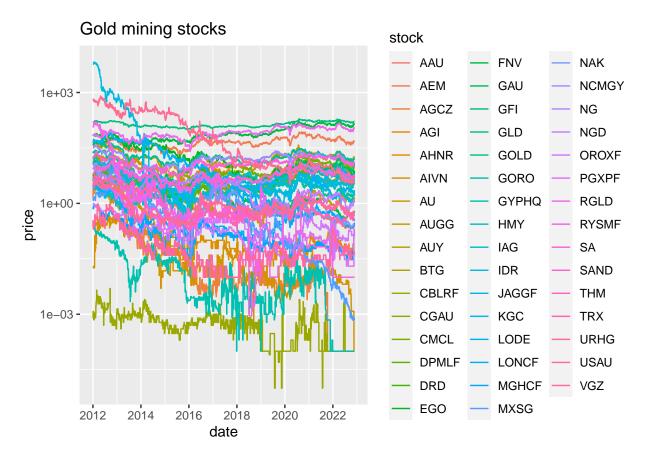
## Kalman filter StatArb Gold and Silver

#### Gold

```
tickers <- c(read.csv("zacks_custom_screen_2022-04-18.csv")$Ticker,"GLD" )
prices <- tq_get(tickers,get = "stock.prices",to="2022-11-28") %>% select(date,symbol,close) %>% spread
## Warning: x = 'DTRC', get = 'stock.prices': Error in getSymbols.yahoo(Symbols = "DTRC", env = <environ
## DTRC download failed after two attempts. Error message:
## HTTP error 404.
## Removing DTRC.

date <- prices$date
prices <- prices %>% select(-date)
xy <- xts(as.matrix(prices),order.by = date)
xy <- xts(as.matrix(prices),order.by = date)
xy <- xy[,which(colSums(is.na(xy))==0) %>% names()]
tickers <- xy %>% colnames()
list <- tickers[tickers != "GLD"]
colnames(xy) <- tickers
xy %>% as.data.frame() %>% mutate(date = as.Date(rownames(.))) %>% gather("stock", "price", -date) %>%
ggplot(aes(date,price,color=stock))+geom_line()+scale_y_log10()+ggtitle("Gold mining stocks")
```



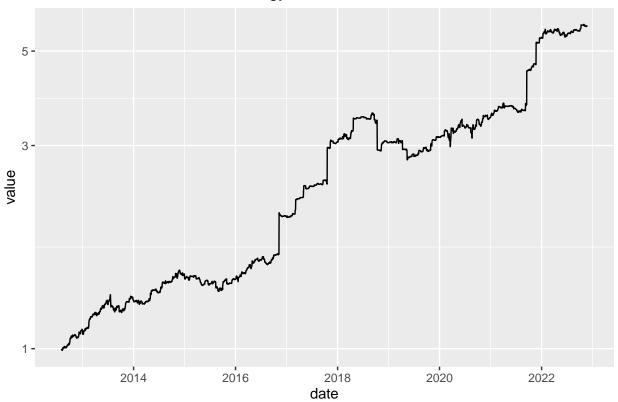
```
func <-function(t){</pre>
i<-t
x <- xy[, i]
y <- xy[, "GLD"]
xint \leftarrow rep(1, nrow(x))
delta <- 0.00001
Vw <- delta/(1-delta)*diag(2)</pre>
Ve <- 0.001
R <- matrix(rep(0, 4), nrow=2)</pre>
P \leftarrow matrix(rep(0, 4), nrow=2)
beta <- matrix(rep(0, nrow(y)*2), ncol=2)</pre>
y_{est} \leftarrow rep(0, nrow(y))
e <- rep(0, nrow(y))</pre>
Q \leftarrow rep(0, nrow(y))
for(i in 1:nrow(y)) {
  if(i > 1) {
    beta[i, ] <- beta[i-1, ]
    R \leftarrow P + Vw
  y_est[i] <- x[i, ] %*% beta[i, ]</pre>
  Q[i] \leftarrow x[i, ] %*% R %*% t(x[i, ]) + Ve
  e[i] <- y[i] - y_est[i]</pre>
  K \leftarrow R \% \% t(x[i, ]) / Q[i]
```

```
beta[i, ] <- beta[i, ] + K * e[i]
 P = R - K \% * \% x[i, ] \% * \% R
}
e <- xts(e, order.by=index(xy))
sqrtQ <- xts(sqrt(Q), order.by=index(xy))</pre>
signals <- merge(e, 15*sqrtQ, 15*-sqrtQ)</pre>
colnames(signals) <- c("e", "sqrtQ", "negsqrtQ")</pre>
colnames(sig) <- "sig"</pre>
sig[sig == 0] \leftarrow NA
sig <- na.locf(sig)</pre>
sig <- diff(sig)/2</pre>
plot(sig)
sim <- merge(lag.xts(sig,1), beta[, 1], x[, 1], y)</pre>
colnames(sim) <- c("sig", "hedge", tickers[1], tickers[2])</pre>
i <- t
sim$posX <- sim$sig * -1</pre>
difference <-c(diff(sim[,3])/sim[,3][-1] )</pre>
pnl <- sim$posX * difference</pre>
print(pnl)
a <- sapply(list,func)</pre>
date <-rownames(as.data.frame(xy))</pre>
## function (x, df1, df2, ncp, log = FALSE)
## {
##
      if (missing(ncp))
##
          .Call(C_df, x, df1, df2, log)
##
      else .Call(C_dnf, x, df1, df2, ncp, log)
## }
## <bytecode: 0x000000030cfbc00>
## <environment: namespace:stats>
a<-a %>% as.data.frame()
a <-a %>% na.omit() %>% rowMeans() %>% as.vector()
gold_strategy <- data.frame(value=a)</pre>
```

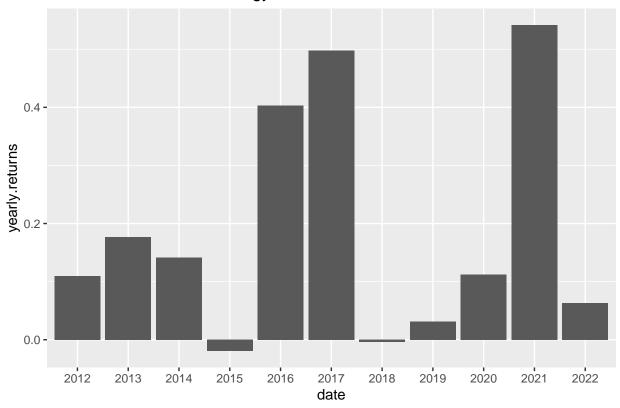
```
rownames(gold_strategy) <- date[(length(date)-(nrow(gold_strategy)-1)):length(date)]
gold_strategy <-gold_strategy %>% as.xts()

gold_strategy %>% as.data.frame() %>% mutate(date=as.Date(rownames(.)),value=cumprod(value+1)) %>%
    ggplot(aes(date,value))+geom_line()+scale_y_log10()+ ggtitle("cumulative returns Gold Strategy")
```

## cumulative returns Gold Strategy



#### Annual returns Gold Strategy



#### Silver

tickers <- xy %>% colnames()
list <- tickers[tickers != "SLV"]</pre>

```
tickers <- c(read.csv("silver_mining.csv")$Ticker,"SLV" )

prices <- tq_get(tickers,get = "stock.prices",to = "2022-11-28") %>% select(date,symbol,close) %>% spr

## Warning: x = 'AXU', get = 'stock.prices': Error in getSymbols.yahoo(Symbols = "AXU", env = <environm
## AXU download failed after two attempts. Error message:
## HTTP error 404.
## Removing AXU.

## Warning: x = 'GPL', get = 'stock.prices': Error in getSymbols.yahoo(Symbols = "GPL", env = <environm
## GPL download failed after two attempts. Error message:
## HTTP error 404.
## Removing GPL.

date <- prices$date
prices <- prices %>% select(-date)
xy <- xts(as.matrix(prices),order.by = date)
xy <- xts(as.matrix(prices),order.by = date)
xy <- xts(as.matrix(prices),order.by = date)
xy <- xts(as.matrix(prices),order.by = date)</pre>
```

```
colnames(xy) <- tickers
xy %>% as.data.frame() %>% mutate(date = as.Date(rownames(.))) %>% gather("stock","price",-date) %>%
ggplot(aes(date,price,color=stock))+geom_line()+scale_y_log10()+ggtitle("Silver mining stocks")
```

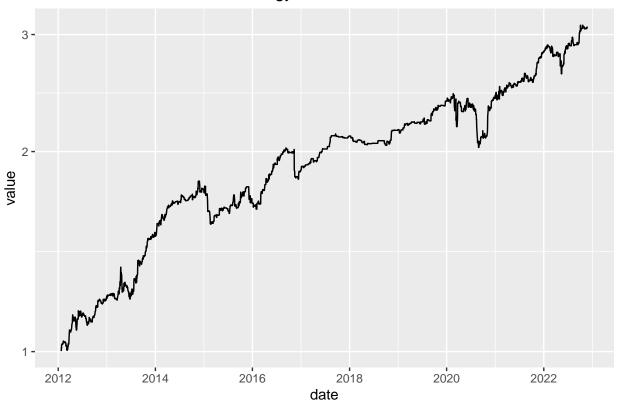
## Silver mining stocks



```
func <-function(t){</pre>
i<-t
x \leftarrow xy[, i]
y <- xy[, "SLV"]
x$int <- rep(1, nrow(x))
delta <- 0.0001
Vw <- delta/(1-delta)*diag(2)</pre>
Ve <- 0.001
R <- matrix(rep(0, 4), nrow=2)</pre>
P <- matrix(rep(0, 4), nrow=2)</pre>
beta <- matrix(rep(0, nrow(y)*2), ncol=2)</pre>
y_{est} \leftarrow rep(0, nrow(y))
e <- rep(0, nrow(y))</pre>
Q \leftarrow rep(0, nrow(y))
for(i in 1:nrow(y)) {
  if(i > 1) {
    beta[i, ] <- beta[i-1, ]
    R <- P + Vw
  y_est[i] <- x[i, ] %*% beta[i, ]</pre>
  Q[i] \leftarrow x[i, ] %*% R %*% t(x[i, ]) + Ve
```

```
e[i] <- y[i] - y_est[i]</pre>
  K \leftarrow R \% \% t(x[i, ]) / Q[i]
  beta[i, ] <- beta[i, ] + K * e[i]
  P = R - K \% * \% x[i, ] \% * \% R
e <- xts(e, order.by=index(xy))
sqrtQ <- xts(sqrt(Q), order.by=index(xy))</pre>
signals <- merge(e, 3*sqrtQ, 3*-sqrtQ)</pre>
colnames(signals) <- c("e", "sqrtQ", "negsqrtQ")</pre>
sig <- ifelse((signals[1:length(index(signals))]$e > signals[1:length(index(signals))]$sqrtQ) & (lag.xt
            ifelse((signals[1:length(index(signals))]$e < signals[1:length(index(signals))]$negsqrtQ) &</pre>
colnames(sig) <- "sig"</pre>
sig[sig == 0] \leftarrow NA
sig <- na.locf(sig)</pre>
sig <- diff(sig)/2</pre>
plot(sig)
sim <- merge(lag.xts(sig,1), beta[, 1], x[, 1], y)</pre>
colnames(sim) <- c("sig", "hedge", tickers[1], tickers[2])</pre>
i <- t
sim$posX <- sim$sig * -1</pre>
difference <-c(diff(sim[,3])/sim[,3][-1] )</pre>
pos<- sim$posX * difference</pre>
print(pos)
a <- sapply(list,func)</pre>
date <-rownames(as.data.frame(xy))</pre>
a<-a %>% as.data.frame()
a <-a %>% na.omit() %>% rowMeans() %>% as.vector()
silver_strategy <- data.frame(value=a)</pre>
rownames(silver_strategy) <- date[(length(date)-(nrow(silver_strategy)-1)):length(date)]</pre>
silver_strategy <-silver_strategy %>% as.xts()
silver_strategy %% as.data.frame() %>% mutate(date=as.Date(rownames(.)), value=cumprod(value+1)) %>%
  ggplot(aes(date,value))+geom_line()+scale_y_log10()+ ggtitle("cumulative returns Silver Strategy")
```

## cumulative returns Silver Strategy



annualReturn(cumprod(silver\_strategy+1)) %>% as.data.frame() %>% mutate(date=as.factor(round(year(as.Darggplot(aes(date,yearly.returns))+geom\_bar(stat = 'identity')+ ggtitle("Annual returns Silver Strategy

# Annual returns Silver Strategy

