

Assignment 2, Question 1

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1a) $[X, Y \mid Z]$ and $[a, b, c \mid [d, e, Y]]$

Left side can be written as: $[X, Y \mid Z] = [X, Y, Z]$

Right side can be written as: $[a, b, c \mid [d, e, Y]] = [a, b, c, d, e, Y]$

Take $X = a, Y = b, Z = [c, d, e, b]$

Yes, given the variables above, the first list becomes $[a, b, c, d, e, b]$ and the second list becomes $[a, b, c, d, e, b]$ and the two lists match.

1b) $[q, [A \mid [r, s]], t]$ and $[q, [r, [r, s]] \mid B]$

Left side can be written as: $[q, [A, r, s], t]$

Right side can be written as: $[q, [r, [r, s]], B]$

Take $A = r, B = t$

Then the first list becomes $[q, [r, r, s], t]$ and the second list becomes $[q, [r, [r, s]], t]$ and the two lists do not match as $[r, r, s]$ does not equal $[r, [r, s]]$.

1c) $[[Cow \mid [cat, dog]], bird, bug, chicken]$ and $[[ant, [cat, dog]] \mid Horse]$

Left side: $[[Cow \mid [cat, dog]], bird, bug, chicken] = [[Cow, cat, dog], bird, bug, chicken]$

Right side: $[[ant, [cat, dog]] \mid Horse] = [[ant, [cat, dog]], Horse]$

$Cow = ant$

$Horse = [bird, bug, chicken]$

The two lists do not match. Even if Cow was assigned the value ant, then the expression on the left would be $[[ant, cat, dog], bird, bug, chicken]$, and the $[[ant, [cat, dog]], bird, bug, chicken]$ and the lists would not be the same.

1d) $[1, A, 2 \mid [A, 3, 4]]$ and $[B \mid [2, C \mid [D \mid E]]]$

Left side can be written as: $[1, A, 2, A, 3, 4]$

Right side can be written as: $[B, 2, C, D \mid E]$

Take $B = 1, A = 2, C = 2, D = 2, E = 3, 4$

Then the first list becomes $[1, 2, 2, 2, 3, 4]$ and the second list becomes $[1, 2, 2, 2, 3, 4]$ and the two lists match.

1e) $[A[A[A[A[A]]]]]$ and $[b|C]$

Left side: $[A[A[A[A[A]]]]] = [A, A[A[A[A]]]] = [A, A, [A[A]]] = [A, A, [A, A]]$

Right side: $[b|C]$

Take $A = b$ and $C = [b, [b, [b]]]$.

The left side becomes $[b, b, [b, [b]]]$ and the right side becomes $[b, b, [b, [b]]]$. The two sides match and the lists are equal with the given variables above.

1f) $[X | [Y | [Z | [X]]]]$ and $[all, around, the, world, Y]$

Left side: $[X | [Y | [Z | [X]]]] = [X | [Y | [Z, X]]] = [X | [Y, Z, X]] = [X, Y, Z, X]$

Take $X = all$, $Y = around$, $Z = the$, $X = World$

No, the lists are not equal because X is a single variable and can not represent two different values. The variable Y in the right list also does not map to any elements in the left list.

1g) $[1, 2 | [X | [Y, Z | X]]]$ and $[Q | [R, S, [], [Y]]]$

Left side: $[1, 2 | [X | [Y, Z | X]]] = [1, 2, X | [Y, Z | X]] = [1, 2, X, Y, Z | X]$

Right side: $[Q | [R, S, [], [Y]]] = [Q, R, S, [], [Y]]$

Take $Q = 1$,

$R = 2$,

$S = []$,

$Y = []$,

$Z = [Y] = [[]]$,

$X = []$

Then $[Q, R, S, [], [Y]] = [1, 2, [], [], [[]]]$ and $[1, 2, X, Y, Z | X] = [1, 2, [], [], [[]]]$

Yes, the two lists are equal using the variables above.

1h) $[Lions, [[and], tigers], [and], bears, oh | [[my]]]$ and $[[I, have], [[A], Bad], Feeling | [About | This]]$

Left side: $[Lions, [[and], tigers], [and], bears, oh, [my]]$

Right side = $[[I, have], [[A], Bad], Feeling, About | This] = [[I, have], [[A], Bad], Feeling, About, This]$

Take $Lions = [I, have]$, $A = and$, $Bad = tigers$, $Feeling = [and]$, $About = bears$, $This = [oh, [my]]$

Then $[[I, have], [[A], Bad], Feeling, About, This] = [[I, have], [[A], Bad], Feeling, About, This]$

Yes, the left side is equal to the right side given the variables above.