

## MECHANICS

$$\begin{aligned}
 \vec{v}_x &= v_{x0} + a_x t \\
 x &= x_0 + v_{x0} t + \frac{1}{2} a_x t^2 \\
 v_x^2 &= v_{x0}^2 + 2a_x(x - x_0) \\
 \vec{a} &= \frac{\sum \vec{F}}{m} = \frac{\vec{F}_{net}}{m} \\
 \vec{F} &= \frac{d\vec{p}}{dt} \\
 \vec{J} &= \int \vec{F} dt = \Delta\vec{p} \\
 \vec{p} &= m\vec{v} \\
 |\vec{F}_f| &\leq \mu |\vec{F}_N| \\
 \Delta E &= W = \int \vec{F} \cdot d\vec{r} \\
 K &= \frac{1}{2} mv^2 \\
 p &= \frac{dE}{dt} \\
 \vec{p} &= \vec{F} \cdot \vec{v} \\
 \Delta U_g &= mg\Delta h \\
 a_c &= \frac{v^2}{r} = \omega^2 r \\
 \vec{\tau} &= \vec{r} \times \vec{F} \\
 \vec{\alpha} &= \frac{\sum \vec{\tau}}{I} = \frac{\vec{\tau}_{net}}{I} \\
 I &= \int r^2 dm = \sum mr^2 \\
 x_{cm} &= \frac{\sum m_i x_i}{\sum m_i} \\
 v &= r\omega \\
 \vec{L} &= \vec{r} \times \vec{p} = I\vec{\omega} \\
 K &= \frac{1}{2} I\omega^2 \\
 \omega &= \omega_0 + \alpha t \\
 \theta &= \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2
 \end{aligned}$$

$a$  = acceleration  
 $E$  = energy  
 $F$  = force  
 $f$  = frequency  
 $h$  = height  
 $I$  = rotational inertia  
 $J$  = impulse  
 $K$  = kinetic energy  
 $k$  = spring constant  
 $\ell$  = length  
 $L$  = angular momentum  
 $m$  = mass  
 $P$  = power  
 $p$  = momentum  
 $r$  = radius or distance  
 $T$  = period  
 $t$  = time  
 $U$  = potential energy  
 $v$  = velocity or speed  
 $W$  = work done on a system  
 $x$  = position  
 $\mu$  = coefficient of friction  
 $\theta$  = angle  
 $\tau$  = torque  
 $\omega$  = angular speed  
 $\alpha$  = angular acceleration  
 $\phi$  = phase angle

$$\begin{aligned}
 \vec{F}_s &= -k\Delta\vec{x} \\
 U_s &= \frac{1}{2} k(\Delta x)^2 \\
 x &= x_{max} \cos(\omega t + \phi) \\
 T &= \frac{2\pi}{\omega} = \frac{1}{f} \\
 T_s &= 2\pi \sqrt{\frac{m}{k}} \\
 T_p &= 2\pi \sqrt{\frac{\ell}{g}} \\
 |\vec{F}_G| &= \frac{Gm_1 m_2}{r^2} \\
 U_G &= -\frac{Gm_1 m_2}{r}
 \end{aligned}$$

## ELECTRICITY AND MAGNETISM

$$\begin{aligned}
 |\vec{F}_E| &= \frac{1}{4\pi\epsilon_0} \left| \frac{q_1 q_2}{r^2} \right| \\
 \vec{E} &= \frac{\vec{F}_E}{q} \\
 \oint \vec{E} \cdot d\vec{A} &= \frac{Q}{\epsilon_0} \\
 E_x &= -\frac{dV}{dx} \\
 \Delta V &= -\int \vec{E} \cdot d\vec{r} \\
 V &= \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i} \\
 U_E &= qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} \\
 \Delta V &= \frac{Q}{C} \\
 C &= \frac{\kappa\epsilon_0 A}{d} \\
 C_p &= \sum_i C_i \\
 \frac{1}{C_s} &= \sum_i \frac{1}{C_i} \\
 I &= \frac{dQ}{dt} \\
 U_C &= \frac{1}{2} Q\Delta V = \frac{1}{2} C(\Delta V)^2 \\
 R &= \frac{\rho\ell}{A} \\
 \vec{E} &= \rho\vec{J} \\
 I &= Nev_d A \\
 I &= \frac{\Delta V}{R} \\
 R_s &= \sum_i R_i \\
 \frac{1}{R_p} &= \sum_i \frac{1}{R_i} \\
 P &= I\Delta V
 \end{aligned}$$

$A$  = area  
 $B$  = magnetic field  
 $C$  = capacitance  
 $d$  = distance  
 $E$  = electric field  
 $\mathcal{E}$  = emf  
 $F$  = force  
 $I$  = current  
 $J$  = current density  
 $L$  = inductance  
 $\ell$  = length  
 $n$  = number of loops of wire per unit length  
 $N$  = number of charge carriers per unit volume  
 $P$  = power  
 $Q$  = charge  
 $q$  = point charge  
 $R$  = resistance  
 $r$  = radius or distance  
 $t$  = time  
 $U$  = potential or stored energy  
 $V$  = electric potential  
 $v$  = velocity or speed  
 $\rho$  = resistivity  
 $\Phi$  = flux  
 $\kappa$  = dielectric constant

$$\begin{aligned}
 \vec{F}_M &= q\vec{v} \times \vec{B} \\
 \oint \vec{B} \cdot d\vec{\ell} &= \mu_0 I \\
 d\vec{B} &= \frac{\mu_0}{4\pi} \frac{I d\vec{\ell} \times \hat{r}}{r^2} \\
 \vec{F} &= \int I d\vec{\ell} \times \vec{B} \\
 B_s &= \mu_0 nI \\
 \Phi_B &= \int \vec{B} \cdot d\vec{A} \\
 \mathcal{E} &= \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt} \\
 \mathcal{E} &= -L \frac{dI}{dt} \\
 U_L &= \frac{1}{2} LI^2
 \end{aligned}$$

**TABLE OF INFORMATION DEVELOPED FOR 2012**

CONSTANTS AND CONVERSION FACTORS	
Proton mass, $m_p = 1.67 \times 10^{-27}$ kg	Electron charge magnitude, $e = 1.60 \times 10^{-19}$ C
Neutron mass, $m_n = 1.67 \times 10^{-27}$ kg	1 electron volt, $1 \text{ eV} = 1.60 \times 10^{-19}$ J
Electron mass, $m_e = 9.11 \times 10^{-31}$ kg	Speed of light, $c = 3.00 \times 10^8$ m/s
Avogadro's number, $N_0 = 6.02 \times 10^{23}$ mol <sup>-1</sup>	Universal gravitational constant, $G = 6.67 \times 10^{-11}$ m <sup>3</sup> /kg·s <sup>2</sup>
Universal gas constant, $R = 8.31$ J/(mol·K)	Acceleration due to gravity at Earth's surface, $g = 9.8$ m/s <sup>2</sup>
Boltzmann's constant, $k_B = 1.38 \times 10^{-23}$ J/K	
1 unified atomic mass unit,	$1 \text{ u} = 1.66 \times 10^{-27}$ kg = 931 MeV/c <sup>2</sup>
Planck's constant,	$h = 6.63 \times 10^{-34}$ J·s = $4.14 \times 10^{-15}$ eV·s
	$hc = 1.99 \times 10^{-25}$ J·m = $1.24 \times 10^3$ eV·nm
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12}$ C <sup>2</sup> /N·m <sup>2</sup>
Coulomb's law constant, $k = 1/4\pi\epsilon_0 = 9.0 \times 10^9$ N·m <sup>2</sup> /C <sup>2</sup>	
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7}$ (T·m)/A
Magnetic constant, $k' = \mu_0/4\pi = 1 \times 10^{-7}$ (T·m)/A	
1 atmosphere pressure,	$1 \text{ atm} = 1.0 \times 10^5$ N/m <sup>2</sup> = $1.0 \times 10^5$ Pa

UNIT SYMBOLS	meter,	m	mole,	mol	watt,	W	farad,	F
	kilogram,	kg	hertz,	Hz	coulomb,	C	tesla,	T
	second,	s	newton,	N	volt,	V	degree Celsius,	°C
	ampere,	A	pascal,	Pa	ohm,	Ω	electron-volt,	eV
	kelvin,	K	joule,	J	henry,	H		

PREFIXES		
Factor	Prefix	Symbol
$10^9$	giga	G
$10^6$	mega	M
$10^3$	kilo	k
$10^{-2}$	centi	c
$10^{-3}$	milli	m
$10^{-6}$	micro	μ
$10^{-9}$	nano	n
$10^{-12}$	pico	p

VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES							
$\theta$	0°	30°	37°	45°	53°	60°	90°
$\sin \theta$	0	1/2	3/5	$\sqrt{2}/2$	4/5	$\sqrt{3}/2$	1
$\cos \theta$	1	$\sqrt{3}/2$	4/5	$\sqrt{2}/2$	3/5	1/2	0
$\tan \theta$	0	$\sqrt{3}/3$	3/4	1	4/3	$\sqrt{3}$	∞

The following conventions are used in this exam.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.
- IV. For mechanics and thermodynamics equations,  $W$  represents the work done on a system.

$10^{-15}$  femto F