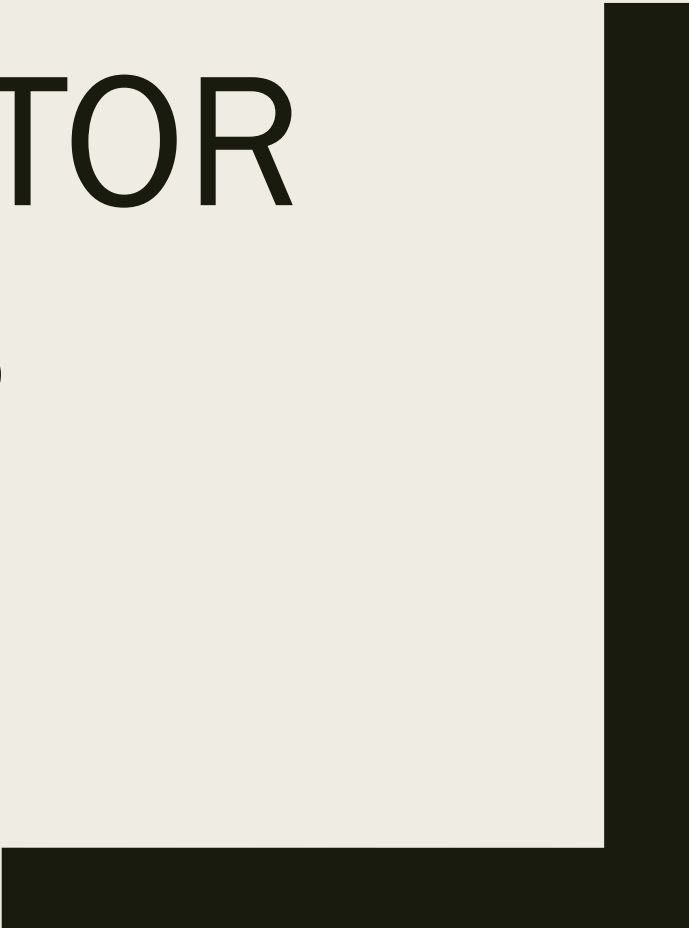


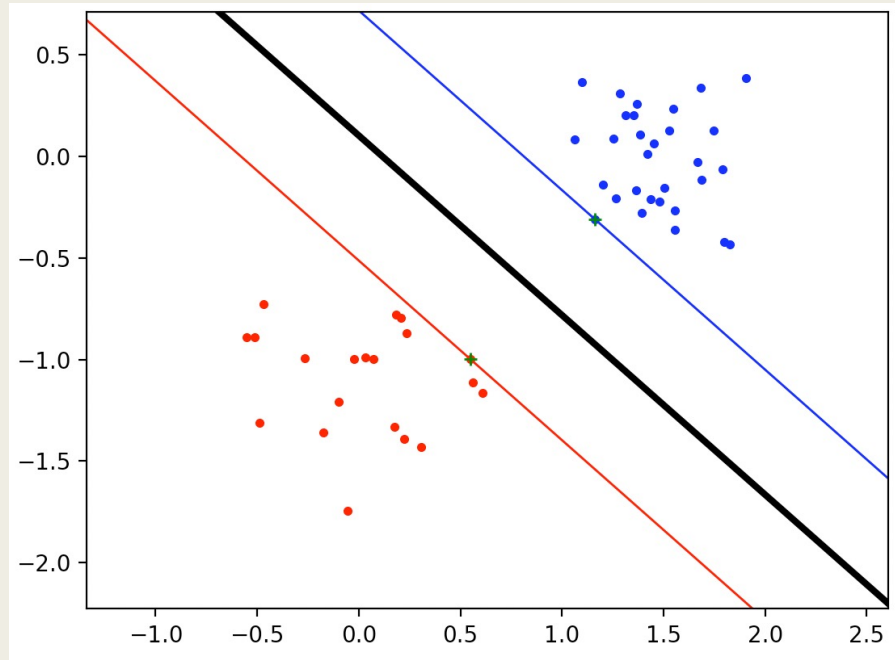


# SUPPORT VECTOR MACHINES

Lab 02 – Machine Learning  
Ivan & Simon

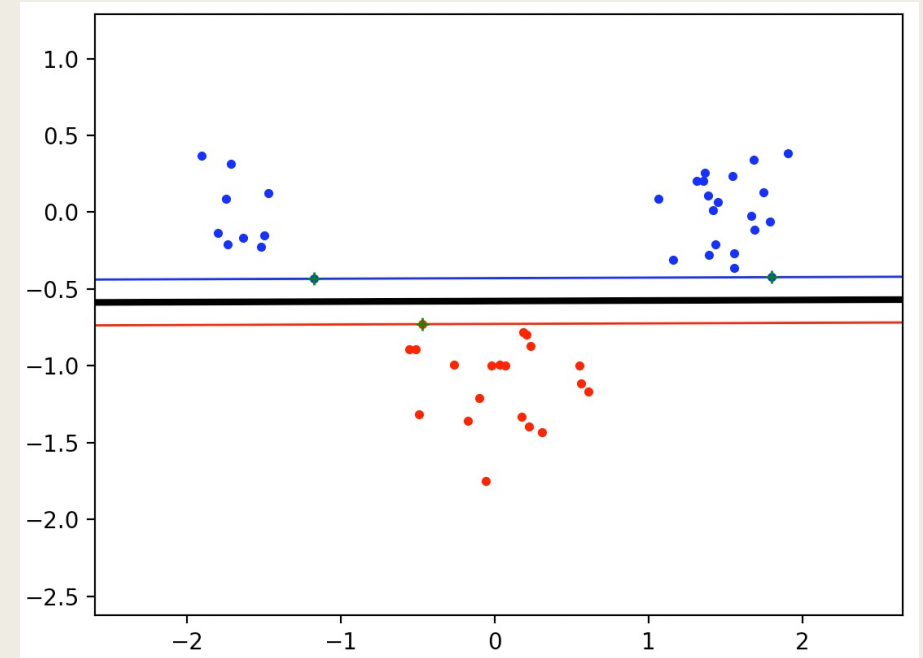


# Linear kernel



"easiest" case

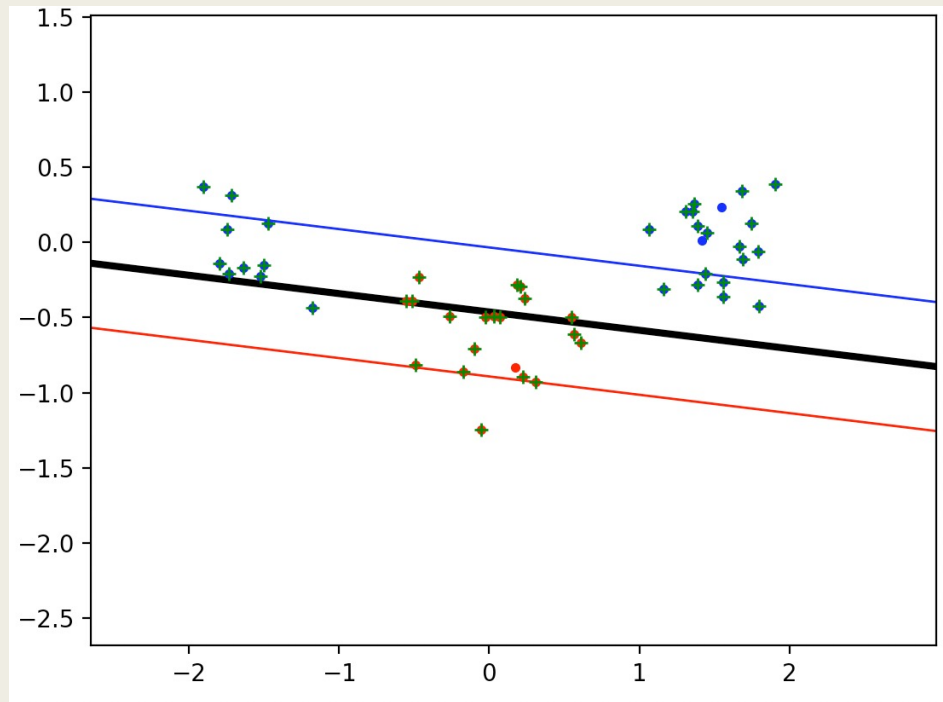
- two data clusters
- clearly linearly separable



Harder case

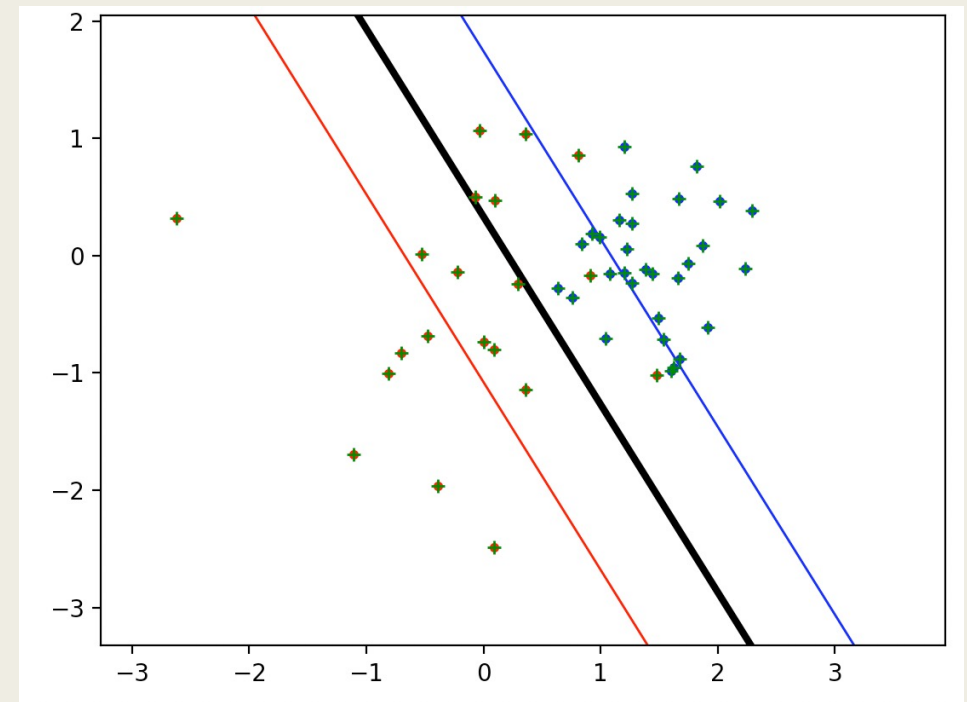
- three data clusters
- clusters reasonably close but not trivial

# Linear kernel – problem cases



No overlap, but not linearly separable

➤ New kernel functions



Overlapping data

➤ Introduction of slack

# Non-Linear Kernels

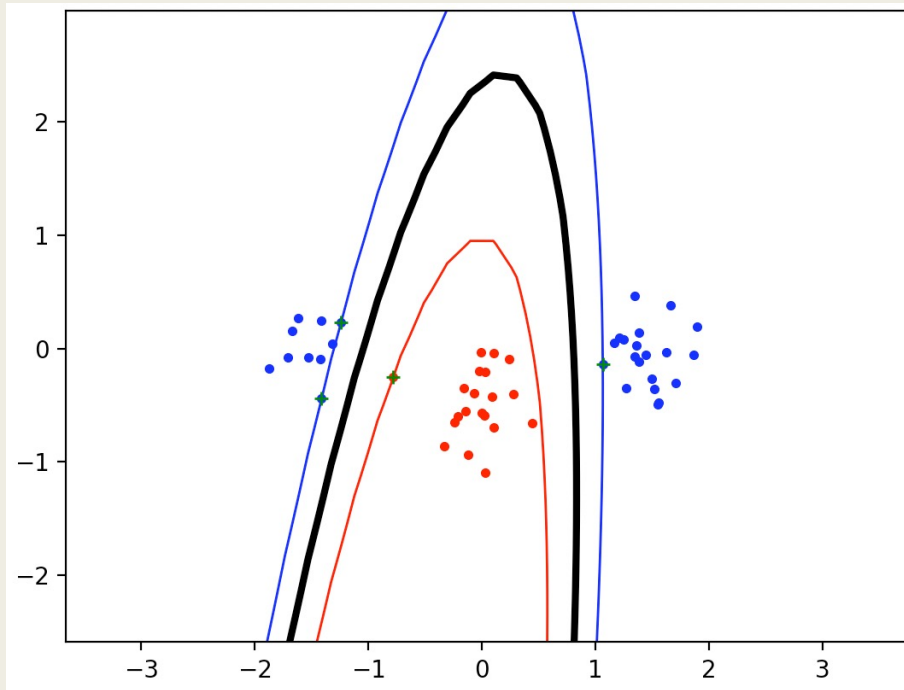
Polynomial Kernel

$$\mathcal{K}(\vec{x}, \vec{y}) = (\vec{x}^T \cdot \vec{y} + 1)^p$$

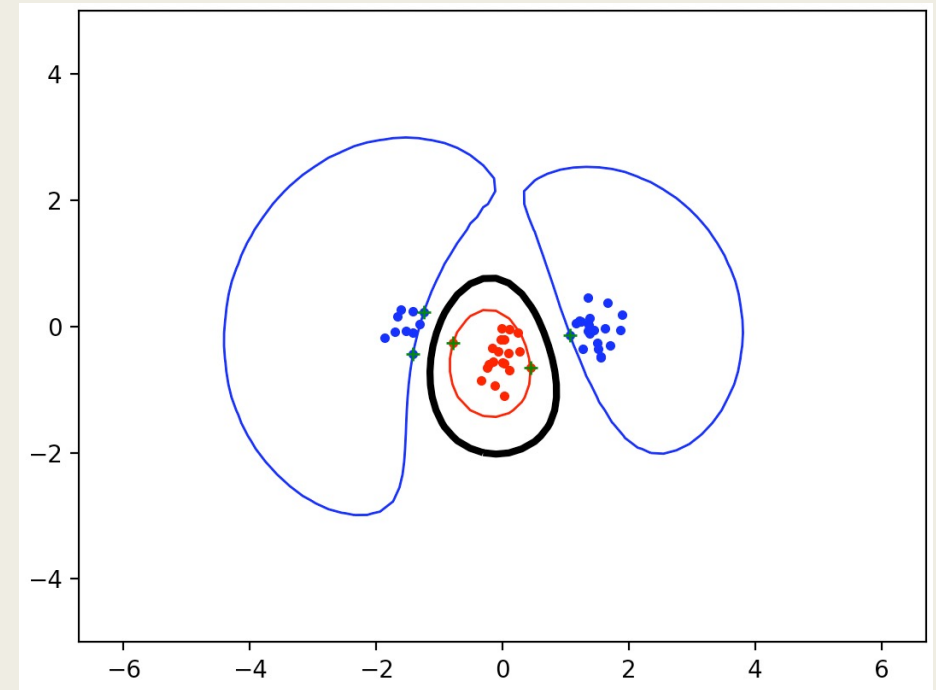
Radial Basis Function  
Kernel

$$\mathcal{K}(\vec{x}, \vec{y}) = e^{-\frac{||\vec{x} - \vec{y}||^2}{2\sigma^2}}$$

# Non-linear kernels

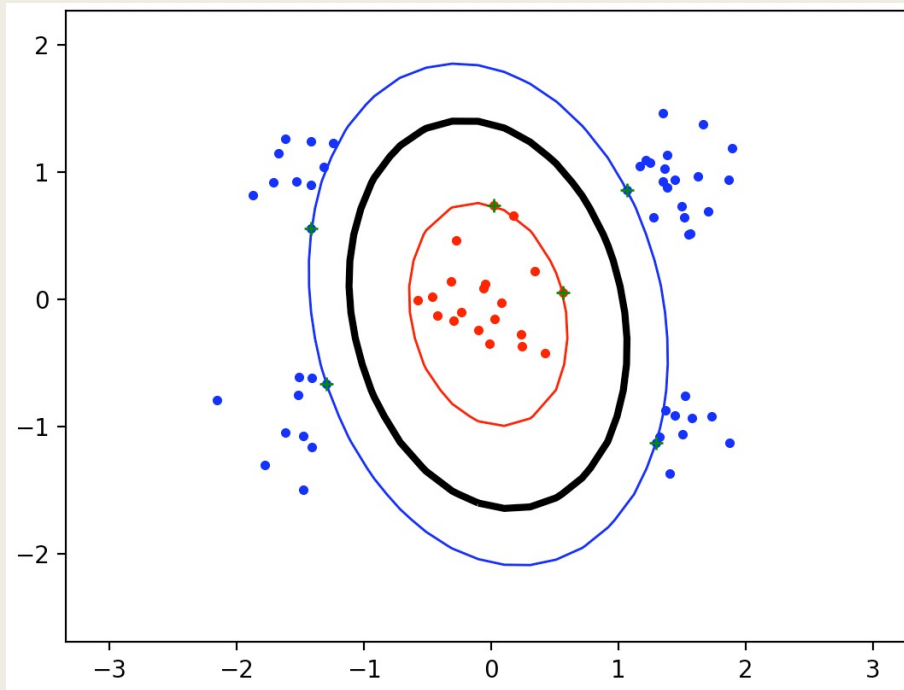


## Polynomial kernel with order 2

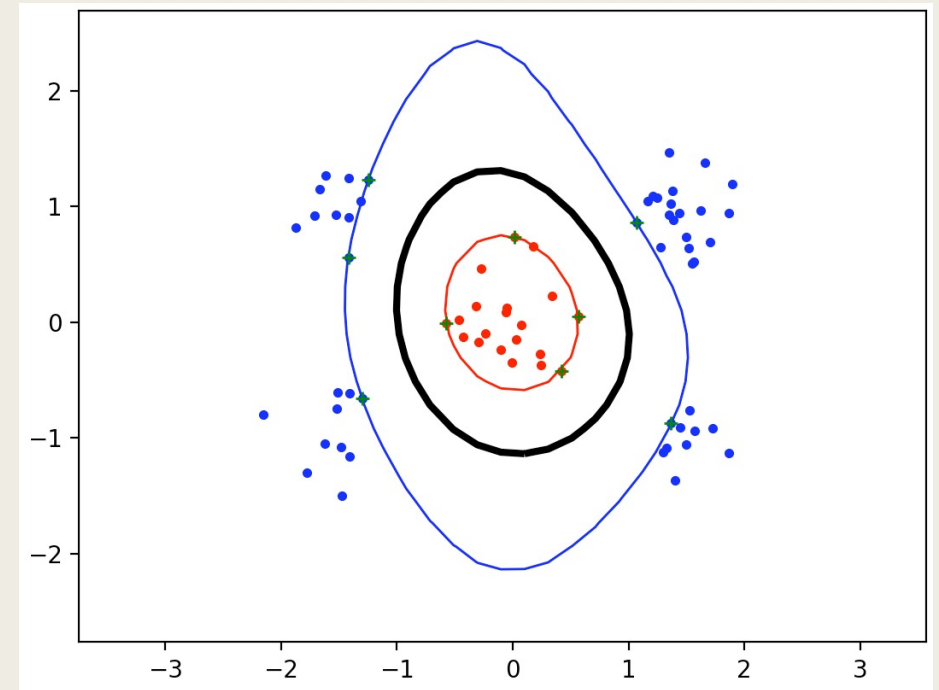


RBF kernel with sigma = 1.0

# Non-linear kernels

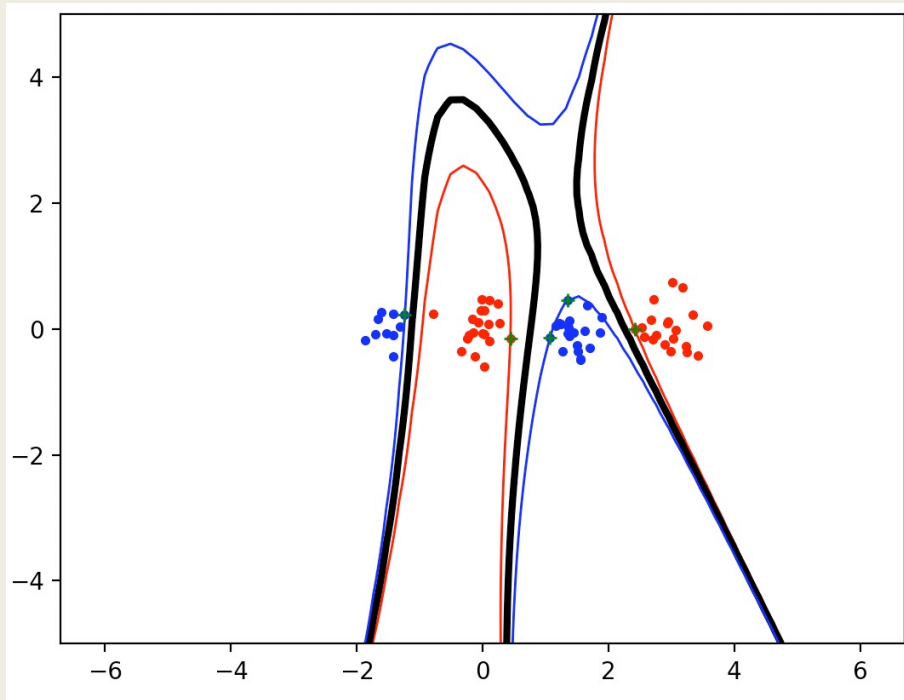


Polynomial kernel with order 2

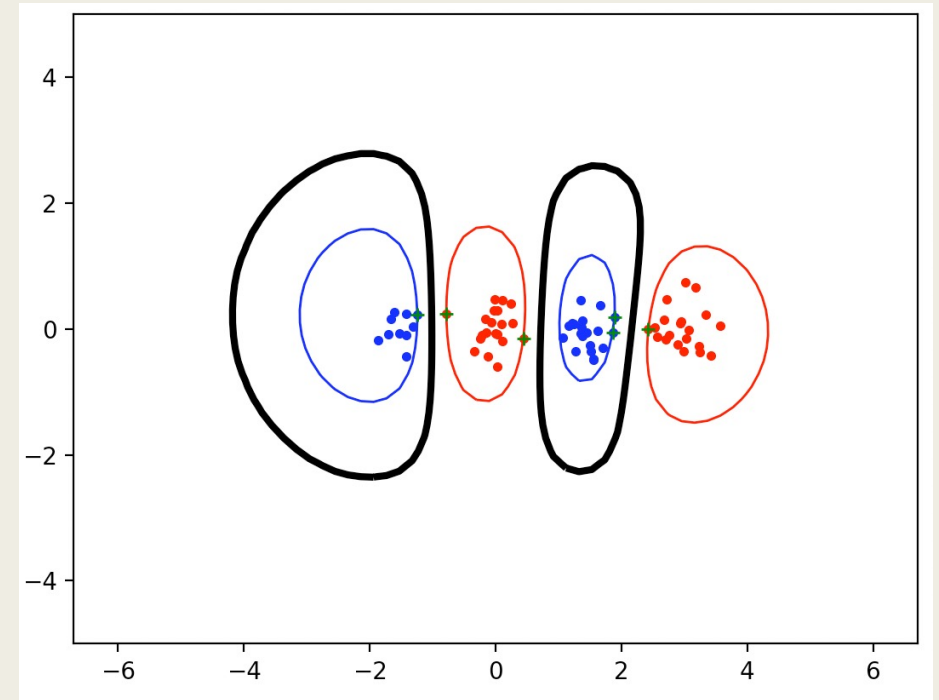


RBF kernel with sigma = 1.0

# Non-linear kernels



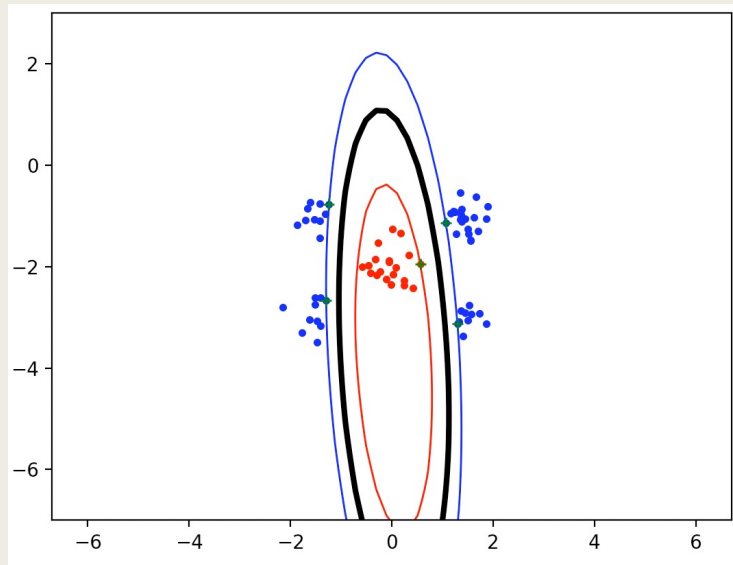
Polynomial kernel with order 3  
- Order 2 was not “enough” to solve  
the problem



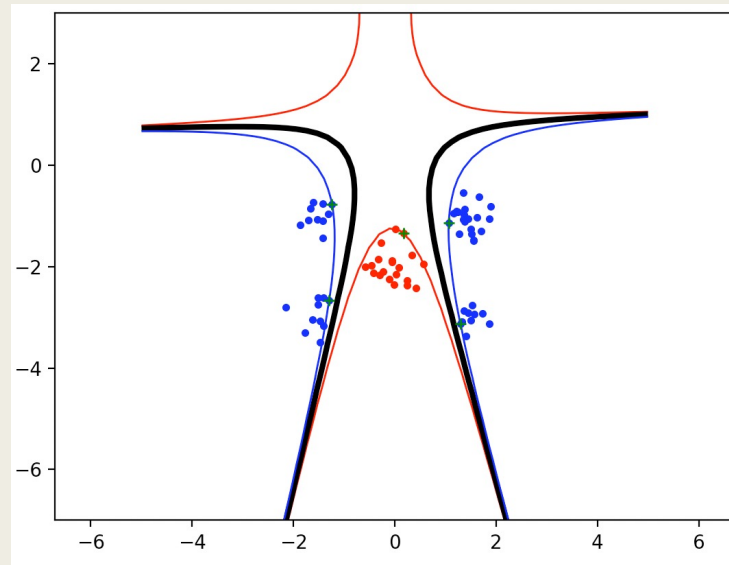
RBF kernel with  $\sigma = 1.0$

# Bias-variance tradeoff

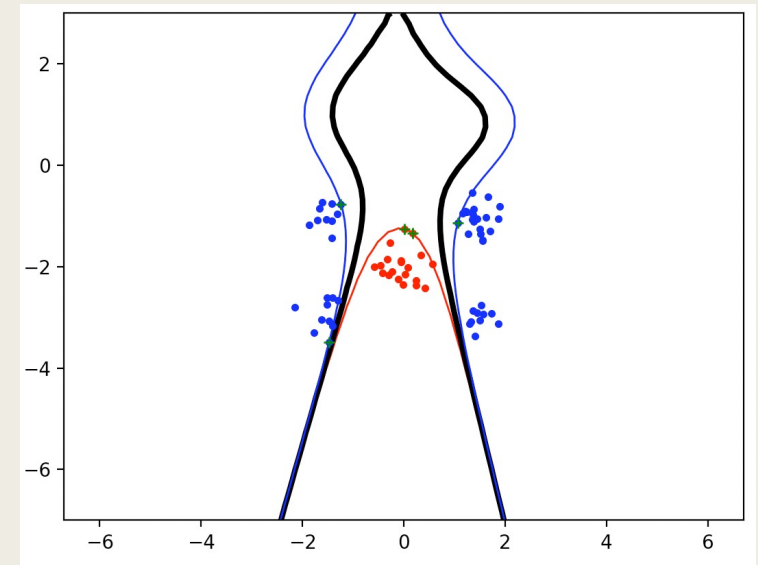
## Polynomial kernel - order



2



3



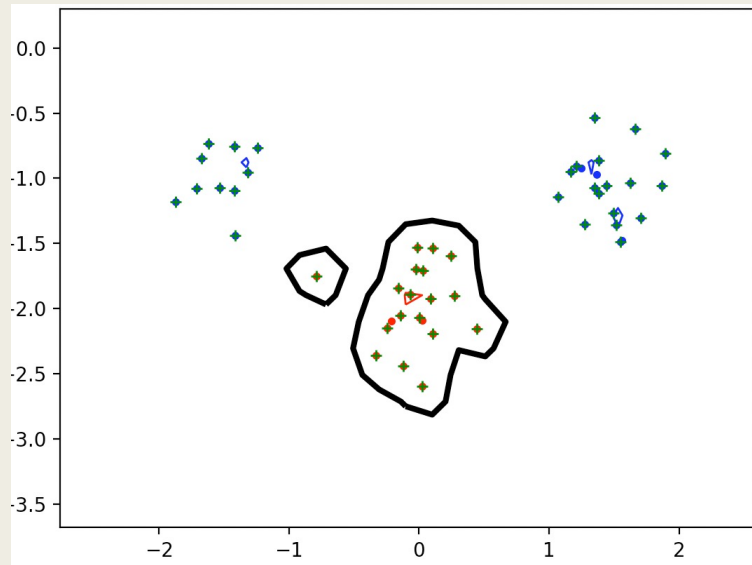
4

low variance, high bias ← → high variance, low bias

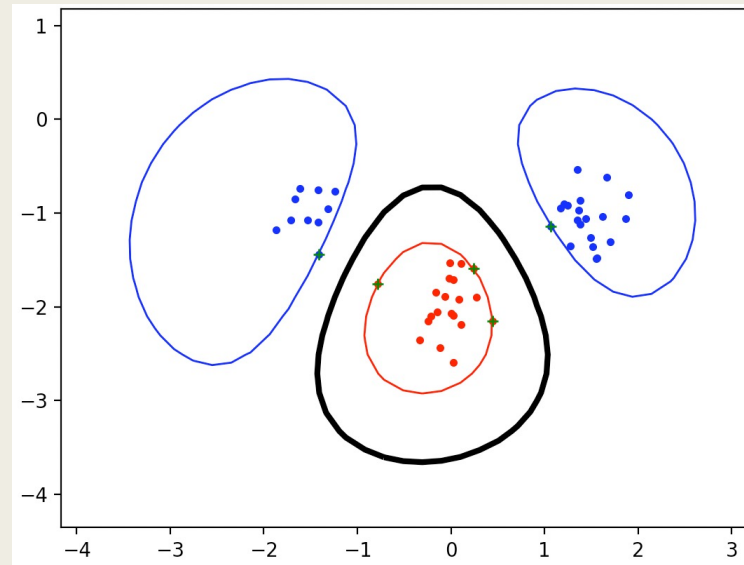


# Bias-variance tradeoff

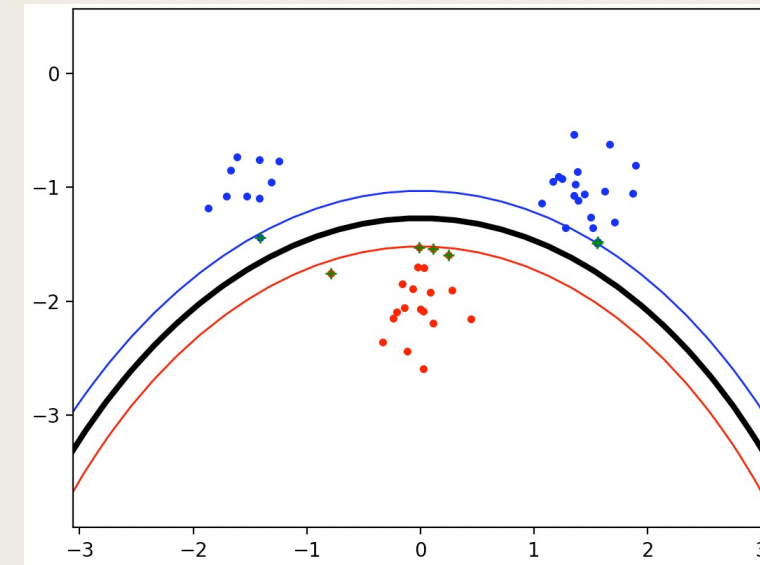
## RBF kernel - sigma



.1



1



10

high variance, low bias

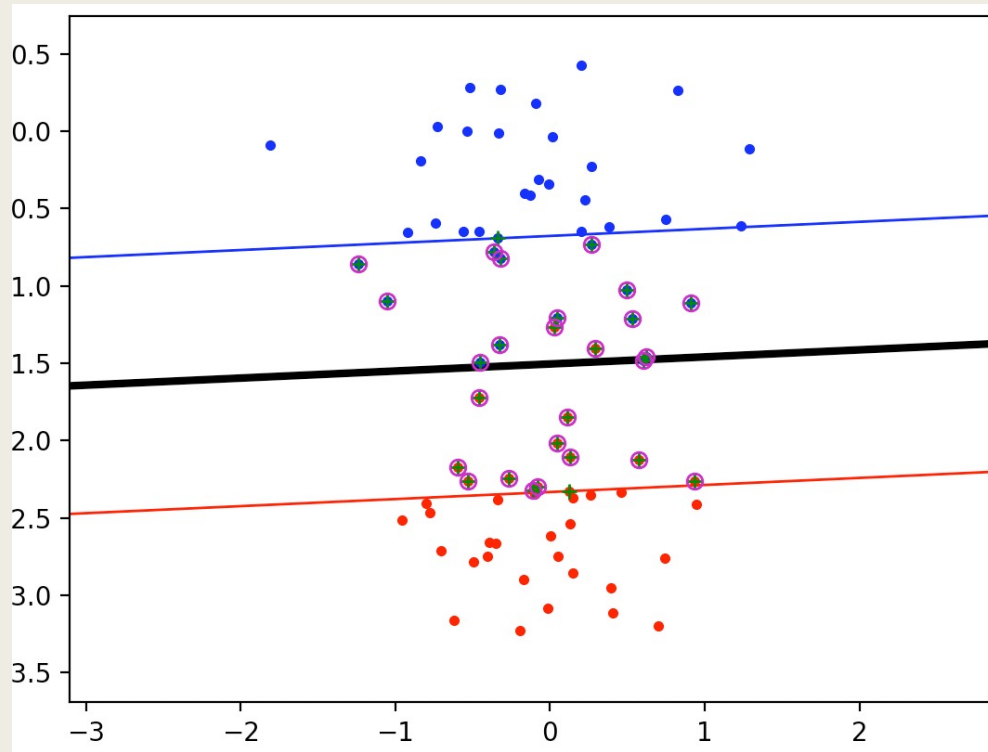
low variance, high bias

# Slack variables

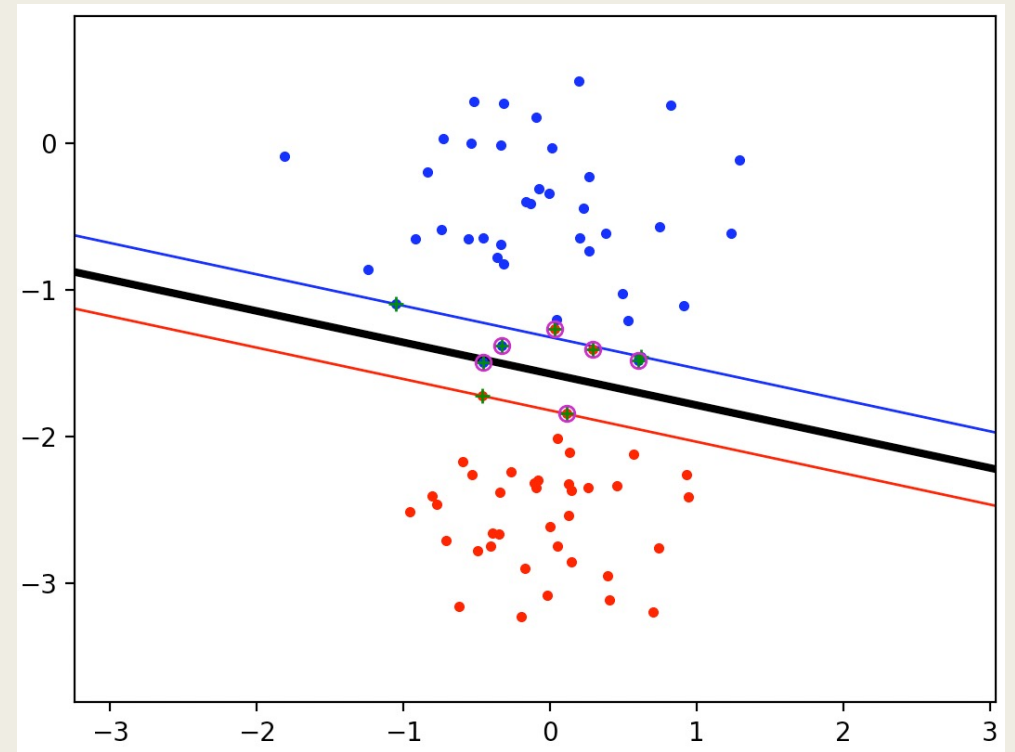
Weakening the constraints

$$t_i(\vec{w}^T \cdot \phi(\vec{x}_i) - b) \geq 1 - \xi_i$$

# Influence of slack parameter C - noise



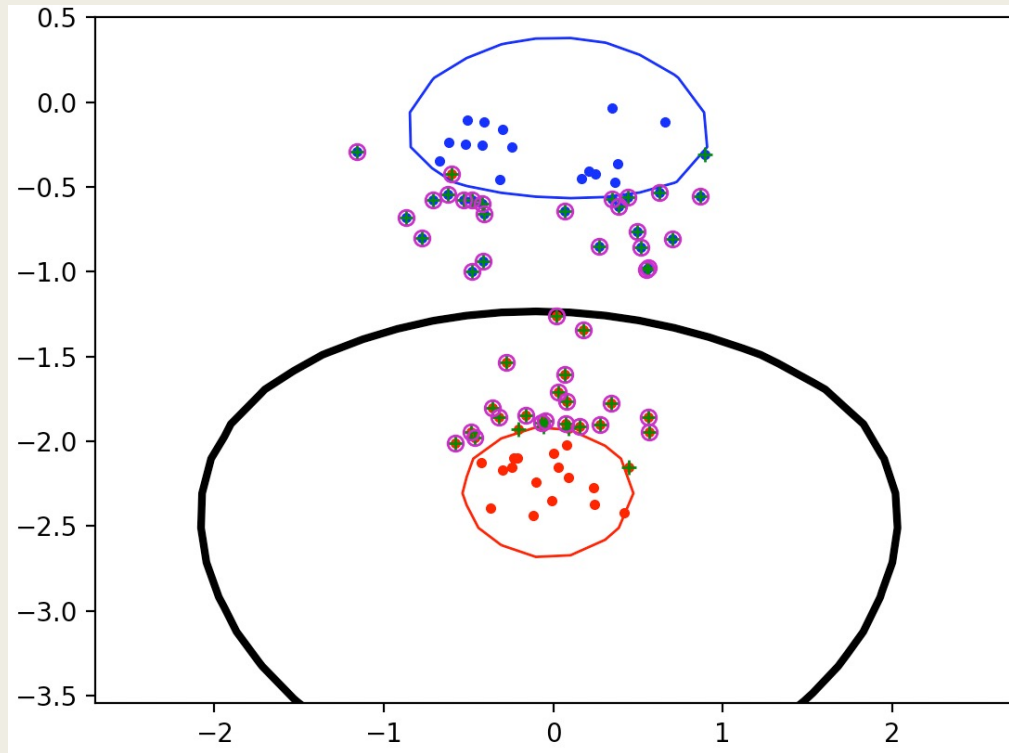
.1



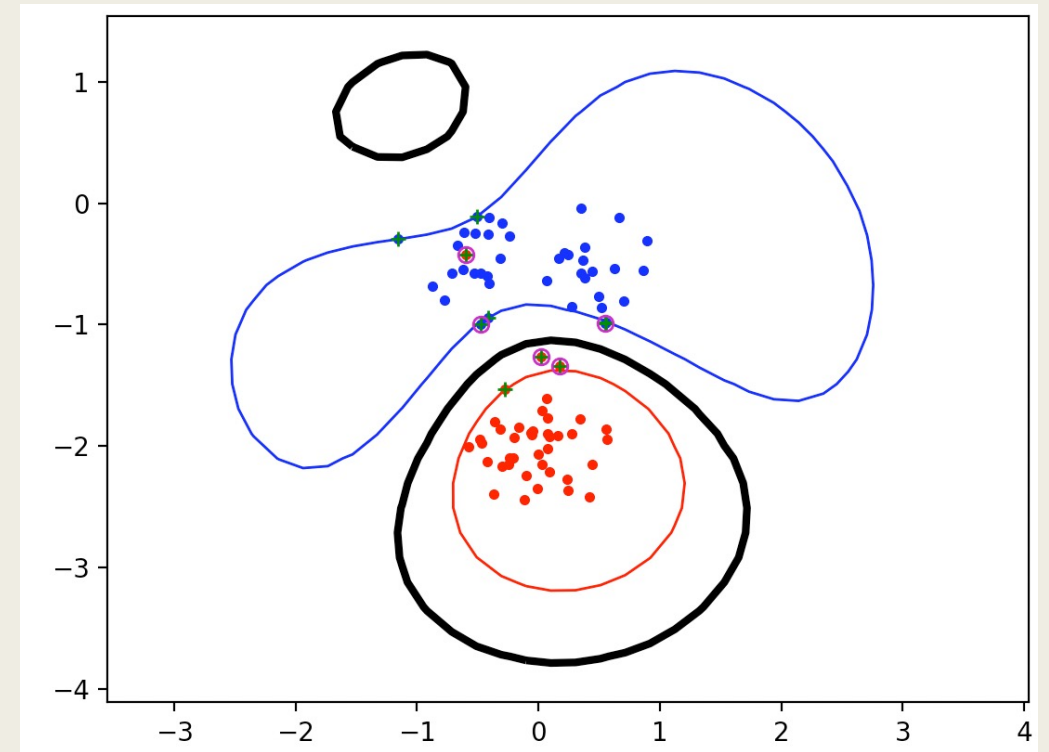
10

$C$  controls how much we penalize points lying inside of the margin

# Influence of slack parameter C – wrong label



.1



10

$C$  controls how much we penalize points lying inside of the margin

What to do with difficult data?  
More slack or complex model?

High noise? —————> More slack!  
Otherwise overfitting

Complicated data? —————> Complex model!  
Otherwise underfitting