Algorithm 1: ComputeAlpha

```
Data: out_{m\times n} (result of softmax), where m = \bar{W}_{\mathbf{unpadded}}/4, n = |\hat{A}|,
label (encoded by alphabet),
T, L, bl = 0 (blank index)
begin
    a = zeros(T, L)
    a[0][0] = out[0][bl]
    a[0][1] = out[0][label[0]]
    c = a[0][0] + a[0][1]
    if c > \theta then
        a[0][0] = \frac{a[0][0]}{c}
        a[0][1] = \frac{a[0][1]}{c}
    for t := 1 to T do
        start = \max(0, L - 2 \times (T - t))
        end = \min(2 \times t + 2, L)
        for s := start to L do
            i = \frac{s-1}{2}
             a[t][s] = a[t-1][s]
            if s > 0 then
              [a[t][s] = a[t][s] + a[t-1][s-1]
             if s \bmod 2 = 0 then
             | a[t][s] = a[t][s] \times out[t][bl]
             else if s = 1 or label[i] = label[i-1] then
             a[t][s] = a[t][s] \times out[t][label[i]]
             a[t][s] = (a[t][s] + a[t-1][s-2]) \times out[t][label[i]]
        c = \sum_{i=start}^{end} a[t][i]
if c > \theta then
             \mathbf{for}\ s := start\ \mathbf{to}\ end\ \mathbf{do}
               a[t][s] = \frac{a[t][s]}{c}
  _ return a
```

Algorithm 2: CTC Loss and softmax gradient computation

```
Data: out_{M\times N} (result of softmax), where M = \bar{W}_{padded}/4, N = |\hat{A}|,
label (encoded by alphabet),
w = W_{\mathbf{unpadded}}/4,
bl = 0 (blank index)
begin
   l = len(label)
    L = 2 \times l) + 1
    T = w
    out_{unpadded} = zeros(T, N)
    for t := 0 to T do
        for n := 0 to N do
         a = ComputeAlpha(out_{unpadded}, label, T, L, bl)
   out_{unpadded}^{flipped} = flipud(fliplr(out_{unpadded}))
    label_{reversed} = reverse(label) \\
   b = Compute Alpha (out_{unpadded}^{flipped}, label_{reversed}, T, L, bl)
    b = flipud(fliplr(b))
    ab = a * b
    lab = (T, N)
    for s := 0 to L do
        if s \bmod 2 = 0 then
            for t := 0 to T do
                ab[t][s] = \frac{ab[t][s]}{out[t][bl]}
               lab[t][bl] = lab[t][bl] + ab[t][s]
        else
            for t := 0 to T do
               i = \frac{s-1}{2}
              \begin{array}{l} ab[t][s] = \frac{ab[t][s]}{out[t][label[i]]} \\ ab[t][i] = lab[t][i] + ab[t][s] \end{array}
    lh = zeros(T)
   loss = -\sum_{t=1}^{T} \ln lh[t]
    softmax \overline{Grad} = zeros(M, N)
    for t := 0 to T do
        for n := 0 to N do
            softmaxGrad[t][n] = out[t][n] - \frac{lab[t][n]}{out[t][n]*lh[t]}
   return\ loss,\ softmaxGrad
```