Sinus je neparna funkcija:  $\sin(-\alpha) = -\sin \alpha$ Kosinus je parna funkcija:  $\cos(-\alpha) = \cos \alpha$ 

Veze sa  $\pi, \frac{\pi}{2}, 2\pi...$ :

• 
$$\sin(\pi - \alpha) = \sin \alpha$$

• 
$$\cos(\pi - \alpha) = -\cos\alpha$$

• 
$$\sin(\pi + \alpha) = -\sin\alpha$$

• 
$$\cos(\pi + \alpha) = -\cos\alpha$$

• 
$$tg(\pi - \alpha) = -tg \alpha$$

• 
$$\operatorname{ctg}(\pi - \alpha) = -\operatorname{ctg}\alpha$$

• 
$$\sin(2\pi - \alpha) = -\sin\alpha$$

• 
$$\cos(2\pi - \alpha) = \cos \alpha$$

• 
$$tg(-\alpha) = -tg \alpha$$

• 
$$\operatorname{ctg}(-\alpha) = -\operatorname{ctg}\alpha$$

• 
$$\sin(\frac{\pi}{2} - \alpha) = \cos \alpha$$

• 
$$\cos(\frac{\pi}{2} - \alpha) = \sin \alpha$$

• 
$$tg(\frac{\pi}{2} - \alpha) = ctg \alpha$$

• 
$$\operatorname{ctg}(\frac{\pi}{2} - \alpha) = \operatorname{tg} \alpha$$

Peridičnost (za  $k \in \mathbb{Z}$ ):

• 
$$\sin(\alpha + 2k\pi) = \sin\alpha$$

• 
$$\cos(\alpha + 2k\pi) = \cos\alpha$$

• 
$$tg(\alpha + k\pi) = tg \alpha$$

• 
$$\operatorname{ctg}(\alpha + k\pi) = \operatorname{ctg}\alpha$$

Identiteti:

• 
$$\sin^2 \alpha + \cos^2 \alpha = 1$$

• 
$$\operatorname{tg} \alpha = \frac{\sin \alpha}{\cos \alpha}$$

• 
$$\operatorname{ctg} \alpha = \frac{\cos \alpha}{\sin \alpha}$$

Dvostruki ugao:

• 
$$\sin 2\alpha = 2\sin \alpha\cos \alpha$$

• 
$$\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$$

• 
$$\operatorname{tg} 2\alpha = \frac{2\operatorname{tg}\alpha}{1 - \operatorname{tg}^2\alpha}$$

• 
$$\operatorname{ctg} 2\alpha = \frac{\operatorname{ctg}^2 \alpha - 1}{2\operatorname{ctg} \alpha}$$

Trigonometrijske funkcije pola ugla:

$$\bullet \sin^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{2}$$

$$\bullet \cos^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{2}$$

• 
$$tg^2 \frac{\alpha}{2} = \frac{1 - \cos \alpha}{1 + \cos \alpha}$$

• 
$$\operatorname{ctg}^2 \frac{\alpha}{2} = \frac{1 + \cos \alpha}{1 - \cos \alpha}$$

## Proizvodi:

• 
$$\cos \alpha \cos \beta = \frac{1}{2}(\cos(\alpha + \beta) + \cos(\alpha - \beta))$$

• 
$$\sin \alpha \sin \beta = \frac{1}{2}(\cos(\alpha - \beta) - \cos(\alpha + \beta))$$

• 
$$\sin \alpha \cos \beta = \frac{1}{2}(\sin(\alpha + \beta) + \sin(\alpha - \beta))$$

Zbir trigonometrijskih funkcija:

• 
$$\cos \alpha + \cos \beta = 2\cos \frac{\alpha + \beta}{2}\cos \frac{\alpha - \beta}{2}$$

• 
$$\cos \alpha - \cos \beta = -2\sin \frac{\alpha + \beta}{2}\sin \frac{\alpha - \beta}{2}$$

• 
$$\sin \alpha + \sin \beta = 2 \sin \frac{\alpha + \beta}{2} \cos \frac{\alpha - \beta}{2}$$

• 
$$\sin \alpha - \sin \beta = 2 \sin \frac{\alpha - \beta}{2} \cos \frac{\alpha + \beta}{2}$$

• 
$$\operatorname{tg} \alpha \pm \operatorname{tg} \beta = \frac{\sin(\alpha \pm \beta)}{\cos \alpha \cos \beta}$$

• 
$$\operatorname{ctg} \alpha \pm \operatorname{ctg} \beta = \frac{\sin(\beta \pm \alpha)}{\sin \alpha \sin \beta}$$

Trigonometrijske funkcije od zbira uglova:

• 
$$\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$$

• 
$$\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$$

• 
$$\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$$

• 
$$\cos(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$$

• 
$$\operatorname{tg}(\alpha \pm \beta) = \frac{\operatorname{tg} \alpha \pm \operatorname{tg} \beta}{1 \mp \operatorname{tg} \alpha \operatorname{tg} \beta}$$

• 
$$\operatorname{ctg}(\alpha \pm \beta) = \frac{\operatorname{ctg} \alpha \operatorname{ctg} \beta \mp 1}{\operatorname{ctg} \beta \pm \operatorname{ctg} \alpha}$$