

DSA1Uebung-003 -- Karnaugh-Veitch Method

- a) Create Truth Tables
 - b) Optimize the Boolean expression using the Karnaugh-Veitch method
-

1) [3 Variables]

A

A	B	C	P(A,B,C)
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0

..hier könnten weitere Zeilen stehen..

B

	AB	A¬B	¬A¬B	¬AB
C	\$\color{gray}{0}\$	\$\color{gray}{0}\$	\$\color{gray}{0}\$	\$\color{royalblue}{1}\$
¬C	\$\color{gray}{0}\$	\$\color{gray}{0}\$	\$\color{yellow}{1}\$	\$\color{lime}{1}\$

Ergebnis :

$$P(A, B, C) \equiv (\color{yellow}{\neg A \wedge \neg C}) \vee (\color{royalblue}{\neg A \wedge B})$$

Quot erat demonstrandum.

2) [4 Variables]

A

A	B	C	D	P(A,B,C,D)
1	0	0	0	1
0	1	1	1	0
1	1	0	1	1
0	1	0	1	1
1	1	0	0	1
1	0	1	0	0
1	0	0	1	1

..hier könnten weitere Zeilen stehen..

B

$\neg A \neg B$	AB	$A \neg B$	$\neg A \neg B$
CD	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$
$C \neg D$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$
$\neg C \neg D$	$\text{\color{gray}{0}}$	$\text{\color{royalblue}{1}}$	$\text{\color{royalblue}{1}}$
$\neg CD$	$\text{\color{yellow}{1}}$	$\text{\color{lime}{1}}$	$\text{\color{gray}{0}}$

Ergebnis :

$$P_{(A,B,C,D)} \equiv (\text{\color{royalblue}{A \wedge \neg C}}) \vee (\text{\color{yellow}{\neg C \wedge D}})$$

Quot erat demonstrandum.