

# Collective Robotics

## Part 3: Scenarios

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# A collection of common swarm-robotic behaviors

implementation ideas by example

aggregation, dispersion, clustering & sorting,  
cooperative construction, cooperative transport,  
cooperative manipulation, flocking, foraging

for an overview see Brambilla et al. (2013)

# Aggregation – biological inspiration



# Aggregation – overview

Task: robots position themselves close to each other by aggregating in one spot

⇒ minimization of distances between robots

position of aggregation spot can be unspecified

⇒ robot swarm self-organizes to find a consensus position  
(cf. decision making)

position of aggregation spot can be specified

(e.g., brightest/warmest spot)

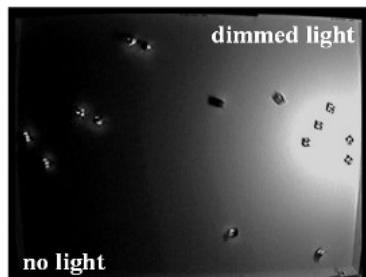
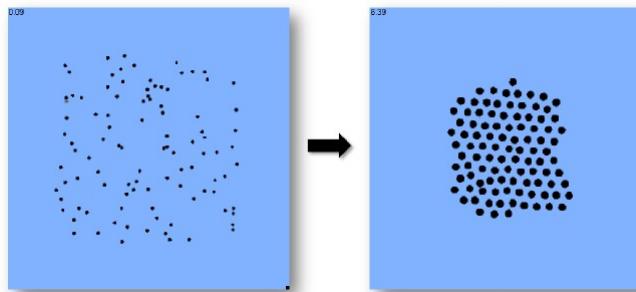
⇒ each robot has to find that position and stop there

examples of biological systems:

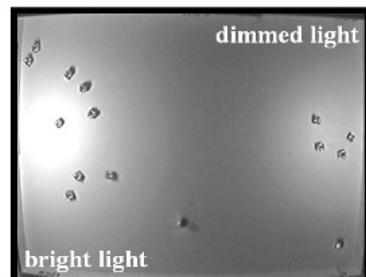
honey bees, ladybugs, nest site selection in ants



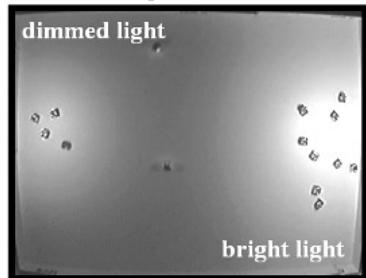
# Aggregation – aggregation with/without specified position



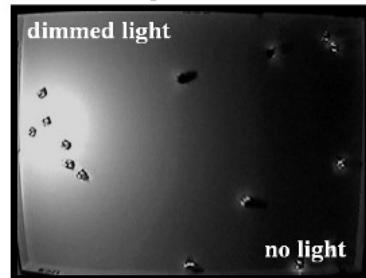
phase 1



phase 2



phase 3



phase 4

top left: aggregated ladybugs  
left: aggregation with specified position of  
aggregation spot (BEECLUST algorithm)

# Aggregation – global vs local information

global task: minimization of distances between robots

local task: position yourself close to as many robots as possible

simple case if GPS & global communication are available:

agree on spot and go there

with local knowledge only:

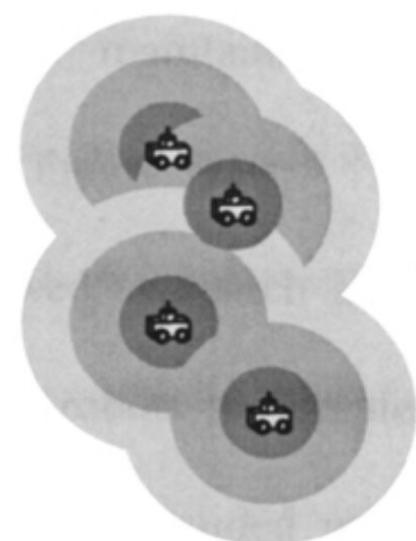
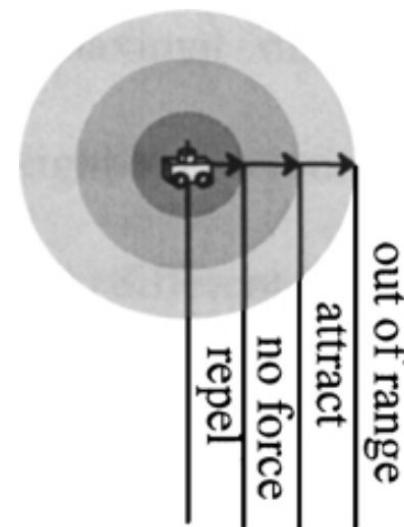
go to next neighbor? what if there is no one?

⇒ will be discussed later in detail

# Aggregation – simple approach using potential fields

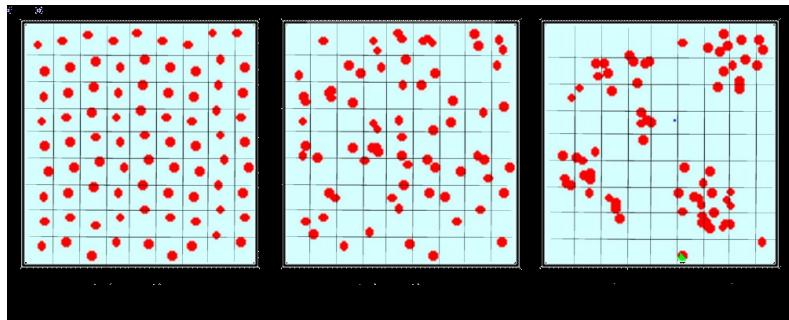
example: a potential field method to implement aggregation  
if neighbor is. . .

- too close then assign repelling force
- about at the right distance then do nothing
- too far away then assign attracting force
- out of range then is no reaction possible

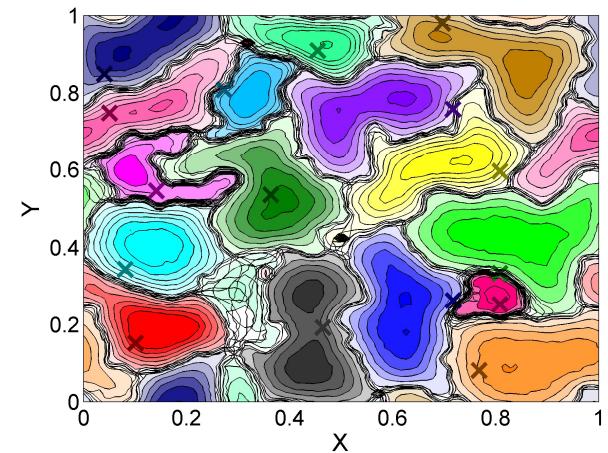


# Dispersion – overview

Task: robots position themselves as far as possible from each other while staying in contact  
⇒ maximization of distances between robots  
examples of biological systems: territory selection

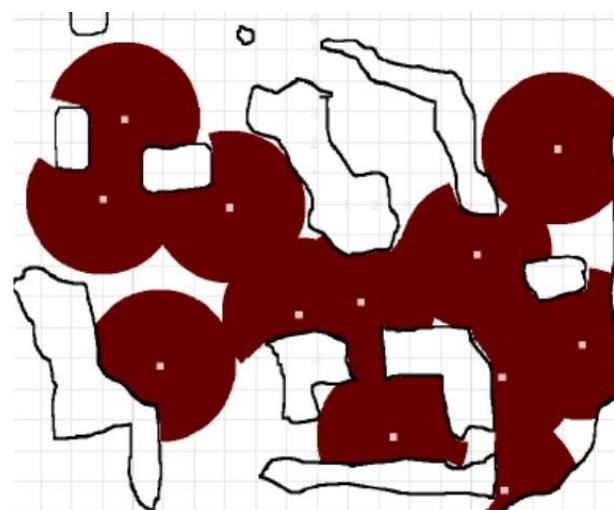
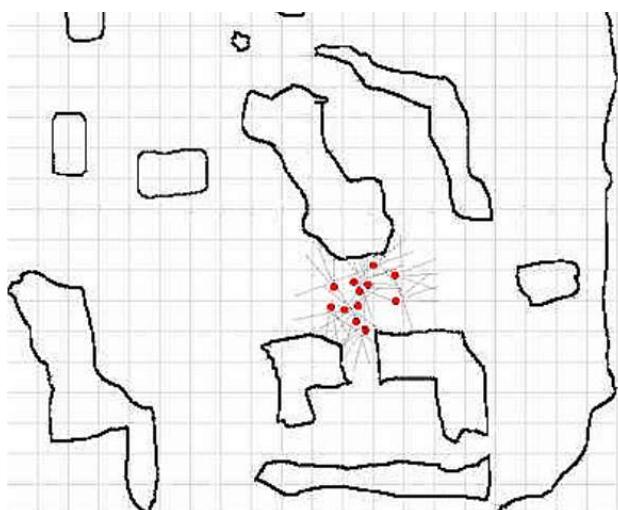


types of dispersion: uniform, random, clustered



## Dispersion (2/3)

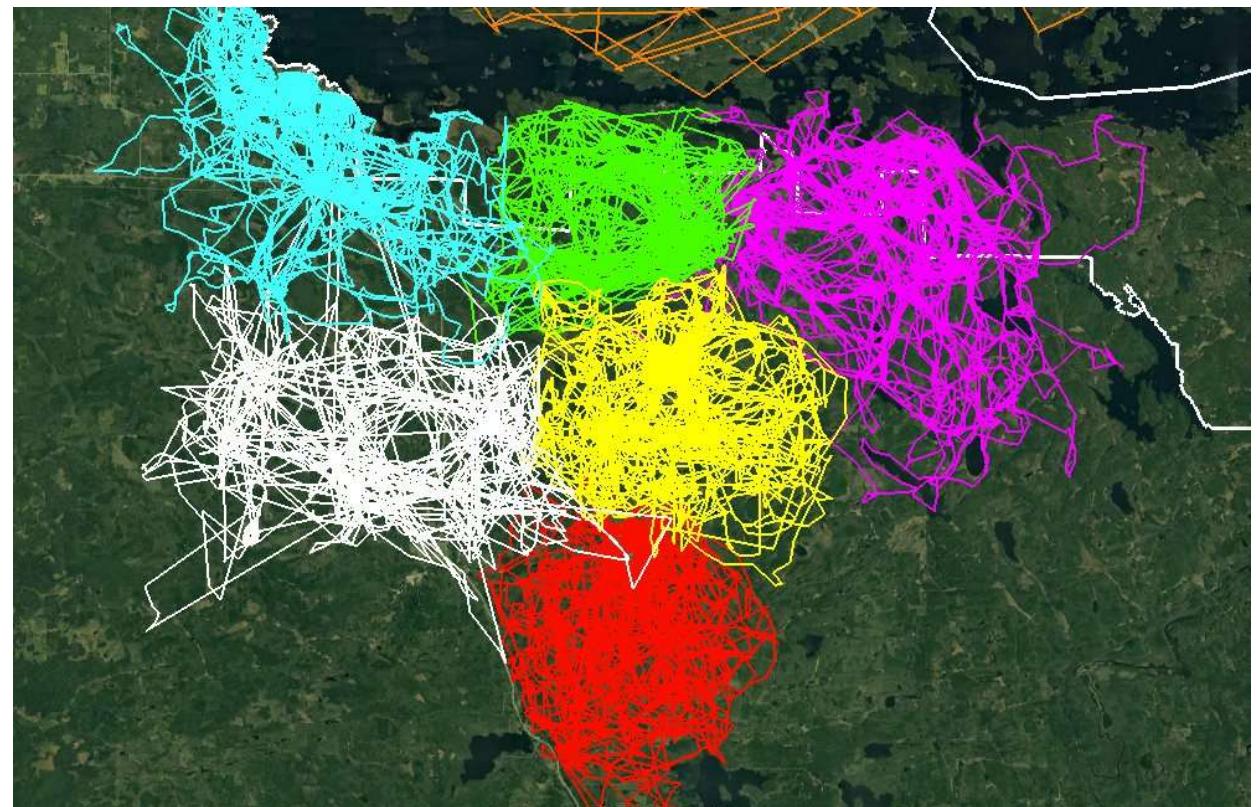
allelopathy: production of toxins that keep others from establishing nearby in plants and microorganisms



dispersion of robot swarm using wireless intensity signals  
(Luke Ludwig , Maria Gini, 2006)

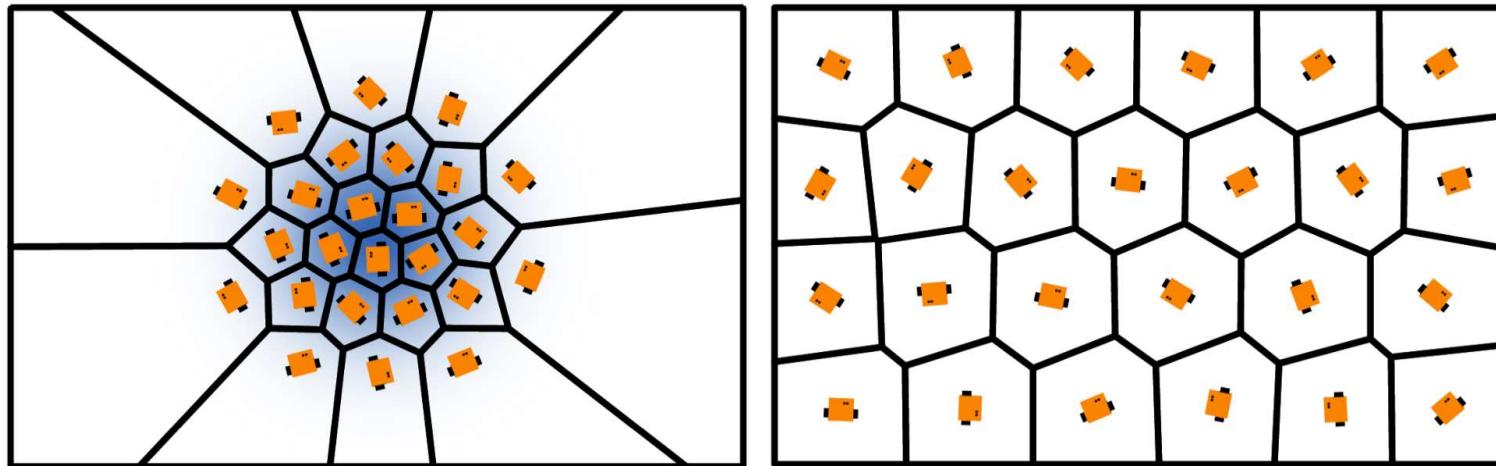
# Dispersion (3/3)

“6 wolves from different adjacent packs move around their territories at the same time (based on GPS-collar locations)”



source: <https://www.voyageurswolfproject.org/>

# Dispersion – with equal shares of resource



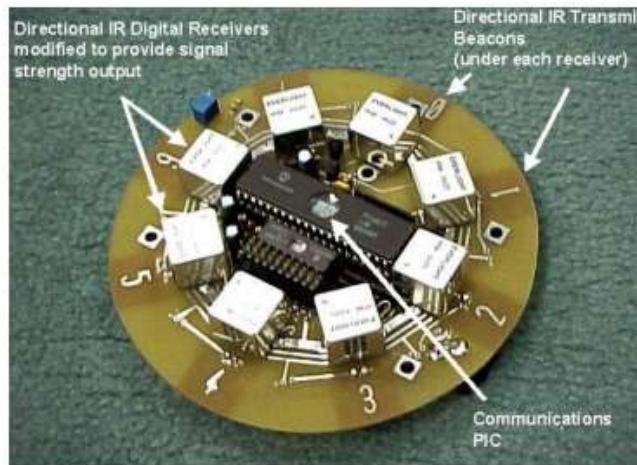
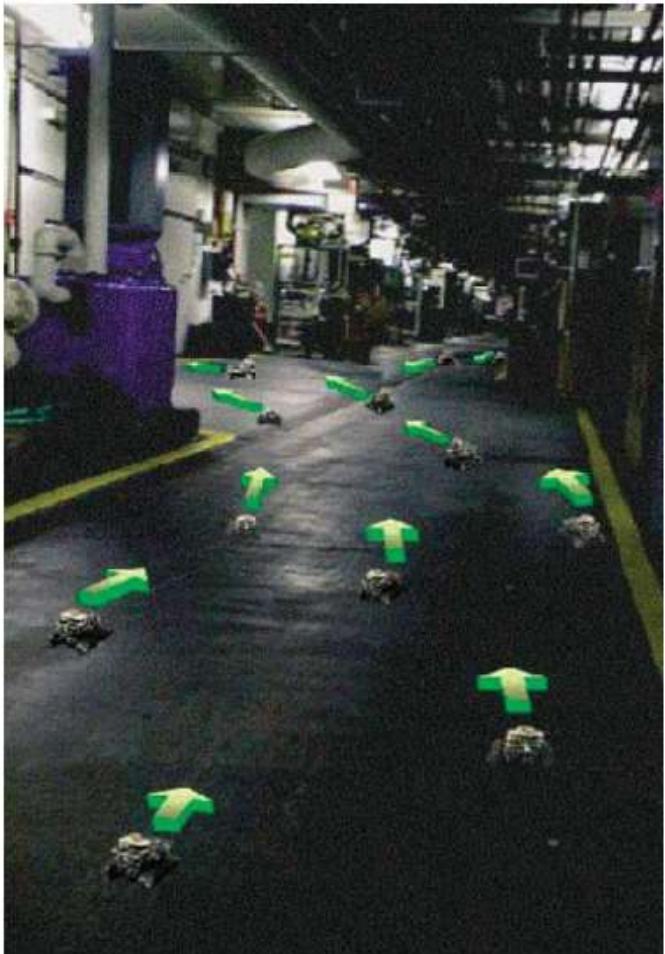
Centroidal Voronoi tessellation

left: in a gradient (spatially centered Gaussian density function) such that each Voronoi cell contains the same amount

right: uniformly distributed resources across the domain

(Egerstedt, Robot Ecology, 2021)

# Dispersion – Pheromone Robotics (1/2)



broadcast of optical signals (virtual pheromones)

used information:

- signal intensity

- hop count

- direction

(Payton et al., 2001)

# Dispersion – Pheromone Robotics (2/2)

virtual pheromones are . . .

- broadcasted optical signals
- not faithful copies of chemical pheromones
- transmitted at a known intensity

a received signal indicates . . .

- existence of line of sight
- viable path toward source of signal
- signal identity
- hop count
- estimated distances on the basis of signal strength

received signals are tagged with direction and intensity

# Clustering and sorting of objects – biological example

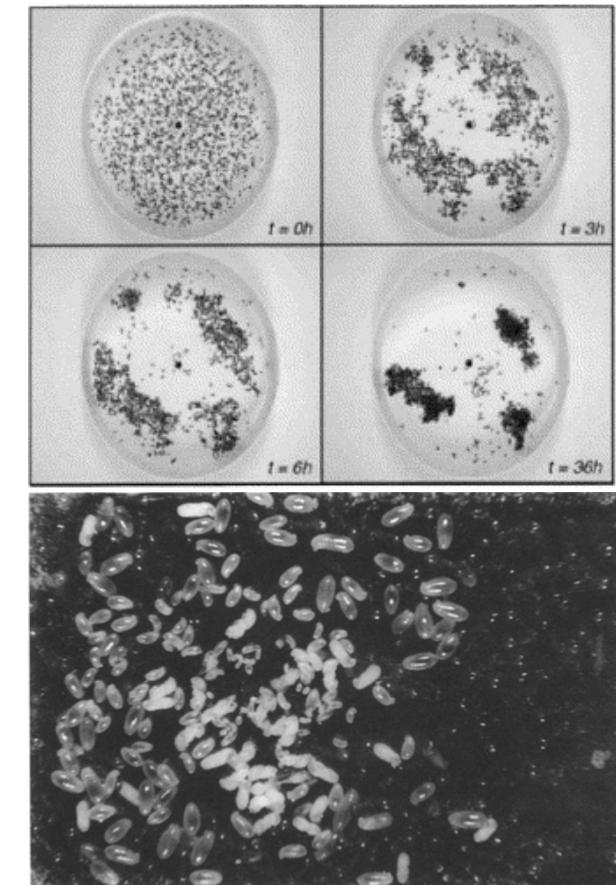
Task: robots position objects close to each other by clustering them in one spot  $\Rightarrow$  minimization of distances between objects

ants cluster . . .

. . . corpses of dead ants

. . . sand pellets to form a circular wall that protects the colony

. . . eggs of similar maturation



# Clustering and sorting of objects – behavioral model

simple behavioral model of clustering:

- the probability, that an ant picks up an object, is inversely proportional to the number of objects it has experienced within a short time window (memory required)
- consequently the probability of picking up isolated objects is high
- removing objects from a cluster is unlikely
- the probability that an ant deposits an object is directly proportional to the number of perceived objects within a short time window

sorting may be explained by adding different response probabilities for different types of objects in the environment

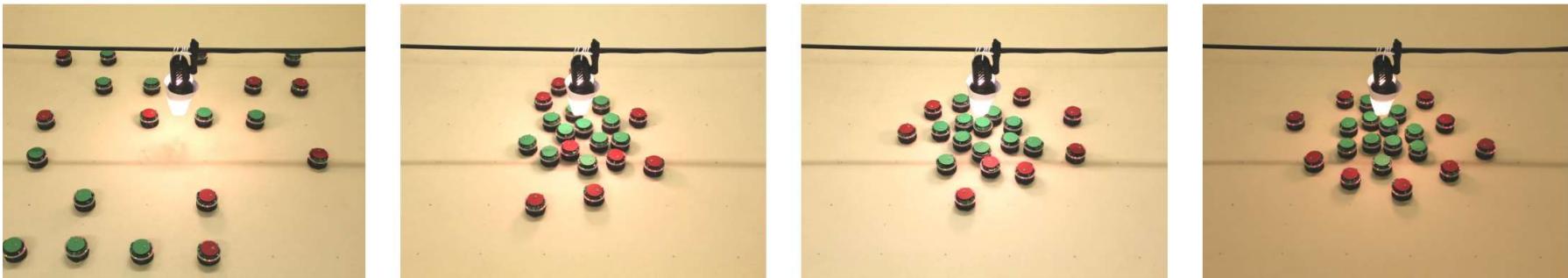
Floreano and Mattiussi (2008)

## Clustering and sorting of objects – Brazil nut effect (1/2)



The Brazil nut effect as inspiration for robot segregation, Chen et al. (2012)

## Clustering and sorting of objects – Brazil nut effect (2/2)



consider 2 groups of robots:

robots of **group 1** represented disks of radius  $r_1 = 8$  cm,

robots of **group 2** represented disks of radius  $r_2 = 8b$  cm, with  $b \in \{1, 2, 3, 4, 5\}$

for  $b > 1$ : **group-1** robots (small nuts) basically ignore **group-2** robots (big nuts)  $\Rightarrow$  sorting effect

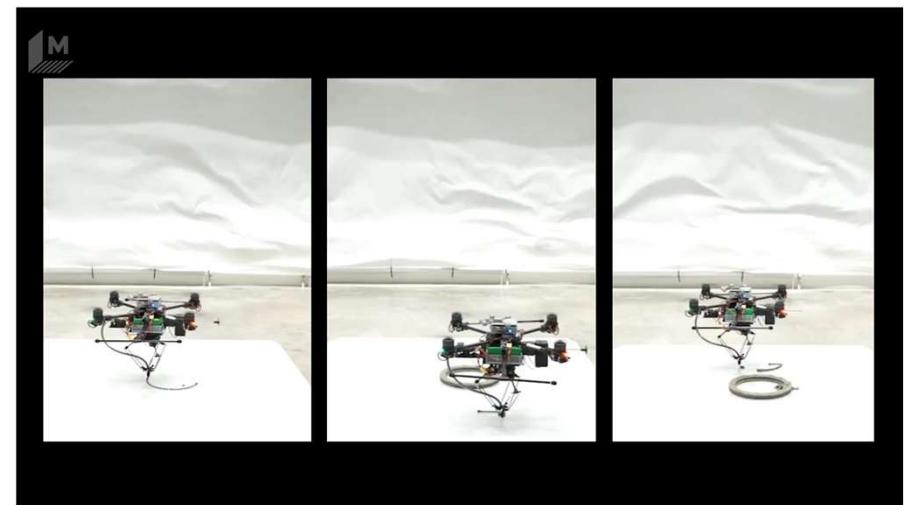
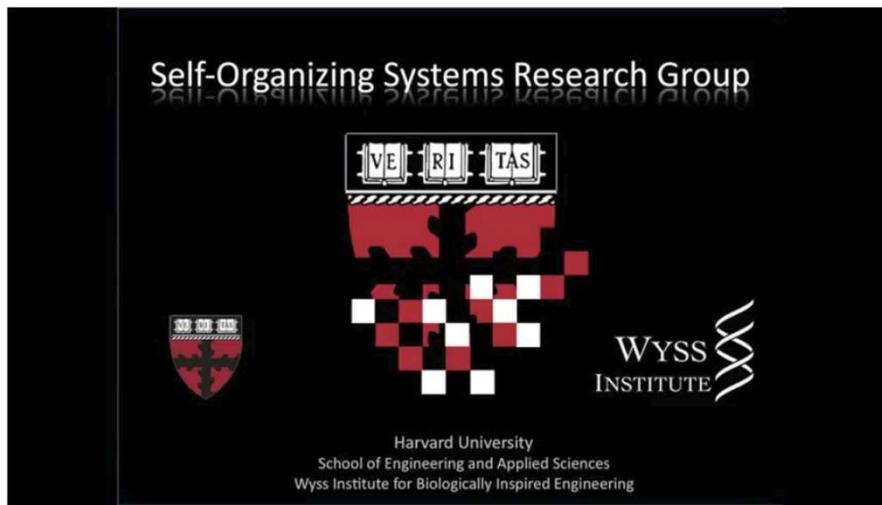
Chen et al. (2012)

# Recap

- What did you note from last time as what did you learn?
- What did you note from last lecture as challenging?

# Cooperative construction (1/3)

Task: robots repeatedly position building blocks at appropriate positions to construct a particular architecture  
example from biology: nest construction in wasps and termites



## Cooperative construction (2/3)

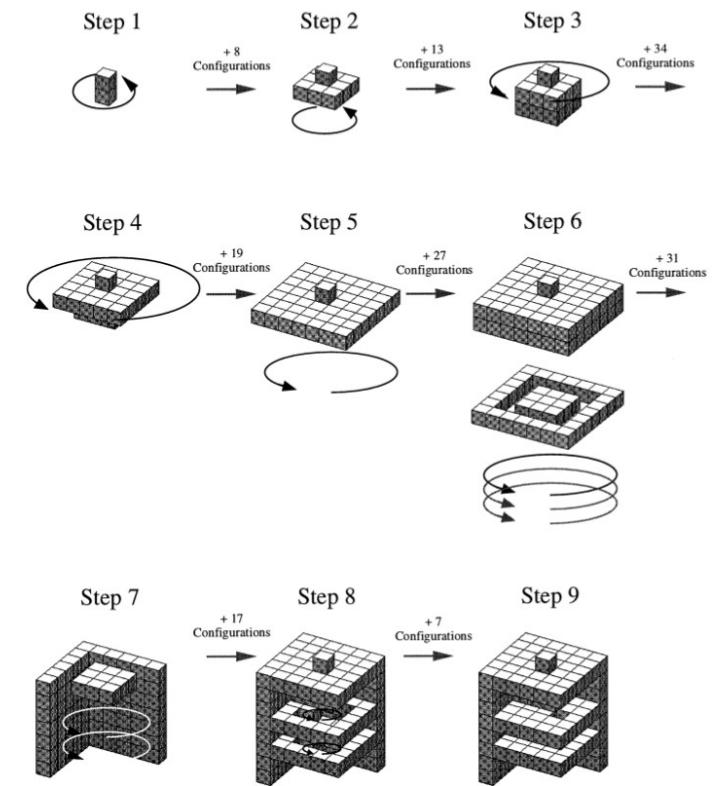
The architectural complexities exceed the perceptual and cognitive abilities of single individuals. Coordination between builders adds complexity.

Suggested models rely on stigmergic communication, specific construction behaviors are believed to be encoded genetically as stimulus–response associations.

Theraulaz and Bonabeau (1995); Floreano and Mattiussi (2008)

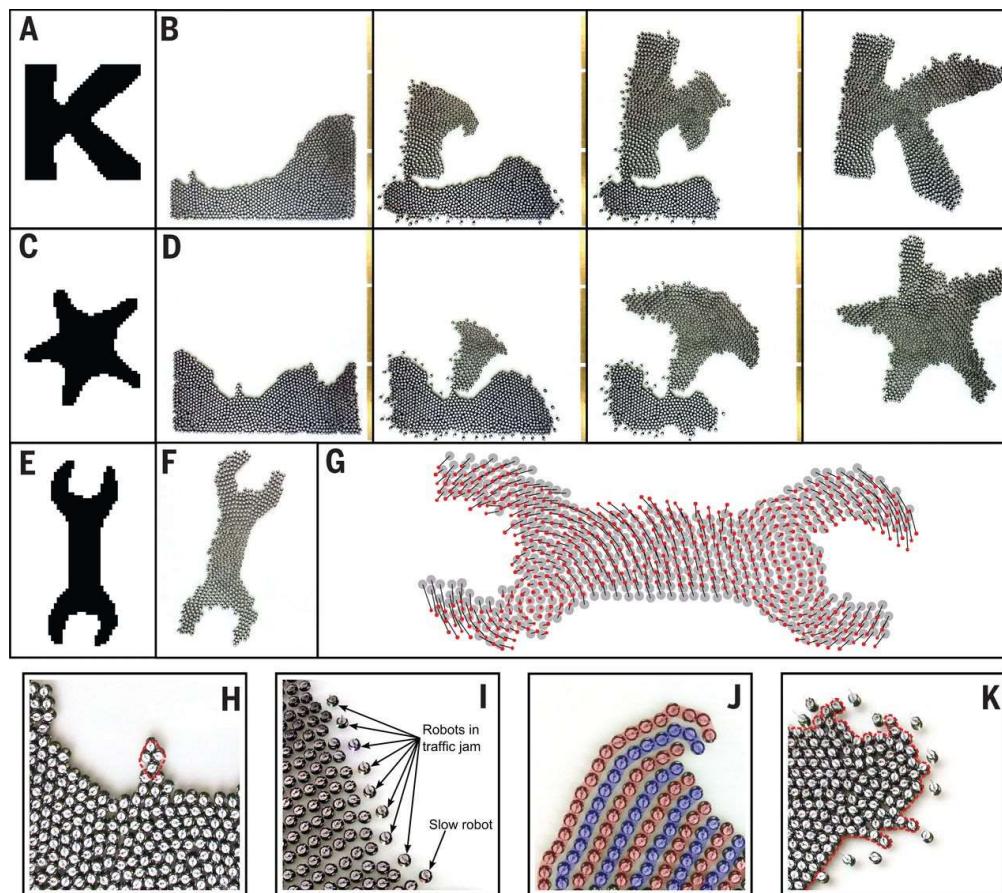
# Cooperative construction (3/3)

A model by Theraulaz and Bonabeau operates like a cellular automaton; a local perception of the current construction site defines the next construction step.



Theraulaz and Bonabeau (1995)

# Self-assembly



Emulation of self-assembly with Kilobots by Rubenstein et al. (2014)

1024 Kilobots

**task:** position robots to form predefined shapes (A, C, E)

four seed robots as anchor (H) to form a gradient as coordinate system, robots move along edge of aggregation in a line

**challenge 1:** error propagation using the gradient approach

**challenge 2:** time overhead as waiting times scale linearly with the swarm size ( $O(N)$ )

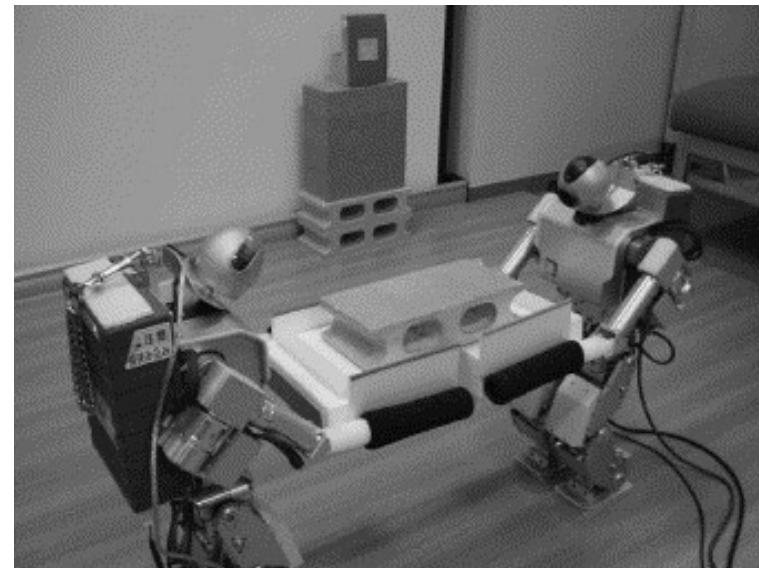
option: self-organized disassembly

# Cooperative transport (1/2)

Task: robots cooperate in moving a heavy payload

subtasks: aggregation, synchronization, collective motion

example from biology: ants



# Cooperative transport (2/2)



[aparat.com/she9erd](http://aparat.com/she9erd)

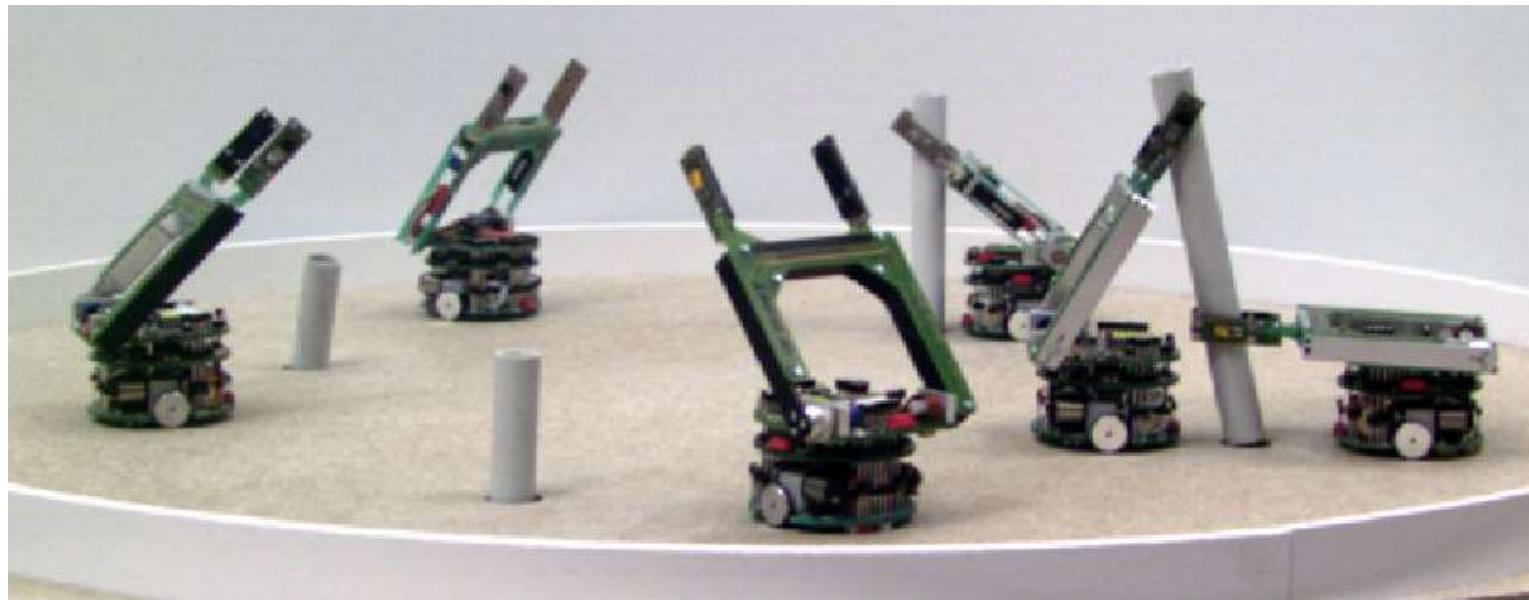
## Cooperative Grasping and Transport Using Multiple Quadrotors

Daniel Mellinger, Michael Shomin, Nathan Michael, Vijay Kumar  
GRASP Lab, University of Pennsylvania

# Cooperative manipulation (1/3)

Desert ants cooperate to pull out of the ground long sticks (too long for a single ant). This behavior can be reproduced with a group of robots as study case.

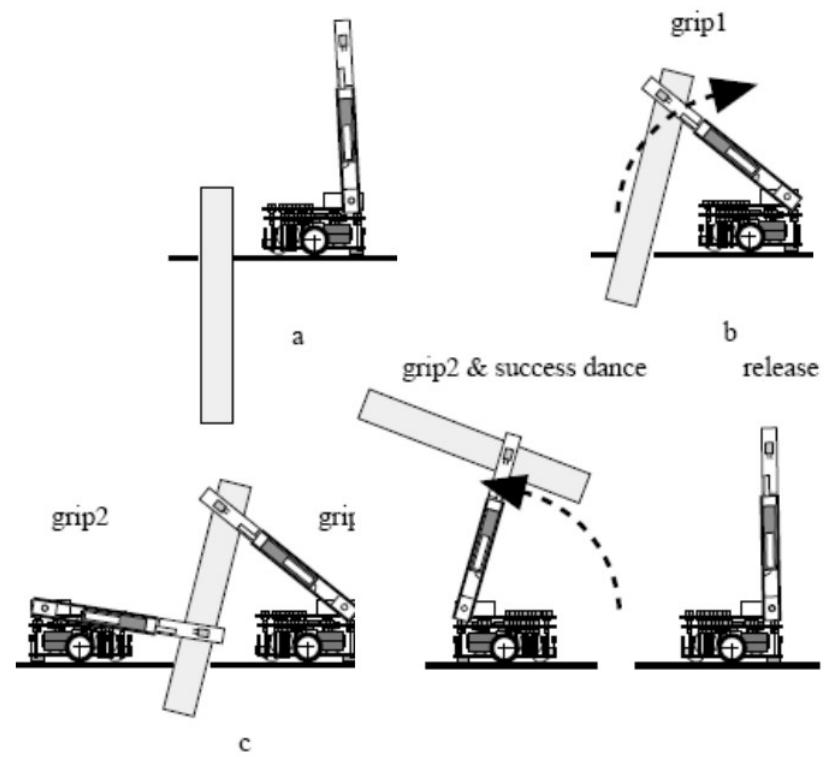
optimization problem: How long to wait for a teammate?



# Cooperative manip. (2/3): gripping & waiting

waiting too long: deadlocks

waiting too short: many unfinished grips



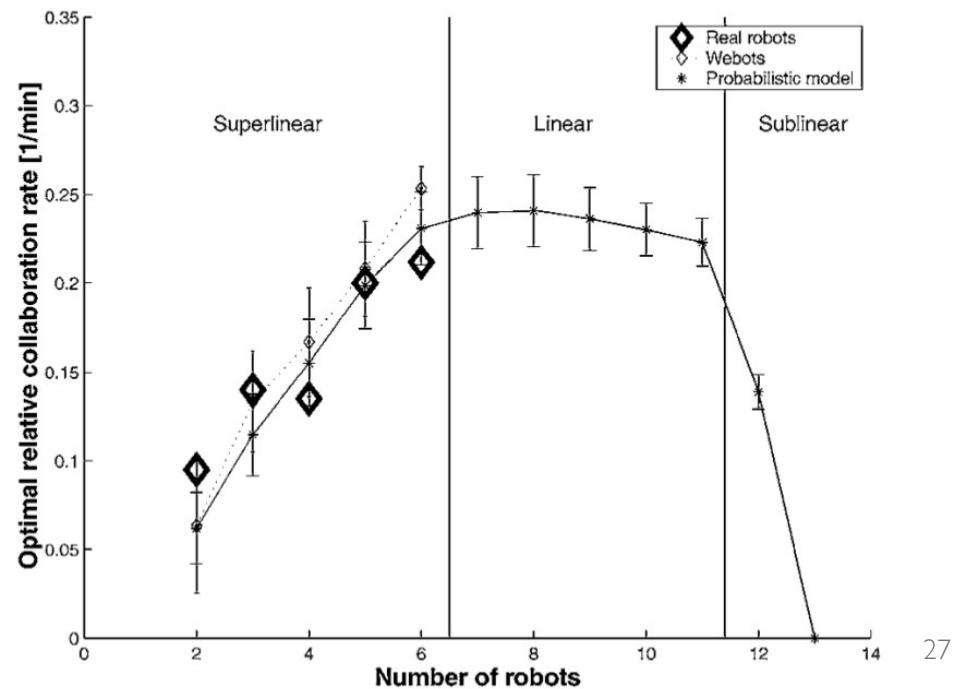
# Cooperative manip. (3/3): super-linear performance

relative collaboration rate per robot

⇒ the number of a robot's collaborations over time

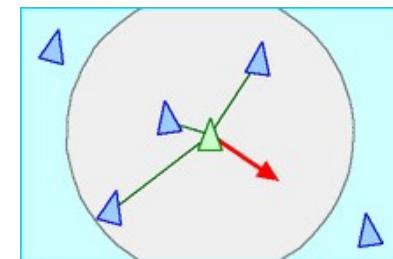
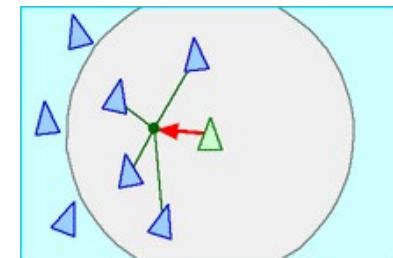
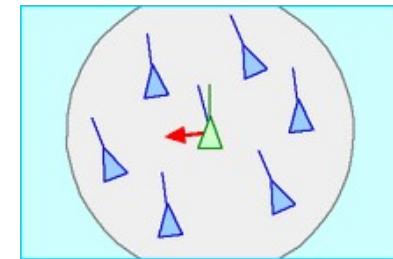
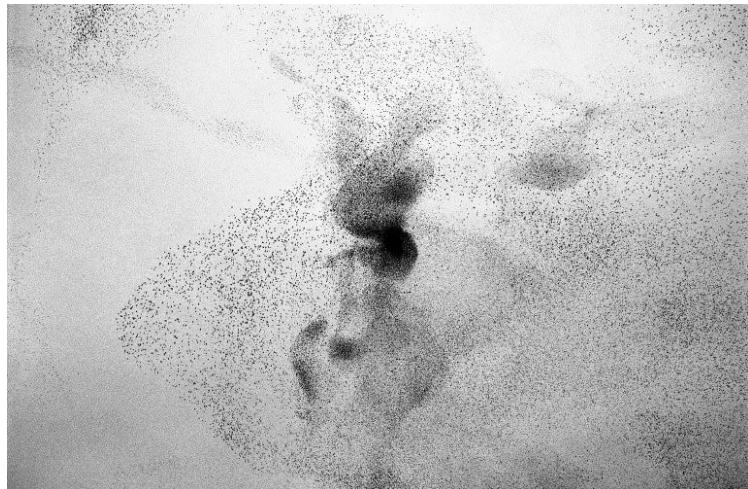
with 4 robots about  
3 times more collaborations per  
robot than with 2 robots;  
summed over the whole swarm  
about 6 times more  
collaborations

(Ijspeert et al., 2001)

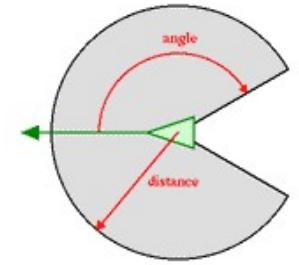


# Flocking / shoaling / herding (1/4)

Task: stay together, move in the same direction, avoid collisions  
examples from biology: starlings, herring, buffalos



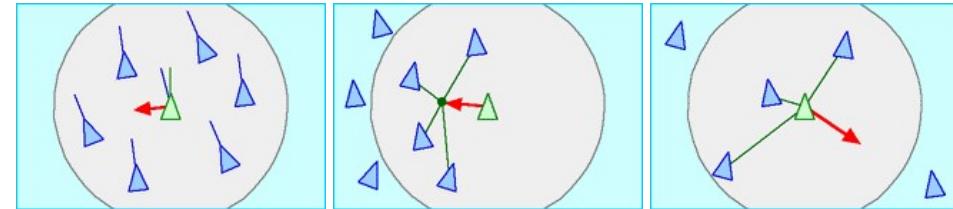
# Flocking / shoaling / herding (2/4)



generation of flocking behavior by  
3 simple rules:

- alignment: adapt direction to that of neighbors
- cohesion: stay close to neighbors
- separation: if too close increase distance to avoid collisions

+ ignoring flockmates in the back



COURSE: 07  
COURSE ORGANIZER: DEMETRI TERZOPoulos

"BOIDS DEMOS"  
CRAIG REYNOLDS  
SILICON STUDIOS, MS 3L-980  
2011 NORTH SHORELINE BLVD.  
MOUNTAIN VIEW, CA 94039-7311

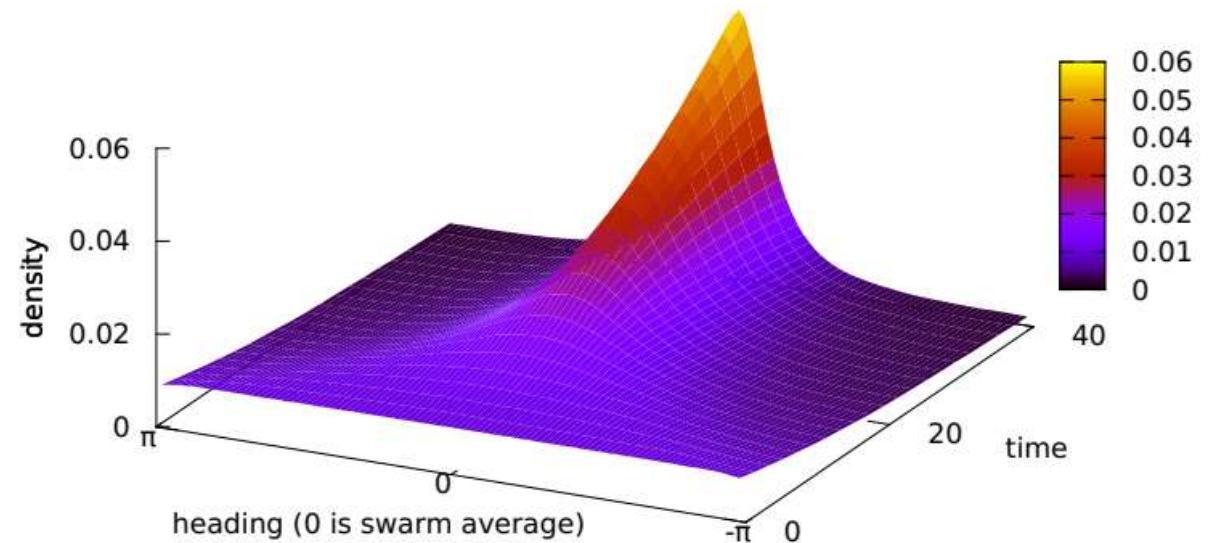
Reynolds (1987)

recent results: in natural systems dependence on network topology instead of distance (Ballerini et al., 2008)

# Flocking / shoaling / herding (3/4)

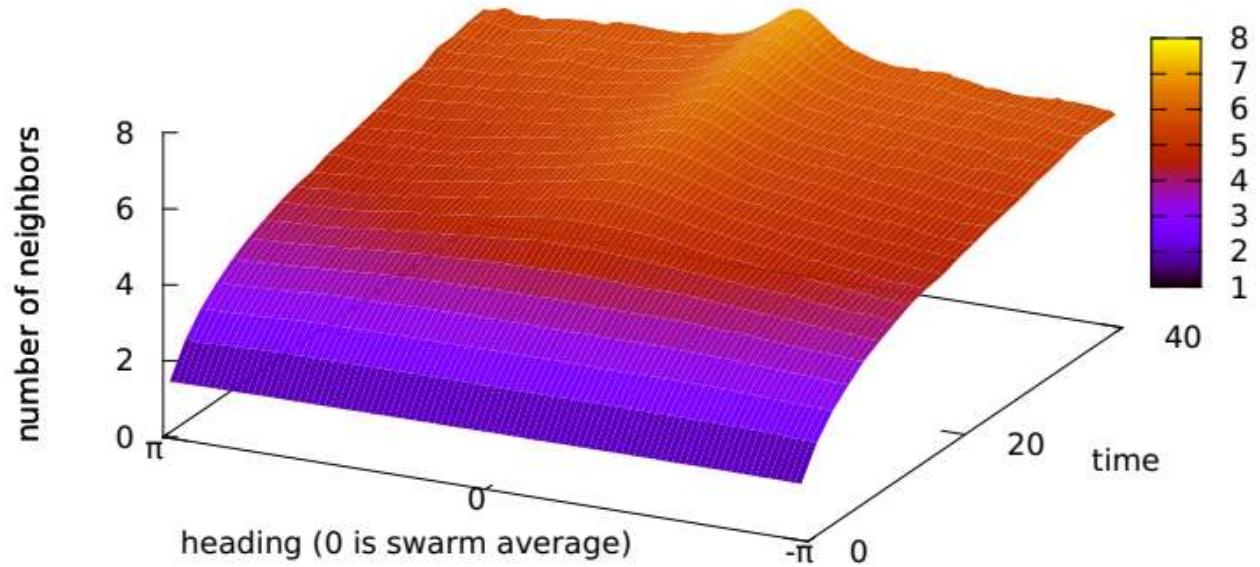
example measurements in a simulation of flocking (part 1):  
distribution of agent headings over time  
relative to the average heading over all headings of the swarm

→ Effective aggregation



# Flocking / shoaling / herding (4/4)

example measurements in a simulation of flocking (part 2):  
number of neighbors per agent over time  
relative to the average heading over all headings of the swarm



→ Effective aggregation

# Foraging

task:

collect items,

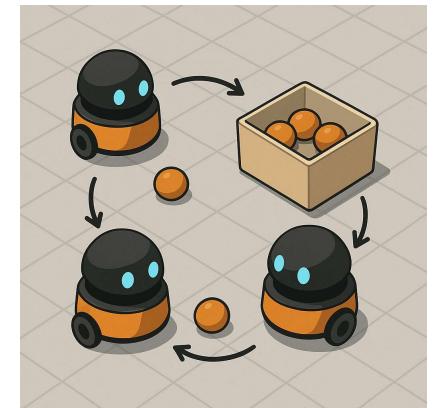
find food source (any target area), exploit it (e.g., establish trail)



subtasks:

exploration, navigation, recruitment, (collective) transport

biological examples: ants, wasps (building material)



# Foraging – overview

Exploration: random walk or special strategy, e.g., when to explore, risk management etc.

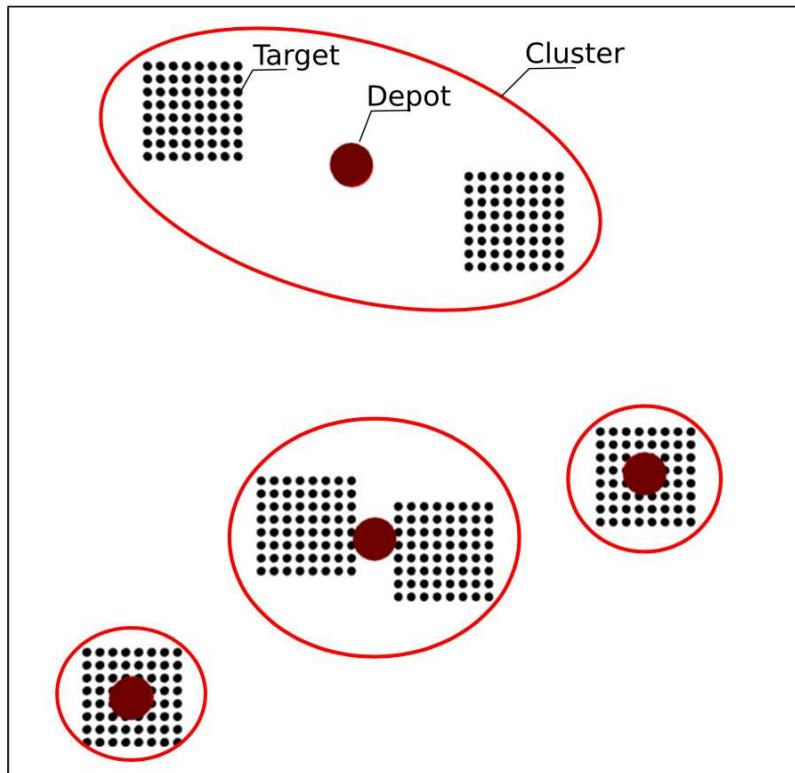
Navigation: GPS(?), light beacon, pheromones, landmarks, etc.

Recruitment: attract other robots to rich food sources (e.g., social cues)

(Collective) transport strategy: pushing only, grasping, caging (forming a closure with robots to trap the object)

according to survey paper by Tuci et al. (2018)

# Foraging – multiple (dynamic) depots



**Central place foraging:** does not scale as more and more robots will try to enter the 'nest'

**Multiple place foraging:** more depots are added with increasing swarm size

**Multiple place foraging with dynamic depots:** depots can be strategically placed offline before runtime and/or depots can move at runtime

(Lu et al., 2018)

# Foraging – example recruitment by social cue



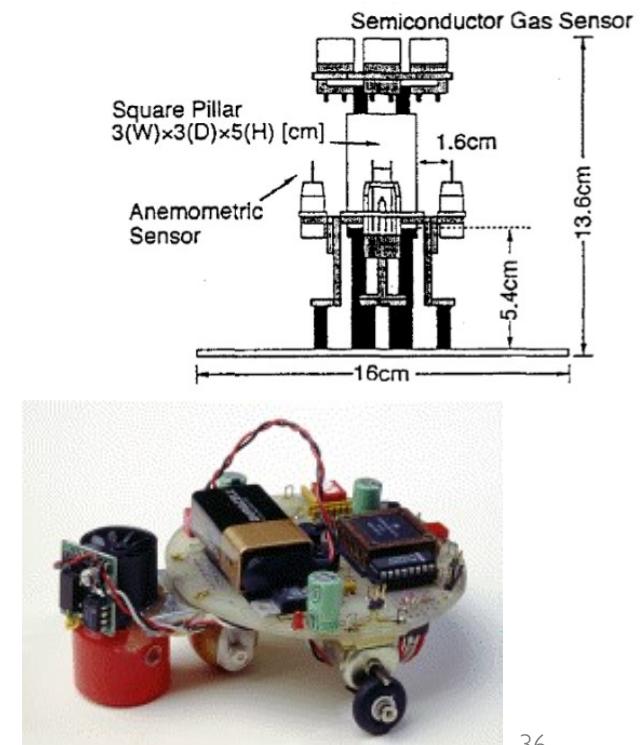
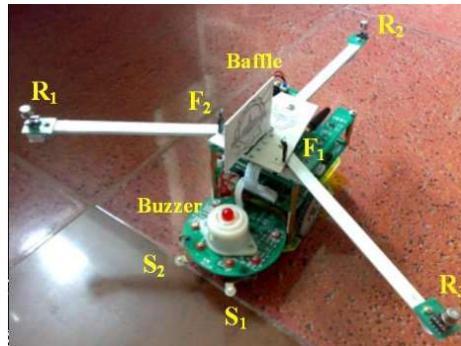
Minecraft and ‘fireworks’ as (honest) social signal/cue of foraging  
(project with Ralf Kurvers and Paweł Romanczuk, SClol Berlin)

# Foraging – stigmergy in robotics

idea to implement stigmergy: real liquids/gases instead of virtual pheromones

→ massive technical challenges with pheromones

chemical sensing is difficult  
due to limits in sensors and  
complex dynamics  
of air flow (e.g., turbulences)



# Foraging – robots form paths

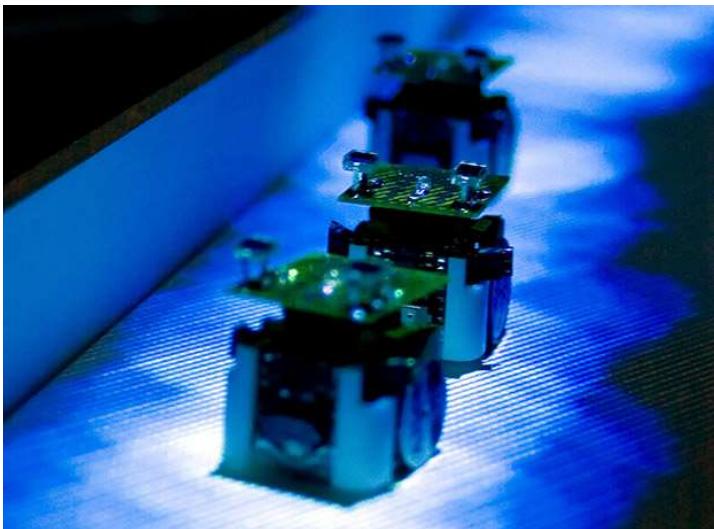
instead of pheromones: robots mark path by forming a chain



# Foraging – emulating pheromones (1/3)

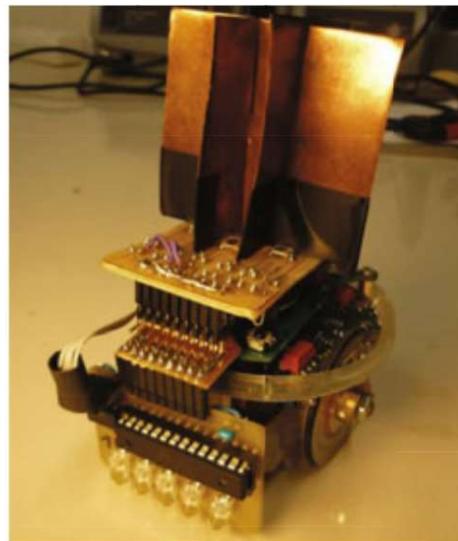
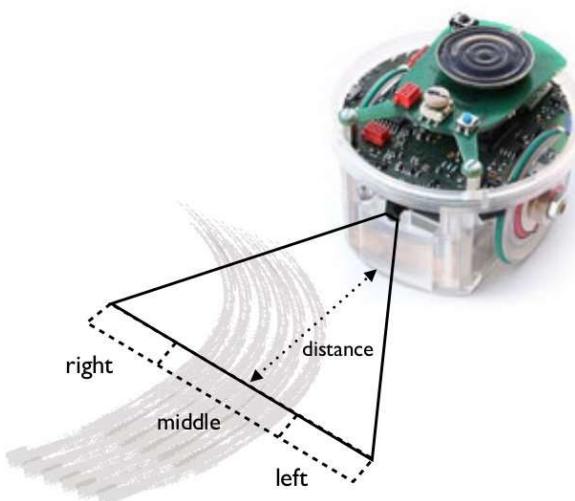
Optical simulation of pheromones, option 1: projection

video projector simulates pheromone trails with differences in brightness,  
robots are tracked and signal pheromone deposit with LED (tracking is a  
central element!)



# Foraging – emulating pheromones (2/3)

optical simulation of pheromones, option 2: ultraviolet light + glow paint (phosphorescence)



## Foraging – emulating pheromones (3/3)



<https://www.youtube.com/watch?v=i3ht90lX9XY>

# Division of labor and task partitioning

division of labor: work is organized, not everyone is doing the same tasks, and consequently the work needs to be usefully distributed among the workers

task partitioning is the problem of defining smaller pieces of work (tasks)

# Task allocation

Task allocation is the problem of assigning tasks to the robots, hopefully in an efficient way.

If the task allocation is dynamic, then a strategy for task switching is required:

- (a) monitor current supply & demand,
- (b) determine if task switch would be efficient,
- and (c) if so, do it.

# Classroom Activity

Materials:

- A large sheet (physical or virtual whiteboard) representing the environment.
- Colored dots or markers representing tasks (each with a type or difficulty level).
- Tokens representing robots (can be done via cards, coins, or software like Google Jamboard/Miro for online).
- Optional: Timer and score sheet.

Instructions:

- Each group simulates a team of robots operating in an environment with multiple scattered tasks.

Define Task Environment (Instructor provides)

- Eg., 15 tasks of different types (red = high priority, green = low priority).
- 5 robots per team, each with a unique ability (e.g., speed, task type compatibility).
- Design a Task Allocation Method

Each group must:

- Choose or invent a task allocation mechanism (e.g., market-based, threshold-based, auction, role assignment, first-come-first-served, stigmergy).
- Write down how tasks will be assigned, resolved, and re-allocated in case of failure or conflict.

Groups report:

- chosen method
- How it performed under simulated conditions
- Strengths, weaknesses, and potential improvements

Discussion Points (Instructor-led):

- Which methods scaled better with more tasks/robots?
- How did groups balance fairness, efficiency, and robustness?
- What mechanisms supported reallocation under failure?
- How do these strategies relate to biological systems?

# Multi-robot task allocation – taxonomy

## Single-task robots (ST) vs. multi-task robots (MT)

ST: each robot is capable of executing at most one task at a time

MT: some robots can execute multiple tasks simultaneously

## single-robot tasks (SR) vs. multi-robot tasks (MR)

SR: each task requires exactly one robot to achieve it

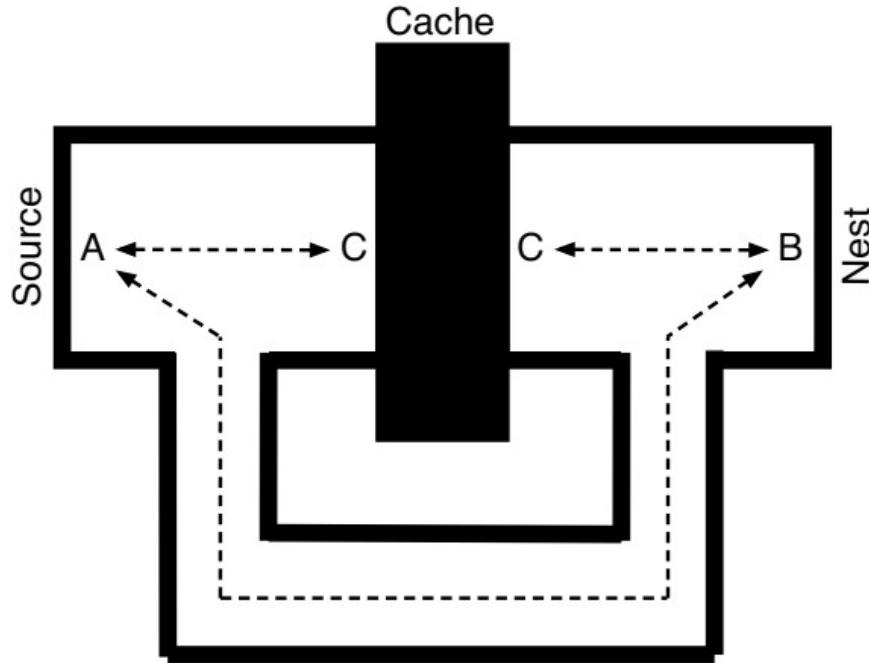
MR: some tasks can require multiple robots

## instantaneous assignment (IA) vs. time-extended assignment (TA)

IA: instantaneous allocation of tasks to robots, with no planning for future allocations

TA: information is available, such as the set of all tasks that will need to be assigned, or a model of how tasks are expected to arrive over time

# Task alloc. as multi-armed bandit problem (1/2)



Pini et al. (2012): a robot can decide against task partitioning and transport objects from A to B directly, or a robot can decide to go for task partitioning and transport objects only from A to C or from C to B; when to do what?

# Task alloc. as multi-armed bandit problem (2/2)

## Multi-Armed Bandit (MAB) for Task Selection

- K levers, each with unknown reward distribution  $R_i$
- Goal: Choose which lever to play
- Challenge: Exploration–Exploitation tradeoff

## Robot Task Allocation

- Each robot selects between Task B and Task C
- Measures cost  $\hat{t}_j$ : estimated time to complete task  $j \in \{B, C\}$

## Decision Rule (UCB1 Policy)

**Go to B if:**

$$\hat{t}_B - \gamma \sqrt{\frac{2 \ln(n_B + n_C)}{n_B}} < \hat{t}_C - \gamma \sqrt{\frac{2 \ln(n_B + n_C)}{n_C}}$$

$n_B$  num. of times went to B,  $n_C$  num. of times went to C

$\gamma$  to tune degree of exploration



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