

DSAIUebung-003 -- Karnaugh-Veitch Method

- a) Create Truth Tables
- b) Optimize the Boolean expression using the Karnaugh-Veitch method

1) [3 Variables]

A

A	B	C	P(A,B,C)
0	0	0	1
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0

..hier könnten weitere Zeilen stehen..

B

	AB	A¬B	¬A¬B	¬AB
C	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{royalblue}{1}}$
¬C	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{yellow}{1}}$	$\text{\color{lime}{1}}$

Ergebnis :

$$P(A,B,C) \equiv (\text{\color{yellow}{\neg A \wedge \neg C}}) \vee (\text{\color{royalblue}{\neg A \wedge B}})$$

Quot erat demonstrandum.

2) [4 Variables]

A

A	B	C	D	P(A,B,C,D)
1	0	0	0	1
0	1	1	1	0
1	1	0	1	1
0	1	0	1	1
1	1	0	0	1
1	0	1	0	0
1	0	0	1	1

..hier könnten weitere Zeilen stehen..

B

	$\neg AB$	AB	$A \neg B$	$\neg A \neg B$
CD	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$
$C \neg D$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$	$\text{\color{gray}{0}}$
$\neg C \neg D$	$\text{\color{gray}{0}}$	$\text{\color{royalblue}{1}}$	$\text{\color{royalblue}{1}}$	$\text{\color{gray}{0}}$
$\neg CD$	$\text{\color{yellow}{1}}$	$\text{\color{lime}{1}}$	$\text{\color{lime}{1}}$	$\text{\color{gray}{0}}$

Ergebnis :

$P_{(A,B,C,D)} \equiv (\text{\color{royalblue}{A}} \wedge \neg \text{\color{gray}{C}}) \vee (\text{\color{yellow}{\neg C}} \wedge \text{\color{lime}{D}})$

Quot erat demonstrandum.