

Multigrid Method

Fast Iterative Solvers, Project 2

Johannes Leonard Grafen, 380149

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1 Remarks on used architecture and compiler options

The code was written in C++, compiled using the Clang compiler and executed on an Apple Silicon M1 Pro Chip featuring the ARM64 architecture. To measure timings, the high resolution clock of the std chrono library was employed. The following flags were passed to the compiler to enhance code performance of the aforementioned architecture: -march=native, -O2.

2 Multigrid Method - MG

2.1 Convergence Plots

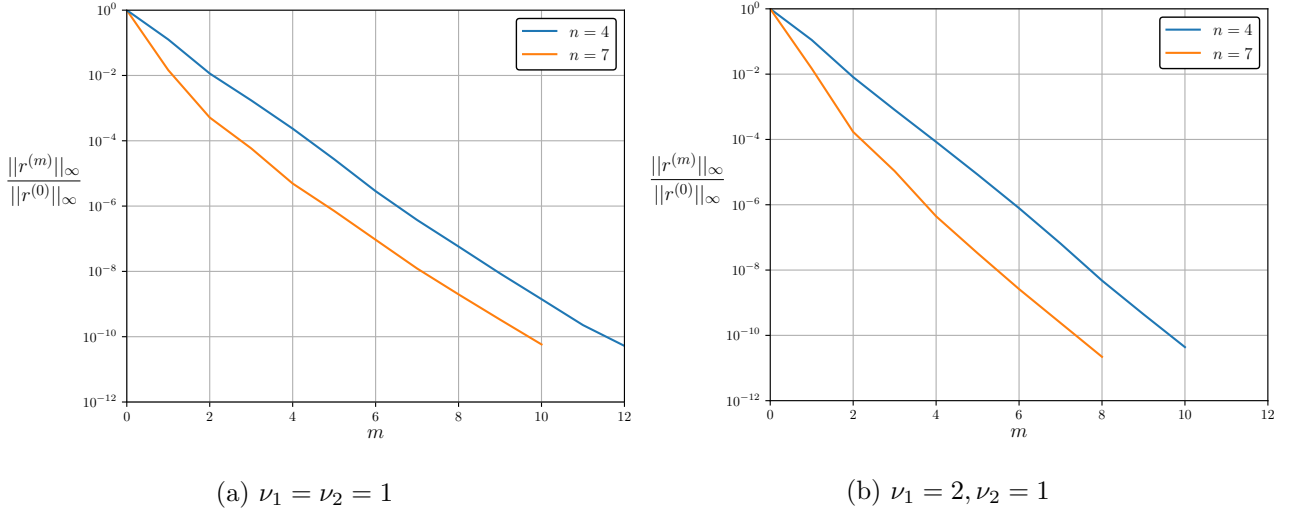


Figure 1: Convergence against multigrid iterations m for meshes $n = 4$ and $n = 7$

2.2 Convergence for different ν_1

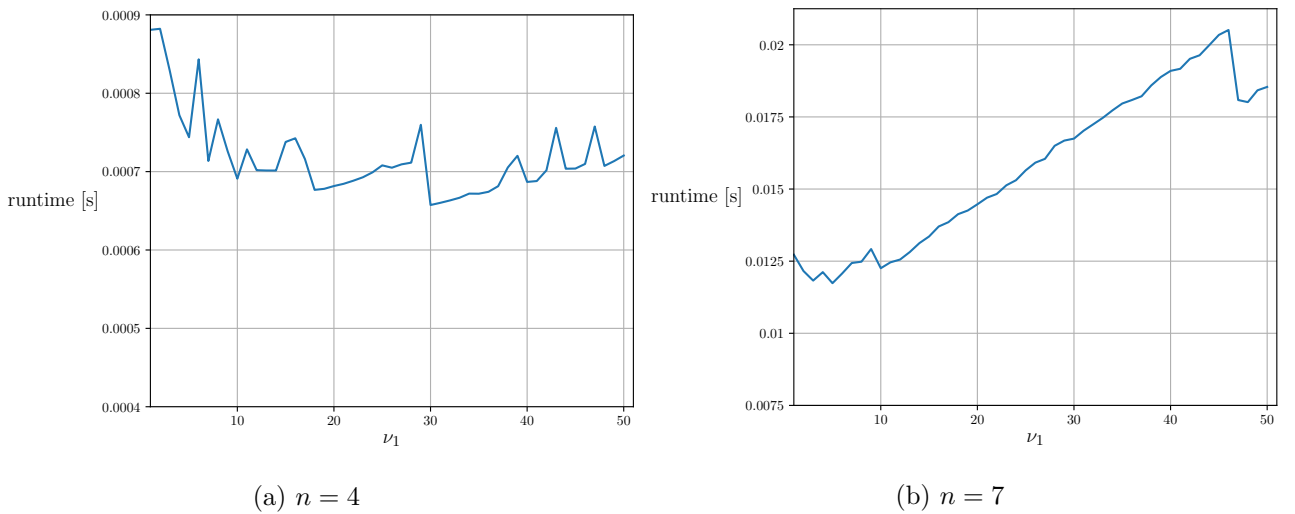
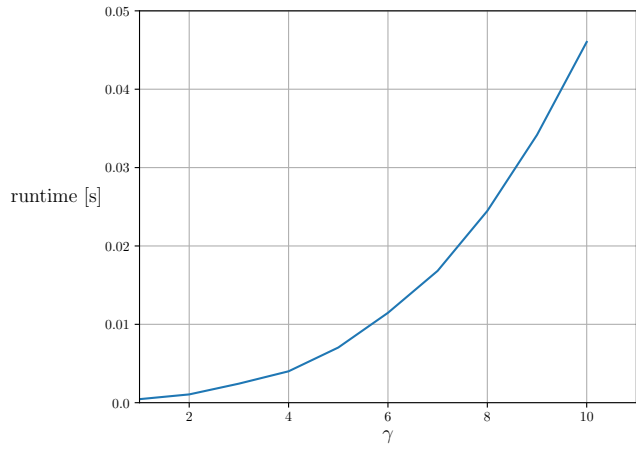
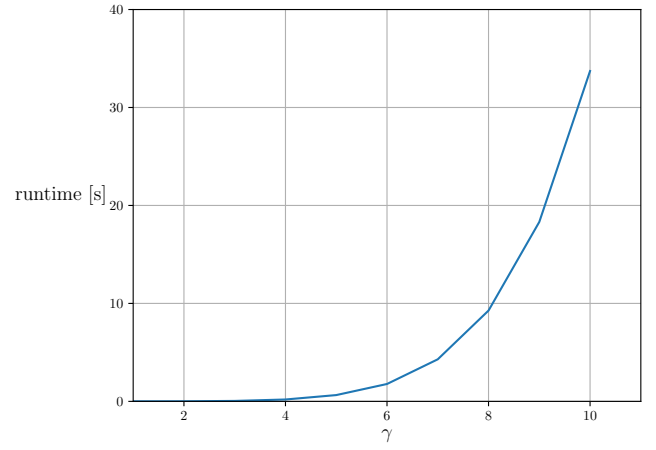


Figure 2: Runtime against number of smoothing iterations $\nu_1 = 1 \dots 50$ for meshes $n = 4$ and $n = 7$

2.3 Convergence for different γ



(a) $n = 4$



(b) $n = 7$

Figure 3: Runtime against number of γ -cycles for $\gamma = 1 \dots 10$ for meshes $n = 4$ and $n = 7$