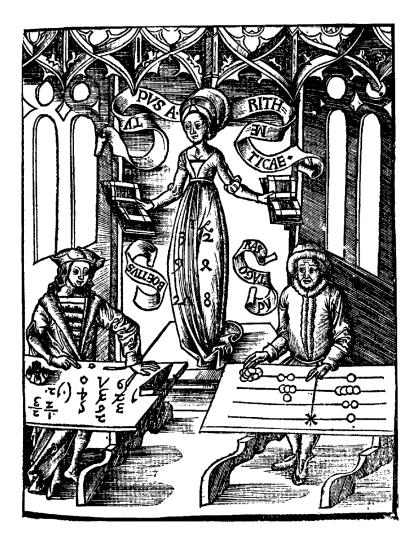
Cahier de calcul

— réponses —



Margarita philosophica (La perle philosophique), Gregor REISCH (1508)

Cette gravure, extraite d'un manuel d'université de l'époque, représente Arithmetica, allégorie des mathématiques, arbitrant une compétition entre Boèce, qui utilise les chiffres indo-arabes, et Pythagore, qui utilise un boulier.

Ce cahier de calcul a été écrit collectivement.

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Le pictogramme • de l'horloge a été créé par Ralf SCHMITZER (The Noun Project). L'illustration de la couverture vient de Wikimedia.

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Sommaire

Fiche nº 1. Fractions

Réponses

1.1 a) $ \frac{4}{5} $	1.3 c) $ \frac{-10}{3} $	$1.7 \dots \left[\frac{n^3 + n}{n+1} \right]$
1.1 b)	1.3 d)	1.8 a) $4 + \frac{5}{6}$
1.1 c)	1.4 $\left \frac{16}{35} \right $	6
1.1 d) $-2 \times 3^{3k-2}$	1.5 a)	1.8 b) $1 + \frac{1}{k-1}$
1.2 a)	1.5 b)	1.8 c) $3 + \frac{5}{x-2}$
1.2 b) $\left \frac{7}{15} \right $	1.5 c)	1.9 2t
1.2 c)	1.5 d)	1.10 a) $\left[\frac{3}{5} > \frac{5}{9}\right]$
1.2 d)	1.6 a) $\frac{-1}{n(n+1)^2}$	1.10 b)
1.3 a)	1.6 b)	1.10 c)
1.3 b) $\left\lfloor \frac{203}{24} \right\rfloor$		$\begin{array}{c c} 1.10 \text{ c} \\ \hline 25 \\ \hline \end{array} \begin{array}{c} -\frac{1}{21} \\ \hline \end{array}$
24	1.6 c) $\left[\frac{3}{2}n\right]$	1.11
		1.12 $\dots A > B$

Fiche nº 1. Fractions

Fiche nº 2. Puissances

Réponses

2.1 a) 10^8	2.2 b) 5^{-6}	2.3 b) $2^{21} \cdot 3$	2.5 a)
2.1 b)	2.2 c) 2^7	2.3 c) 2	
2.1 c) 10^2	2.2 d) $(-7)^{-2}$	2.3 d) $2^{38} \cdot 3^{26}$	2.5 b) $\left[\frac{1}{x-2}\right]$
2.1 d) 10^{-2}	2.2 e)	2.4 a)	2.5 c)
2.1 e)	2.2 f)	2.4 b)	
2.1 f)	2.3 a) $2^{-4} \cdot 3^{-1}$	2.4 c)	2.5 d) $\left \frac{2}{x-2} \right $
2.2 a) 15^4		2.4 d) $2^6 \cdot 5$	

2 Fiche n° 2. Puissances

Fiche nº 3. Calcul littéral

Réponses

3.1 a) $8x^3 - 6x^2 + \frac{3}{2}x - \frac{1}{8}$	3.4 c)
3.1 b) $x^5 - 2x^4 + x^3 - x^2 + 2x - 1$	3.4 d)
3.1 c)	
3.1 d) $x^5 + 2x^4 + x^3 - x^2 - 2x - 1$	3.4 e) $2\left(x + \frac{3 - \sqrt{233}}{4}\right)\left(x + \frac{3 + \sqrt{233}}{4}\right)$
3.1 e)	3.4 f) $-5(x-1)\left(x-\frac{1}{5}\right)$
3.1 f) $x^4 + x^2 + 1$	
3.2 a) $\boxed{-2 + 12x - 17x^2 + 8x^3 - 3x^4}$	3.5 a) $(x+y-z)(x+y+z)$
3.2 b)	3.5 b) $3(14x+3y)(-4x+y)$
3.2 c) $2 + x^3 - x^4 - x^5$	3.5 c) $(x+1)(y+1)$
3.2 d) $\boxed{-1 - 3x - 3x^2 + x^3}$	3.5 d) $(x-1)(y-1)$
3.2 e)	3.5 e) $(x+y)(x+1)^2$
3.2 f) $1 + 2x + 3x^2 + 2x^3 + x^4$	3.5 f) $(a^2 + b^2)(y - 4x^2)(y + 4x^2)$
3.3 a) $-6(6x+7)$	3.6 a)
3.3 b) $4(5x+4)(-5x+1)$	3.6 b) $-8(x^2+1)(x-4)(x+4)$
3.3 c)	3.6 c)
3.3 d) $ -8(x+1)(x+16) $	
	3.6 d)
3.4 a) $(x-1)^2$	3.6 e) $ (a^2 + b^2 + c^2 + d^2)(p^2 + q^2 + r^2 + s^2) $
3.4 b)	<u>, , , , , , , , , , , , , , , , , , , </u>

Fiche nº 3. Calcul littéral

Fiche nº 4. Racines carrées

Réponses

4.3 a) $2 - \sqrt{2} - \sqrt{3} + \frac{1}{2}\sqrt{6}$ **4.1** b)..... **4.1** c) $-\sqrt{3}+2$ **4.3** c) $1 - \sqrt{10} + \sqrt{15}$ **4.1** d) $\sqrt{7}$ – 2 **4.3** d) $\sqrt{15} + \sqrt{10} - \sqrt{6} - 2$ **4.1** e)..... $\pi - 3$ **4.3** e) $-(\sqrt{2}+\sqrt{3})$ **4.1** f) |3-a| $-\frac{3+\sqrt{2}+\sqrt{3}+\sqrt{6}}{}$ **4.3** f) **4.2** c) $1 + \sqrt{3}$ **4.3** h) $|50 - 25\sqrt{3}|$ **4.2** d) $3 + \sqrt{2}$ $\sqrt{2} + 2 - \sqrt{6}$ **4.2** g) **4.5** b) $|x - \sqrt{x^2 - 1}|$

4.7 c) $1 + \sqrt{2}$

4.7 e) $1 + \sqrt{5}$

4.7 f) $\ln(1+\sqrt{2})$

Fiche nº 4. Racines carrées

4.7 d).....

4.5 c) $1 + \sqrt{x-1}$

 $\overline{2} \overline{x-1}$

x(x-2)

Fiche nº 5. Expressions algébriques

5.1 a) $\boxed{7a^2 + 12a + 7}$	5.3 c) $\boxed{-4 + 43i\sqrt{5}}$	5.6 a) $a^2 - 2b$
5.1 b) $a^2 - a - 1$	5.3 d)	5.6 b)
5.1 c)	5.4 a)	5.6 c)
5.1 d) $-a^2 + 1$	5.4 b) 1	5.6 d)
5.2 a)	5.4 c)	5.6 e)
5.2 b)	5.4 d)	5.6 f) $\boxed{-2ac + b^2}$
5.2 c)	5.4 e)	5.7 a) $a^2b - ac - 2b^2$
5.2 d)	5.4 f)	5.7 b) $a^4 - 4a^2b + 4ac + 2b^2$
5.3 a)	5.5 a)	5.7 c)
5.3 b)	5.5 b) $a^3 + 3a$	5.7 d) 1
2101	5.5 c)	5.7 e)

Fiche nº 6. Équations du second degré

6.1 a)	6.4 c) $m \operatorname{donc} -(m+a+b)$
6.1 b)	6.4 d) $m \operatorname{donc} m(a-b)/(b-c)$
6.1 c)	6.4 e)
6.1 d)	6.4 f) $a + b$ puis $2ab/(a + b)$.
6.1 e)	6.5 a) $x^2 - 22x + 117 = 0$
6.1 f)	6.5 b) $x^2 - 6x - 187 = 0$
6.1 g)	6.5 c) $x^2 - 4x + 1 = 0$
6.1 h)	6.5 d) $x^2 - 2mx + 3 = 0$
6.1 i)	6.5 e) $2x^2 - (4m+1)x + (2m^2 + m - 15) = 0$
6.1 j)	6.5 f) $m^2x^2 + (m-2m^2)x + (m^2-m-2) = 0$
6.2 a)	6.6 a) $m = -3/4$ et $x = 3/4$
6.2 c)	6.6 b) $m = -1$ et $x = -2$, ou $m = 7$ et $x = 2/3$
6.2 d)	6.6 c) $m = 1$ et $x = -1$ ou $m = -1$ et $x = 1$
6.2 e)	6.7 a) $a = 2$ et $b = 3$
6.2 f)	6.7 b) $a = -2$ et $b = 1$
6.3 a)	6.7 c)
6.3 b)	6.7 d) $a = 1/2$ et $b = 8$
6.3 c)	6.7 e)
6.3 d)	6.8 a) $]-\infty,1] \cup [\sqrt{2},+\infty[]$
6.4 a)	6.8 b) [-3,5]
6.4 b)	6.8 c) $] - \infty, -1] \cup [2/3, +\infty[]$
	6.8 d) $] - \infty, -1/2[\cup [4, +\infty[]]$

Fiche nº 7. Exponentielle et logarithme

7.1 a)	7.5 b)	7.8 a)
7.1 b)	7.5 c)	7.8 b) ok 7.8 c) 1
7.1 d) $ \frac{1}{2} \ln 2 $	7.5 d) $ \frac{1}{9} $	7.8 d)
7.1 e) $3 \ln 2$ 7.1 f) $2 \ln 2 + 2 \ln 3$	7.5 e) $-\frac{1}{2}$	7.9 b) $\frac{\mathrm{e}^x}{\sqrt{1+x}}$
7.2 a)	7.5 f)	7.9 c)
7.2 b) $2 \ln 3 - 2 \ln 2$ 7.2 c) $\ln 3 + 11 \ln 2$	7.6 a)	7.9 d) $\left[-\frac{1}{1+x} \right]$
7.2 d) $3 \ln 5 + 2 \ln 2$	7.6 b)	7.9 e) $e^{x \ln(1+x)}$
7.2 e)	7.6 c)	7.10 a) $x \ge \frac{\ln 12 + 5}{3}$
7.2 f) $2 \ln 5 - 2 \ln 2$ 7.3 $-2 \ln 2 - 2 \ln 5$	7.6 d)	7.10 b)
7.4 a) $\left[\frac{25}{8}\ln(\sqrt{2}-1)\right]$	7.6 f)	7.10 c) $x \ge \frac{2}{e}$
7.4 b) $17 + 12\sqrt{2}$	7.7 a) impaire 7.7 b) impaire	7.10 d) $x \ge -\frac{1}{12}$
7.4 c)	7.7 c) [impaire]	7.10 e)
7.4 d)	7.7 d) [impaire]	7.10 f) $ \frac{-13 - \sqrt{273}}{2} $

Fiche nº 8. Trigonométrie

8.1 a)	8.7 b) $\left[\left\{ \frac{-2\pi}{3}, \frac{-\pi}{3} \right\} \right]$
8.1 c) $-1 - \sqrt{3}$	8.7 b) $\left\{ \frac{4\pi}{3} + 2k\pi, k \in \mathbb{Z} \right\} \cup \left\{ \frac{5\pi}{3} + 2k\pi, k \in \mathbb{Z} \right\}$
8.1 d)	8.7 c)
8.2 a)	
8.2 b) $ -\sin x $	8.7 c) $\left \left\{ -\frac{5\pi}{6}, -\frac{\pi}{6} \right\} \right $
8.2 c)	
8.2 d)	8.7 c) $\left\{ \frac{7\pi}{6} + 2k\pi, k \in \mathbb{Z} \right\} \cup \left\{ \frac{11\pi}{6} + 2k\pi, k \in \mathbb{Z} \right\} $
8.3 a) $\frac{\sqrt{6} - \sqrt{2}}{4}$	8.7 d) $\left[\frac{\pi}{4}, \frac{5\pi}{4}\right]$
8.3 b) $ \frac{\sqrt{6} + \sqrt{2}}{4} $	8.7 d) $\left[\frac{-3\pi}{4}, \frac{\pi}{4} \right]$
8.3 c)	8.7 d) $\left\{\frac{\pi}{4} + k\pi, k \in \mathbb{Z}\right\}$
8.3 d)	8.7 e) $\left[\frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}\right]$
8.4 a)	8.7 e) $\left\{-\frac{3\pi}{4}, -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}\right\}$
8.4 b) $\frac{1}{\cos x}$ 8.4 c) 0	8.7 e)
8.4 d) $4\cos^3 x - 3\cos x$	8.7 f) $\left[\left\{ \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}, \frac{11\pi}{6} \right\} \right]$
8.5 a) $\frac{\sqrt{2+\sqrt{2}}}{2}$	8.7 f) $\left\{ -\frac{5\pi}{6}, -\frac{\pi}{6}, \frac{\pi}{6}, \frac{5\pi}{6} \right\}$
8.5 b)	8.7 f) $\left\{\frac{\pi}{6} + k\pi, k \in \mathbb{Z}\right\} \cup \left\{\frac{5\pi}{6} + k\pi, k \in \mathbb{Z}\right\}$
8.6 a) $\tan x$	$\boxed{ \left(\begin{array}{cccccccccccccccccccccccccccccccccccc$
8.6 b)	8.7 g) $\left \left\{ \frac{\pi}{12}, \frac{11\pi}{12}, \frac{13\pi}{12}, \frac{23\pi}{12} \right\} \right $
8.6 c) $8\cos^4 x - 8\cos^2 x + 1$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
8.7 a)	8.7 g) $\left\{-\frac{11\pi}{12}, -\frac{\pi}{12}, \frac{\pi}{12}, \frac{11\pi}{12}\right\}$
	8.7 g) $\left\{ \frac{\pi}{12} + k\pi, k \in \mathbb{Z} \right\} \cup \left\{ \frac{11\pi}{12} + k\pi, k \in \mathbb{Z} \right\}$
8.7 a) $\left\{-\frac{\pi}{3}, \frac{\pi}{3}\right\}$	8.7 h)
8.7 a) $\left\{ \frac{\pi}{3} + 2k\pi, k \in \mathbb{Z} \right\} \cup \left\{ -\frac{\pi}{3} + 2k\pi, k \in \mathbb{Z} \right\}$	
8.7 b)	8.7 h)

8.7 h).....
$$\left\{ \frac{\pi}{6} + k \frac{2\pi}{3}, k \in \mathbb{Z} \right\}$$

8.7 i)
$$\left\{ \frac{\pi}{7}, \frac{13\pi}{7} \right\}$$

8.7 i).....
$$\left\{ \frac{\pi}{7} + 2k\pi, k \in \mathbb{Z} \right\} \cup \left\{ -\frac{\pi}{7} + 2k\pi, k \in \mathbb{Z} \right\}$$

8.7 j).....
$$\left\{ \frac{5\pi}{14}, \frac{9\pi}{14} \right\}$$

8.7 j).....
$$\left\{ \frac{5\pi}{14} + 2k\pi, k \in \mathbb{Z} \right\} \cup \left\{ \frac{9\pi}{14} + 2k\pi, k \in \mathbb{Z} \right\}$$

8.8 b)
$$\left[\left[-\pi, -\frac{\pi}{3} \right] \cup \left[\frac{\pi}{3}, \pi \right] \right]$$

8.8 c)
$$\left[0, \frac{\pi}{6}\right] \cup \left[\frac{5\pi}{6}, 2\pi\right]$$

8.8 d)
$$\left[\left[0, \frac{\pi}{6} \right] \cup \left[\frac{5\pi}{6}, \frac{7\pi}{6} \right] \cup \left[\frac{11\pi}{6}, 2\pi \right] \right]$$

8.8 d).....
$$\left[\left[-\pi, -\frac{5\pi}{6} \right] \cup \left[-\frac{\pi}{6}, \frac{\pi}{6} \right] \cup \left[\frac{5\pi}{6}, \pi \right] \right]$$

8.8 f)
$$\boxed{ \left[\frac{\pi}{4}, \frac{\pi}{2} \left[\cup \right] \frac{\pi}{2}, \frac{3\pi}{4} \right] \cup \left[\frac{5\pi}{4}, \frac{3\pi}{2} \left[\cup \right] \frac{3\pi}{2}, \frac{7\pi}{4} \right] }$$

8.8 f)
$$\left[-\frac{3\pi}{4}, -\frac{\pi}{2} \left[\cup \right] - \frac{\pi}{2}, -\frac{\pi}{4} \right] \cup \left[\frac{\pi}{4}, \frac{\pi}{2} \left[\cup \right] \frac{\pi}{2}, \frac{3\pi}{4} \right]$$

8.8 h)
$$\left[0, \frac{3\pi}{8}\right] \cup \left[\frac{7\pi}{8}, \frac{11\pi}{8}\right] \cup \left[\frac{15\pi}{8}, 2\pi\right]$$

Fiche nº 9. Dérivation

Réponses

9.1 a)
$$6x^2 + 2x - 11$$

9.1 b)
$$5x^4 - 6x^2 + 4x - 15$$

9.1 c)
$$(2x^2 - 2x + 10) \exp(2x)$$

9.2 a)
$$5(x^2 - 5x)^4 (2x - 5)$$

9.2 d).....
$$-3(3\cos(x) - \sin(x))^2(3\sin(x) + \cos(x))$$

9.3 a)
$$\frac{2x}{x^2+1}$$

9.3 b)
$$\frac{1}{x \ln(x)}$$

9.3 c)
$$(-2x^2 + 3x + 1) \exp(x^2 + x)$$

9.3 d)
$$6\cos(2x)\exp(3\sin(2x))$$

9.4 a)
$$\left| \frac{6x}{(x^2+1)^2} \cos\left(\frac{2x^2-1}{x^2+1}\right) \right|$$

9.4 b)
$$\frac{2x^2 + 2x - 8}{(x^2 + 4)^2} \sin\left(\frac{2x + 1}{x^2 + 4}\right)$$

9.4 c)
$$\frac{\cos(x)}{2\sqrt{\sin(x)}}$$

$$9.4 \text{ d}) \dots \qquad \qquad \boxed{\frac{\cos(\sqrt{x})}{2\sqrt{x}}}$$

9.5 a)
$$\frac{(2x+3)(2\sin(x)+3)-(x^2+3x)\times 2\cos(x)}{(2\sin(x)+3)^2}$$

9.5 c).....
$$-2\frac{(x^2+1)\sin(2x+1)+x\cos(2x+1)}{(x^2+1)^2}$$

9.5 d).....
$$\frac{(4x+3)\ln(x) - 2x - 3}{(\ln(x))^2}$$

9.6 b)
$$\frac{9}{(9-x^2)\sqrt{9-x^2}}$$

9.6 d)
$$\frac{x\cos(x) - \sin(x)}{x\sin(x)}$$

9.7 a)
$$\frac{10x-5}{(3-x)^2(2+x)^2}$$

9.7 c)
$$\frac{2x^2 + 2x + 5}{(x+2)(x-1)^2}$$

9.7 d)
$$\frac{x^2}{(x+1)^2}$$

9.7 e)
$$\frac{2}{x(1-\ln(x))^2}$$

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Fiche no 10. Primitives

Réponses

10.1 a)	10.5 c) $ -\ln \cos t $
10.1 b) $ -\frac{3}{t+2} $	10.5 d)
3	10.5 e)
10.1 c) $\left[-\frac{\sigma}{2(t+2)^2} \right]$	10.5 f) $\left \frac{1}{\pi} \sin(\pi \ln t) \right $
10.1 d) $\left[-\frac{\cos(4t)}{4} \right]$	10.5 g) $\tan t - t$
10.2 a) $ \frac{2}{3}(1+t)^{\frac{3}{2}} - \frac{3}{4}t^{\frac{4}{3}} $	10.5 h) $\frac{1}{2} \tan^2 t + \ln \cos t $
10.2 b)	10.5 i)
10.2 c) $ \frac{1}{2} Arcsin(2t) $	10.5 j) $2\sqrt{\tan t}$
10.2 d $\boxed{\frac{1}{3} \operatorname{Arctan}(3t)}$	10.5 k) $\left[-\frac{1}{\tan t} \right]$
	10.5 l) $ \frac{1}{2} \frac{1}{(1-\sin t)^2} $
10.3 a)	
10.3 b) $\left \frac{1}{6} (1 + 2t^2)^{\frac{3}{2}} \right $	10.5 m) $\left\lfloor \frac{1}{2} \operatorname{Arctan}(2t) \right\rfloor$
10.3 c)	10.5 n
10.3 d)	10.5 o) $\left[\frac{1}{2}(Arcsin(t))^2\right]$
1	10.5 p) $\ln \operatorname{Arcsin}(t) $
10.3 e)	10.6 a) $ \frac{t}{2} + \frac{\sin(2t)}{4} $
10.3 f) $\left[-\frac{1}{(1+3t^2)^2} \right]$	10.6 b)
10.4 a)	10.6 c) $-\cos t + \frac{1}{3}\cos^3 t$
10.4 b)	10.6 d) $\ln(1 + \sin^2 t)$
10.4 c) $\frac{2}{(3-e^{2t})^2}$	10.6 e)
10.4 d)	10.6 f) $-\cot nt + \tan t$
10.4 d)	10.6 g) $\frac{1}{4} \ln \tan 2t $
10.4 f) $-e^{\frac{1}{t}}$	10.7 a) $t + \ln t - \frac{1}{t}$
10.5 a) $-\frac{1}{3}\cos^3 t$	10.7 b) $\ln t - \frac{1}{2t^2}$
10.5 b)	2t2

Fiche n° 10. Primitives

12 Fiche n° 10. Primitives

Fiche nº 11. Calcul d'intégrales

11.1 a) Positif	11.3 e) $ -\frac{1}{30} $	11.5 e)	11.7 c) e^2
11.1 b)		11.5 f) $\boxed{\frac{1}{2} - \frac{\sqrt{3}}{2}}$	11.7 d)
11.1 c)	11.3 f) $-\frac{2}{101}$	11.6 a)	11.7 e)
11.2 a)	11.4 a)	<u> </u>	
11.2 b)	11.4 b)	11.6 b)	11.7 f) $\left \frac{5}{8} \right $
11.2 c) $\left\lfloor \frac{147}{2} \right\rfloor$	11.4 c) $\boxed{\frac{1}{2}}$	11.6 c) $\left[\ln\left(\frac{2}{\sqrt{3}}\right)\right]$	11.8 a)
11.2 d)	11.4 d)	11.6 d) $ \frac{1}{384} $	11.8 b) $\left \frac{\pi}{4} \right $
11.2 e)	11.4 e) $e^2 - e^{-3}$		11.8 c)
11.2 f) $\left \frac{5}{2} \right $	11.4 f)	11.6 e) $\left[\frac{1}{2}\left(1-\frac{1}{e}\right)\right]$	
11.3 a)	11.5 a)	11.6 f)	$11.8 \text{ d}) \dots \qquad \boxed{\frac{e - \frac{1}{e}}{2}}$
11.3 b)	11.5 b) $2(e^3 - 1)$		2
11.3 c)	11.5 c) . $\left[\frac{1}{\pi}\ln\left(1+\frac{\pi}{2}\right)\right]$	11.7 a) $\left[\frac{1}{2} - \frac{1}{e+1}\right]$	11.8 e) $\left[\frac{2}{3}\right]$
	n (2)	11.7 b)	11.8 f) $\left \frac{2\pi}{9} \right $
11.3 d)	11.5 d) $\frac{\sqrt{2}}{6}$	2	

Fiche nº 12. Intégration par parties

12.1 d)
$$\frac{(\ln(2))^2 2^{\ln(2)} - 2\ln(2) - 2^{\ln(2)} + 2}{(\ln(2))^2}$$

12.1 g)
$$\ln(2) - 2 + \frac{\pi}{2}$$

12.1 h)
$$\left| \frac{\pi}{4} - \frac{1}{2} \right|$$

12.1 i)
$$\left| \frac{\pi}{12} + \frac{\sqrt{3}}{2} - 1 \right|$$

12.1 j)
$$\left| -\frac{2\sqrt{2}}{3} + \frac{4}{3} \right|$$

12.1 l)
$$\frac{\pi}{4} - \frac{1}{2} \ln 2 - \frac{\pi^2}{32}$$

12.2 a)
$$\begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto (-x+2)e^x \end{cases}$$

12.2 b)
$$\begin{cases} \mathbb{R}_+^* \to \mathbb{R} \\ x \mapsto -\frac{1 + \ln x}{x} \end{cases}$$

12.2 c)
$$\begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto x \arctan(x) - \frac{1}{2} \ln(1 + x^2) \end{cases}$$

12.2 d)
$$\begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto x \operatorname{sh}(x) - \operatorname{ch}(x) \end{cases}$$

$$[2.3 \text{ a}] \dots$$
 $\left[\frac{5}{2} - e^2\right]$

12.3 b)
$$\frac{e^{\frac{\pi}{2} + 1}}{2}$$

12.4 a)...
$$\begin{cases} \mathbb{R} \to \mathbb{R} \\ x \mapsto \frac{1}{2}(-\cos(x)\operatorname{sh}(x) + \sin(x)\operatorname{ch}(x)) \end{cases}$$

12.4 c).....
$$\begin{cases} \mathbb{R}_{+}^{*} \to \mathbb{R} \\ x \mapsto x^{3} \left(\frac{1}{3} \ln^{2} x - \frac{2}{9} \ln x + \frac{2}{27} \right) \end{cases}$$

12.4 d) ..
$$\begin{cases}]-1,1[\to \mathbb{R} \\ x \mapsto \frac{1}{2}e^{\arccos(x)}\left(x-\sqrt{1-x^2}\right) \end{cases}$$

Fiche nº 13. Changements de variable

13.1 a)	13.2 e)
13.1 b)	13.2 f) $ \frac{1}{2} \ln \frac{5}{2} $
13.1 c) $2\arctan(e) - \frac{\pi}{2}$	13.3 a)
13.1 d)	13.3 b) $ -2((\sqrt{3}-1)\ln(\sqrt{3}-1)-4+2\sqrt{3}) $
13.1 e) $ \frac{1}{12} $	13.4 a) $\left\{ \begin{array}{ccc} \left[0, \frac{\pi}{2} \right] & \to & \mathbb{R} \\ x & \mapsto & \tan x + \ln \tan(x) \end{array} \right]$
13.1 f)	13.4 b)
13.2 a) $\frac{\pi}{3\sqrt{3}}$	13.4 c) $ \begin{bmatrix} \mathbb{R}_+^* & \to & \mathbb{R} \\ x & \mapsto & 2\arctan(\sqrt{e^x - 1}) \end{bmatrix} $
13.2 b)	13.4 d) $ \begin{bmatrix} \mathbb{R}_{+}^{*} \rightarrow \mathbb{R} \\ x \mapsto \frac{3}{2}\ln(x^{\frac{2}{3}} + 1) \end{bmatrix} $
13.2 c)	
13.2 d)	13.4 e) $ \begin{cases} 1, +\infty[\rightarrow \mathbb{R} \\ x \mapsto \arctan \sqrt{x^2 - 1} \end{cases} $

Fiche nº 14. Intégration des fractions rationnelles

14.1 a)
$$\ln\left(\frac{3}{2}\right)$$

14.2 a)
$$2 \ln \frac{9}{10}$$

14.2 b)
$$\ln(a+1)$$

14.3 a)......
$$\frac{3}{2} + \ln(3) - \ln(2)$$

14.3 b).....
$$-\frac{1}{48} + \frac{51}{64} \ln \frac{21}{19}$$

14.4 a)
$$\ln\left(\frac{7}{3}\right)$$

14.4 b)
$$\ln \frac{33}{28}$$

14.5 a)
$$\ln\left(2\sqrt{\sqrt{2}-1}\right)$$

14.5 b)
$$\left[\frac{1}{2a}\ln\left(\frac{a+1}{2}\right)\right]$$

14.6 b)
$$A = -1$$
 et $B = 1$

14.6 c)
$$2 \ln \frac{4}{3}$$

14.7 a)
$$\ln \frac{1}{3}$$

14.7 b)
$$2 \ln \frac{4}{3}$$

14.7 c)
$$\frac{1}{2} \ln \frac{3}{2}$$

14.7 d)
$$\frac{1}{4} \ln \frac{1}{5}$$

14.8
$$\frac{1}{2\sqrt{a}} \ln \left(\frac{\sqrt{a} - a}{a + \sqrt{a}} \right)$$

14.9 a).....
$$a$$
 $a^2 + x^2$

14.9 b)
$$\left| \frac{1}{a} \arctan \left(\frac{x}{a} \right) \right|$$

14.10 a)
$$\frac{\pi}{4}$$

14.10 b)
$$\frac{\pi}{6\sqrt{3}}$$

$$14.11 \quad \dots \qquad \boxed{\frac{\pi}{2\sqrt{2}}}$$

14.12 a)......
$$\left(x+\frac{1}{2}\right)^2+\frac{3}{4}$$

14.12 b)
$$2\left(x-\frac{3}{4}\right)^2-\frac{1}{8}$$

14.12 c)..
$$\sqrt{2}(x+\frac{1}{4})^2 + \sqrt{2}\frac{15}{16}$$

14.12 d)....
$$a(x+\frac{a}{2})^2 + \frac{3a^3}{4}$$

14.13 a)
$$\frac{1}{2}$$

14.13 b)
$$\frac{2\pi}{3\sqrt{3}}$$

14.13 d)
$$\ln(2)$$

14.14 a)
$$\frac{\pi}{12}$$

14.14 b)
$$\ln\left(\frac{a^2}{a^2-1}\right)$$

14.15
$$\frac{1}{3} \left(\ln(2) + \frac{\pi}{\sqrt{3}} \right)$$

Fiche nº 15. Systèmes linéaires

Fiche no 16. Nombres complexes

16.1 a)
$$\boxed{4 + 32i}$$

16.1 e) . .
$$\boxed{-119 + 120i}$$

16.1 f)
$$\left[\frac{3}{10} + \frac{1}{10}i\right]$$

16.1 g)
$$\left[\frac{4}{29} - \frac{19}{29}i\right]$$

16.1 h)
$$\left| \frac{1}{2} - \frac{\sqrt{3}}{2} i \right|$$

16.2 c)
$$\sqrt{3}e^{i\frac{\pi}{2}}$$

16.2 d)
$$2e^{-i\frac{\pi}{2}}$$

16.2 e)
$$2e^{i\frac{8\pi}{5}}$$

16.2 f)
$$5\sqrt{2}e^{-i\frac{\pi}{4}}$$

16.2 h)
$$2\cos(\frac{\pi}{12})e^{i\frac{\pi}{4}}$$

16.3 b) ...
$$\boxed{\frac{1}{\sqrt{2}} + i\frac{1}{\sqrt{2}}}$$

16.3 c)..
$$-\frac{1}{\sqrt{2}} - i\frac{1}{\sqrt{2}}$$

Fiche nº 17. Trigonométrie et nombres complexes

Fiche no 18. Sommes et produits

Réponses

18.3 b) $3^{\frac{n(n+1)}{2}}$	18.6 d) $\frac{n+1}{2n}$
18.3 d) $5^n(n!)^{\frac{3}{2}}$	18.7 a)
18.4 a) $\boxed{\frac{n(n+1)}{2}}$	18.7 b) $ \frac{1}{2} - \frac{1}{n+3} $
18.4 b)	18.8 a)
18.4 c) $n2^{n+1} + 2(1-2^n)$	18.8 b) $n(3n+1)$
18.4 d) $\frac{n^2(n+1)^2}{4}$	18.9 a) $n^2(n+1)$
18.5 a) $(n+2)^3 - 2^3$ 18.5 b) $\ln(n+1)$	18.9 b) $n(n+3)$
18.5 c) $1 - \frac{1}{(n+1)!}$	18.9 c)
18.5 d) $(n+1)!-1$	18.9 d) $ \frac{n(n+1)(7n^2+13n+4)}{12} $
18.6 a) $n+1$ 18.6 b) $1-4n^2$	18.9 e)
18.6 c)	18.9 f) $n(n+1)(4n-1)$

Fiche nº 19. Coefficients binomiaux

19.1 a)	19.3 b)	19.5 d) 12×15^n
19.1 b) $ \frac{720}{30} $	19.3 c)	19.6 a) $2 \times \sum_{p=0}^{\lfloor \frac{n}{2} \rfloor} \binom{n}{2p}$
19.1 d)	19.3 d) $(n+2)(n+1)$	19.6 b)
19.1 e)	10 3 a)	19.7 a) 2^n
19.1 f)	19.3 e) $\left[\frac{1}{(n+1)!}\right]$	19.7 b)
19.2 a) $ \frac{9!}{5!} $	19.3 f) $\boxed{\frac{n! \times (n-3)}{2^{2n+2}}}$	19.7 c) $n(n+1)2^{n-2}$
19.2 b) $\binom{9}{4}$	19.4 a)	19.7 d) $\left\lfloor \frac{2^{n+1}-1}{n+1} \right\rfloor$
19.2 c) $2^n \times n!$	19.4 b) $\boxed{\frac{3(3n+2)(3n+1)}{a^3(n+1)^2}}$	19.8 a)
19.2 d) $\left[\frac{(2n+1)!}{2^n \times n!} \right]$	19.5 a)	19.8 b) $ \sum_{k=0}^{n} \binom{n}{k}^{2} $
19.3 a) $ \frac{n(n-1)}{2} $	19.5 b)	k=0 (h)
2	19.5 c)	19.8 c) $\binom{2n}{n}$

Fiche n^o 20. Manipulation des fonctions usuelles

•		
20.1 a) $ \frac{\pi}{6} $	20.4 d) $\frac{\ln(4)}{\ln(20/3)}$	20.7 e) $\left[\ln(3+\sqrt{10}),\right[$
20.1 b)	$ \frac{\ln\left(\frac{\sqrt{17}-1}{2}\right)}{\ln\left(\frac{\sqrt{17}-1}{2}\right)} $	20.7 f)
20.1 c)	20.5 a) $\frac{\ln(\frac{-2}{2})}{\ln(2)}$	20.8 a) $x \mapsto \ln(2) \times 2^x + 2x$
20.1 d) $ \frac{\pi}{6} $	20.5 b) $\left\{0; \frac{1}{2}\right\}$	20.8 b). $x \mapsto \frac{15^x \ln(3/5) + 3^x \ln(3)}{(5^x + 1)^2}$
20.1 e)	20.5 c) $1 - \frac{\ln(2)}{\ln(3)}$	20.8 c) $x \mapsto (\ln(x) + 1)x^x$
20.1 f) $\left[\frac{\pi}{3}\right]$	$\ln\left(\frac{\sqrt{5}-1}{2}\right)$	20.8 d). $x \mapsto \frac{\pi}{2\sqrt{1-x^2}\arccos(x)^2}$.
20.2 a)	20.5 d) $\left \frac{\binom{2}{-\ln(3)}}{\ln(3)} \right $	20.9 a) $x \mapsto 2x \frac{1}{\sqrt{1-x^4}}$
20.2 b)	20.6 a)	$\sqrt{1-x^4}$
20.2 c) $\left \frac{5}{4} \right $	20.6 b)	20.9 b) $x \mapsto \text{ch}^{2}(x) + \text{sh}^{2}(x)$
20.2 d)	20.6 c) $ \left\{ \frac{\pi}{2} + k\pi, \ k \in \mathbb{Z} \right\} $	20.9 c) $x \mapsto \frac{1 - \text{th}^2(x)}{1 + \text{th}^2(x)}$
20.2 e)	20.6 d). $ \left\{ \frac{\pi}{3} + 2k\pi, \ k \in \mathbb{Z} \right\} $ $ \cup \left\{ \frac{2\pi}{3} + 2k\pi, \ k \in \mathbb{Z} \right\} $	20.9 d) $x \mapsto \operatorname{sh}(x)\operatorname{ch}(\operatorname{ch}(x))$ 20.10 a) $x \mapsto 0$
20.2 f)	20.6 e) $ \begin{cases} \frac{1}{3} + 2k\pi, \ k \in \mathbb{Z} \\ 0 \\ \left\{ \pi - \frac{1}{3} + 2k\pi, \ k \in \mathbb{Z} \right\} \end{cases} $	20.10 b)
20.3 a) $sh(x + y)$	20.6 f)	20.11 a) $x \mapsto (\ln(x) + 1)x^x e^{-x^{2x}}$
20.3 b) $ \cosh(x+y) $	20.7 a). $\left[\{ \ln(\sqrt{5} - 2); \ln(\sqrt{5} + 2) \} \right]$	20.11 b). $x \mapsto \frac{\operatorname{sh}(x)}{\operatorname{ch}(x)^2} \frac{1}{2\sqrt{\ln(\operatorname{ch}(x))}}$
20.4 a)	20.7 b) $\ln(1+\sqrt{2})$	20.11 c)
20.4 b)	20.7 c) $\frac{1}{2} \ln(2)$	20.11 d) $x \mapsto \arctan(x)$
20.4 c) $-\frac{\ln(3)}{\ln(2)}$	20.7 d). $\left[-\ln(4+\sqrt{15}), \ln(4+\sqrt{15})\right]$	

Fiche nº 21. Suites numériques

21.1 a)	21.9 a)
21.1 b)	$2 \ 001$ 21.9 b) $11\sqrt{5}$
21.1 c) $\left \frac{(2n+5) \cdot 2^{n+3}}{5} \right $ 21.6 d)	10 201
,	21.10 a) $3^n + (-2)^n$
21.1 d) $\boxed{\frac{3(2n+1) \cdot 2^{3n+2}}{5}}$ 21.7 a)	21.10 b)
21.2 a)	$\left[\frac{1}{24} \right]$ 21.11 a) $\left[\frac{(1+\sqrt{2})^n - (1-\sqrt{2})^n}{2} \right]$
21.2 b)	$\boxed{\frac{3}{512}}$ 21.11 b)
21.3 a) $2^{\frac{1}{8}}$	3069 21.12 a)
21.3 b) $2^{\frac{1}{64}}$ 21.8 b)	
21.4 a)	3 21.12 c) F_n
21.4 b)	21.12 d) $F_{n+1} - 2$
21.5 a)	6141
21.5 b) $4n \ln(2n)$	21.12 f) F_{n+2}

Fiche nº 22. Développements limités

22.1 a) $3x - x^2 + \frac{x^3}{2} - \frac{x^4}{2} + \underset{x \to 0}{\text{o}}(x^4)$
22.1 b)
22.1 c)
22.1 d)
22.2 a) $e - \frac{ex}{2} + \frac{11ex^2}{24} - \frac{7ex^3}{16} + \frac{2447ex^4}{5760} + \underset{x \to 0}{O}(x^5)$
22.2 b)
22.2 c) $e\left(1 + ix - x^2 - \frac{5}{6}ix^3\right) + \mathop{\text{o}}_{x\to 0}(x^3)$
22.2 d) $1-x+\frac{3}{2}(x-1)^2+\mathop{\text{o}}_{x\to 1}((x-1)^2)$
22.3 a) $ 1 - \frac{3\pi^2}{8} \left(x - \frac{\pi}{3} \right)^2 + \underset{x \to \frac{\pi}{3}}{\text{o}} \left(\left(x - \frac{\pi}{3} \right)^2 \right) $
22.3 b)
22.3 c) $ -1 + \frac{\pi^2}{8} \left(x - \frac{\pi}{2} \right)^4 - \frac{\pi^2}{48} \left(x - \frac{\pi}{2} \right)^6 + \underset{x \to \frac{\pi}{2}}{\text{o}} \left(\left(x - \frac{\pi}{2} \right)^7 \right) $
22.4 a)
22.4 b) $ \frac{1}{x^2} - \frac{1}{x^3} + \frac{5}{6x^4} - \frac{5}{6x^5} + O(\frac{1}{x^6}) $
22.4 c)
22.4 d) $e^{-\frac{1}{2}\left(e^{x} + \frac{e^{x}}{3x} - \frac{7e^{x}}{36x^{2}}\right) + o_{x \to +\infty}\left(\frac{e^{x}}{x^{2}}\right)}$

Fiche no 23. Arithmétique

Réponses

23.1 a)	23.4 1	23.7 a) (-5,2)	23.9 d). il est premier
23.1 b)	23.5 a)	23.7 b) 8 (mod 13)	23.10 a)
23.1 c)	23.5 b) $\boxed{\frac{65}{18}}$	23.7 c) 11 (mod 13)	23.10 b)
23.1 d)	23.5 c)	23.8 a)	23.11 a)
23.2 a)	23.5 d) $\boxed{\frac{1}{29 \ 160}}$	23.8 b) (2023, 6406)	23.11 c)
23.2 b)		23.9 a) $2 \times 3 \times 337$	23.11 d)
23.3 a)	23.6 a)	23.9 b) 7×17^2	23.11 e)
23.3 b)	23.6 b) (12,30)	23.9 c) 43×47	23.11 f)

Fiche n° 23. Arithmétique 25

Fiche nº 24. Polynômes

Réponses

24.1 a)
$$Q = X^2 + 2X + 1$$
 $R = 2$

24.1 b)
$$Q = X^2 - 4X + 7$$
 $R = -3X - 8$

24.1 c)
$$Q = X^2 - 1$$
 $R = -X^2 + X + 1$

24.1 d)
$$Q = 13X + \frac{25}{2}$$
 $R = \frac{1}{2}(29X^2 - 5X - 23)$

24.2 b)
$$R = 0$$

24.2 c)
$$R = -2nX + 4n - 1$$

24.2 d)......
$$R = X^2 + X - 1$$

24.3 a)......
$$R = 2X - 3$$

24.4 a)......
$$R = -36X + 24$$

24.5 a)
$$R = -108X - 150$$

24.5 b)
$$-150 - 108\sqrt{2}$$

24.7 a)
$$(X-1)^2(X^2+1)$$

24.7 b)
$$(X^2 - 2X + 2)(X^2 - 2X + 5)$$

24.7 c)
$$(X^2 - 2X + 2)(X^2 - 2X + 5)$$

26 Fiche n° 24. Polynômes

Fiche nº 25. Décomposition en éléments simples

Fiche nº 26. Calcul matriciel

rteponses	
26.1 a) $ \begin{bmatrix} 1 & -3 & -1 \\ 3 & 3 & 4 \\ 9 & -7 & 3 \end{bmatrix} $	26.2 i)
26.1 b)	$26.2 \; \mathbf{j}) \dots \qquad \qquad \left[\begin{pmatrix} n & \cdots & n \\ \vdots & (n) & \vdots \\ n & \cdots & n \end{pmatrix} \right]$
26.1 c)	$26.2 \; \mathrm{k)} \ldots \ldots \ldots \left[\begin{pmatrix} n^2 & \cdots & n^2 \\ \vdots & (n^2) & \vdots \\ n^2 & \cdots & n^2 \end{pmatrix} \right]$
26.1 d) $\begin{pmatrix} 1 & 7 & -2 \\ 2 & 14 & -4 \\ -1 & -7 & 2 \end{pmatrix}$	$ \begin{array}{c ccccc} & n^2 & n^2 \\ \hline 26.2 & n & n^{k-1}D \end{array} $
	26.3 a) $2 \times 3^{j-i} \times 5^{i-1}$
26.1 e)	26.3 b) $2^{i+1}3^{j-i}(2^n-1)$
26.1 f)	26.3 c)
$26.1 \text{ g}) \left[\begin{pmatrix} 5 & 4 \\ 4 & 5 \end{pmatrix} \right]$	26.3 d)
26.1 h)	26.4 a) $2^{i-j} \binom{i-1}{j-1}$
26.1 i) $\begin{bmatrix} 1 & 7 & -2 \\ 7 & 49 & -14 \\ -2 & -14 & 4 \end{bmatrix}$	26.4 b) $(1 - \delta_{i,1})(\delta_{i-1,j+1} + \delta_{i,j}) + (1 - \delta_{i,n})(\delta_{i,j} + \delta_{i+1,j-1})$
26.2 a)	26.5 a) $ \boxed{ \frac{1}{2(\pi - e)} \begin{pmatrix} 2 & -e \\ -2 & \pi \end{pmatrix} } $
26.2 b)	26.5 b) $ \boxed{ \frac{1}{3} \begin{pmatrix} 1 & -1 - 2i \\ 1 & -1 + i \end{pmatrix} } $
26.2 c)	26.5 c) $ \frac{1}{2} \begin{pmatrix} 5 & 2 & -1 \\ 3 & 2 & -1 \\ -6 & -2 & 2 \end{pmatrix} $
26.2 d)	26.5 d) $ \frac{1}{4\pi} \begin{pmatrix} 0 & 4 & 0 \\ 0 & -2 & -2 \\ 2 & -1 & 1 \end{pmatrix} $
26.2 e)	
26.2 f)	26.5 e) $ \frac{1}{8} \begin{pmatrix} 8 & 4 & -2 \\ -16 & -6 & 7 \\ 0 & -2 & 1 \end{pmatrix} $
26.2 g) $\left[\begin{pmatrix} \cos(2\theta) & -\sin(2\theta) \\ \sin(2\theta) & \cos(2\theta) \end{pmatrix} \right]$	26.5 f) $ \frac{1}{6} \begin{pmatrix} -2 & 2 & 2 \\ 1 & -1 & 2 \\ 4 & 2 & -4 \end{pmatrix} $
26.2 h) $ \left[\begin{pmatrix} \cos(3\theta) & -\sin(3\theta) \\ \sin(3\theta) & \cos(3\theta) \end{pmatrix} \right] $	

26.5 i)
$$\frac{1}{2} \begin{pmatrix} 0 & -1 & 0 & -1 \\ 1 & 1 & 0 & 0 \\ -1 & 0 & -1 & 0 \\ 0 & 0 & 1 & -1 \end{pmatrix}$$

26.6 a)
$$\lambda \neq 1$$

26.6 b).....
$$\frac{1}{1-\lambda} \begin{pmatrix} -4 & -1 & 3\\ 2\lambda + 2 & \lambda & -2\lambda - 1\\ \lambda - 1 & 0 & 1 - \lambda \end{pmatrix}$$

26.6 c)
$$\lambda \neq 1$$

26.6 d)
$$\frac{1}{1-\lambda} \begin{pmatrix} -1-\lambda+\lambda^2 & 1-\lambda & 2-\lambda \\ 1 & 0 & -1 \\ 1-\lambda^2 & \lambda-1 & \lambda-1 \end{pmatrix}$$

Fiche nº 27. Algèbre linéaire

27.1 a)	27.2 d)	27.4 c) $\boxed{\frac{1}{2} \begin{pmatrix} -19 & -43 \\ 9 & 21 \end{pmatrix}}$
27.1 b)	27.2 f)	27.4 d)
27.1 d) $(-2, 4/5, 11/5)$ 27.1 e) $(-1, 1/2, 1/2)$	27.3 b)	27.4 e)
27.1 f)	27.3 d)	
27.2 a)		27.5 a)
27.2 b)	27.4 b)	27.5 b) $ \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} $

Fiche nº 28. Équations différentielles

28.1 a) $x \mapsto 56e^{12x}$	28.3 d) $x \mapsto (2-3i)e^x + (3i-1)e^{2x}$
28.1 b) $x \mapsto 6e^x - 1$	28.4 a) $x \mapsto e^x$
28.1 c) $x \mapsto \frac{8e^{3x} - 5}{3}$	28.4 b)
28.1 d)	28.4 c) $x \mapsto \frac{4}{3}e^x - \frac{1}{3}e^{-2x}$
28.2 a) $x \mapsto e^{(6-x)/5}$	28.4 d) $x \mapsto (2-x)e^x$
28.2 b)	28.4 e) $x \mapsto (2-x)e^{2-2x}$
28.2 c) $x \mapsto \left(\frac{6}{\sqrt{5}} + \pi\right) e^{\sqrt{5}x} - \frac{6}{\sqrt{5}}$	28.5 a) $x \mapsto \cos x + 2\sin x$
28.2 d) $x \mapsto \left(12 + \frac{2e}{\pi}\right)e^{\pi x - \pi^2} - \frac{2e}{\pi}$	28.5 b) $x \mapsto e^{-x/2} \left(\cos \frac{\sqrt{3}x}{2} - \frac{1}{\sqrt{3}} \sin \frac{\sqrt{3}x}{2} \right)$
	28.5 c) $x \mapsto e^{-x} \sin(x)$
28.3 a)	
$28.3 \text{ b)} \dots \qquad \qquad \boxed{x \mapsto e^x}$	28.5 d) $x \mapsto e^x \left(\frac{-1+i}{2} e^{2ix} + \frac{1+i}{2} e^{-2ix} \right)$
28.3 c) $x \mapsto 2e^{2x} - e^x$	

Fiche nº 29. Séries numériques

29.1 a) divergente	29.2 c) $e^{\frac{1}{2}}$	29.4 a)	29.5 c) divergente
29.1 b)	29.3 a)	29.4 b)	29.5 d)
20 1 c)	29.3 a) <u>6</u>		29.6 a)
29.1 c) $\left \frac{2}{2 - \sqrt{2}} \right $	29.3 b) divergente	29.4 c)	20 6 b)
29.1 d) $\left[\frac{1}{2 \times 3^9}\right]$	29.3 c) divergente	29.4 d)	29.6 b) $\left\lfloor \frac{11}{4} \right\rfloor$
		4	29.6 c)
29.2 a) e	29.3 d) $\left \frac{1-7i}{350} \right $	29.5 a) $\left \frac{1}{12} \right $	$2e^3$
29.2 b) $e^2 - 3$	29.3 e) $\boxed{\frac{-2-5\sqrt{2}i}{}}$		29.6 d) $\left[\frac{2e^3}{(e-1)^3}\right]$
	29.3 e) 2 3 4 2 t	29.5 b)	· · · · · · · · · · · · · · · · · · ·

Fiche nº 30. Structures euclidiennes

30.1 a)	30.3 c) $ \frac{1}{3} $
30.1 b)	30.4 a) $(1, 2\sqrt{3}(X - \frac{1}{2}))$
30.1 c)	
30.1 d) $ \frac{1}{2}(e^2 - 1) $	30.4 b) $\left[(\sqrt{3}X, \sqrt{\frac{240}{43}}(X^2 - \frac{9}{4}X + 1)) \right]$
30.2 a)	$\begin{bmatrix} 1 & 2 & -1 & -1 \\ 1 & 2 & 2 & 1 \end{bmatrix}$
30.2 b)	30.5 a)
30.2 c)	(1, 0, 2)
30.3 a)	30.5 b)
30.3 b) $\boxed{\frac{1}{5\sqrt{3}}}$	30.5 c)

Fiche nº 31. Groupes symétriques

31.1 a)	$\begin{pmatrix} 1 \\ 4 \end{pmatrix}$	2	3	4 2	5 6	$\begin{pmatrix} 6 \\ 5 \end{pmatrix}$
31.1 b)	$\begin{pmatrix} 1 \\ 2 \end{pmatrix}$	2 6	3 5	4	5 3	$\begin{pmatrix} 6 \\ 4 \end{pmatrix}$
31.1 c)	$\begin{pmatrix} 1 \\ 6 \end{pmatrix}$	2 4	3	4 2	5 5	$\begin{pmatrix} 6 \\ 1 \end{pmatrix}$
31.1 d)	$\begin{pmatrix} 1 \\ 1 \end{pmatrix}$	2 2	3 6	4 5	5 3	$\begin{pmatrix} 6 \\ 4 \end{pmatrix}$
31.1 e)	$\begin{pmatrix} 1 \\ 1 \end{pmatrix}$	2 6	3 5	4 4	5 2	$\begin{pmatrix} 6 \\ 3 \end{pmatrix}$
31.1 f)	$\begin{bmatrix} 1 \\ 6 \end{bmatrix}$	2 3	3 2	4	5 5	$\begin{pmatrix} 6 \\ 4 \end{pmatrix}$
31.2 a)					. [((a b)

31.2 b)	31.4 b) [id]
31.2 c)	31.4 c)
$31.2 \; \mathbf{d}) \dots \left[(a \; c \; b) \right]$	31.4 d) (1 6 7 4)(2 5 3)
31.2 e)	31.5 a)
31.2 f)	31.5 b)
()	31.5 c)
31.3 a) (1 7 4)(2 6 8 10)(3 9 5)	01.0 c)
31.3 a) (1 7 4)(2 0 8 10)(3 9 3)	31.5 d)
(4.2.42.2.1)(7.7)(2.2)	
31.3 b) (1 3 10 6 4)(5 7)(8 9)	31.5 e)
31.3 c)	31.5 f)
31.3 d)	31.6 a)
31.3 e)	31.6 b)
	31.6 c)
31.4 a)	
	31.6 d)
	<u>—</u>

Fiche nº 32. Déterminants

Réponses

32.1 a) $-2a^2$	32.2 c)	32.4 b)
32.1 b)	32.2 d)	32.4 c)
32.1 c)	32.2 e) $7\sqrt{2} + 13$	32.5 a) $x^3 + y^3 + z^3 - 3xyz$
32.1 d)	32.3 a)	32.5 b) $-6 \ln^3(a)$
32.2 a)	32.3 b)40	
32.2 b)	32.3 c)	32.5 c) $(y-x)(z-y)(z-x)$
	32.4 a)	32.5 d)

Fiche n° 32. Déterminants