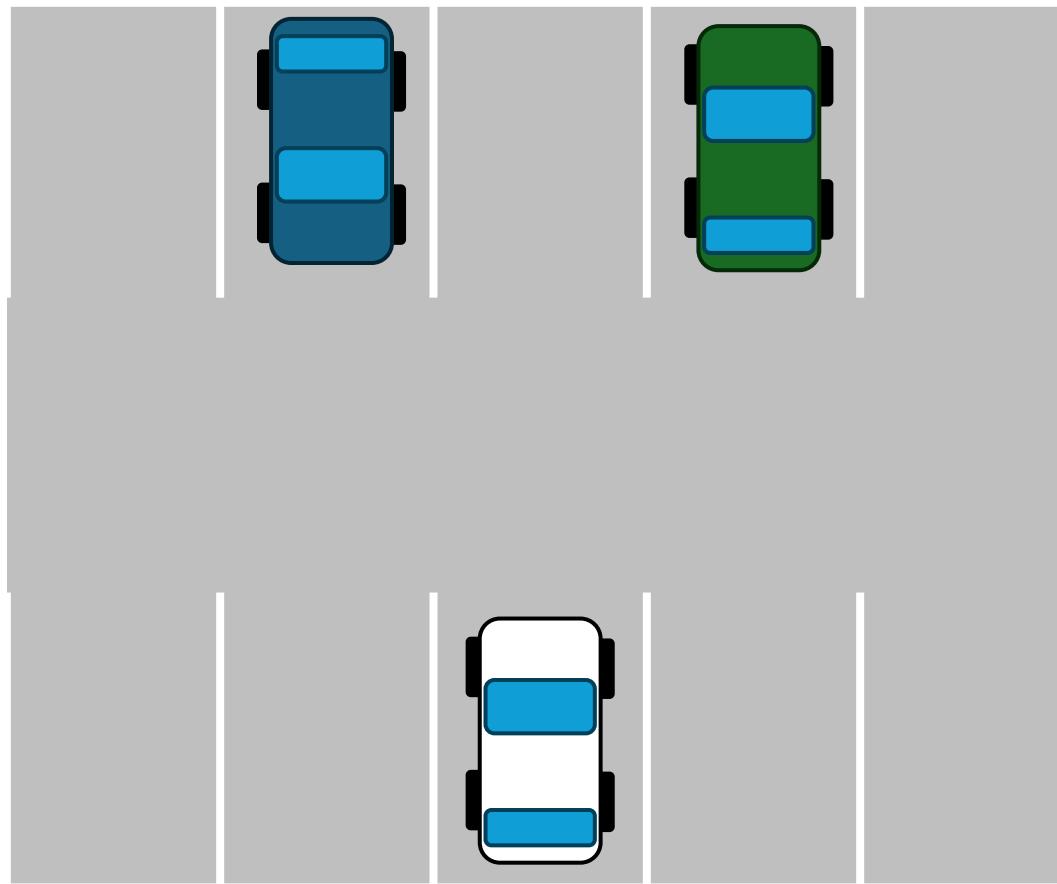
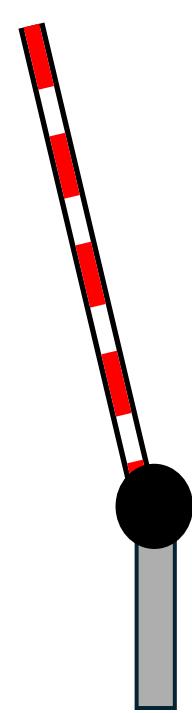
# Condition Variables

## A weakness



# Condition Variables

**Another weakness**



# Condition Variables

## Condition Variables

- No ‘state’

## Semaphores

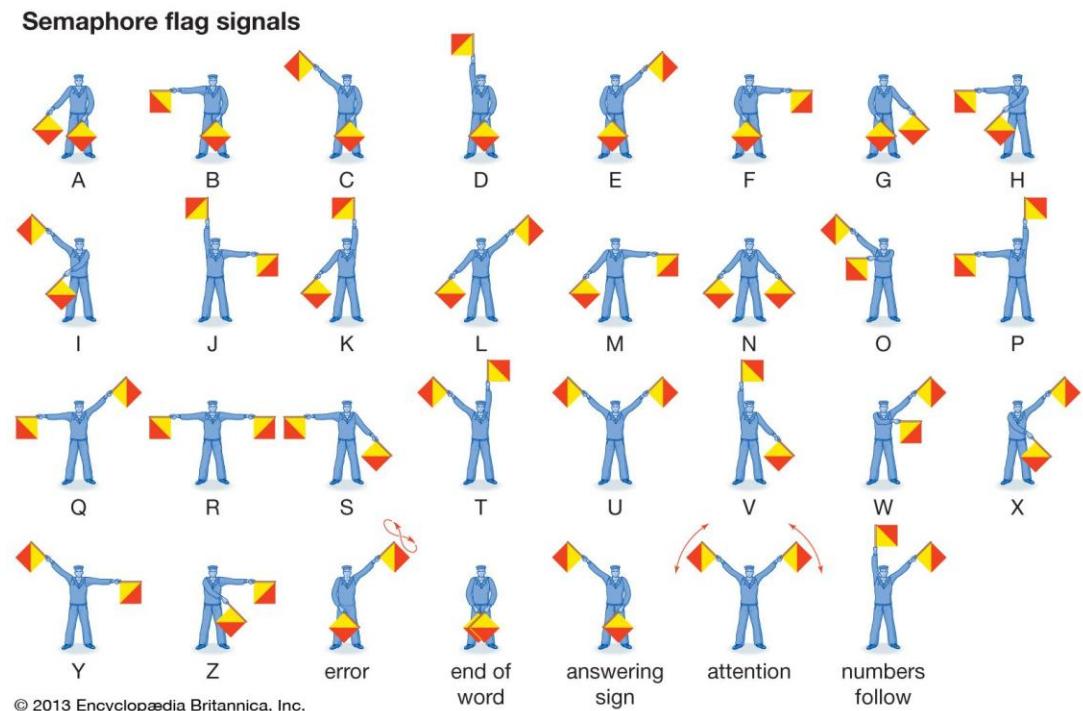
- Has a ‘state’
  - Non-negative **integer**

# Semaphores

## History

- Dijkstra (60s)

## Etymology



# Semaphores (In Practice)

## **wait():**

Wait for the semaphore to become positive ( $>0$ ) and then decrement.

## **post():**

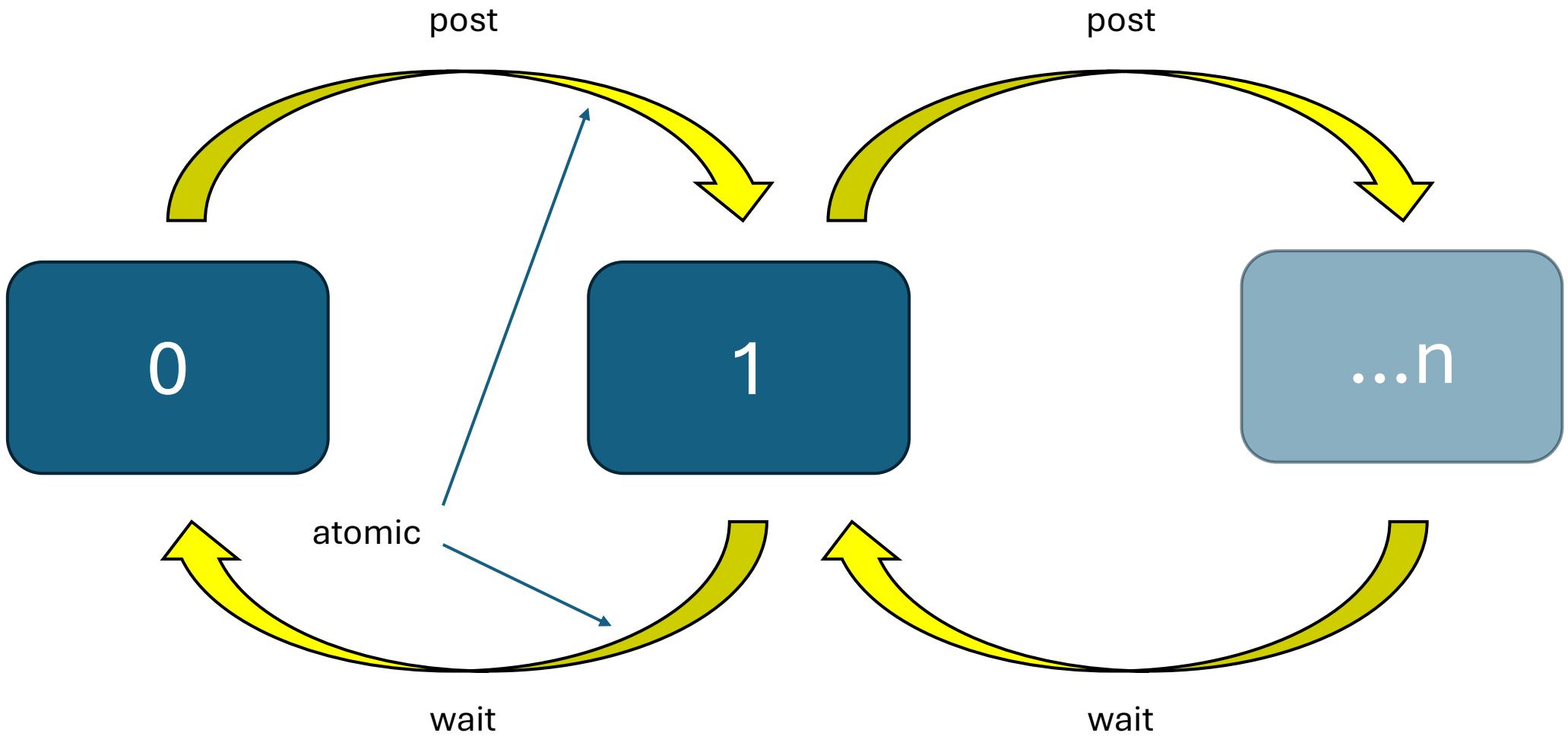
Increment the semaphore by 1, waking up a waiting **wait()** (if any).

Sometimes referred to as V & P

verhogen: to increase  
proberen: to probe

# Semaphores

No negative values



# Semaphores (Code)

```
sem_t sem;  
  
sem_init(sem_t * s, int initval)  
{  
    s->value = initval;  
}
```

## **wait(), test(), P()**

- Waits until the value of **sem** >0, then decrements **sem**

## **signal(), post(), V()**

- Increases **sem** value, then wake a single waiter

# CV vs Semaphore

CV

```
void thread_join() {  
    mutex_lock (&lock);  
    // do stuff  
    done = true;  
    cond_signal(&cond);  
    mutex_unlock(&lock);  
}
```

```
void thread_exit() {  
    mutex_lock (&lock);  
    if (!done)  
        cond_wait(&cond, &lock);  
    //do stuff  
    mutex_unlock(&lock);  
}
```

Semaphore

```
void thread_join() {  
    sem_wait(&s);  
}
```

```
void thread_exit() {  
    sem_post(&s);  
}
```

```
sem_t s;  
semi_init(&s, ???);
```

# Semaphores and Fairness...

Depends on implementation

- Some implementations provide queues
  - FIFO => Performance overhead

# Equivalence

One of these things is just like the others...

# So... which is best?



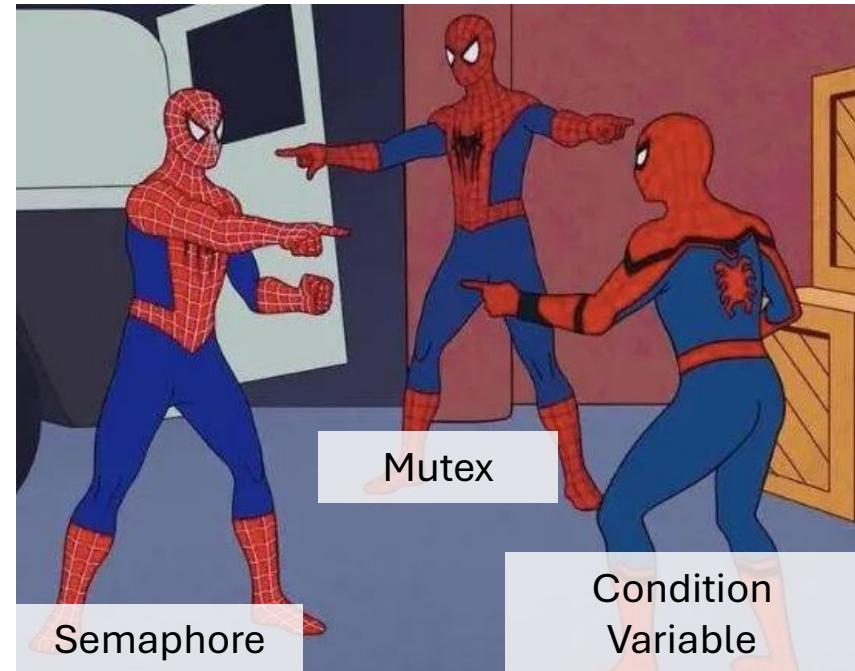
# Equivalence

## Differences:

- Implementations are different
- Some are more convenient

## Similarity:

- One can make from the other...



# Building a Lock from a Semaphore

```
typedef struct __lock_t {  
    sem_t sem;  
} lock_t;  
  
void init(lock_t *lock) {  
    sem_init(&lock->sem, ??);  
}  
  
void acquire(lock_t *lock) {  
    sem_wait(&lock->sem, ??);  
}  
  
void release(lock_t *lock) {  
    sem_post(&lock->sem, ??);  
}
```

Oh wow...

# Building a CV from a Semaphore

Can be done...

Much harder...

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {  
    int value;  
    cond_t cond;  
    lock_t lock;  
} sem_t;  
  
void sem_init(sem_t *s, int value) {  
    s->value = value;  
    cond_init(&s->cond);  
    lock_init(&s->lock);  
}  
  
void wait(sem_t *s) {  
    ???  
}  
  
void post(sem_t *s) {  
    ???  
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {  
    ???  
} sem_t;  
  
void sem_init(sem_t *s) {  
    ???  
}  
  
void wait(sem_t *s) {  
    ???  
}  
  
void post(sem_t *s) {  
    ???  
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {  
    int value;  
    cond_t cond;  
    lock_t lock;  
} sem_t;  
  
void sem_init(sem_t *s) {  
    ???  
}  
  
void wait(sem_t *s) {  
    ???  
}  
  
void post(sem_t *s) {  
    ???  
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {  
    int value;  
    cond_t cond;  
    lock_t lock;  
} sem_t;  
  
void sem_init(sem_t *s, int value) {  
    s->value = value;  
    cond_init(&s->cond);  
    lock_init(&s->lock);  
}  
  
void wait(sem_t *s) {  
    ???  
}  
  
void post(sem_t *s) {  
    ???  
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {  
    int value;  
    cond_t cond;  
    lock_t lock;  
} sem_t;  
  
void sem_init(sem_t *s, int value) {  
    s->value = value;  
    cond_init(&s->cond);  
    lock_init(&s->lock);  
}  
  
void wait(sem_t *s) {  
    ???  
}  
  
void post(sem_t *s) {  
    ???  
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {
    int value;
    cond_t cond;
    lock_t lock;
} sem_t;

void sem_init(sem_t *s, int value) {
    s->value = value;
    cond_init(&s->cond);
    lock_init(&s->lock);
}

void wait(sem_t *s) {
    lock_acquire(&s->lock);
    // Stuff
    lock_release(&s->lock);
}

void post(sem_t *s) {
    lock_acquire(&s->lock);
    // Stuff
    lock_release(&s->lock);
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {
    int value;
    cond_t cond;
    lock_t lock;
} sem_t;

void sem_init(sem_t *s, int value) {
    s->value = value;
    cond_init(&s->cond);
    lock_init(&s->lock);
}

void wait(sem_t *s) {
    lock_acquire(&s->lock);
    while (s->value <= 0)
        cond_wait(&s->cond, &s->lock);
    s->value--;
    lock_release(&s->lock);
}

void post(sem_t *s) {
    lock_acquire(&s->lock);
    // Stuff
    lock_release(&s->lock);
}
```

# Building a Semaphore from a Lock and CV

```
typedef struct __sem_t {
    int value;
    cond_t cond;
    lock_t lock;
} sem_t;

void sem_init(sem_t *s, int value) {
    s->value = value;
    cond_init(&s->cond);
    lock_init(&s->lock);
}

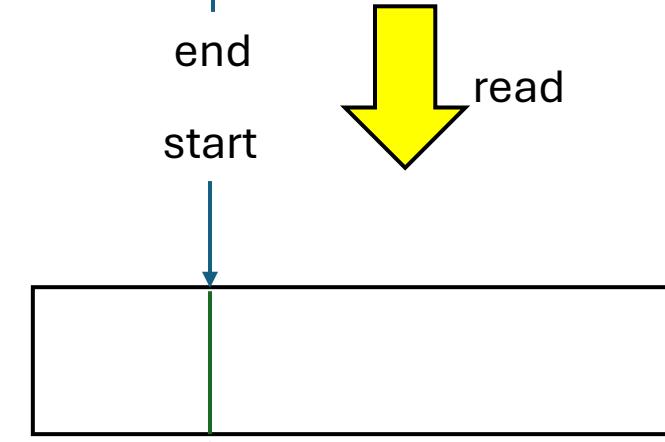
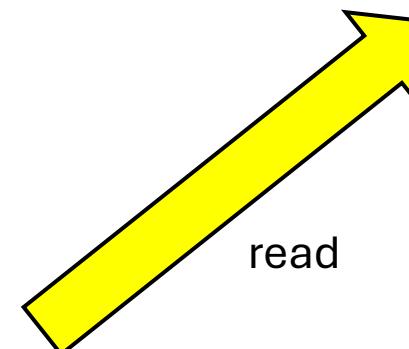
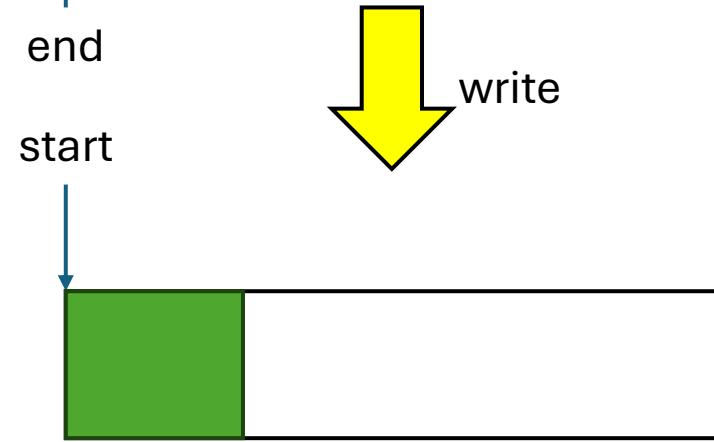
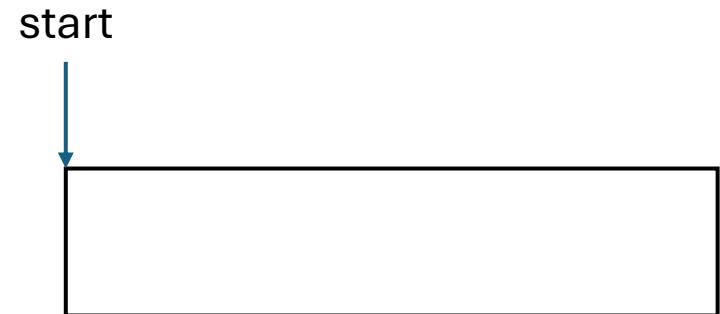
void wait(sem_t *s) {
    lock_acquire(&s->lock);
    while (s->value <= 0)
        cond_wait(&s->cond, &s->lock);
    s->value--;
    lock_release(&s->lock);
}

void post(sem_t *s) {
    lock_acquire(&s->lock);
    s->value++;
    cond_signal(&s->cond);
    lock_release(&s->lock);
}
```

# Building with Semaphores

Let's make something

# Revision: Buffer



# Building a Buffer

**How many semaphores?**

**How many constraints?**

sem\_t full;

sem\_t empty;

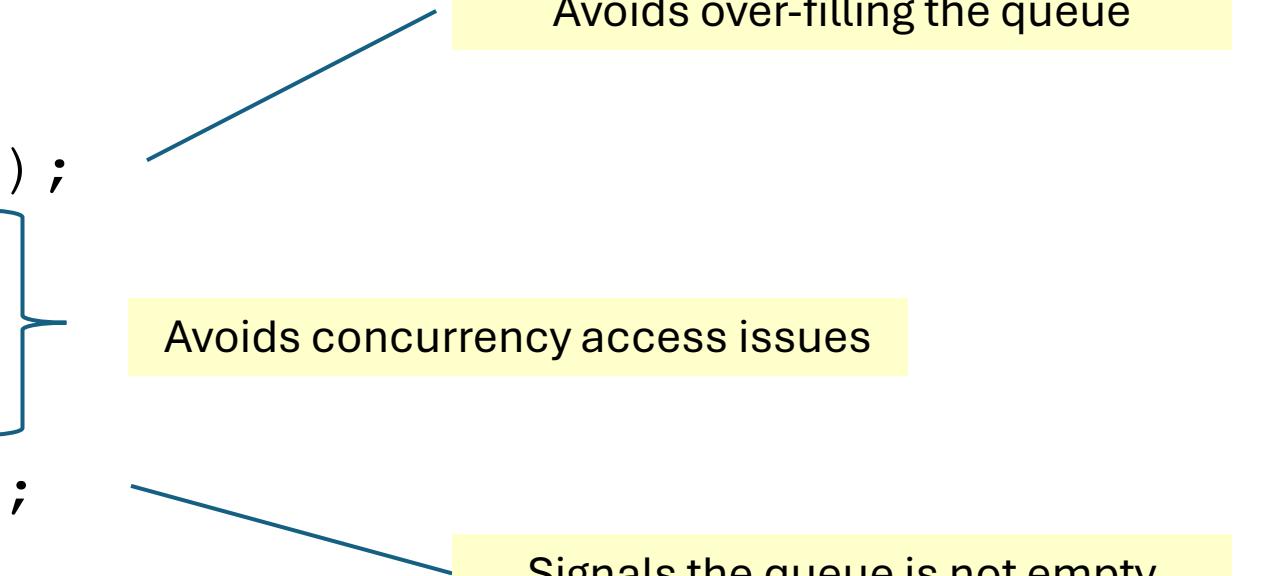
sem\_t mutex;

# Bounded Buffer

```
sem_t fullSlots = 0;  
sem_t emptySlots = bufferSize;  
sem_t mutex = 1;
```

# Bounded Buffer

```
sem_t fullSlots = 0;  
sem_t emptySlots = bufferSize;  
sem_t mutex = 1;  
  
Producer(item) {  
    sem_wait(&emptySlots);  
    sem_wait(&mutex);  
    Enqueue(item);  
    sem_post(&mutex);  
    sem_post(&fullSlots);  
}
```



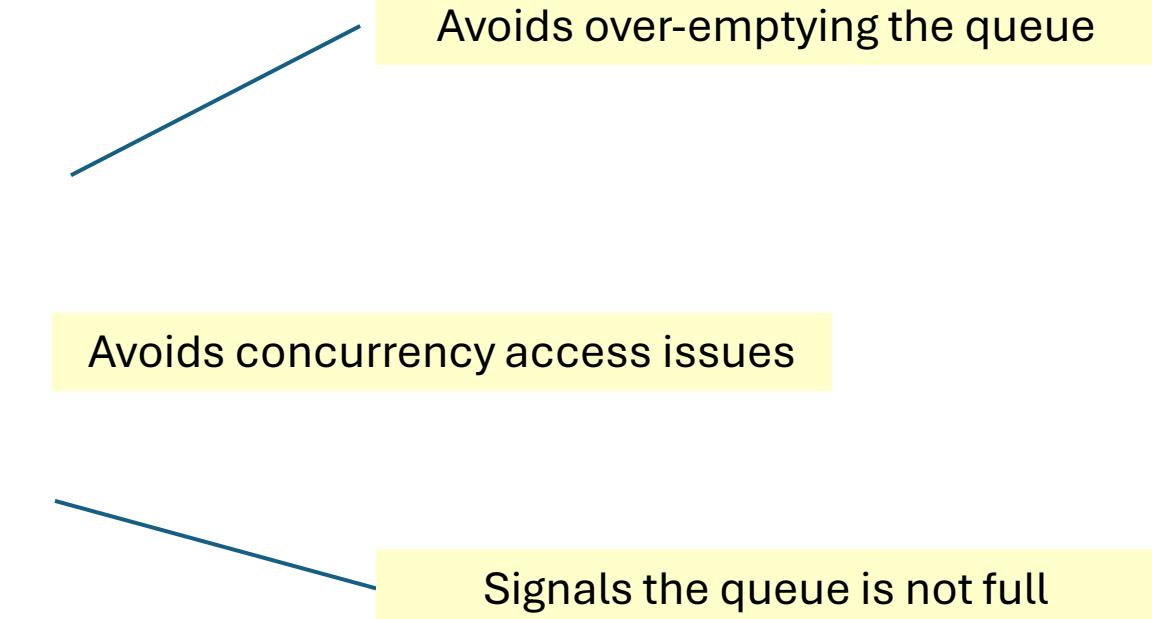
Avoids over-filling the queue

Avoids concurrency access issues

Signals the queue is not empty

# Bounded Buffer

```
sem_t fullSlots = 0;  
sem_t emptySlots = bufferSize;  
sem_t mutex = 1;  
  
Consumer(item) {  
    sem_wait(&fullSlots);  
    sem_wait(&mutex);  
    Dequeue(item);  
    sem_post(&mutex);  
    sem_post(&emptySlots);  
    return item;  
}
```



Avoids over-emptying the queue

Avoids concurrency access issues

Signals the queue is not full

# All Together (very simple implementation)

```
Producer(item) {  
    sem_wait(&emptySlots);  
    sem_wait(&mutex);  
    Enqueue(item);  
    sem_post(&mutex);  
    sem_post(&fullSlots);  
}
```

```
Consumer(item) {  
    sem_wait(&fullSlots);  
    sem_wait(&mutex);  
    Dequeue(item);  
    sem_post(&mutex);  
    sem_post(&emptySlots);  
    return item;  
}
```

Symmetry

# Deadlock

```
Producer(item) {  
    sem_wait(&mutex);  
    sem_wait(&emptySlots);  
    Enqueue(item);  
    sem_post(&mutex);  
    sem_post(&fullSlots);  
}
```

```
Consumer(item) {  
    sem_wait(&fullSlots);  
    sem_wait(&mutex);  
    Dequeue(item);  
    sem_post(&mutex);  
    sem_post(&emptySlots);  
    return item;  
}
```

Order is important

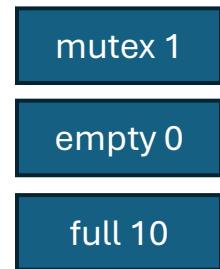
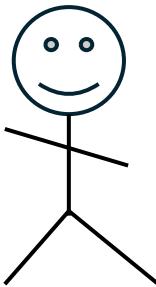
# Deadlock

```
Producer(item) {  
    sem_wait(&mutex);  
    sem_wait(&emptySlots);  
    Enqueue(item);  
    sem_post(&mutex);  
    sem_post(&fullSlots);  
}
```

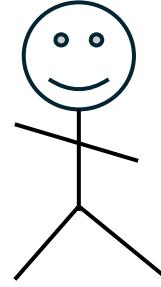
Full Buffer

```
Consumer(item) {  
    sem_wait(&fullSlots);  
    sem_wait(&mutex);  
    Dequeue(item);  
    sem_post(&mutex);  
    sem_post(&emptySlots);  
    return item;  
}
```

Producer



Consumer



# Semaphores: Summary

## **Summary:**

- Equivalent to locks + condition variables
- Have a state (single integer)
- `sem_wait()`      wait until  $>0$ , then decrement (atomic)
- `sem_post()`      increment, then wake a single waiter (atomic)
- Convenient and ‘clean’ for:
  - producer/consumer
  - reader/writer

# Timing

Dread...

# Case Study: Therac-25

Computer controlled ‘radiation therapy machine’.

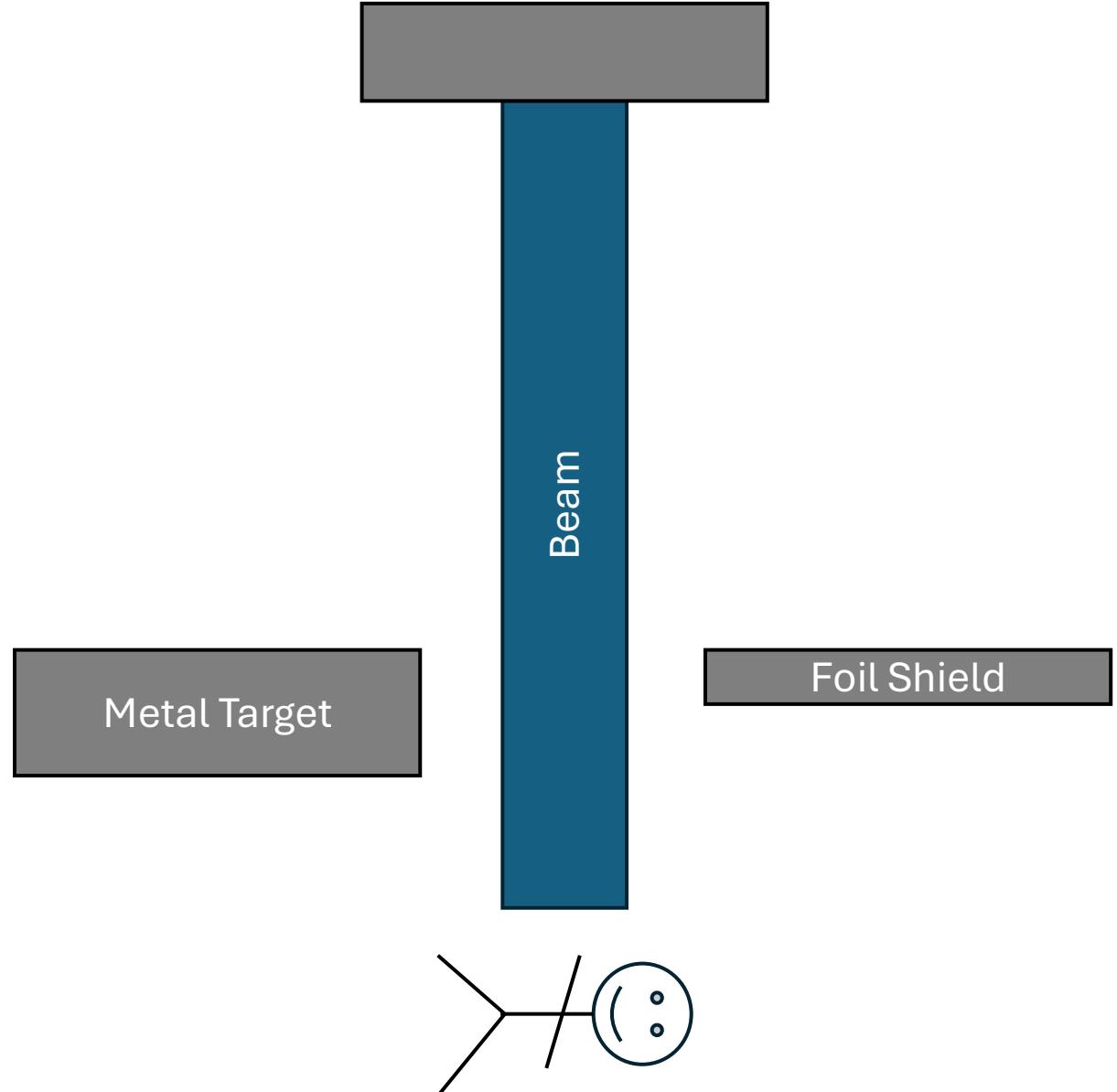
- High Dose, Wide Area
- Low Dose, Narrow Area



# Case Study: Therac-25

Computer controlled ‘radiation therapy machine’.

- High Dose, Wide Area
- Low Dose, Narrow Area



# Problem

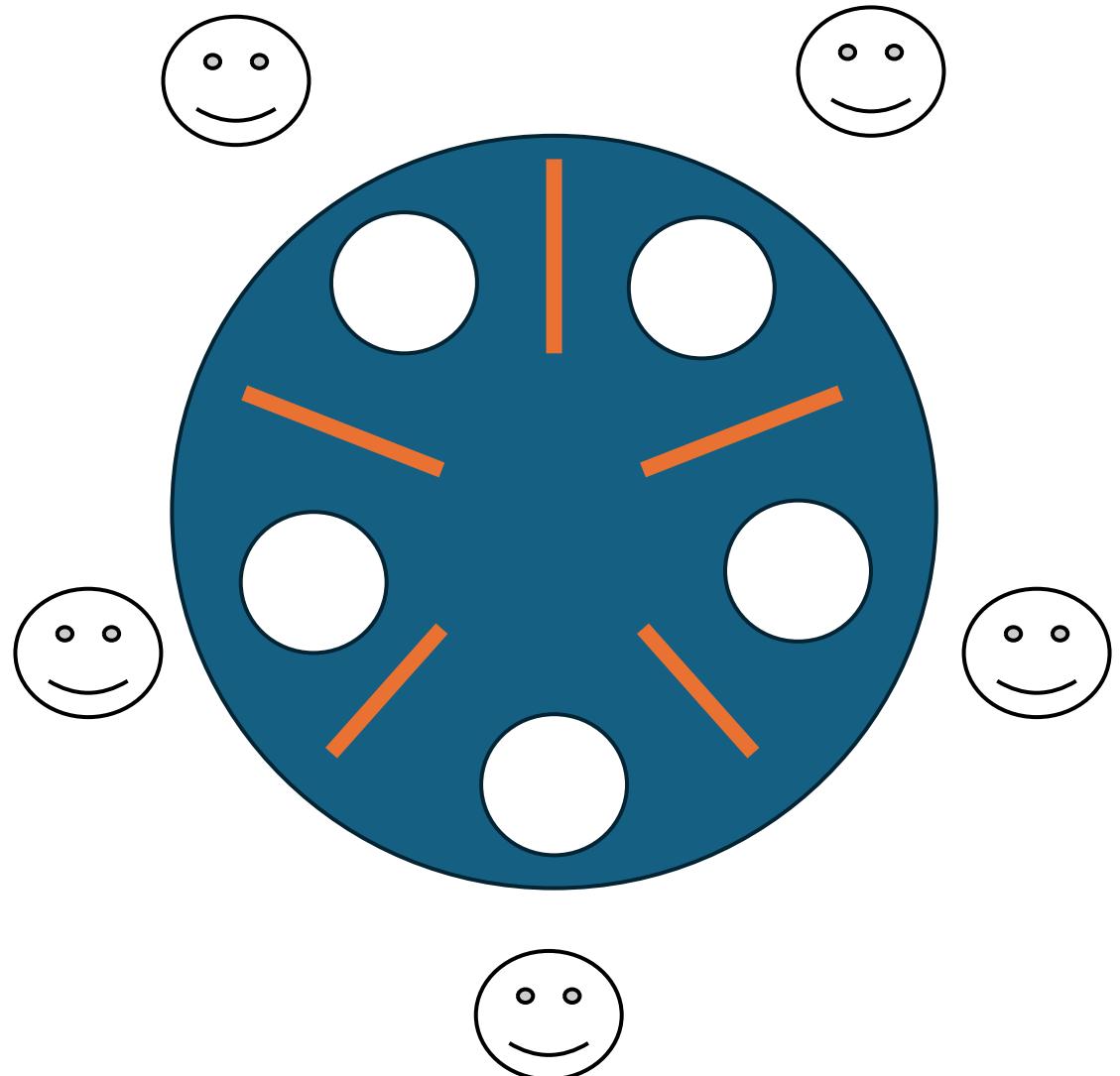
There are 5 people.

Each has a bowl of noodles.

To the left and right of each, is a single chopstick.

You can't talk.

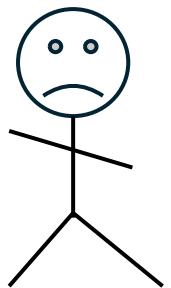
You can only take one chopstick at a time.



# Deadlock

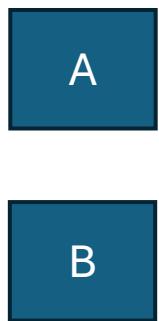
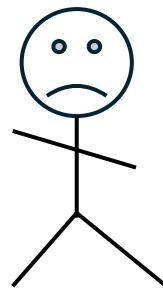
**Thread 1**

lock(&A)  
lock(&B)

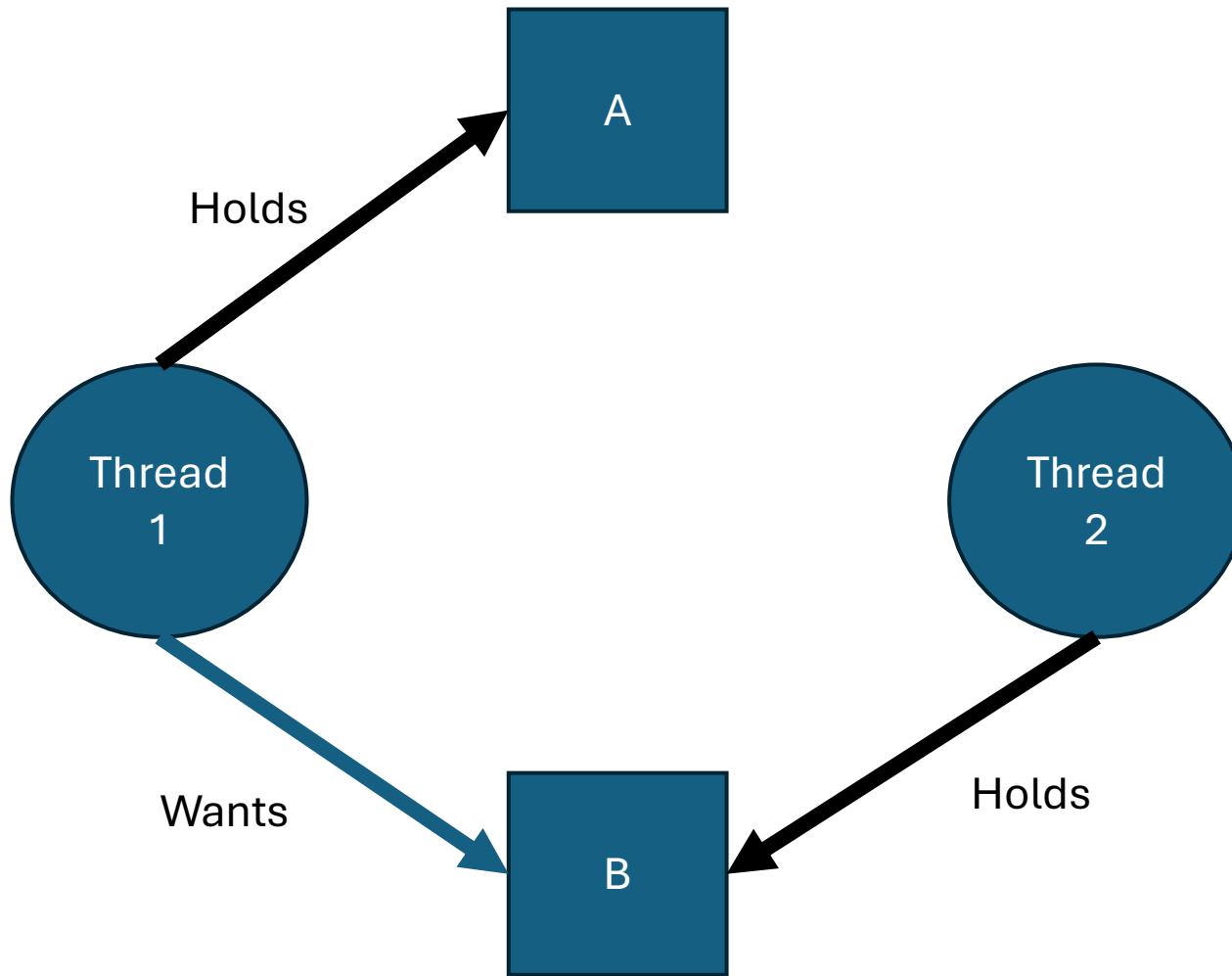


**Thread 2**

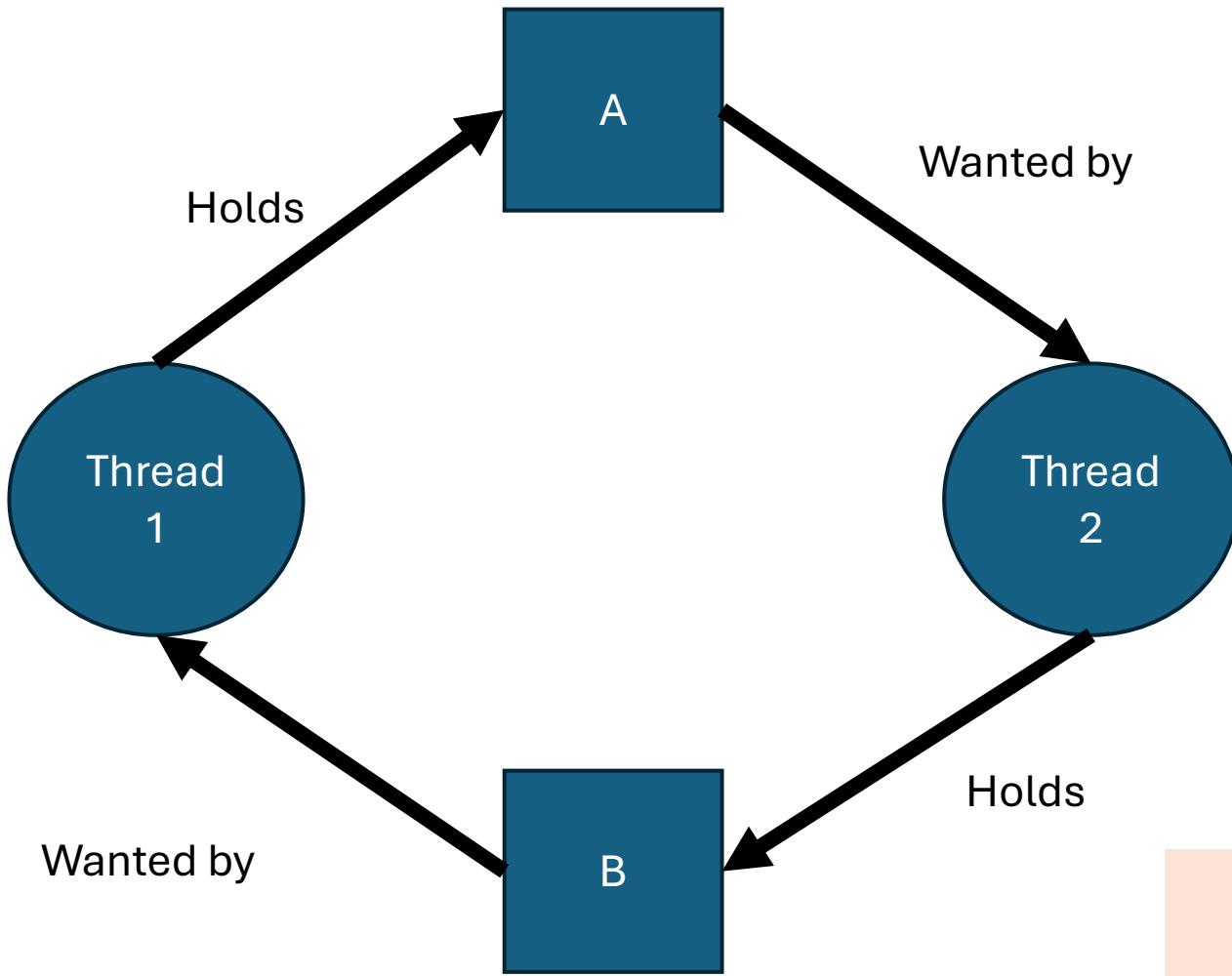
lock(&B)  
lock(&A)



# How to think about this problem?

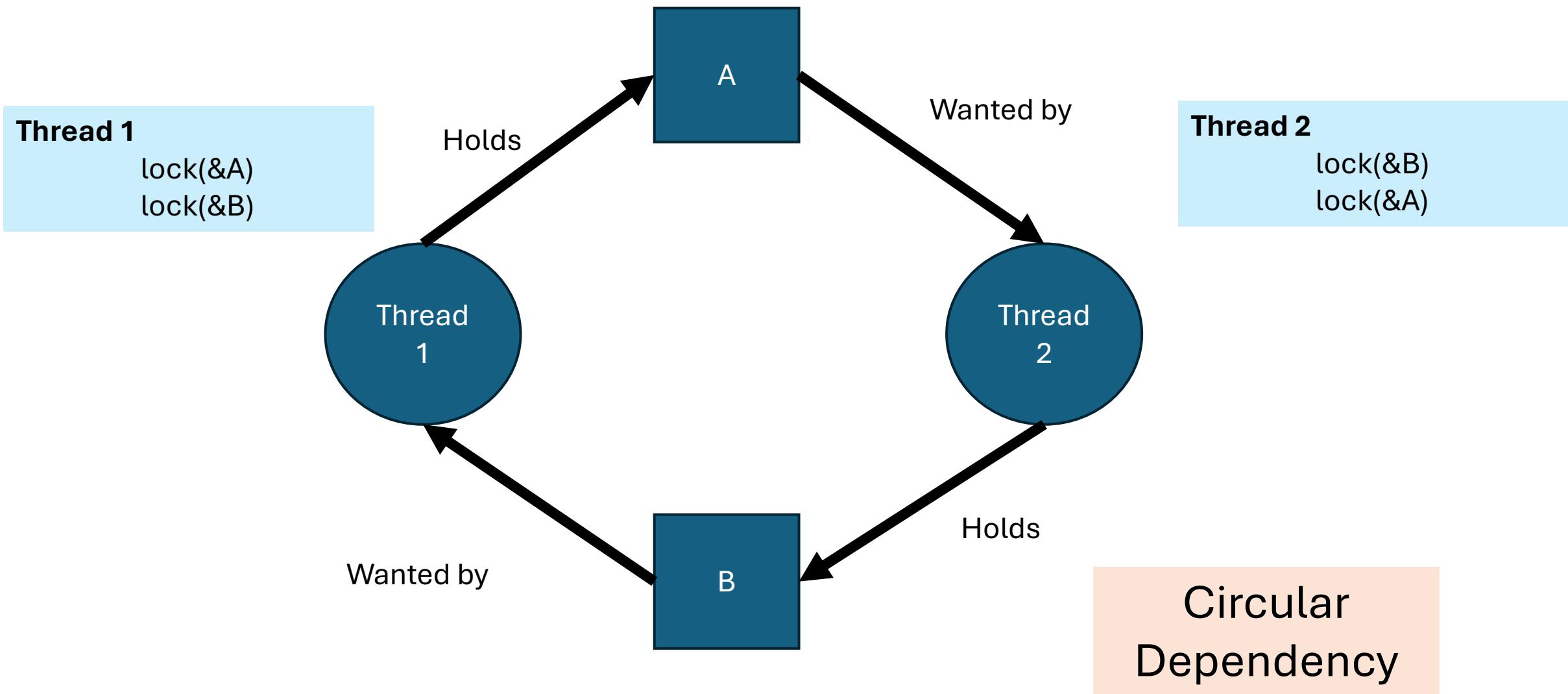


# How to think about this problem?

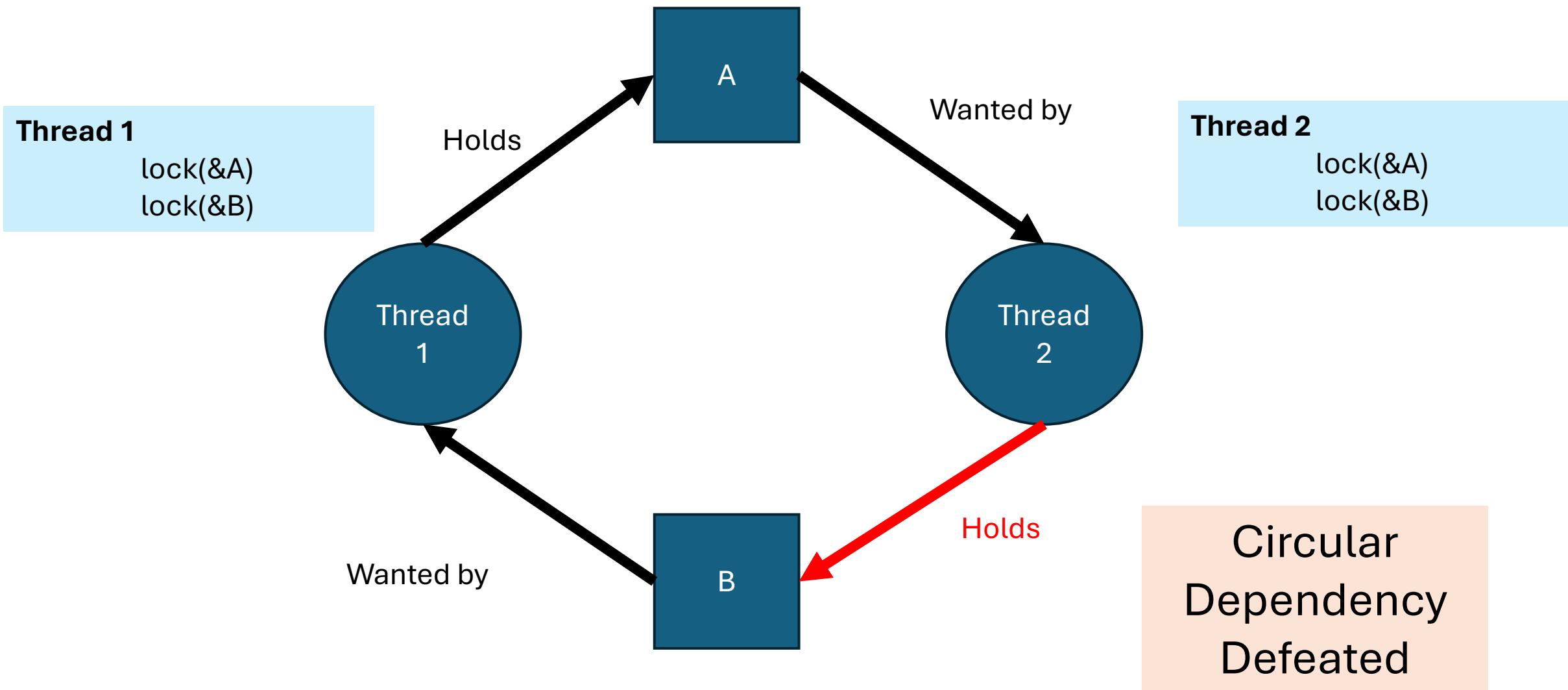


Circular  
Dependency

# How to think about this problem?



# How to think about this problem?



# Set Intersections: Encapsulation gone wrong

```
set_t * set_intersection (set_t * s1, set_t * s2) {  
    set_t *rv = Malloc(sizeof(*rv));  
    mutex_lock(&s1->lock);  
    mutex_lock(&s2->lock);  
    for (int i = 0; i < s1->len; i++) {  
        if (set_contains(s2, s1->items[i])  
            set_add(rv, s1->items[i]);  
    }  
    mutex_unlock(&s2->lock);  
    mutex_unlock(&s1->lock);  
}
```

What is wrong here?

# Are we controlling the lock order?

## Thread 1

```
rv = set_intersection(setA, setB);
```

## Thread 2

```
rv = set_intersection(setB, setA);
```

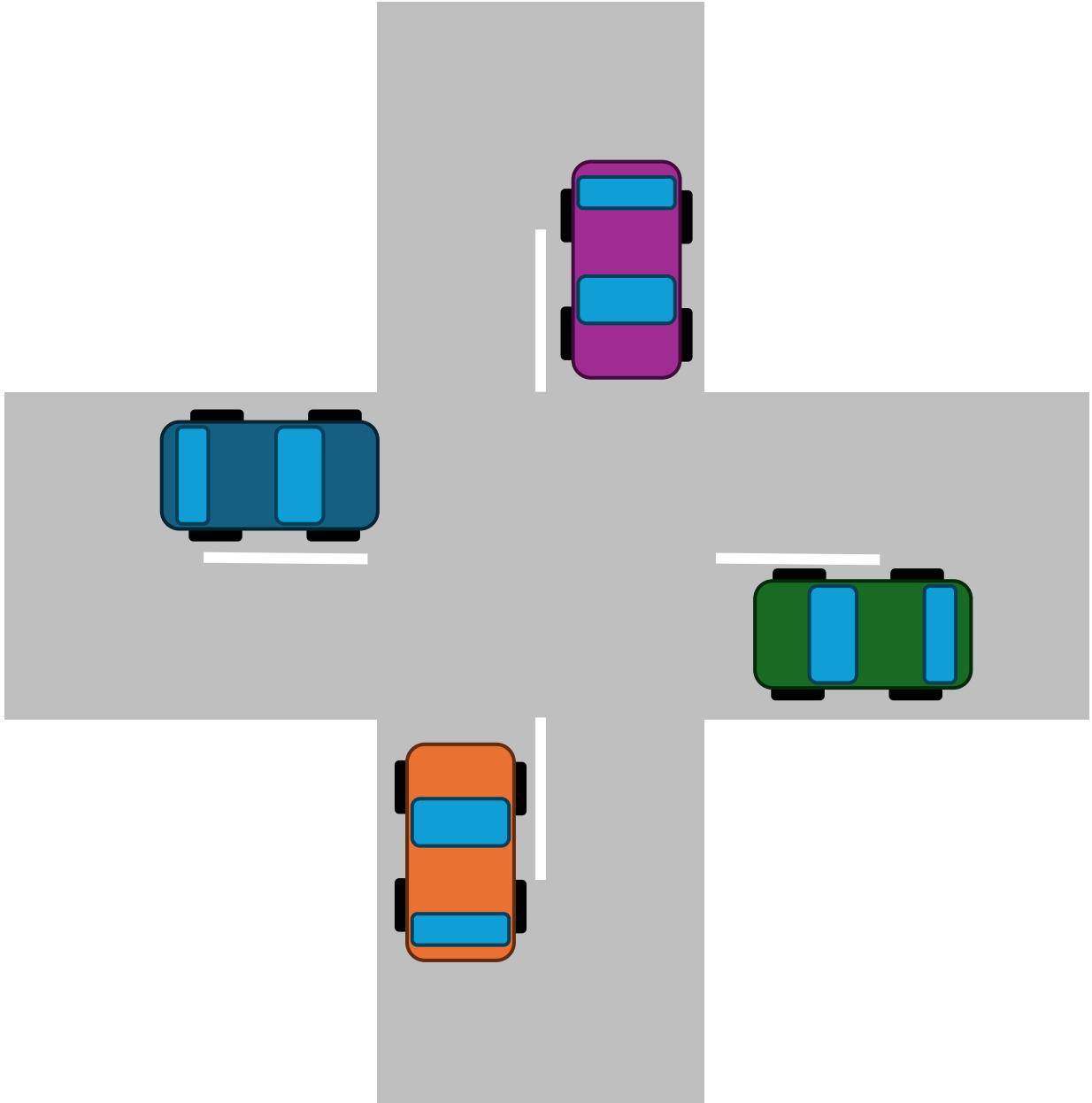
```
if (m1 > m2) {  
    // Grab locks in high-to-low address order  
    pthread_mutex_lock(m1);  
    pthread_mutex_lock(m2);  
} else {  
    pthread_mutex_lock(m2);  
    pthread_mutex_lock(m1);  
}
```

Enforced Ordering

# Deadlock Theory

## Deadlock requires:

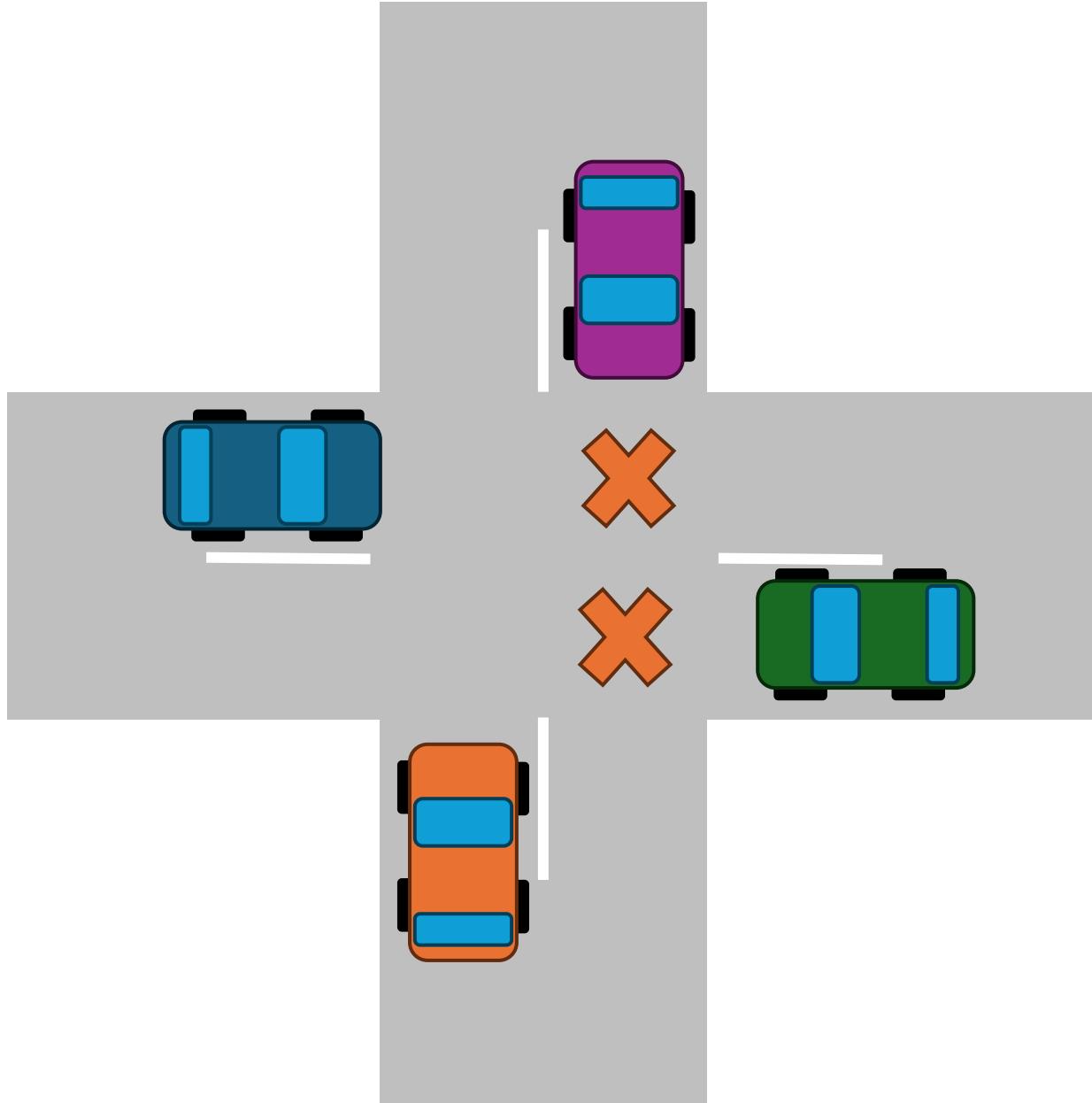
- Mutual Exclusion
- Hold and wait
- No Pre-emption
- Circular wait



# Deadlock Theory

**Deadlock requires:**

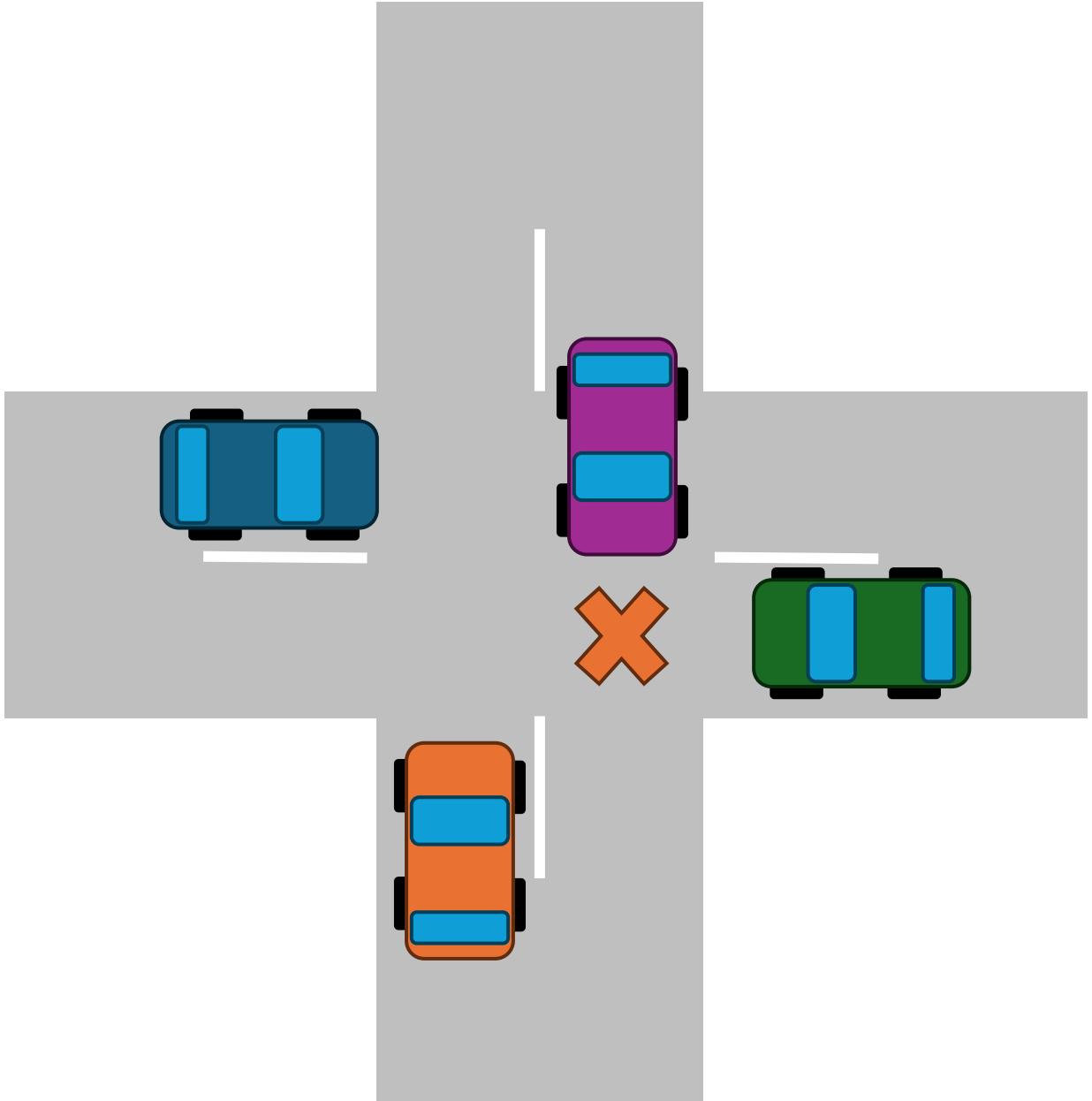
- Mutual Exclusion
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# Deadlock Theory

## Deadlock requires:

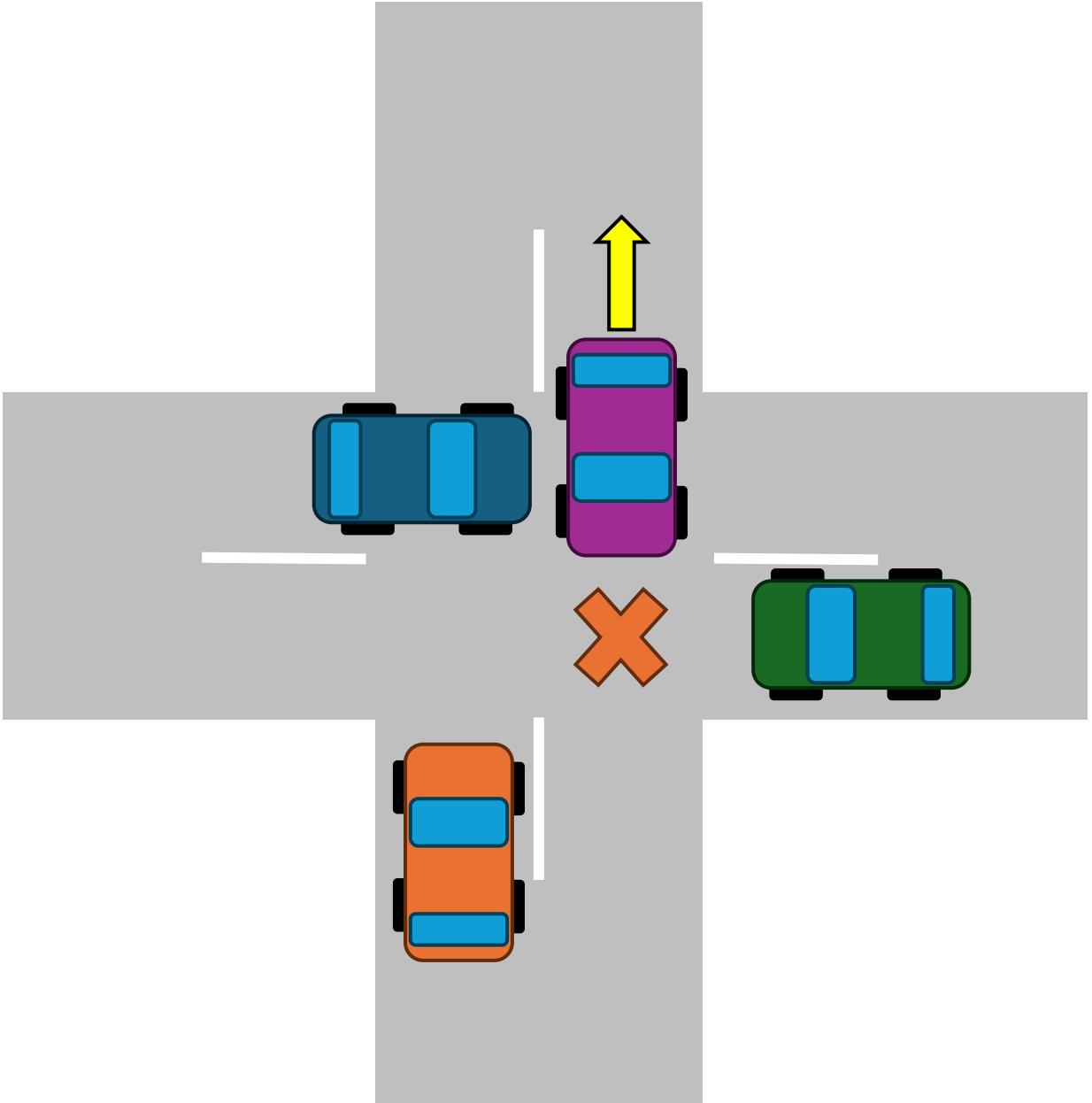
- Mutual Exclusion
- **Hold and wait**
- No Pre-emption
- Circular wait



# Deadlock Theory

## Deadlock requires:

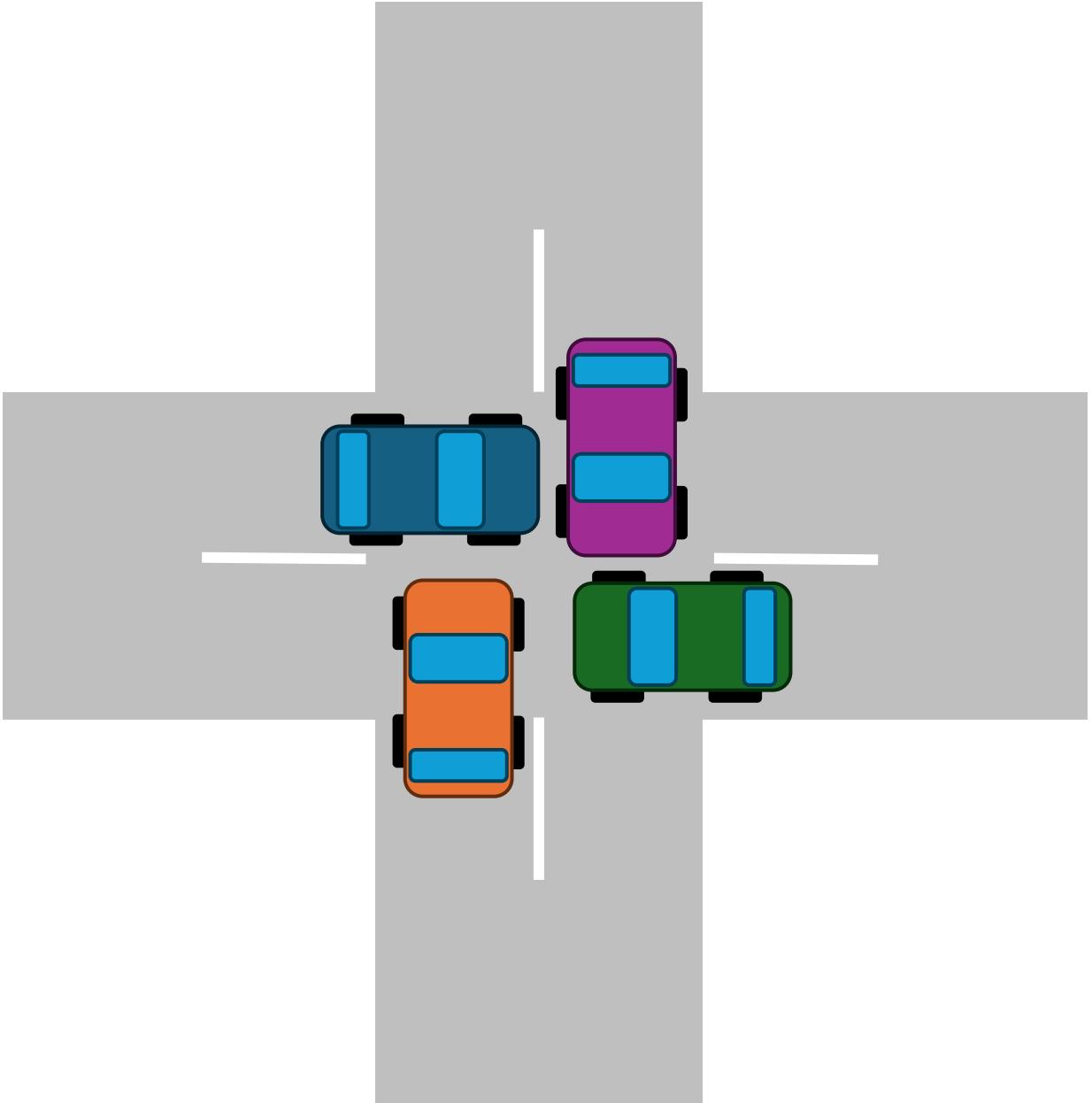
- Mutual Exclusion
- Hold and wait
- **No Pre-emption**
- Circular wait



# Deadlock Theory

## Deadlock requires:

- Mutual Exclusion
- Hold and wait
- No Pre-emption
- **Circular wait**



# Eliminating Mutual Exclusion

**Mutual Exclusion**  
Hold and wait  
No Pre-emption  
Circular wait

Eliminate the lock?

```
void add(int * val, int amt)          void add (int * val, int amt)
{
    mutex_lock(&m);
    *val += amt;
    mutex_unlock(&m);
}

do {
    int old = * value;
} while (!CompAndSwap(val, old, old+amt);
```

Use the primitives and ignore locks entirely!

# Eliminating Mutual Exclusion

**Mutual Exclusion**  
Hold and wait  
No Pre-emption  
Circular wait

Eliminate the lock?

```
void insert(int * val) {  
    node_t * n =  
        malloc(sizeof(*n));  
    n->val = val;  
    lock(&m);  
    n->next = head;  
    head = n;  
    unlock(&m);  
}
```

Linked List

```
void insert(int * val) {  
    node_t * n =  
        malloc(sizeof(*n));  
    n->val = val;  
    do {  
        n->next = head;  
    } while  
        (!CompAndSwap(&head, n->next, n));  
}
```

Use the primitives and ignore locks entirely!

# Eliminate Hold and Wait?

Mutual Exclusion  
**Hold and wait**  
No Pre-emption  
Circular wait

## Meta-Lock

**lock(&meta);**

lock(&a);

lock(&b);

...

**unlock(&meta);**

## Problems?

- Must know which locks are needed, ahead of time
- Must be conservative (acquiring everything)
- How is this different from 1 lock?
- Bottleneck...

# Adding Pre-emption

Mutual Exclusion  
Hold and wait  
**No Pre-emption**  
Circular wait

**Give up!**

**top:**

```
lock(a);  
if (tryLock(b) == -1) {  
    unlock(A);  
    goto top;  
}
```

**Problems?**

- Busy-waiting
- No guarantee of progress

**Livelock:**

- No process makes progress, but the state of involved processes is in flux

# Eliminate Circular Wait

Mutual Exclusion  
Hold and wait  
No Pre-emption  
**Circular wait**

## Solve the problem

- Decide ordering of locks
- Ensure no A->B + B->A etc.
- Document it and write the code

## Advantages

- Works well with systems with distinct layers
- Useful within the OS kernel
- Enforces a strict lock hierarchy

# Banker's Algorithm (Dijkstra)

## Core Idea:

- Before acquiring a resource, will the system be in a ‘safe state’.
  - Safe: Exists one sequence of processes such that all processes can finish with the currently available resources

## What do we need to know?

- Maximum resources needed
  - [MAX]  $n \times m$
- How much do you have
  - [ALLOCATION]  $n \times m$
- How much is available
  - [AVAILABLE]  $m$

# Banker's Algorithm: Example

# Banker's Algorithm: Example

# Banker's Algorithm: Example

	Allocation				Max				Available			
	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0
P <sub>1</sub>	1	0	0	0	1	7	5	0				
P <sub>2</sub>	1	3	5	4	2	3	5	6				
P <sub>3</sub>	0	6	3	2	0	6	5	2				
P <sub>4</sub>	0	0	1	4	0	6	5	6				

# Banker's Algorithm: Example

	Allocation				Max				Available			
	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Are we safe?			
P <sub>2</sub>	1	3	5	4	2	3	5	6				
P <sub>3</sub>	0	6	3	2	0	6	5	2				
P <sub>4</sub>	0	0	1	4	0	6	5	6				

# Banker's Algorithm: Example

	Allocation				Max				Available			
	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Are we safe?			
P <sub>2</sub>	1	3	5	4	2	3	5	6				
P <sub>3</sub>	0	6	3	2	0	6	5	2				
P <sub>4</sub>	0	0	1	4	0	6	5	6				
Tot	3	14	12	12								

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0				
P <sub>1</sub>	1	0	0	0	1	7	5	0								
P <sub>2</sub>	1	3	5	4	2	3	5	6								
P <sub>3</sub>	0	6	3	2	0	6	5	2								
P <sub>4</sub>	0	0	1	4	0	6	5	6								
Tot	3	14	12	12												

MAX  
- ALLOCATION

# Banker's Algorithm: Example

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0					0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6								
P <sub>3</sub>	0	6	3	2	0	6	5	2								
P <sub>4</sub>	0	0	1	4	0	6	5	6								
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0					0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6								
P <sub>3</sub>	0	6	3	2	0	6	5	2								
P <sub>4</sub>	0	0	1	4	0	6	5	6								
Tot	3	14	12	12												

# Banker's Algorithm: Example

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Can we using available satisfy need?				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Can we using available satisfy need?				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Yes!				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	Can we using available satisfy need?				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	No				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	No				0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												

# Banker's Algorithm: Example

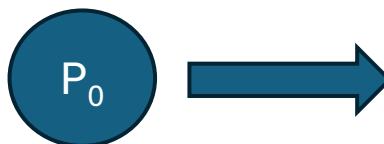
	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0					0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	<b>3</b>	<b>14</b>	<b>12</b>	<b>12</b>												

P<sub>0</sub>

P<sub>3</sub>

# Banker's Algorithm: Example

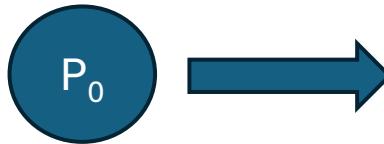
	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0					0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



0	0	1	2	1	5	3	2
---	---	---	---	---	---	---	---

# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	<b>3</b>	<b>14</b>	<b>12</b>	<b>12</b>												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6					1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	<b>3</b>	<b>14</b>	<b>12</b>	<b>12</b>												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2					0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	<b>3</b>	<b>14</b>	<b>12</b>	<b>12</b>												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	<b>3</b>	<b>14</b>	<b>12</b>	<b>12</b>												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					0	6	4	2
Tot	3	14	12	12												



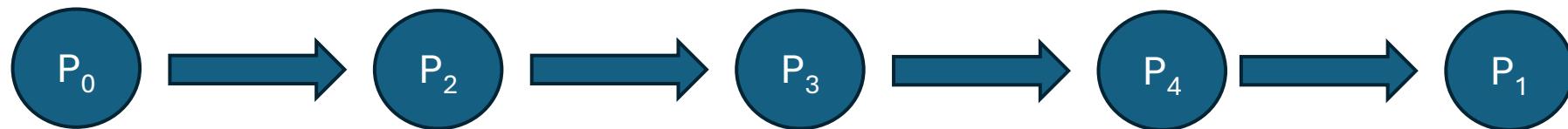
# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6	2	14	12	12	0	6	4	2
Tot	3	14	12	12												



# Banker's Algorithm: Example

	Allocation				Max				Available				Need			
	A	B	C	D	A	B	C	D	A	B	C	D	A	B	C	D
P <sub>0</sub>	0	0	1	2	0	0	1	2	1	5	2	0	0	0	0	0
P <sub>1</sub>	1	0	0	0	1	7	5	0	1	5	3	2	0	7	5	0
P <sub>2</sub>	1	3	5	4	2	3	5	6	2	8	8	6	1	0	0	2
P <sub>3</sub>	0	6	3	2	0	6	5	2	2	14	11	8	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6	2	14	12	12	0	6	4	2
Tot	3	14	12	12					3	14	12	12				



# Banker's Algorithm: Summary

## Summary

1. Set processes not ready.
2. Find processes needs!       $\text{NEED} = (\text{MAX} - \text{ALLOCATION})$
3. Find runnable processes!     $\text{NEED} \leq \text{AVAILABLE}?$
4. Run runnable processes!     $\text{AVAILABLE} += \text{ALLOCATION}_i$
5. Repeat from #3

Also known as the... duh algorithm?

# Summary

- Semaphores
- Deadlock
- Livelock
- Banker's Algorithm

# Questions?

