Lecture 3.3 Supervised learning: Decision Trees & Ensemble Learning



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11752 Machine Learning
Máster Universitario
en Sistemas Inteligentes

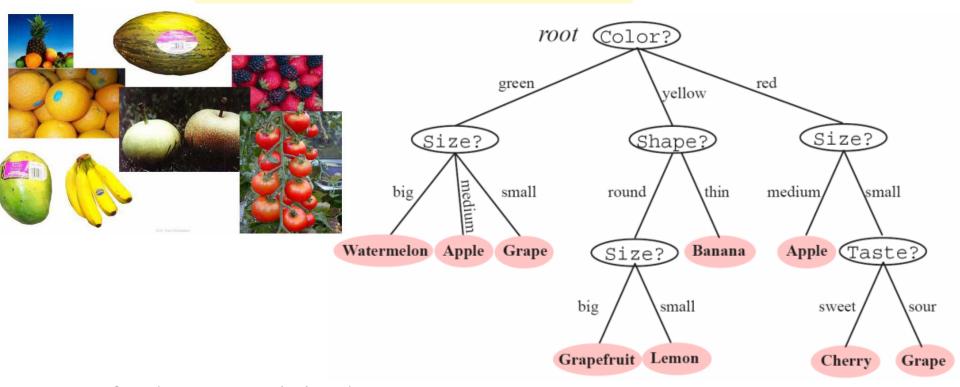
Alberto ORTIZ RODRÍGUEZ

Contents

- Decision trees
- Regression trees
- Ensemble learning
- Random forests

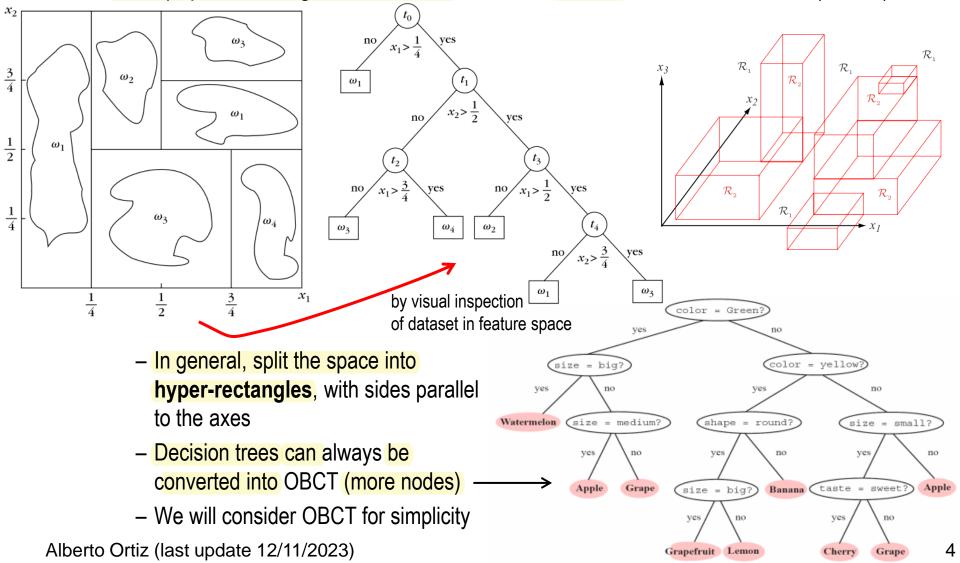
Definition

- The classification process consists in the sequential application of a set of questions, in which the next question depends on the result of the previous ones
 - The set of questions is organized over a directed tree as a multistage decision system.
 - Naturally handle all kind of data: metric and non-metric, any number of dimensions
 - The sequence of questions split the feature space into non-overlapping regions
 - Not all features need to be evaluated to make a decision



Definition

Most popular among decision trees: Ordinary Binary Classification Tree (OBCT)



Set of Questions

- For the OBCTs, questions are of the form is feature $x_k \leq \alpha_k$?
 - Once α_k has been selected, a split of the training set X is defined
 - How to select $x_k & \alpha_k$?
 - A priori, it seems there are infinite possibilities
 - Actually, only the $n_k \le N$ different values taken by feature k within X have to be considered

 α_k would be taken halfway between consecutive distinct values of x_k e.g. if $X = \{(0.4, 0.2), (0.56, 0.1), (1.0, -0.5), (3.2, 2.0), (-1.5, -1.5)\}$ the **candidate** questions would be as follows:

x_1	$\leq \frac{-1.5 + 0.4}{2} = -0.55$	$\leq \frac{0.4 + 0.56}{2} = 0.48$	$\leq \frac{0.56+1}{2} = 0.78$	$\leq \frac{1+3.2}{2} = 2.1$
x_2	$\leq \frac{-1.5 - 0.5}{2} = -1$	$\leq \frac{-0.5 + 0.1}{2} = -0.25$	$\leq \frac{0.1 + 0.2}{2} = 0.15$	$\leq \frac{0.2+2.0}{2} = 1.1$

- Now, we have to choose which question from the candidates \Rightarrow which $x_k \& \alpha_k$?
 - Choose the best split according to a splitting criterion

Splitting Criterion

- Quantify **node impurity** and split so that the overall impurity $I(N_t^Y)$ and $I(N_t^N)$ of the descendant nodes N_t^Y and N_t^N is optimally decreased with respect to the ancestor node's impurity $I(N_t)$:
 - Impurity for node N_t comprising $X_t \subseteq X$: entropy H (ID3), Gini index G (CART), ...

$$I(N_t) = H(X_t) = -\sum_{i=1}^{M} P(\omega_i | N_t) \log_2 P(\omega_i | N_t)$$

$$I(N_t) = G(X_t) = 1 - \sum_{i=1}^{M} P(\omega_i | N_t)^2$$
where $P(\omega_i | N_t) = P(x \in \omega_i | x \in X_t)$

- In practice: $P(\omega_i|N_t) = \frac{n_t^i}{n_t}$, where $n_t^i = \text{no. elements of } X_t \text{ belonging to } \omega_i$
- Impurity is maximum if $P(\omega_i|N_t) = 1/M \ \forall i$, and minimum if $\exists i \mid P(\omega_i|N_t) = 1$ for a certain class ω_i $(H: 0 \cdot \log_2 0 \rightarrow 0)$
- After a split, the decrease in **node impurity** is defined as:

$$\Delta I(N_t) = I(N_t) - \frac{n_t^Y}{n_t} I(N_t^Y) - \frac{n_t^N}{n_t} I(N_t^N)$$

 The goal is thus to adopt, from the set of candidate questions, the one that performs the split leading to the highest decrease of impurity:

$$(x_k^*, \alpha_k^*) = \operatorname{argmax} \Delta I(N_{xk,\alpha k})$$

Classification Rules

Stop-splitting rule:

When one decides to stop splitting a node N_t and declares it as a leaf of the tree?

- 1. Stop if node N_t is pure, i.e. all the samples belong to a single class
- 2. Given a threshold τ_I on the impurity decrease for a node, stop splitting if $\Delta I(N_t) < \tau_I$
- 3. Stop if $n_t^Y < \tau_n$ or $n_t^N < \tau_n$
- 4. Stop if, after the splitting, the depth of the tree is above a threshold τ_D

Alternative approach: make the tree grow to a larger size and then use a **pruning criterion**: which leaf can be suppressed with the least impact on the classification error?

Class assignment rule:

Once a node is declared to be a leaf, which class label it must be given?

– Typically:
$$j= rg \max_i \left\{ P(\omega_i|N_t) \right\} = rg \max_i \left\{ \frac{n_t^i}{n_t} \right\}$$

Algorithm (for building OBCTs)

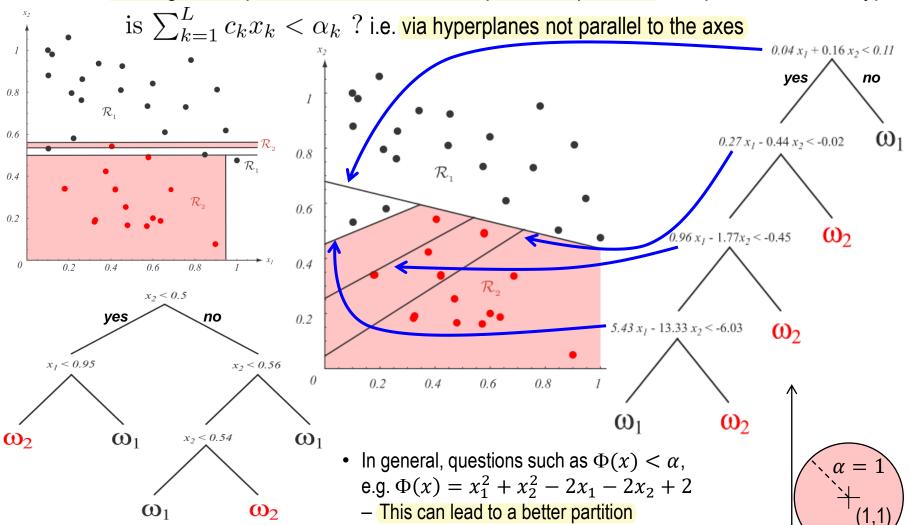
```
NL \leftarrow X
                         # node list
while non-empty(NL) do
                                                    # and remove it from the list
      N_t \leftarrow \text{next-element(NL)}
      if stop-splitting (N_t) then
             Declare N_t as a leaf node and designate it with class label \omega_i:
                j = \underset{i}{\operatorname{arg max}} \left\{ P(\omega_i | N_t) \right\} = \underset{i}{\operatorname{arg max}} \left\{ \frac{n_t^i}{n_t} \right\}
      else
            for every feature x_k, k = 1, 2, \dots, L
                  for every different value \alpha_{ki}, i = 1, 2, \ldots, taken by x_k in X_t
                         Generate N_t^Y and N_t^N according to the question
                         is x_k < \alpha_{ki}?
                        Calculate \Delta I(N_t) = I(N_t) - \frac{n_t^Y}{n_t} I(N_t^Y) - \frac{n_t^N}{n_t} I(N_t^N)
                  end
                 For feature x_k, choose \alpha_{ki^*} leading to the maximum \Delta I(N_t)
            end
            Choose x_{k^*} leading to the maximum \Delta I(N_t) for \alpha_{k^*i^*}
            Insert the two associated subnodes N_t^Y and N_t^N in NL
      end
end
```

Final remarks

- Algorithms for building decision trees:
 - ID3 (Iterative Dichotomiser 3) was developed in 1986 by Ross Quinlan. The algorithm creates a multiway tree, finding for each node (i.e. in a greedy manner) the categorical feature that will yield the largest information gain for categorical targets. Trees are grown to their maximum size and then a pruning step is usually applied to improve the ability of the tree to generalize to unseen data.
 - C4.5 is the successor of ID3. The restriction that features must be categorical was removed by dynamically defining a discrete attribute (based on numerical variables) that partitions the continuous attribute value into a discrete set of intervals. C4.5 converts the trained trees (i.e. the output of the ID3 algorithm) into sets of if-then rules. The accuracy of each rule is then evaluated to determine the order in which they should be applied. Pruning is done by removing a rule's precondition if the accuracy of the rule improves without it.
 - **C5.0** is Quinlan's latest version release under a proprietary license. It uses less memory and builds smaller rule-sets than C4.5 while being more accurate.
 - CART (Classification and Regression Trees) is very similar to C4.5, but it differs in that it supports numerical target variables (regression) and does not compute rule sets. CART constructs binary trees using the feature and threshold that yield the largest information gain at each node.
- Scikit-learn implements an **optimized version of the CART algorithm**, although the scikit-learn implementation does not support categorical variables for now.

Final remarks

More general partitions of the feature space are possible via questions of the type:



of the feature space but training gets more difficult !!

Alberto Ortiz (last update 11/12/2023)

Examples

• **Example 1**. In a tree classification task, the set X_t , associated with node N_t , contains $n_t = 10$ samples. Four of these belong to class ω_1 , four to class ω_2 , and two to class ω_3 . The node splitting results into two new subsets X_t^Y , with three samples from ω_1 , and one from ω_2 , and X_t^N , with one sample from ω_1 , three from ω_2 , and two from ω_3 . Determine the decrease in impurity after splitting.

$$\Delta I(N_t) = I(N_t) - \frac{n_t^Y}{n_t} I(N_t^Y) - \frac{n_t^N}{n_t} I(N_t^N)$$

$$I(N_t) = -\frac{4}{10} \log_2 \frac{4}{10} - \frac{4}{10} \log_2 \frac{4}{10} - \frac{2}{10} \log_2 \frac{2}{10} = 1.521$$

$$I(N_t^Y) = -\frac{3}{4} \log_2 \frac{3}{4} - \frac{1}{4} \log_2 \frac{1}{4} = 0.815$$

$$I(N_t^N) = -\frac{1}{6} \log_2 \frac{1}{6} - \frac{3}{6} \log_2 \frac{3}{6} - \frac{2}{6} \log_2 \frac{2}{6} = 1.472$$

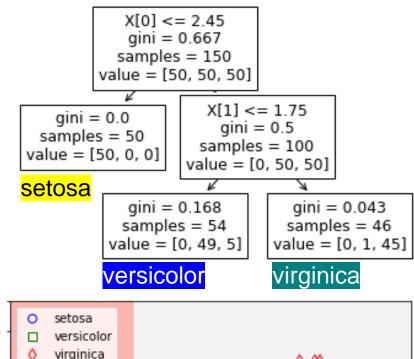
$$\Delta I(N_t) = 1.521 - \frac{4}{10} (0.815) - \frac{6}{10} (1.472) = 0.315$$

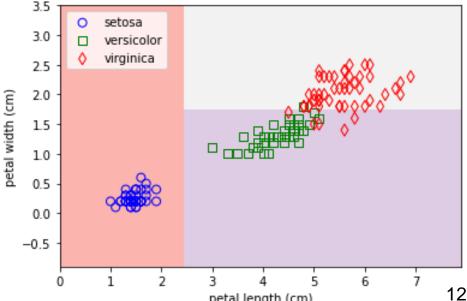
Examples

Example 2

```
from sklearn.datasets import load iris
from sklearn.tree import DecisionTreeClassifier
from sklearn.tree import plot tree
import matplotlib.pyplot as plt
iris = load iris()
X = iris.data[:, 2:] # petal length and width
y = iris.target
tree = DecisionTreeClassifier(
    criterion="gini",
    max depth=2,
    min samples leaf=5,
    min impurity decrease=0.1,
    random state=100)
tree.fit(X, y)
plot tree(tree)
plt.show()
        regularization hyperparameters
```

- avoid overfitting
- only some hyperparameters are shown, there are others

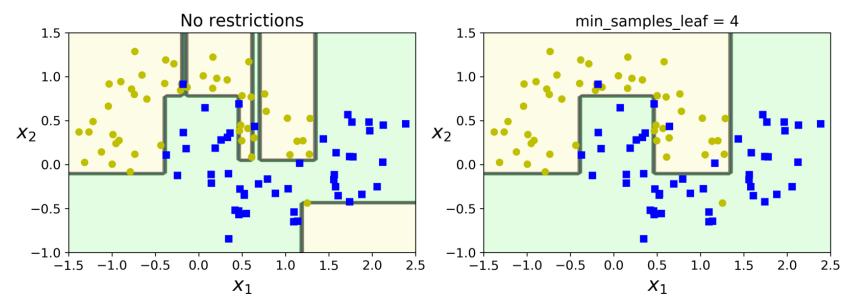




petal length (cm)

Examples

• **Example 3.** Effect of regularization parameters



- Left: overfitting, Right: will probably generalize better
- Left: The splitting process continues until all nodes are pure if not stopped before
- Right: Increasing min_* hyperparameters and/or reducing max_* hyperparameters regularize the model, and avoids overfitting

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• Decision trees are also capable of performing regression tasks.

By way of example, we can build a regression tree using scikit-learn:

```
from sklearn.tree import DecisionTreeRegressor

# 1D quadratic synthetic dataset

m = 100

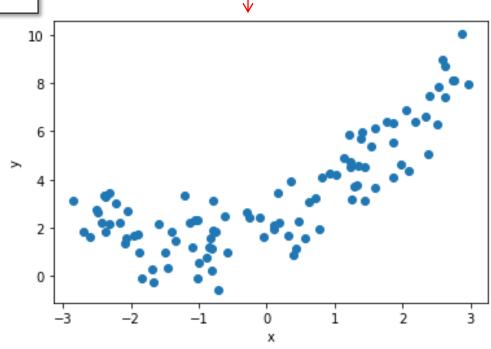
X = 6 * np.random.rand(m,1) - 3

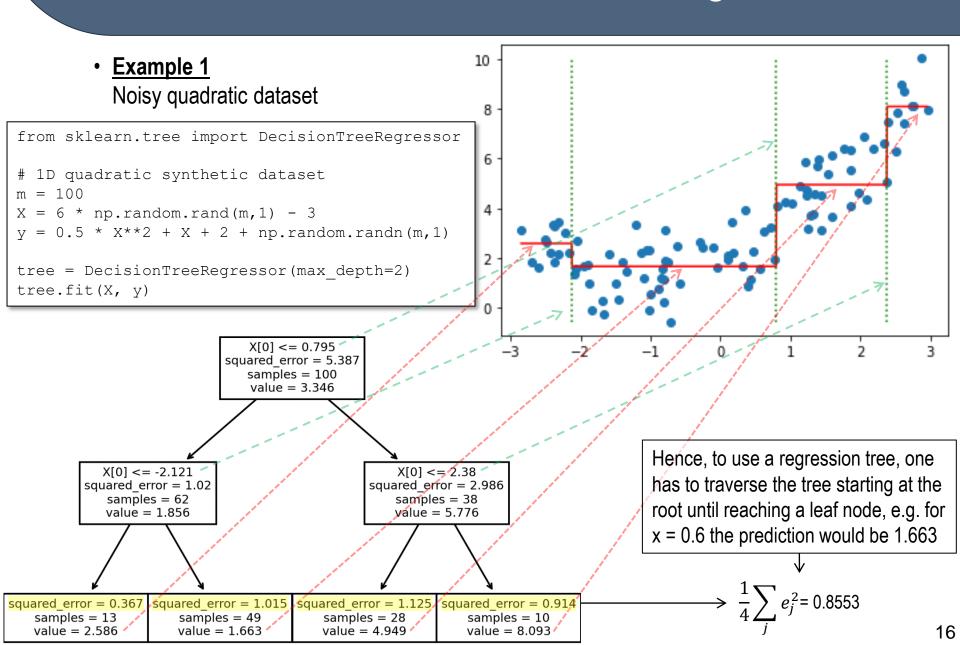
y = 0.5 * X**2 + X + 2 + np.random.randn(m,1)

tree = DecisionTreeRegressor(max_depth=2)

tree.fit(X, y)
```

- The tree will look very similar to the classification tree we have built earlier.
- The main difference is that instead of predicting a class, it will predict a value.





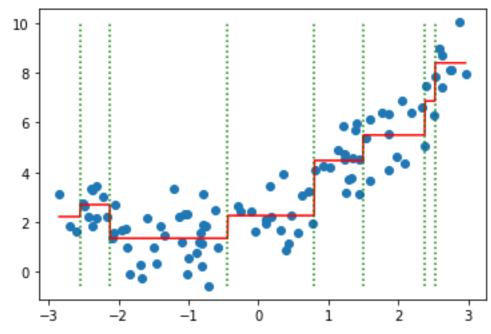
- In regression trees, predictions are obtained as the average target value for the samples associated to the corresponding leaf node
 - The quality of the predictions can then be calculated as the Mean Squared Error (MSE) of the target values for the involved samples, i.e. for a node N_t :

$$MSE(N_t) = \frac{1}{n_t} \sum_{i \in N_t} (y_i - \bar{y}_t)^2, \quad \bar{y}_t = \frac{1}{n_t} \sum_{i \in N_t} y_i$$

• For the previous example, if we increase the tree depth, the MSE values get lower:

MSE at leaves (max. depth = 3)							
1	2	3	4				
0.4450	0.2905	0.9338	0.6226				
5	6	7	8				
0.7204	1.0334	0.3388	0.5881				

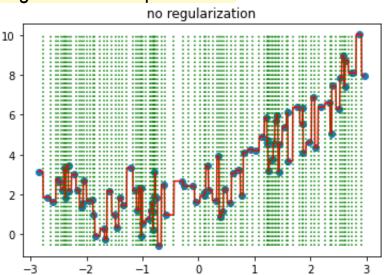
- Average MSE for max_depth = $2 \rightarrow 0.8553$
- Average MSE for max_depth = $3 \rightarrow 0.6216$

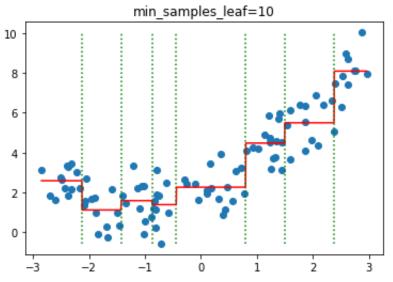


The tree building algorithm works mostly the same way as for classification trees, except that
instead of trying to split the training set in a way that minimizes impurity, it now tries to split the
training set in a way that minimizes the MSE:

$$\Delta MSE(N_t) = MSE(N_t) - \frac{n_t^Y}{n_t} MSE(N_t^Y) - \frac{n_t^N}{n_t} MSE(N_t^N)$$

- The node with the highest reduction in MSE is chosen for splitting
- Just like for classification tasks, regression trees are also prone to overfitting if no regularization is performed:





• Example 2

California housing dataset:

- Median house value for California districts expressed in \$100,000
 (1990 U.S. census, using one row per census block group [= smallest geographical unit that is published])
- -20640 samples, 8 features, target $y \in 0.15 5$

```
from sklearn.datasets import fetch_california_housing
from sklearn.tree import DecisionTreeRegressor

X, y = fetch_california_housing(return_X_y=True)

tree = DecisionTreeRegressor(max_leaf_nodes=10)
tree.fit(X, y)
```

MSE at leaves							
1	2	3	4	5			
0.670	0.394	0.702	1.168	0.536			
6	7	8	9	10			
0.438	0.509	1.006	0.526	0.778			

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Ensemble learning

- Suppose you ask a complex question to thousands of random people and then aggregate their answers
 - In many cases you will find that this aggregated answer is better than a single expert's answer
 - This is called the wisdom of the crowd
- Similarly, if you aggregate the predictions of a group of predictors (classifiers or regressors), you will often get better predictions than with the best individual predictor
 - A group of predictors is called an ensemble
 - Hence, this technique is called Ensemble Learning
 - An Ensemble Learning algorithm is called an Ensemble method
- In general, ensemble classifiers **scale very well** as training and predictions can be performed in parallel, i.e. via different CPU cores/servers
- You will often use ensemble methods **near the end of a project**, once you have already built a few good predictors, to combine them into an even better predictor

Ensemble learning

- It is possible to find a number of ensemble methods:
 - Voting (hard and soft voting)
 - Bagging (and pasting)
 - Stacking (and blending)
 - Boosting (Adaptive boosting/Adaboost and variants, Gradient boosting/Gradient boosted regression trees [GBRT], Extreme gradient boosting [XGB])
 - Others ...
- In this section, we will discuss the voting, bagging and stacking ensemble methods
 - The boosting methods are built by sequentially adding predictors to an ensemble, each one correcting its predecessor
 - ... while **voting**, **bagging** and **stacking** consider all the available predictors at once

Voting classifier

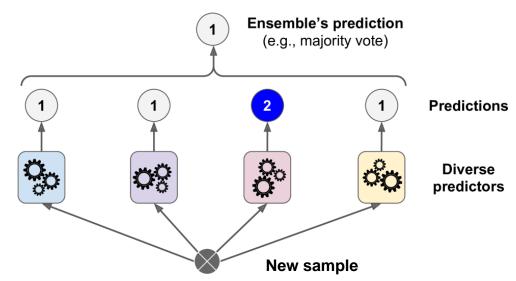
• Suppose you have trained a few classifiers, each one achieving a certain accuracy e.g. a Logistic Regression classifier, a Perceptron, a Decision Tree, and maybe a few more

```
from sklearn.model selection
                                                    Logistic
   import train test split
from sklearn.datasets import make moons
X, y = make moons(n samples=600, noise=0.4)
X train, X test, y train, y test =
   train test split(X, y, test size=0.3)
from sklearn.linear model import LogisticRegression
from sklearn.linear model import Perceptron
from sklearn.tree import DecisionTreeClassifier
from sklearn.metrics import accuracy score
log clf = LogisticRegression()
per clf = Perceptron(tol=1e-3)
tre clf = DecisionTreeClassifier(
    criterion="gini",
    \max depth=2,
    min samples leaf=5,
    min impurity decrease=0.1)
for clf in (per clf, log clf, tre clf):
  clf.fit(X train, y train)
  y pred = clf.predict(X test)
  print(accuracy score(y test, y pred))
```

Decision Regression Perceptron Tree Other -1.0-1.50.7444 # Perceptron 0.8222 # Logistic Regression 0.7778 # Decision Tree

Voting classifier

- A very simple way to create a
 better classifier is to aggregate
 the predictions of each classifier
 and predict the class that gets
 the most votes.
 - This majority-vote classifier is called a hard voting classifier.



Voting classifier

- If the classifiers are able to estimate class probabilities, then you can take them into account and get a **soft voting classifier**.
 - In scikit-learn, the individual classifiers has to have a predict proba() method
 - In such a case, voting = "soft".

Two-class classification problem

Multi-class classification problem

$$f_{1}(x) = p(\omega_{1}|x) = 0.8$$

$$f_{2}(x) = p(\omega_{1}|x) = 0.51$$

$$f_{3}(x) = p(\omega_{1}|x) = 0.1$$

$$f(x) = \frac{0.8 + 0.51 + 0.1}{3} = \frac{0.141}{3} = 0.047 < 0.5$$

$$\Rightarrow x \to \omega_{2}$$

$$f(x) = \begin{bmatrix} 0.05 \\ 0.15 \\ 0.71 \\ 0.09 \end{bmatrix}$$

$$f_{2}(x) = \begin{bmatrix} 0.05 \\ 0.71 \\ 0.09 \end{bmatrix}$$

$$f_{3}(x) = \begin{bmatrix} 0.05 \\ 0.15 \\ 0.71 \\ 0.09 \end{bmatrix}$$

$$f_1(x) = \begin{bmatrix} 0.05 \\ 0.15 \\ 0.71 \\ 0.09 \end{bmatrix} \quad f_2(x) = \begin{bmatrix} 0.26 \\ 0.12 \\ 0.43 \\ 0.25 \end{bmatrix} \quad f_3(x) = \begin{bmatrix} 0.03 \\ 0.51 \\ 0.29 \end{bmatrix}$$

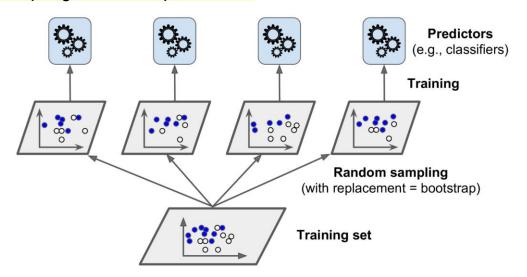
$$f(x) = \frac{1}{3} \begin{bmatrix} 0.05 & + & 0.20 & + & 0.17 \\ 0.15 & + & 0.12 & + & 0.03 \\ 0.71 & + & 0.43 & + & 0.51 \\ 0.09 & + & 0.25 & + & 0.29 \end{bmatrix} = \begin{bmatrix} 0.14 \\ 0.10 \\ 0.55 \\ 0.21 \end{bmatrix}$$

$$\Rightarrow x \to \omega_3$$

0.8167 # soft voting classif.

Bagging

- Apart from using different models and voting on the results, one can use the same model but trained on different random subsets of the training set:
 - Bagging (bootstrap aggregating): sampling with replacement (bootstrapping in statistics)
 - Pasting: sampling without replacement



- Once all predictors are trained, the ensemble can make a prediction for a new sample by simply aggregating the predictions for all:
 - statistical mode for classification
 - average for regression

Bagging

The following code trains an ensemble of **ntree** decision trees, each trained on 100 training samples randomly chosen from the training set with replacement

The bagging classifier automatically performs soft voting if the base classifier can

estimate class probabilities, e.g. decision trees

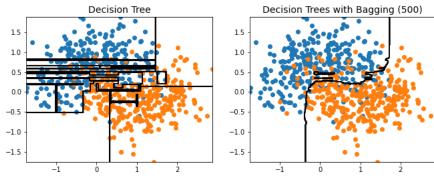
```
from sklearn.model_selection import train_test_split
from sklearn.datasets import make_moons
X, y = make_moons(n_samples=600, noise=0.4)
X_train, X_test, y_train, y_test =
    train_test_split(X, y, test_size=0.3)
```

```
from sklearn.tree import DecisionTreeClassifier
from sklearn.ensemble import BaggingClassifier

tree_clf = DecisionTreeClassifier()
tree_clf.fit(X_train, y_train)
y_pred_t = tree_clf.predict(X_test)
print(accuracy_score(y_test, y_pred_t))

bag_clf = BaggingClassifier(
   DecisionTreeClassifier(), n_estimators=ntree,
   max_samples=100, bootstrap=True, n_jobs=-1)
bag_clf.fit(X_train, y_train)
y_pred_e = bag_clf.predict(X_test)
print(accuracy_score(y_test, y_pred_e))
```

```
2.0
1.5
1.0
0.5
0.0
-0.5
-1.0
-1.5
```



```
0.8056 # tree classifier
0.8722 # bagging classifier (10)
0.8556 # bagging classifier (500)
```

Bagging

- With bagging, some instances may be sampled several times for any given predictor (because it is sampling with replacement), while others may not be sampled at all.
- The training samples that are not chosen are called out-of-bag (oob) samples.
- Since a predictor never sees the oob samples during training, it can be evaluated on these samples, without the need for a separate validation set, as this code shows:

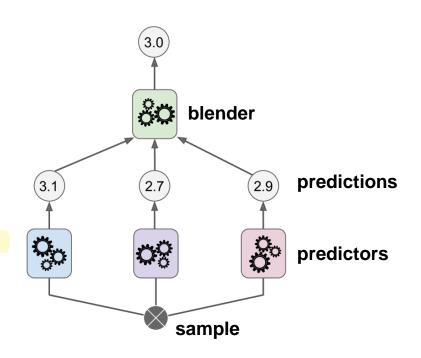
```
from sklearn.tree import DecisionTreeClassifier
from sklearn.ensemble import BaggingClassifier

bag_clf = BaggingClassifier(
   DecisionTreeClassifier(), n_estimators=500,
   max_samples=100, bootstrap=True, n_jobs=-1,
   oob_score=True)
bag_clf.fit(X_train, y_train)
print(bag_clf.oob_score_)
y_pred_e = bag_clf.predict(X_test)
print(accuracy_score(y_test, y_pred_e))

0.8690 # from OOB
0.8556 # from test set
```

 Bagging can be easily applied to regression problems (provided the base model is also a regression model):

- Stacking is a short form for stacked generalization
- Instead of using trivial functions (such as hard voting) to aggregate the predictions, this ensemble method trains a model to perform the aggregation
- By way of example, let us consider a regression task:
 - Each of the ensemble models,
 named as first-layer predictors,
 predict a different value: 3.1, 2.7, 2.9
 - The final predictor, named as blender,
 meta learner or second-layer predictor,
 takes these predictions as inputs and
 makes the final prediction 3.0

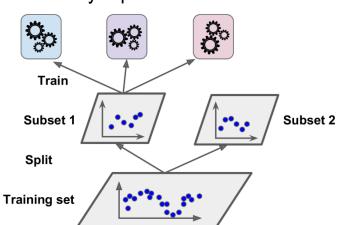


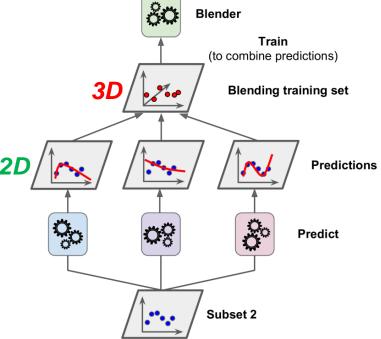
- Training can be accomplished in several ways:
 - by means of the hold-out set concept, leading to blending instead of stacking
 or
 - by means of out-of-fold predictions, giving rise to the stacking method itself
- Let us illustrate the **blending** method first: the holdout set concept splits the training set into two subsets, where

– the subset 1 is used for training the first-layer predictors

- the **subset 2** is used for training the blender

⇒ the blender learns to predict the target value given the first-layer predictions





Alberto Ortiz (last update 12/11/2023)

A python implementation of stacking follows: (moons dataset)

```
import numpy as np
from sklearn.linear_model import LogisticRegression
from sklearn.tree import DecisionTreeClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.ensemble import StackingClassifier
from sklearn.model_selection import train_test_split
```

```
X train, X test, y train, y test = train test split(X, y,
                                           test size=0.3)
# build layer 1
layer1 = []
layer1.append(('bc', GaussianNB()))
layer1.append(('lr', LogisticRegression()))
layer1.append(('dt', DecisionTreeClassifier()))
# build stack
layer2 = LogisticRegression(penalty=None)
ensemble clf = StackingClassifier(estimators=layer1,
                       final estimator=layer2, cv=5)-
# 1. train & evaluate individual classifiers
for name, model in layer1:
acc = model.fit(X train, y train).score(X test, y test)
print('%s %.3f' % (name, acc))
# 2. train & evaluate ensemble classifier
acc = ensemble clf.fit(X, y).score(X test, y test)
print('%s %.3f (%.3f)' % ('stacking',acc))
```

In this case, only the 2nd layer estimator is trained through cross-validation

```
bc 0.828
lr 0.822
dt 0.806
stacking 0.833
```

A python implementation of stacking follows: (moons dataset)

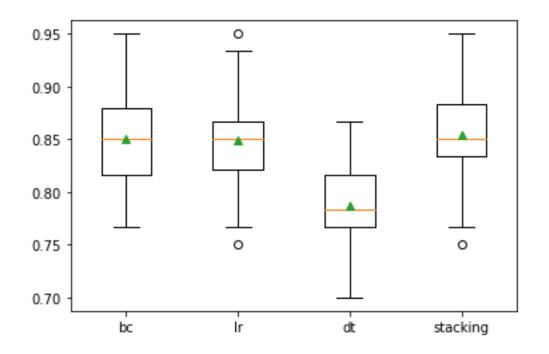
```
import numpy as np
from sklearn.linear_model import LogisticRegression
from sklearn.tree import DecisionTreeClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.ensemble import StackingClassifier
from sklearn.model_selection import cross_val_score
from sklearn.model_selection import RepeatedStratifiedKFold
```

```
# build layer 1
layer1 = []
layer1.append(('bc', GaussianNB()))
layer1.append(('lr', LogisticRegression()))
layer1.append(('dt', DecisionTreeClassifier()))
# build stack
layer2 = LogisticRegression(penalty=None)
ensemble clf = StackingClassifier(estimators=layer1,
                       final estimator=layer2, cv=5)
# 1. train & evaluate individual classifiers
for name, model in layer1:
scores = evaluate model(model, X, y)
print('%s %.3f (%.3f)' %
    (name, np.mean(scores), np.std(scores)))
# 2. train & evaluate ensemble classifier
scores = evaluate model(ensemble clf, X, y)
print('%s %.3f (%.3f)' %
   ('stacking', np.mean(scores), np.std(scores)))
```

30 evaluations!!

```
bc 0.850 (0.045)
lr 0.849 (0.045)
dt 0.796 (0.045)
stacking 0.852 (0.047)
```

• A python implementation of **stacking** follows (cont.)



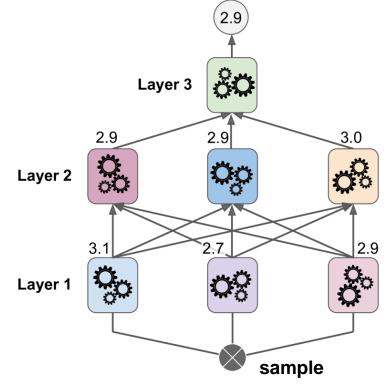
- Notice that the layer 2 can implement any form of aggregation:
 - Therefore, weighted average and even voting can be considered as particular cases of stacking, where the layer 2 implements (a) the average of the predictors' outputs and (b) a majority voting mechanism

• It is actually possible to train several blenders, e.g. using different classifiers, to get a

whole layer of blenders

 Now, the trick is to split the training set into three subsets:

- the 1st subset is used to train the first layer,
- the 2nd subset is used to create the training set for the second layer (using predictions made by the predictors of the first layer), and
- the 3rd subset is used to create the training set for the third layer (using predictions made by the predictors of the second layer)



 Once all this is done, we can make a prediction for a new sample by going through each layer sequentially

Contents

- Decision trees
- Regression trees
- Ensemble learning
- Random forests

• A random forest (RF) is an ensemble of decision trees, generally trained via the bagging method (sometimes pasting):

```
bag_clf = BaggingClassifier(
  DecisionTreeClassifier(), n_estimators=500, bootstrap=True, n_jobs=-1)
bag_clf.fit(X_train, y_train)
```

- It has proved so successful that this ensemble method has its own name and an optimized implementation:

```
from sklearn.ensemble import RandomForestClassifier
rf_clf = RandomForestClassifier(n_estimators=500, n_jobs=-1)
rf_clf.fit(X_train, y_train)
```

 With a few exceptions, an RF has all the hyperparameters of a DT, e.g. to control how trees are grown, plus all the hyperparameters of a bagging classifier to control the ensemble itself

- Actually, an RF introduces extra randomness when growing trees:
 - Instead of searching for the very best feature when splitting a node, it searches for the best feature among a random subset of features
 - This results in a greater tree diversity, and generally yielding an overall better model

```
rf_clf = RandomForestClassifier(n_estimators=500, n_jobs=-1)
rf_clf.fit(X_train, y_train)
```

```
bag_clf = BaggingClassifier(
  DecisionTreeClassifier(splitter="random"),
  n_estimators=500, max_samples=1.0, bootstrap=True, n_jobs=-1)
```

- splitter = "random" → choose the best split for a random subset of features
- max_samples = 1.0 → use all samples for training
- As expected, random forests can be used for both classification and regression

tasks

• An Extremely Randomized Trees ensemble (or Extra-Trees, ET, for short) incorporates more randomness than RF:

Instead of optimizing the threshold at each splitting, these thresholds are chosen randomly

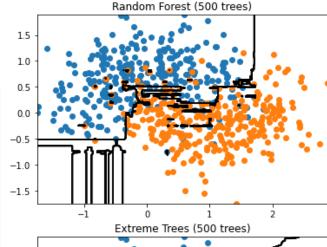
- This trades more bias for a lower variance
- It also makes ET much faster to train than regular RF

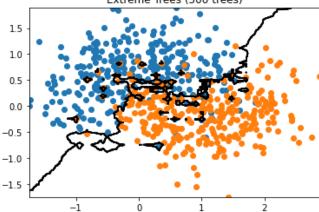
```
from sklearn.ensemble import RandomForestClassifier
from sklearn.ensemble import ExtraTreesClassifier

rf_clf = RandomForestClassifier(n_estimators=500, n_jobs=-1)
rf_clf.fit(X_train, y_train)
yp_rf = rf_clf.predict(X_test)
print(accuracy_score(y_test, yp_rf))

et_clf = ExtraTreesClassifier(n_estimators=500, n_jobs=-1)
et_clf.fit(X_train, y_train)
yp_et = et_clf.predict(X_test)
print(accuracy_score(y_test, yp_et))
```

```
0.8500 (time = 0.5806 \pm 0.0282 seconds, \pm 3\sigma)
0.8278 (time = 0.4552 \pm 0.0257 seconds, \pm 3\sigma)
```





- Yet another great quality of Random Forests is that they make it easy to measure the relative importance of each feature:
 - One can measure the importance of each feature by looking at how much the tree
 nodes that use that feature reduce impurity on average (across all trees in the forest)
 - More precisely, one can give a weighted average, where each node's weight is equal to the fraction of training samples associated with it

```
from sklearn.datasets import load_iris
from sklearn.ensemble import RandomForestClassifier

iris = load_iris()

rf_clf = RandomForestClassifier(n_estimators=500, n_jobs=-1)

rf_clf.fit(iris["data"], iris["target"])

for name, score in zip(iris["feature_names"],rf_clf.feature_importances_):
    print(name, score)
```

```
sepal length (cm) 0.1062
sepal width (cm) 0.0269
petal length (cm) 0.4434
petal width (cm) 0.4235
```

Lecture 3.3 Supervised learning: Decision Trees & Ensemble Learning



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