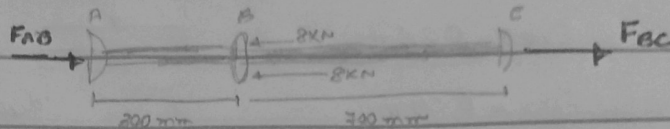


Cap 4 - Carga axial

ex: $d_e = 20 \text{ mm}$

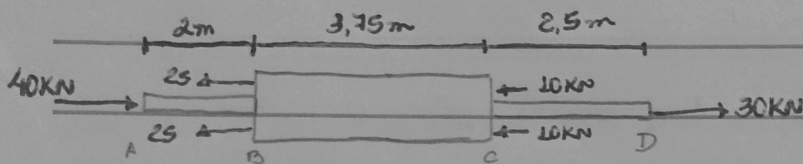
$d_i = 15 \text{ mm}$



$$F_A = P \left(\frac{L_{CB}}{L} \right) \rightarrow 16 \left(\frac{0,7}{1} \right) = 11,2 \text{ KN}$$

$$F_C = P \left(\frac{L_{BA}}{L} \right) \rightarrow 16 \left(\frac{0,3}{1} \right) = 4,8 \text{ KN}$$

Problema 4.4



$d_{AB} = 20 \text{ mm}$

$E_{\text{cobre}} = 126 \text{ GPa}$

$d_{BC} = 25 \text{ mm}$

$d_{CD} = 12 \text{ mm}$

$$\delta_{AB} = - \frac{40 \cdot 10^3 \cdot 2}{\pi \cdot 0,01^2 \cdot 126 \cdot 10^9} = -2,021 \cdot 10^{-3}$$

$$\delta_{BC} = \frac{10 \cdot 10^3 \cdot 3,75}{\pi \cdot 0,0125^2 \cdot 126 \cdot 10^9} = 6,0630 \cdot 10^{-4}$$

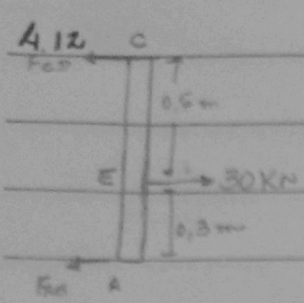
$$\delta_{CD} = - \frac{30 \cdot 10^3 \cdot 2,5}{\pi \cdot 0,006^2 \cdot 126 \cdot 10^9} = -5,2630 \cdot 10^{-3}$$

$$\epsilon = \frac{\delta}{L}$$

$$\delta = \epsilon \cdot L$$

$$\delta_T = \alpha \Delta T L$$

$$\delta = \frac{PL}{AE}$$



$$\sum F_x = 0$$

$$\sum M_C = 0$$

$$-F_{AB} - F_{CD} + 30 = 0$$

$$0,6 F_{CD} - 0,3 F_{AB} = 0$$

$$-F_{AB} - F_{CD} = -30$$

$$0,6 F_{CD} = 0,3 F_{AB}$$

$$F_{AB} + F_{CD} = 30$$

SUBSTITUINDO

$$F_{AB} = 2 F_{CD}$$

$$2 F_{CD} + F_{CD} = 30$$

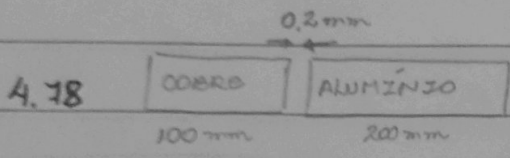
$$= 2 \cdot 10$$

$$F_{CD} = 10 \text{ kN}$$

$$F_{AB} = 20 \text{ kN}$$

$$E = 120 \text{ GPa}$$

$$\delta_{AB} = \frac{P \cdot L}{AE}$$



$$\Delta L_{\text{cobre}} + \Delta L_{\text{aluminio}} \geq 0,2 \cdot 10^{-3}$$

$$17 \cdot 10^{-6} \cdot 135 \cdot 0,1 + 24 \cdot 10^{-6} \cdot 135 \cdot 0,2 \geq 0,2 \cdot 10^{-3}$$

$$2,295 \cdot 10^{-4} + 6,48 \cdot 10^{-4} \geq 0,2 \cdot 10^{-3}$$

$$8,775 \cdot 10^{-4} \geq 0,2 \cdot 10^{-3}$$

$$\Delta L_{\text{cobre}} + \Delta L_{\text{aluminio}} - \delta_{\text{cobre}} - \delta_{\text{aluminio}} = 0,2 \cdot 10^{-3}$$

$$8,775 \cdot 10^{-4} - \frac{F \cdot L_c}{A \cdot E_c} - \frac{F \cdot L_A}{A \cdot E_A} = 0,2 \cdot 10^{-3}$$

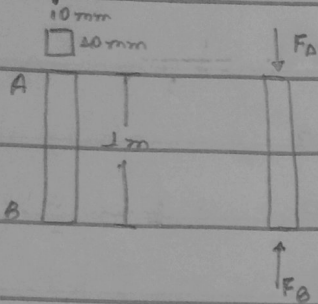
$$\frac{\sigma L_c}{E_c} + \frac{\sigma L_A}{E_A} = 6,775 \cdot 10^{-4}$$

$$\frac{\sigma \cdot 0,1}{126 \cdot 10^9} + \frac{\sigma \cdot 0,2}{70 \cdot 10^9} = 6,775 \cdot 10^{-4}$$

$$7,9365 \cdot 10^{-13} + 2,8571 \cdot 10^{-12} = 6,775 \cdot 10^{-4}$$

$$\sigma = 185,578 \text{ MPa}$$

Exemplo 4.10



$$+\uparrow \sum F_y = 0$$

$$F_B - F_A = 0$$

$$F_B = F_A = F$$

$$\delta_{A/B} = 0 = \delta_T - \delta_F$$

$$0 = \alpha \Delta T L - \frac{FL}{AE} \rightarrow F/L = \alpha \Delta T / AE$$

$$F = \alpha \Delta T A E$$

$$= 12 \cdot 10^{-6} \cdot 30 \cdot 1 \cdot 10^{-4} \cdot 200 \cdot 10^6 \Rightarrow 7,2 \text{ kN}$$

$$\sigma = \frac{F}{A} = \frac{7,2 \cdot 10^3}{10^{-4}} = 75 \text{ MPa}$$