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**Algorithm 1:** *ComputeAlpha* (for single element in the batch)

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**Data:**

$out_{|\hat{A}| \times T}$  (result of softmax), where  $|\hat{A}|$  (alphabet size),  
 $T = \bar{W}_{unpadded}/4$ ;

$label$  (encoded by alphabet);

$bl = 0$  (blank index)

**begin**

$S = len(label) * 2 + 1$

$T = out.shape[1]$

$a = zeros(S, T)$

$a[0][0] = out[bl][0]$

$a[1][0] = out[label[0]][0]$

$c = a[0][0] + a[1][0]$

**if**  $c > 0$  **then**

$a[0][0] = \frac{a[0][0]}{c}$

$a[1][0] = \frac{a[1][0]}{c}$

**for**  $t := 1$  **to**  $T$  **do**

$start = \max(0, S - 2 \times (T - t))$

$end = \min(2 \times t + 2, S)$

**for**  $s := start$  **to**  $end$  **do**

$i = \max(0, floor(\frac{s-1}{2}))$

**if**  $s \bmod 2 = 0$  **then**

**if**  $s = 0$  **then**

$a[s][t] = a[s][t-1] \times out[bl][t]$

**else**

$a[s][t] = (a[s][t-1] + a[s-1][t-1]) \times out[bl][t]$

**else if**  $s = 1$  **or**  $label[i] = label[i-1]$  **then**

$a[s][t] = (a[s][t-1] + a[s-1][t-1]) \times out[label[i]][t]$

**else**

$a[s][t] =$

$(a[s][t-1] + a[s-1][t-1] + a[s-2][t-1]) \times out[label[i]][t]$

$c = \sum_{i=start}^{end} a[i][t]$

**if**  $c > 0$  **then**

**for**  $s := start$  **to**  $end$  **do**

$a[s][t] = \frac{a[s][t]}{c}$

**return**  $a$

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