## ilu(0) Algorithm

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## Algorithm 1 ILU(0) in MSR format. No zero elements on diagonal.

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Input: V, JM (Matrix in MSR Format. Size of both arrays: nz)
Output: PV,PJM (Preconditioner in MSR format. Size of both arrays: nz)
JD (Size: n. Pointer to first non-zero element in upper triangle for each row)
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```
1: JR(1:n) = 0
                            ▷ Initialize reverse pointers. (Column index to index in PJM,PV)
 2: JD(1:n) = 0
                                                            ▶ Initialize pointers to upper triangle
 3: PJM(1:nz) = JM(1:nz)
                                                   ▷ Copy column pointers. These don't change
 4: PV(1:nz) = V(1:nz)
                                         ▷ Copy data pointer. Will be modified in-place below
 5:  for i=1,n do
                                                                                 ▶ Loop over Rows
        JR(i) = i
                                                        ▶ Reverse pointer is identity for diagonal
        for j=JM(i),JM(i+1)-1 do
                                            ▷ Loop over non-zero off-diagonal elements in row i
 7:
           \mathrm{jc} := \mathrm{JM}(\underline{\mathrm{j}})
                                                                 \triangleright Column index: PV(j) = a(i,jc)
 8:
                                        ▷ Reverse pointer (column index to index in PJM,PV)
 9:
           JR(jc):=j
           if jc > i and JD(i) = 0 then
10:
                                                            \triangleright Pointer to upper triangle (i^{th} row)
               JD(i) = i
11:
            end if
12:
        end for
13:
14:
        if JD(i) = 0 then
            JD(i) = j
                                                                ▶ If no elements in upper triangle
15:
        end if
16:
        for j=JM(i),JD(i)-1 do
                                                      ⊳ non-zero elem. in lower triangle of row i
17:
           jc := JM(j)
                                                        \triangleright column index, P(j)=a(i,jc). Note: jc < i
18:
                                                       \triangleright P(jc)=a(jc,jc). Overwrite with L-factor
           PV(j) \leftarrow PV(j)/PV(jc)
19:
            for jj=JD(jc),JM(jc+1)-1 do
                                                           \triangleright all non-zero a(jc,k) (jc < k=JM(jj))
20:
               jk := JR(JM(jj))
                                                                ▶ Points back to a(i,k) (k=JM(jj)
21:
               if jk \neq 0 then
                                                          \triangleright Could be zero, as a(i,k)=0 is possible
22:
                   PV(jk) \leftarrow PV(jk) - PV(j)*PV(jj)
                                                                     \triangleright PV(jj)=a(jc,k) (k=JM(jj))
23:
               end if
24:
25:
            end for
        end for
26:
        JR(i) = 0
27:

    ▶ Reset reverse pointers

        for j=JM(i),JM(i+1)-1 do
28:
            JR(JM(j)) = 0
        end for
31: end for
```