

Assignment-4

Implementation of Trapezoidal Fuzzy Sets

import matplotlib.pyplot as plt

import numpy as np

1. Class to represent a point

class Point:

def __init__(self, x, y):

self.x = x

self.y = y

def __str__(self):

return f"({self.x}, {self.y})"

2. Class to represent a 2D straight line

class Line:

def __init__(self, p1, p2):

self.p1 = p1

self.p2 = p2

def slope(self):

if self.p2.x - self.p1.x == 0:

return float('inf')

return (self.p2.y - self.p1.y) / (self.p2.x - self.p1.x)

def y_for_x(self, x):

m = self.slope()

if m == float('inf'):

return None

return self.p1.y + m * (x - self.p1.x)

3. Function to display a straight line

def display_line(line, label=""):

x = np.linspace(min(line.p1.x, line.p2.x), max(line.p1.x, line.p2.x), 100)

y = [line.y_for_x(xi) for xi in x]

plt.plot(x, y, label=label)

4. Class to represent a fuzzy set

class Fuzzy_set:

```
def __init__(self, left_bottom, left_top, right_top, right_bottom):
    self.left_bottom = Point(*left_bottom)
    self.left_top = Point(*left_top)
    self.right_top = Point(*right_top)
    self.right_bottom = Point(*right_bottom)
```

5. Function to display the fuzzy set

```
def display(self, label=""):
    x = [self.left_bottom.x, self.left_top.x, self.right_top.x, self.right_bottom.x]
    y = [self.left_bottom.y, self.left_top.y, self.right_top.y, self.right_bottom.y]
    plt.plot(x, y, label=label)
    plt.fill(x, y, alpha=0.3)
```

6. Function to return the complement of the fuzzy set

```
def complement(self):
    return Fuzzy_set(
        (self.left_bottom.x, 1 - self.left_bottom.y),
        (self.left_top.x, 1 - self.left_top.y),
        (self.right_top.x, 1 - self.right_top.y),
        (self.right_bottom.x, 1 - self.right_bottom.y)
    )
```

7. Function to calculate the membership of a point in the fuzzy set

```
def membership(self, x):
    if x < self.left_bottom.x or x > self.right_bottom.x:
        return 0

    if self.left_top.x <= x <= self.right_top.x:
        return 1

    if x < self.left_top.x:
        left_line = Line(self.left_bottom, self.left_top)
        return left_line.y_for_x(x)

    right_line = Line(self.right_top, self.right_bottom)
    return right_line.y_for_x(x)
```

```
def main():
```

```
    # 3. Display two lines
```

```
    line1 = Line(Point(0, 4), Point(4, 0))
```

```
    line2 = Line(Point(0, 0), Point(4, 4))
```

```
    plt.figure(figsize=(10, 5))
```

```
    plt.subplot(1, 2, 1)
```

```
    display_line(line1, "Line 1")
```

```
    display_line(line2, "Line 2")
```

```
    plt.grid(True)
```

```
    plt.legend()
```

```
    plt.title("Two Lines")
```

```
    # 6. Create and display fuzzy set
```

```
    fs = Fuzzy_set((20, 0), (40, 1), (50, 1), (70, 0))
```

```
    fsc = fs.complement()
```

```
    plt.subplot(1, 2, 2)
```

```
    fs.display("Original Set")
```

```
    fsc.display("Complement Set")
```

```
    plt.grid(True)
```

```
    plt.legend()
```

```
    plt.title("Fuzzy Set and its Complement")
```

```
    plt.tight_layout()
```

```
    plt.show()
```

```
    # 8. Calculate memberships
```

```
    test_points = [20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70]
```

```
    print("\nMembership values:")
```

```
    print("Point\tOriginal\tComplement")
```

```
    print("-" * 40)
```

```
    for x in test_points:
```

```
        orig = fs.membership(x)
```

```
        comp = fsc.membership(x)
```

```
        print(f"{x}\t{orig:.2f}\t{comp:.2f}")
```

```
if __name__ == "__main__":  
    main()
```

Output:

Membership values:

Point	Original	Complement
-------	----------	------------

20	0.00	1.00
25	0.25	0.75
30	0.50	0.50
35	0.75	0.25
40	1.00	1.00
45	1.00	1.00
50	1.00	1.00
55	0.75	0.25
60	0.50	0.50
65	0.25	0.75
70	0.00	1.00

