

複素数の復習

例題 9-1, 9-2 を参考に章末問題の[演習 1]～[演習 3]を行う.

[演習 1]

$$(1) e^{j\frac{2\pi}{3}}$$

$$(2) e^{-j*\left(\frac{3\pi}{4}\right)}$$

[演習 2]

$$(1) \left(-\frac{\sqrt{2}}{2} + j * \frac{\sqrt{2}}{2}\right)$$

$$(2) \left(\frac{1}{2} - j * \frac{\sqrt{3}}{2}\right)$$

[演習 3]

$$\cos \theta + j * \sin \theta = \frac{e^{j*\theta} + e^{j*\theta} + e^{-j*\theta} - e^{-j*\theta}}{2} = e^{j*\theta}$$

複素フーリエ級数・係数

例題 9-3, 9-4 を参考に章末問題の[演習 4]～[演習 5]を行う.

[演習 4]

$$(1) C_0 = \frac{1}{2} \int_{-\frac{1}{2}}^{\frac{1}{2}} 1 \, dt = \frac{1}{2}$$

$$C_n = \frac{1}{2} \int_{-\frac{1}{2}}^{\frac{1}{2}} 1 * e^{-jn\omega_0 t} \, dt = \frac{1}{n\pi} \sin \frac{n\pi}{2}$$

(2)

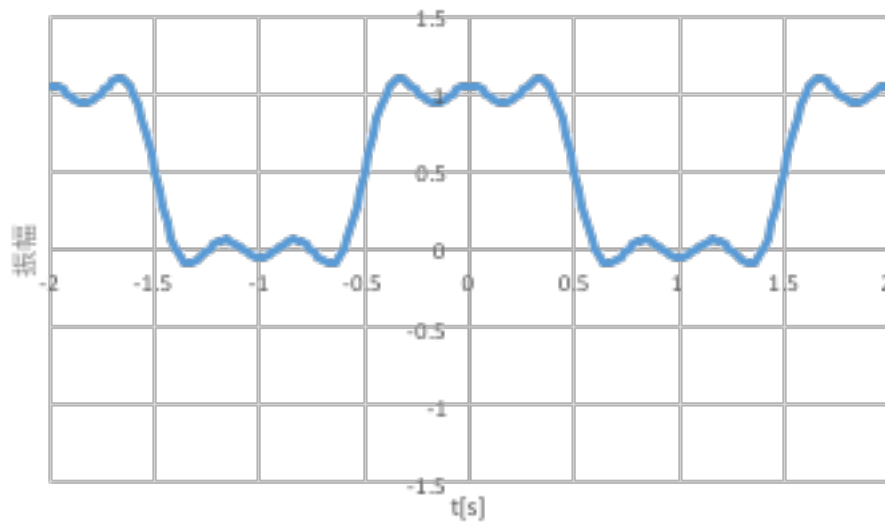
$$f(t) = \frac{1}{2} + \frac{2}{\pi} \cos \pi t - \frac{2}{3\pi} \cos 3\pi t + \dots$$

(3)

$$c_0 = \frac{1}{2}, |c_1| = \frac{1}{\pi}, |c_2| = 0, |c_3| = \frac{1}{3\pi}, |c_4| = 0, |c_5| = \frac{1}{5\pi}$$

$$\theta_1 = 0, \theta_2 = 0, \theta_3 = -\pi, \theta_4 = 0, \theta_5 = 0$$

(4)



[演習 5]

(1)

$$c_0 = \frac{1}{2} \int_0^1 1 dt = \frac{1}{2}$$

$$c_n = \frac{1}{2} \int_0^1 1 * e^{-jn\pi t} dt$$

$$= \frac{1}{n\pi} \sin \frac{n\pi}{2} \left\{ \cos \frac{n\pi}{2} - j \sin \frac{n\pi}{2} \right\}$$

(2)

$$f(t) = \frac{1}{2} + \frac{2}{\pi} \sin \pi t + \frac{2}{3\pi} \sin 3\pi t + \dots$$

(3)

$$c_0 = \frac{1}{2}, |c_1| = \frac{1}{\pi}, |c_2| = 0, |c_3| = \frac{1}{3\pi}, |c_4| = 0, |c_5| = \frac{1}{5\pi}$$

$$\theta_1 = -\frac{\pi}{2}, \theta_2 = 0, \theta_3 = -\frac{\pi}{2}, \theta_4 = 0, \theta_5 = -\frac{\pi}{2}$$

(4)

