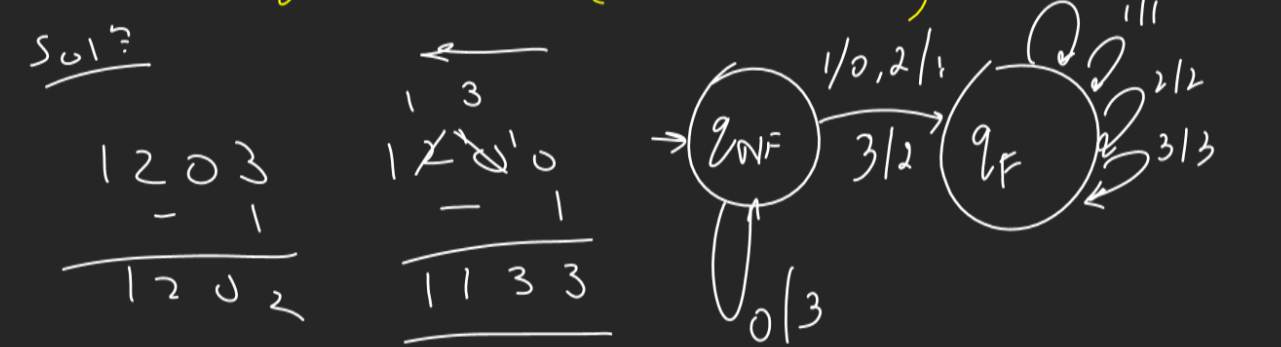


F.S.M.  $\Rightarrow$  F.A  $\begin{cases} \text{w/o o/p} \Rightarrow M = (Q, \Sigma, \delta, q_0, F) \xrightarrow{\text{NFA}} \\ \text{with o/p} \Rightarrow M = (Q, \Sigma, \Delta, \delta, \lambda, q_0) \end{cases}$

Moore & Mealy

$M = (Q, \Sigma, \Delta, \delta, \lambda, q_0)$   
 $Q, \Sigma, \delta, q_0 \Rightarrow$  same as DFA  
 i.e.  $\delta$  maps  $Q \times \Sigma \rightarrow Q$   
 $\Delta$ : finite set of o/p symbols  
 $\lambda$ : Transition function  $\begin{cases} \text{MOORE: } Q \rightarrow \Delta \\ \text{MEALY: } Q \times \Sigma \rightarrow \Delta \end{cases}$

Example: Design Moore & Mealy to decrement a number expressed in base 4 (i.e. input over the set  $\{0, 1, 2, 3\}$ )



$M = (Q, \Sigma, \Delta, \delta, \lambda, q_0)$   
 $Q = \{q_{NF}, q_F\}, \Sigma = \{0, 1, 2, 3\}, \Delta = \{0, 1, 2, 3\}$   
 $q_0 = q_{NF}$

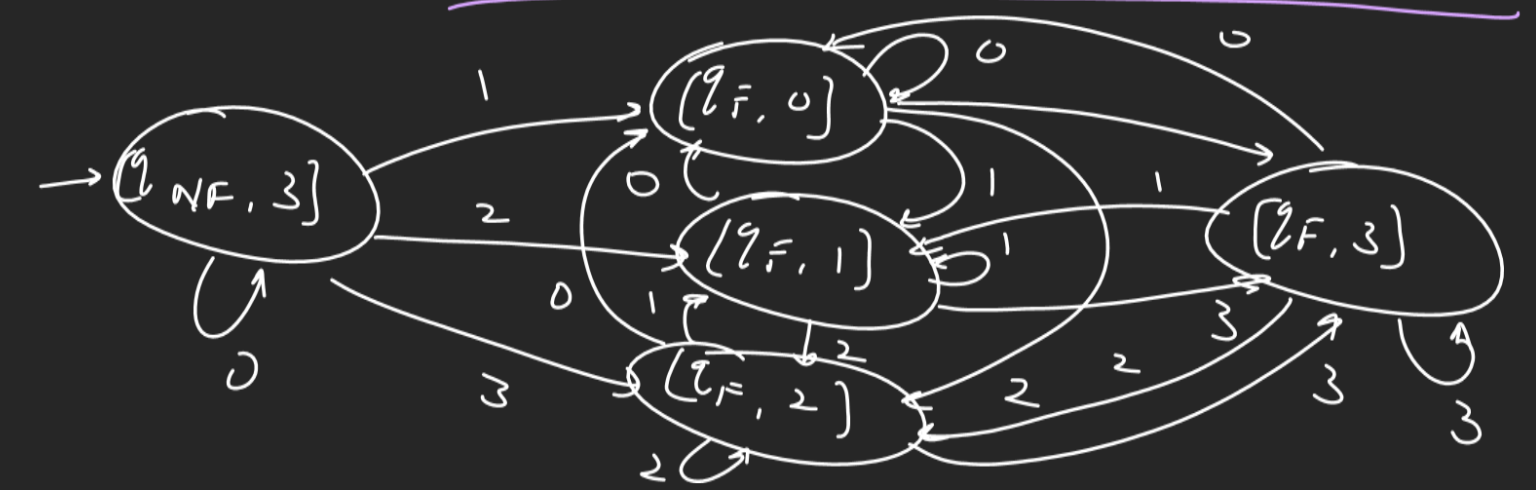
$\delta: Q \times \Sigma \rightarrow Q$        $\lambda: Q \times \Sigma \rightarrow \Delta$

$Q \backslash \Sigma$	0	1	2	3
$q_{NF}$	$q_{NF, 3}$	$q_{F, 0}$	$q_{F, 1}$	$q_{F, 2}$
$q_F$	$q_{F, 0}$	$q_{F, 1}$	$q_{F, 2}$	$q_{F, 3}$

$Q \backslash \Sigma$	0	1	2	3
$q_{NF}$	3	0	1	2
$q_F$	0	1	2	3

Equivalent Moore

$Q \backslash \Sigma$	0	1	2	3
$q_{NF, 3}$	$q_{NF, 3}$	$q_{F, 0}$	$q_{F, 1}$	$q_{F, 2}$
$q_{F, 0}$	$q_{F, 0}$	$q_{F, 1}$	$q_{F, 2}$	$q_{F, 3}$
$q_{F, 1}$	$q_{F, 0}$	$q_{F, 1}$	$q_{F, 2}$	$q_{F, 3}$
$q_{F, 2}$	"	"	"	"
$q_{F, 3}$	"	"	"	"

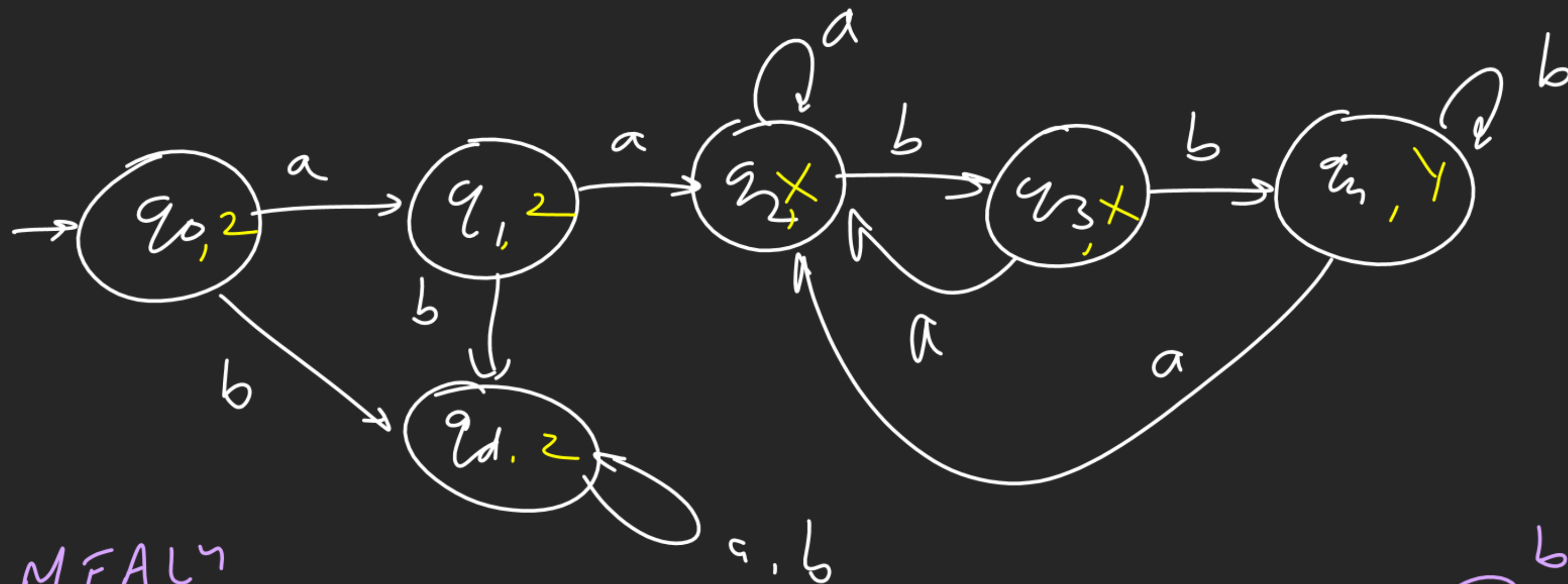


Ex 2 Design Moore & Mealy that receives  
 ip over  $\{a, b\}$  & generates output

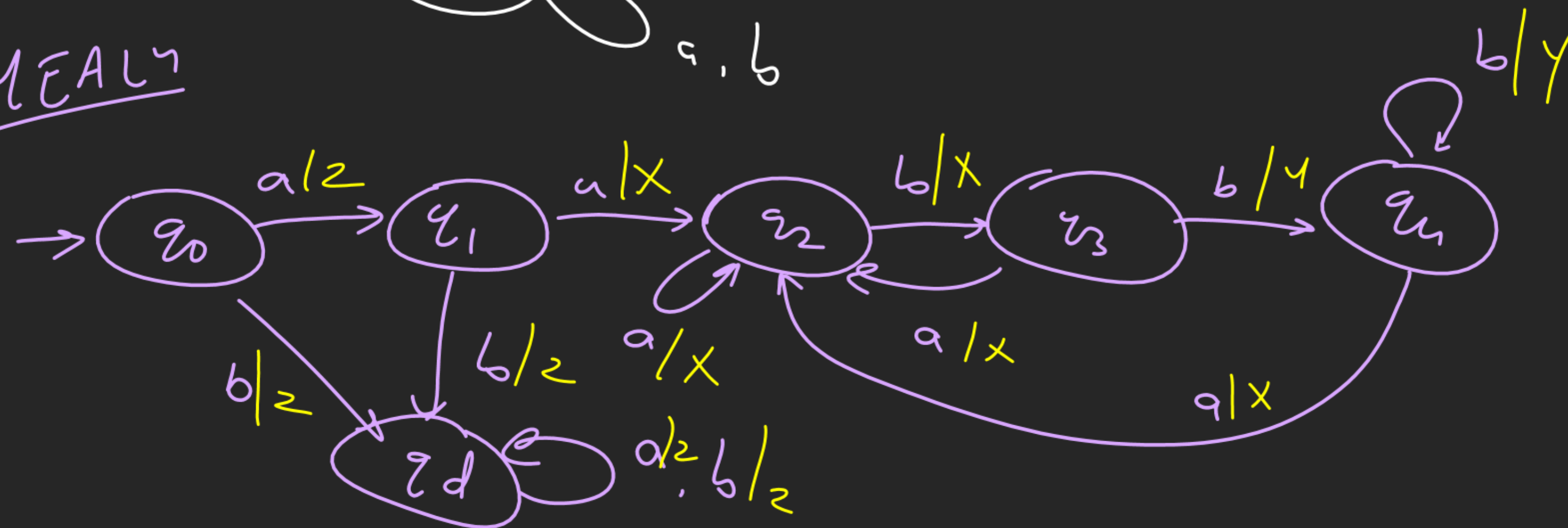
X  $\rightarrow$  if ip starts with aa but not ends  
 sounds with aa and with bb

Y  $\rightarrow$  ends with bb

Z  $\rightarrow$  if ip does not start with 'aa'



MEALY



Assignment 5

Equivalence of Moore & Mealy.