

# The top quark legacy of the LHC Run II for PDF and SMEFT analyses

for HEFT 2023, in Manchester



The University of Manchester



**James Moore, University of Cambridge**



# PBSP: Physics Beyond the Standard Proton

- The **PBSP group** is based at the **University of Cambridge**, and is headed by **Maria Ubiali**; the project is **ERC-funded**.
- The aim is to **investigate interplay between BSM physics and proton structure** - the subject of the rest of this talk!
- The team members are:
  - Postdocs: Zahari Kassabov, Maeve Madigan, Luca Mantani
  - *PhD students*: Mark Costantini, Shayan Iranipour (*former*), Elie Hammou, **James Moore**, Manuel Morales, Cameron Voisey (*former*)



European Research Council

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# Talk overview

- 1. Joint PDF-SMEFT fits**
- 2. The SIMUnet methodology**
- 3. The top quark legacy of the LHC Run II for PDF and SMEFT analyses**

# **1. - Joint PDF-SMEFT fits**

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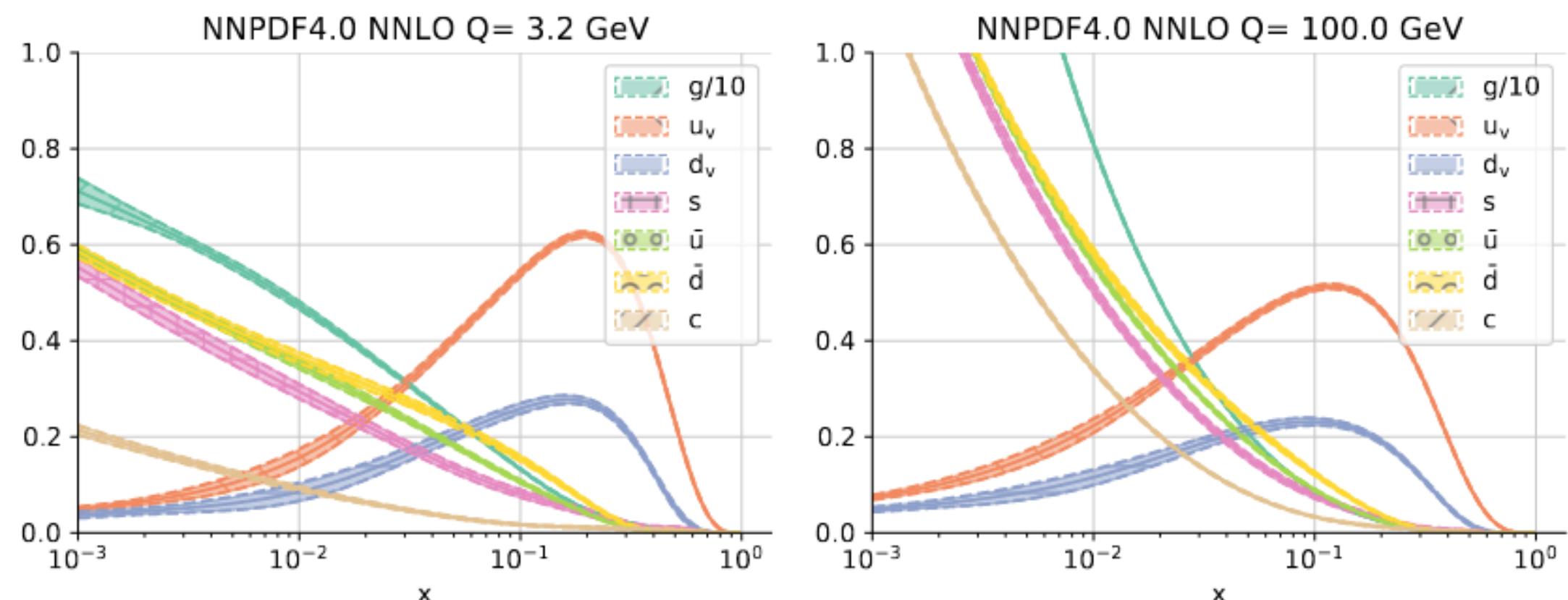
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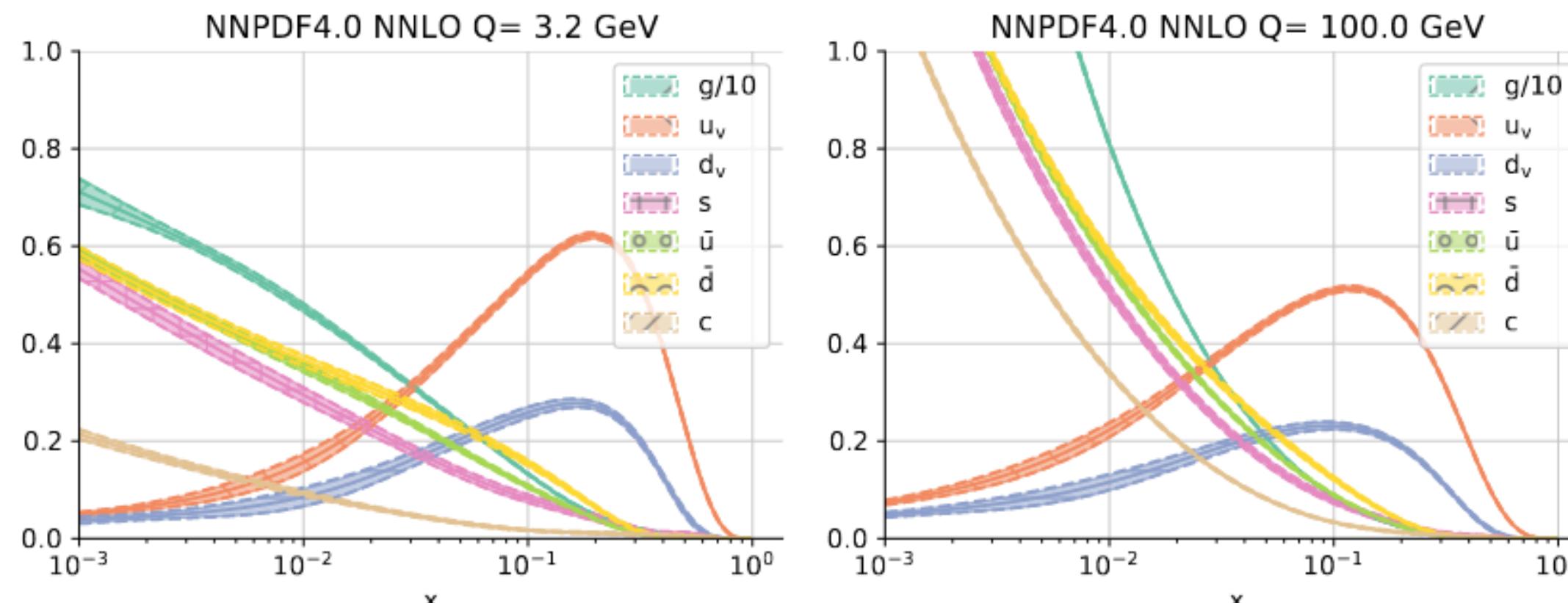
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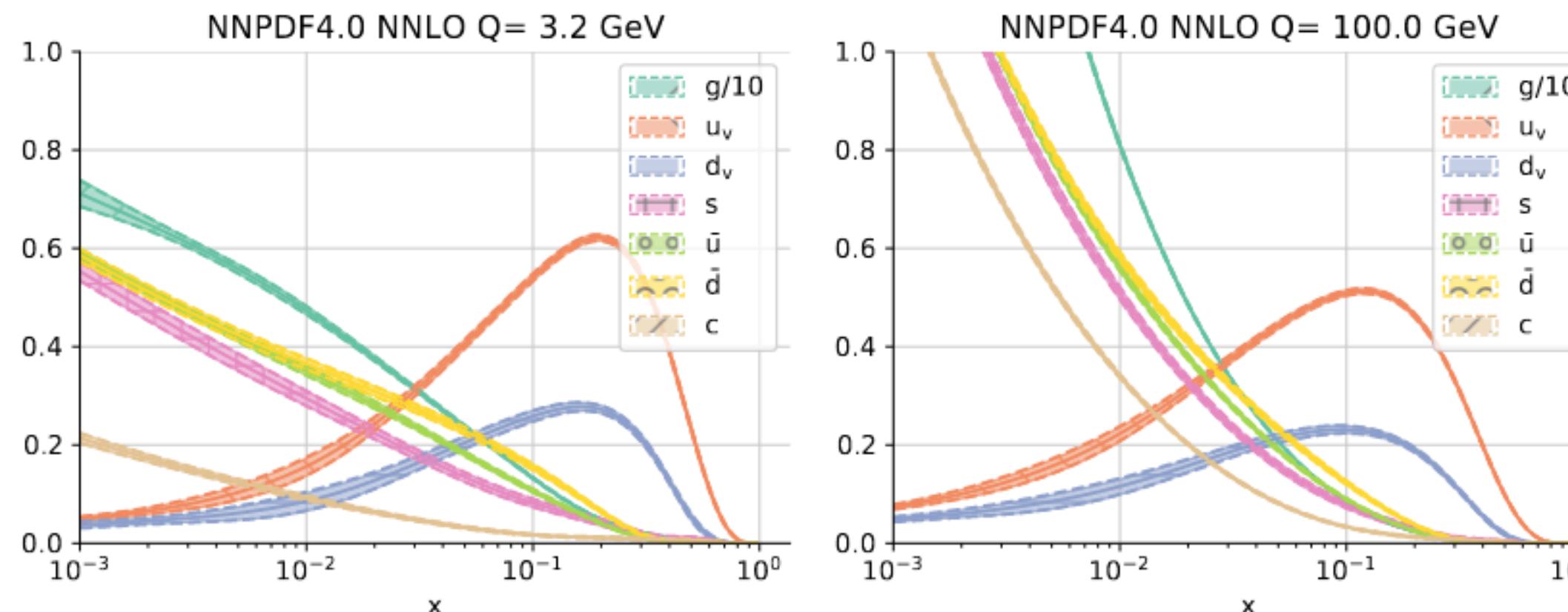
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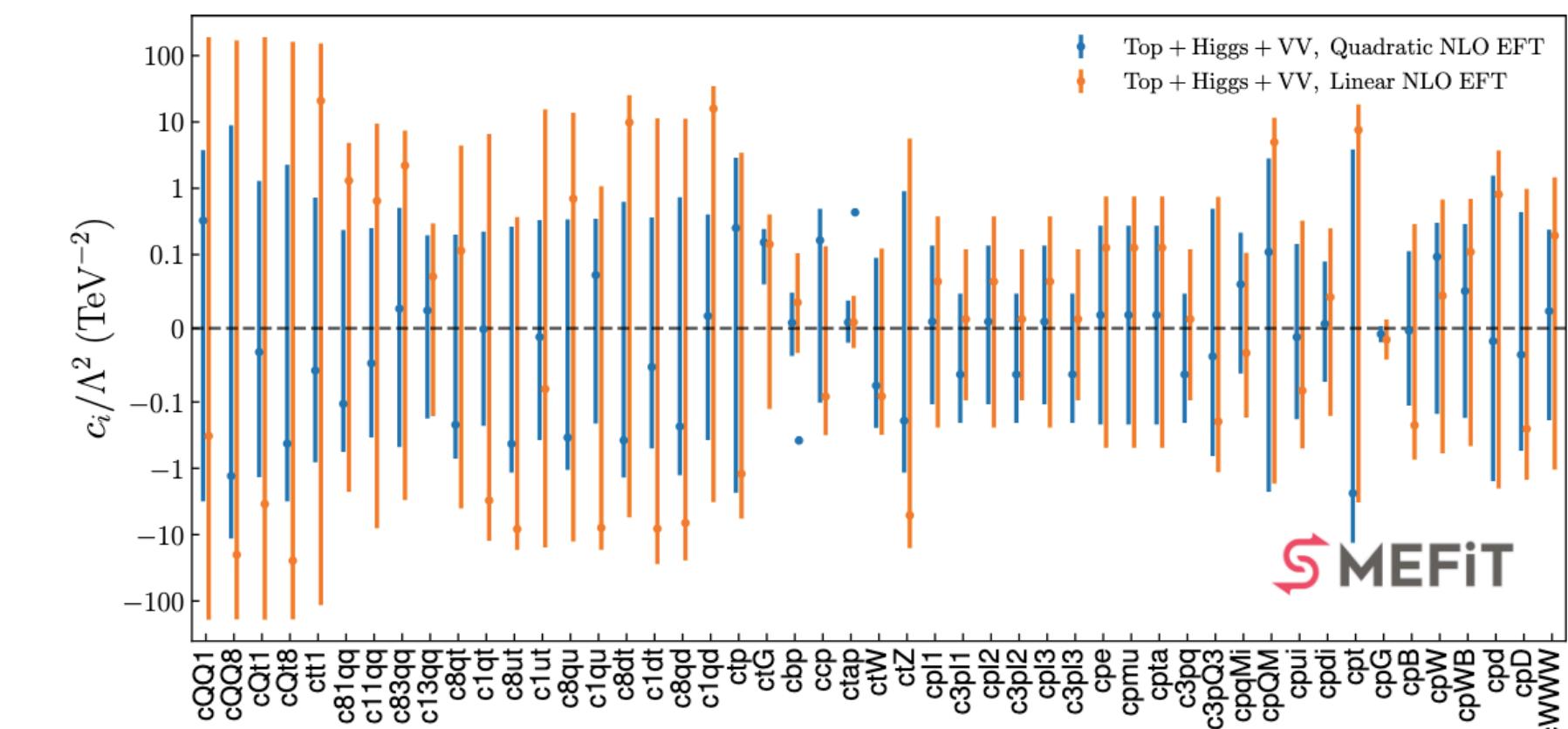
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- E.g. SMEFiT, Ethier et al., 2105.00006.



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- This could lead to inconsistencies.

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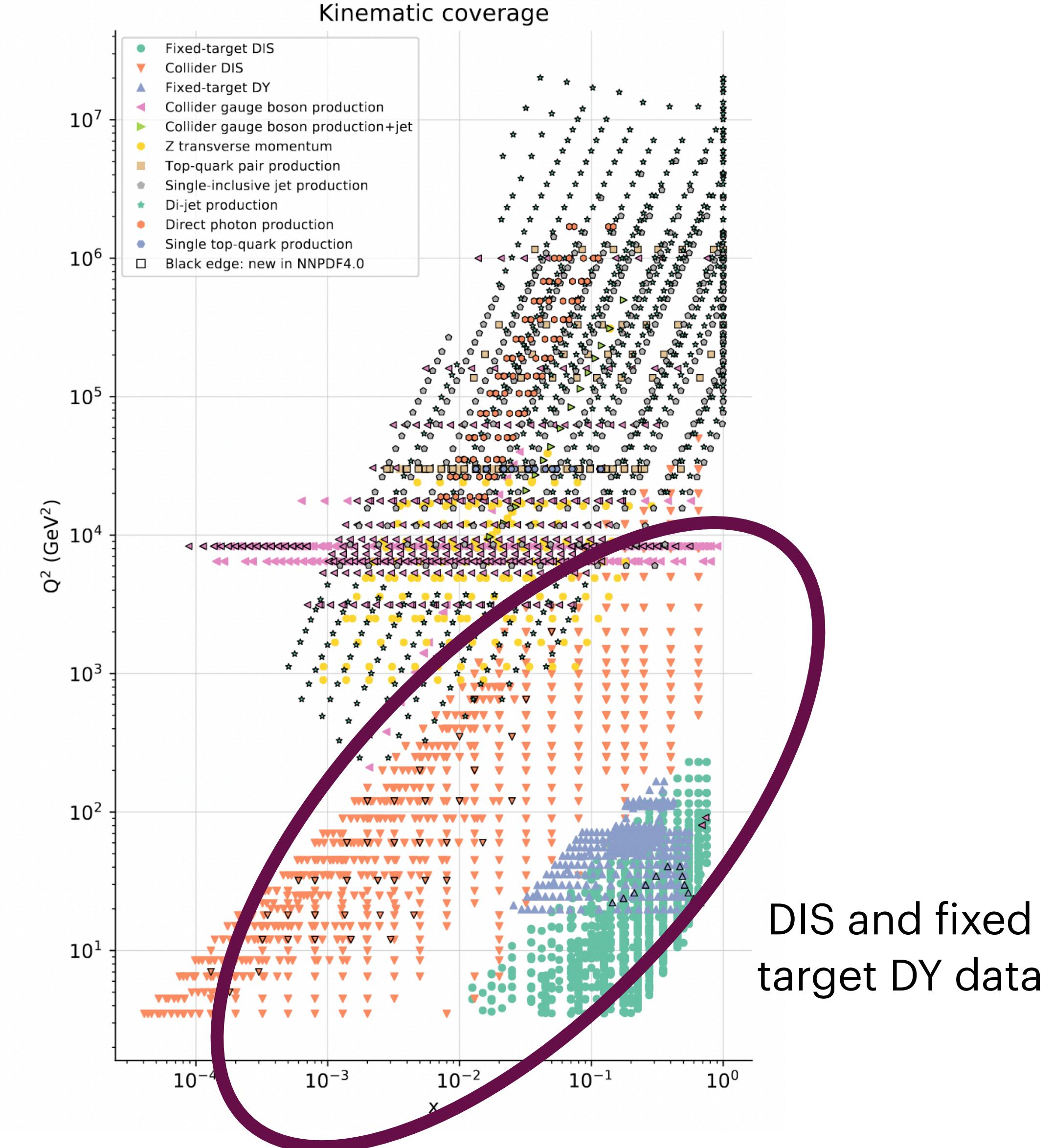
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- In particular, if we fit PDFs **assuming all SMEFT couplings are zero**, but then **use those PDFs in a fit of SMEFT couplings**, our resulting bounds **could be misleading**. The same applies to SM parameters.
- We could even **miss New Physics**, or **see New Physics that isn't really there!**

# PDF-SMEFT interplay: natural questions

- Question 1: **Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**

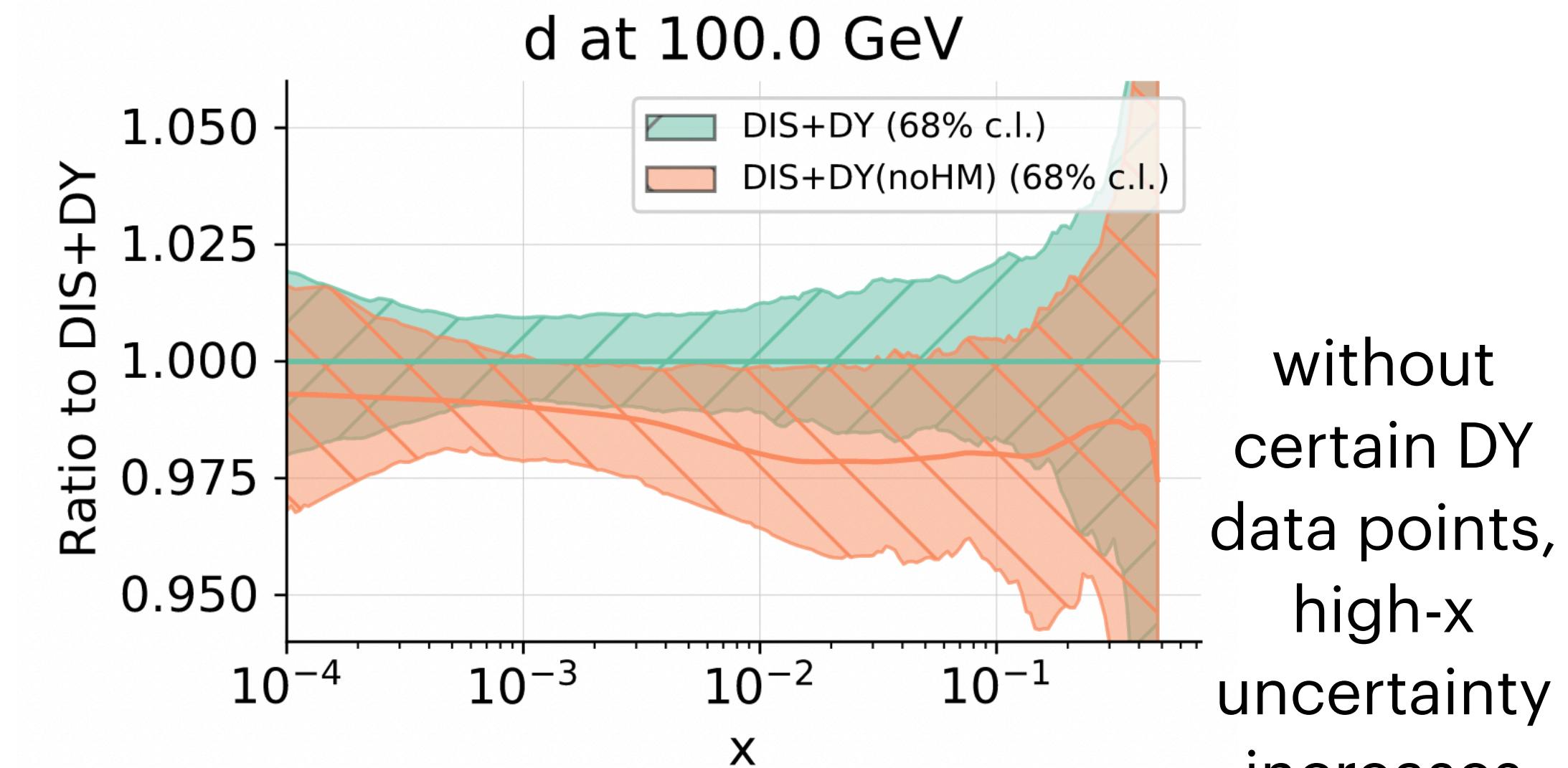
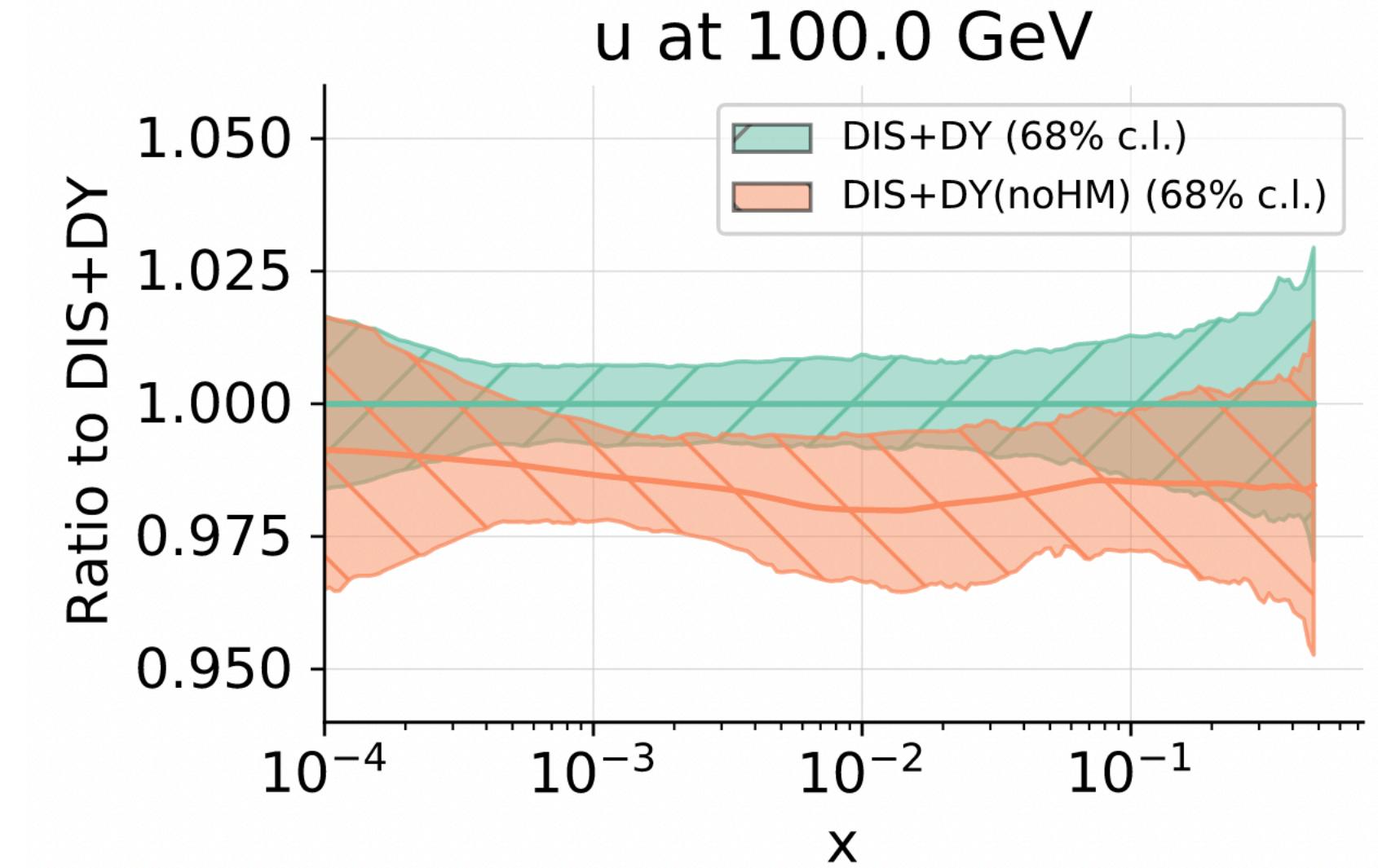
# PDF-SMEFT interplay: natural questions

- Question 1: **Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**
  - It depends on the SMEFT operators. Some operators (e.g. four-fermion operators) will **contaminate DIS and DY data**, which comprise the majority of the data going into PDF fits. So often '*uncontaminated PDFs*' don't exist!
  - Right: kinematic coverage of NNPDF4.0 by dataset.



# PDF-SMEFT interplay: natural questions

- Question 1: **Can't I just use PDF sets which are fitted using data that is not affected by SMEFT operators?**
  - Furthermore, if we include more data in a PDF fit, we obtain **better quality fits**. Therefore, we expect that using ‘uncontaminated’ PDFs will result in **poorer quality SMEFT fits**; we won’t be using the ‘best quality’ PDFs that are available - this is shown explicitly in *Greljo et al.*, 2104.02723, where PDF sets including and excluding high-mass DY data are compared.



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- Question 2: **Won't the PDF-SMEFT interplay be negligible?**

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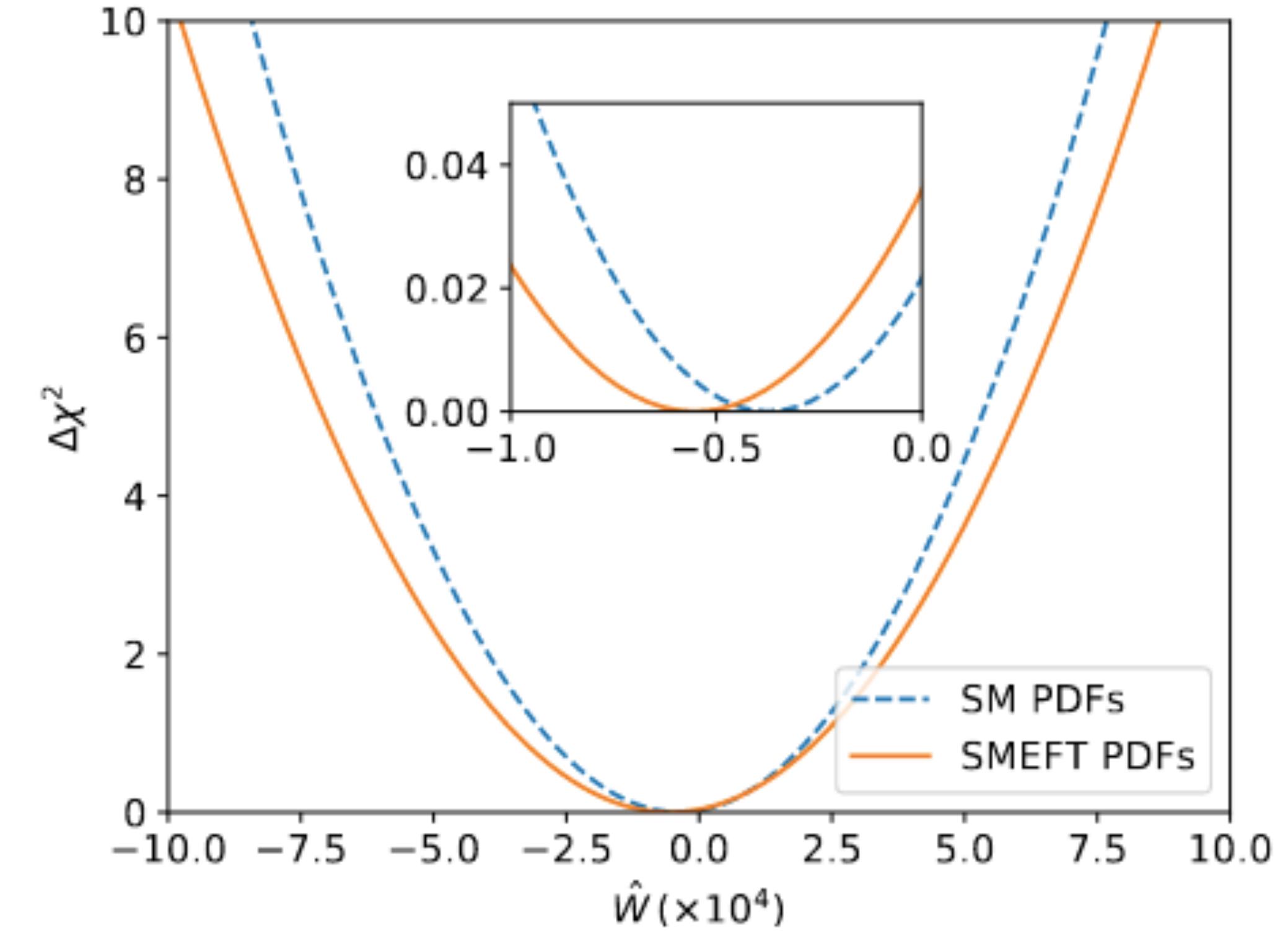
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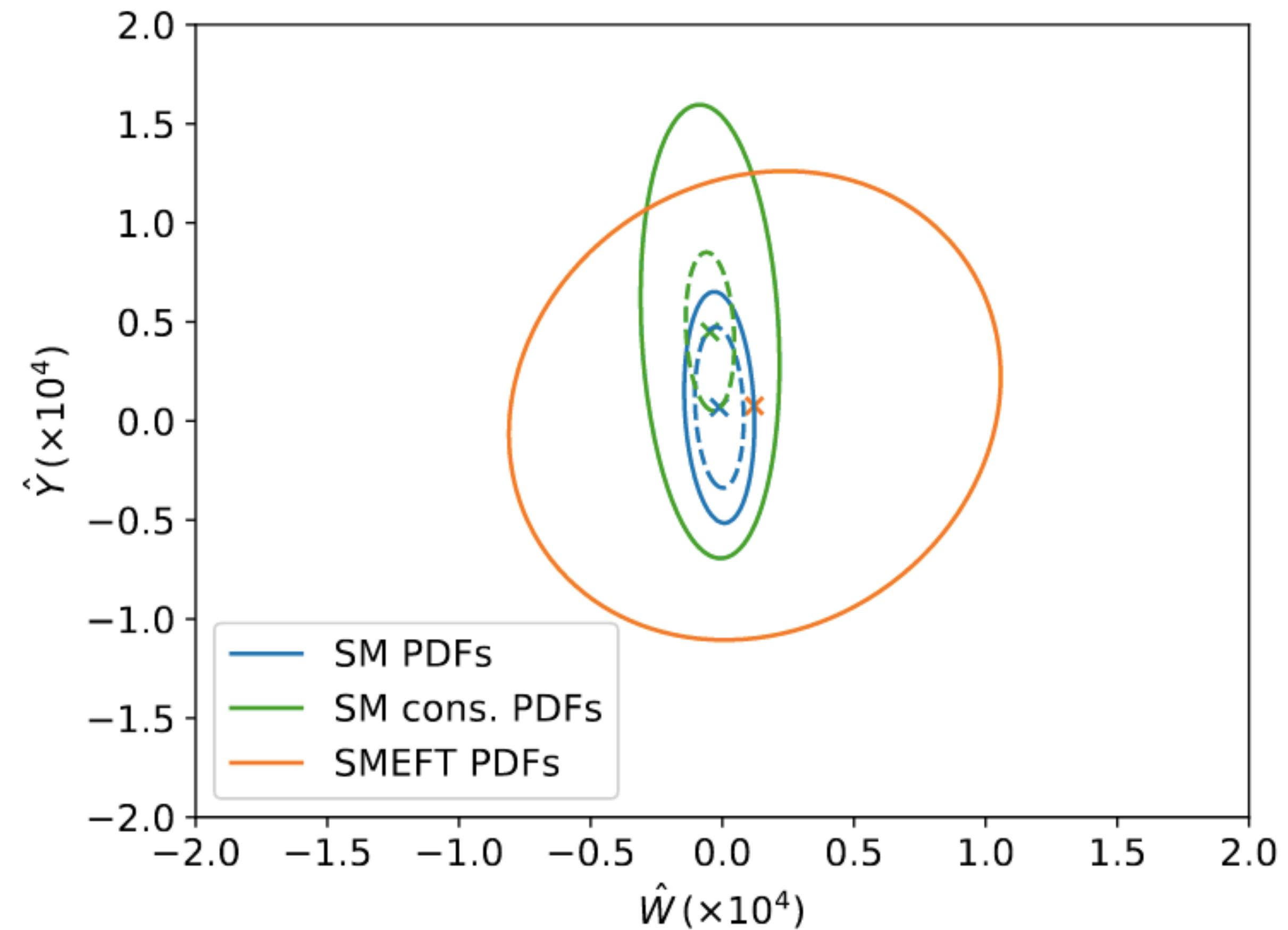
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  - It depends on the scenario!
  - It was shown in *Carrazza et al.*, 1905.05215, that interplay is very mild in the case of simultaneous extractions of four-fermion operators and PDFs using DIS-only data.
  - Similarly, it was shown in the PBSP team's earlier study, *Greljo et al.*, 2104.02723, that interplay is mild between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using current DIS and DY data.



# PDF-SMEFT interplay: natural questions

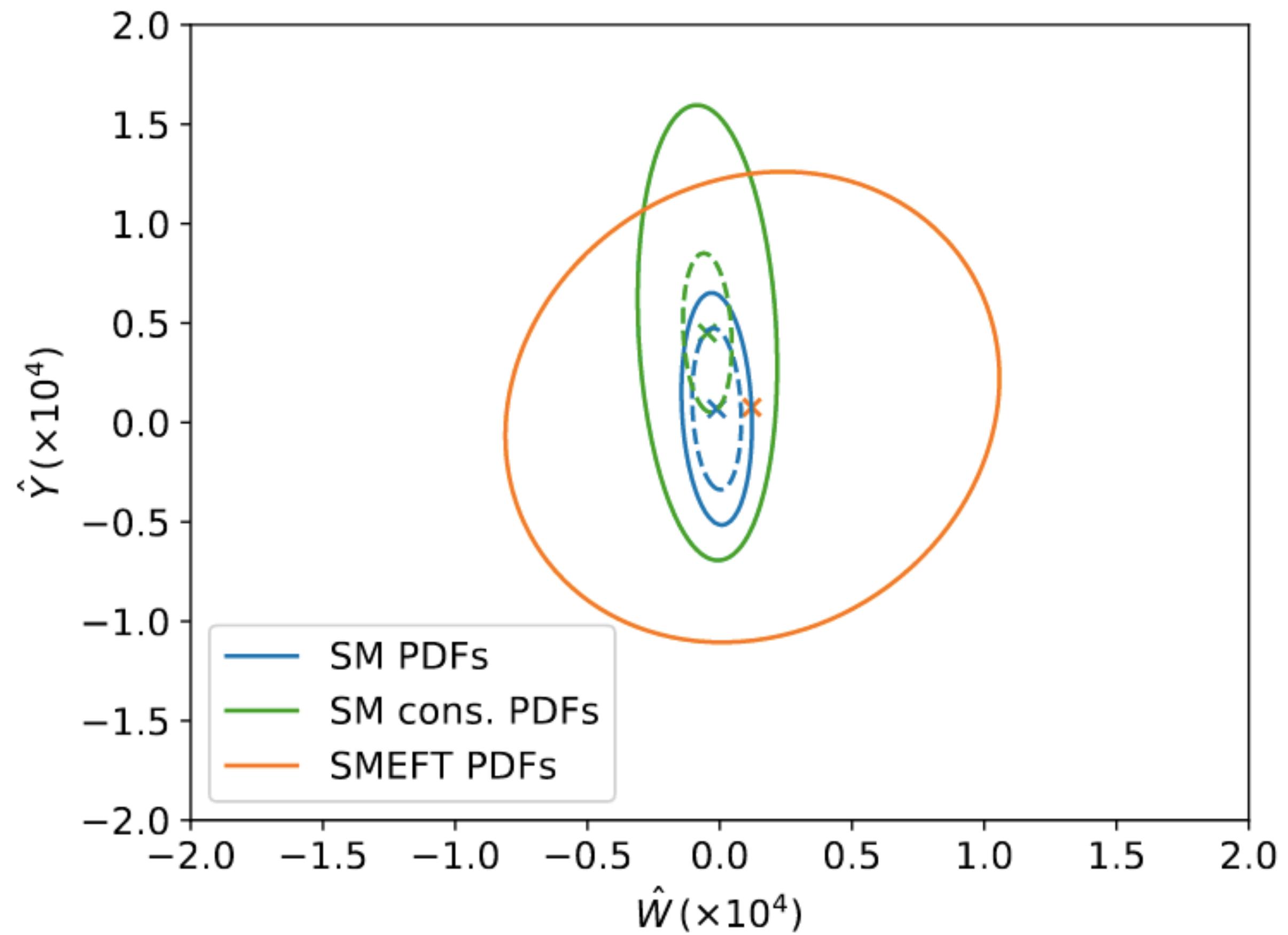
- Question 2: **Won't the PDF-SMEFT interplay be negligible?**

- However, it was also shown in Greljo et al., 2104.02723, that interplay is **very significant** between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using **projected high-luminosity DY data**.



# PDF-SMEFT interplay: natural questions

- Question 2: **Won't the PDF-SMEFT interplay be negligible?**
  - However, it was also shown in Greljo et al., 2104.02723, that interplay is **very significant** between the  $\hat{W}$ ,  $\hat{Y}$  operators and PDFs using **projected high-luminosity DY data**.
  - We see that using fixed PDFs results in a **significant underestimation** of uncertainties on the WCs - we might wrongly conclude **New Physics!**



## **2. - The SIMU $\text{net}$ methodology for joint PDF-SMEFT fits**

# PDF-SMEFT interplay: methodology

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# PDF-SMEFT interplay: methodology

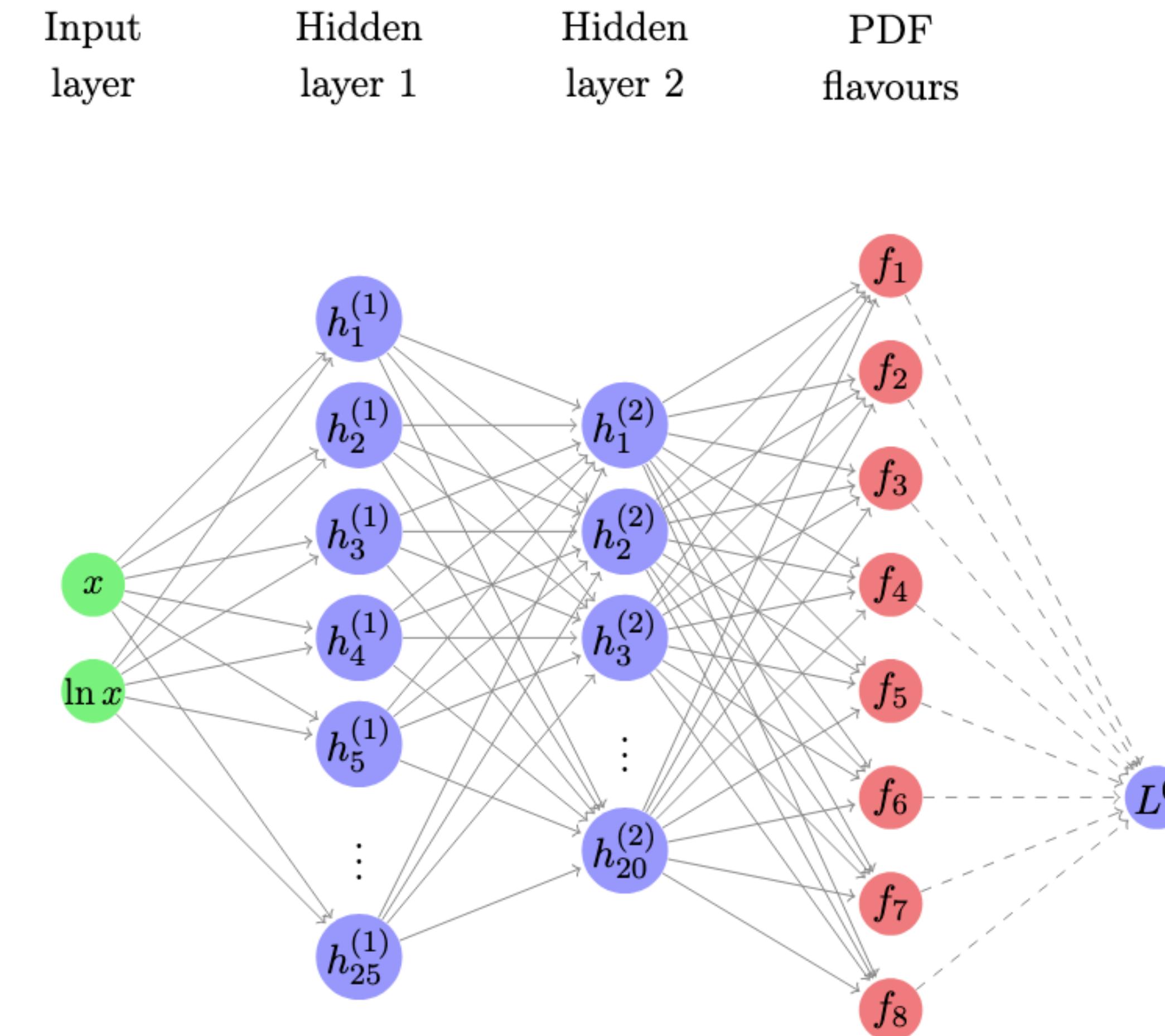
- With the need for simultaneous PDF-SMEFT determinations established, we now need an **efficient methodology** to perform the fits.
- There are three main methodologies available: (i) a **scan** in Wilson coefficient space (see 1905.05215 and 2104.02723); (ii) the **CTEQ-TEA** methodology (see 2201.06586 and 2211.01094); (iii) the **SIMUnet** methodology (see 2201.07240).

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- We will focus only on **SIMUnet**.

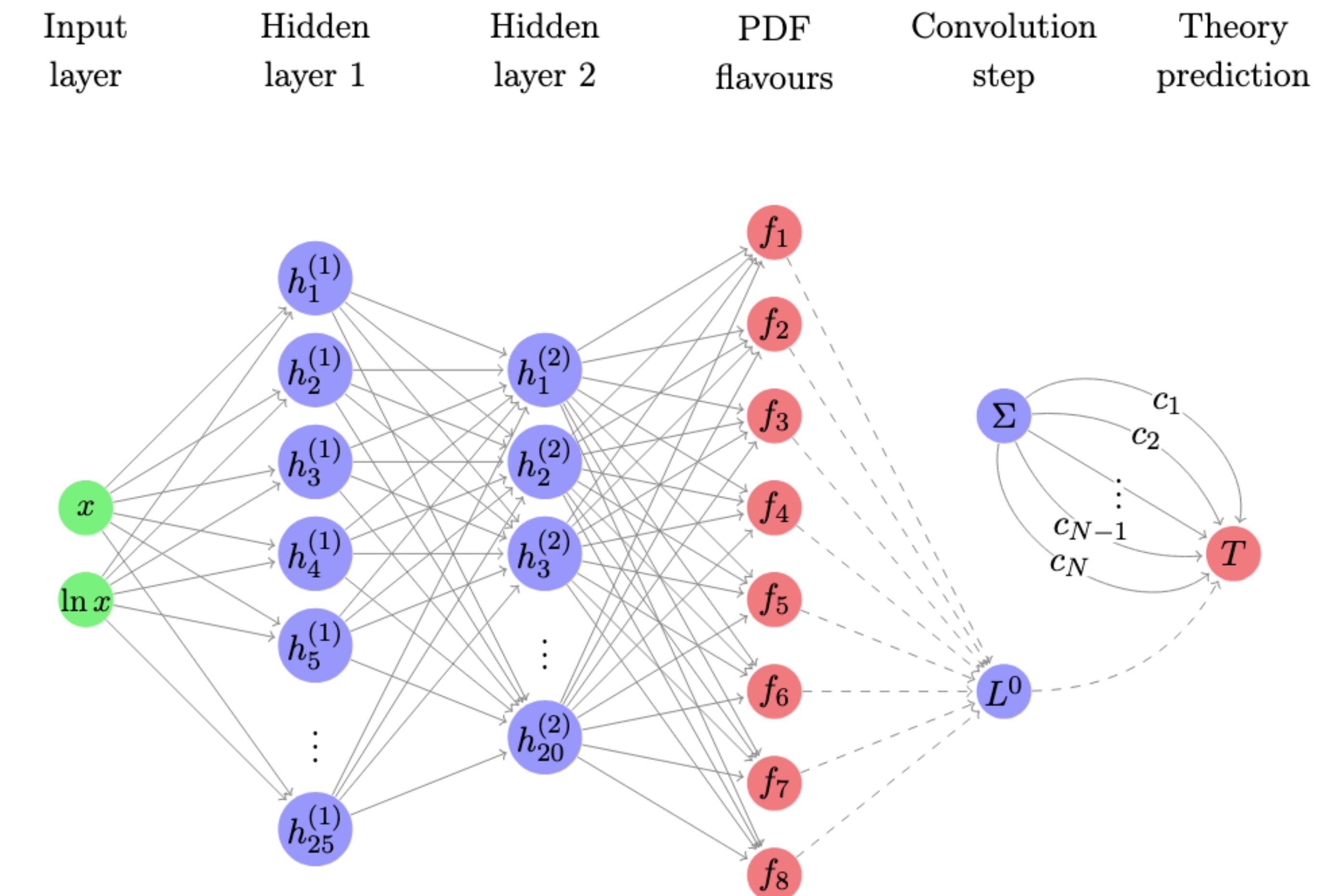
# The SIMUnet methodology: details

- The SIMUnet methodology **extends the existing NNPDF neural network** with an additional **convolution layer**.



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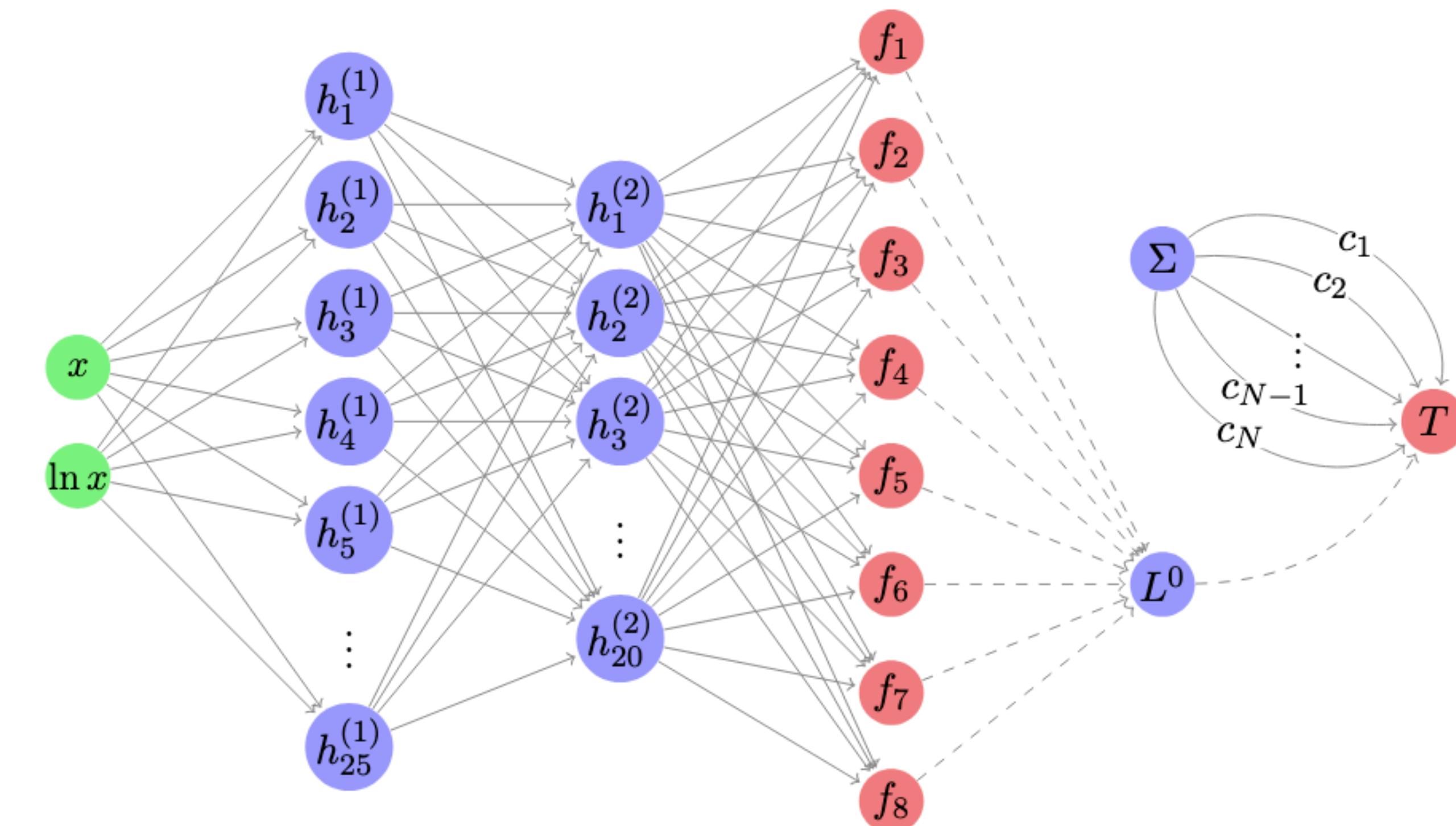
- The SIMUnet methodology **extends the existing NNPDF neural network** with an additional **convolution layer**.
- The SMEFT couplings are added as **weights of neural network edges**, and are **trained alongside the PDFs**.



# The SIMUnet methodology: details

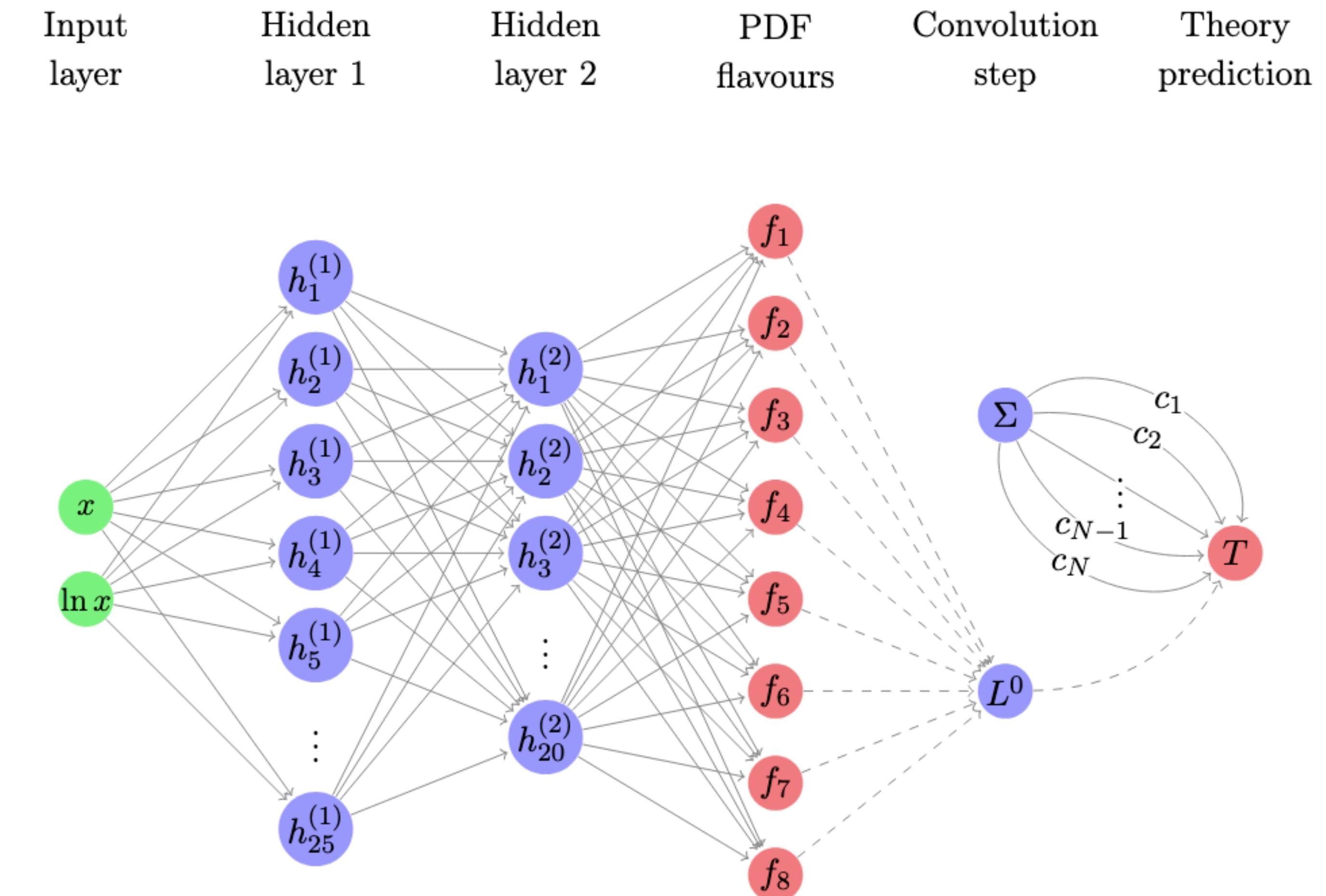
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Input layer	Hidden layer 1	Hidden layer 2	PDF flavours	Convolution step	Theory prediction
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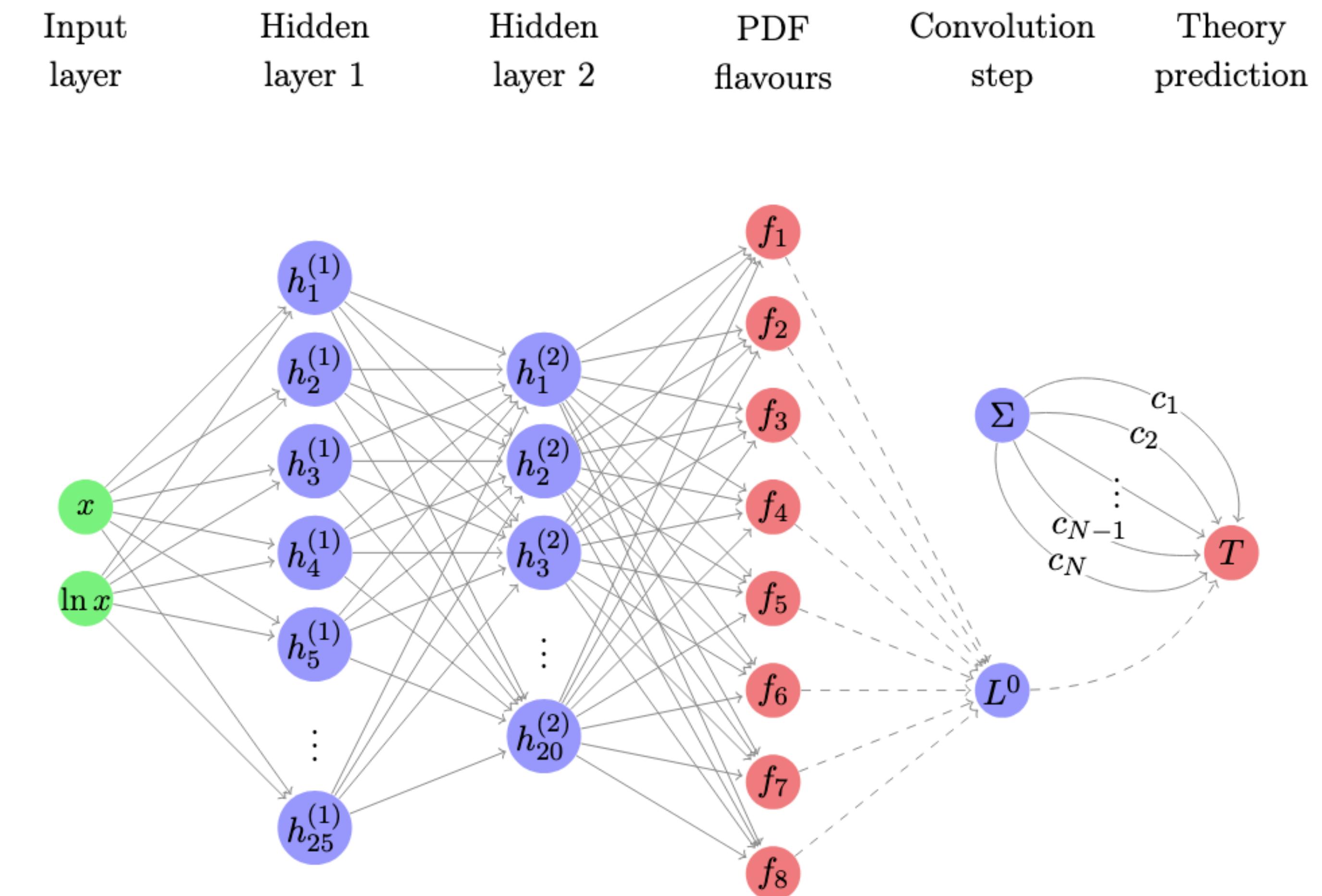
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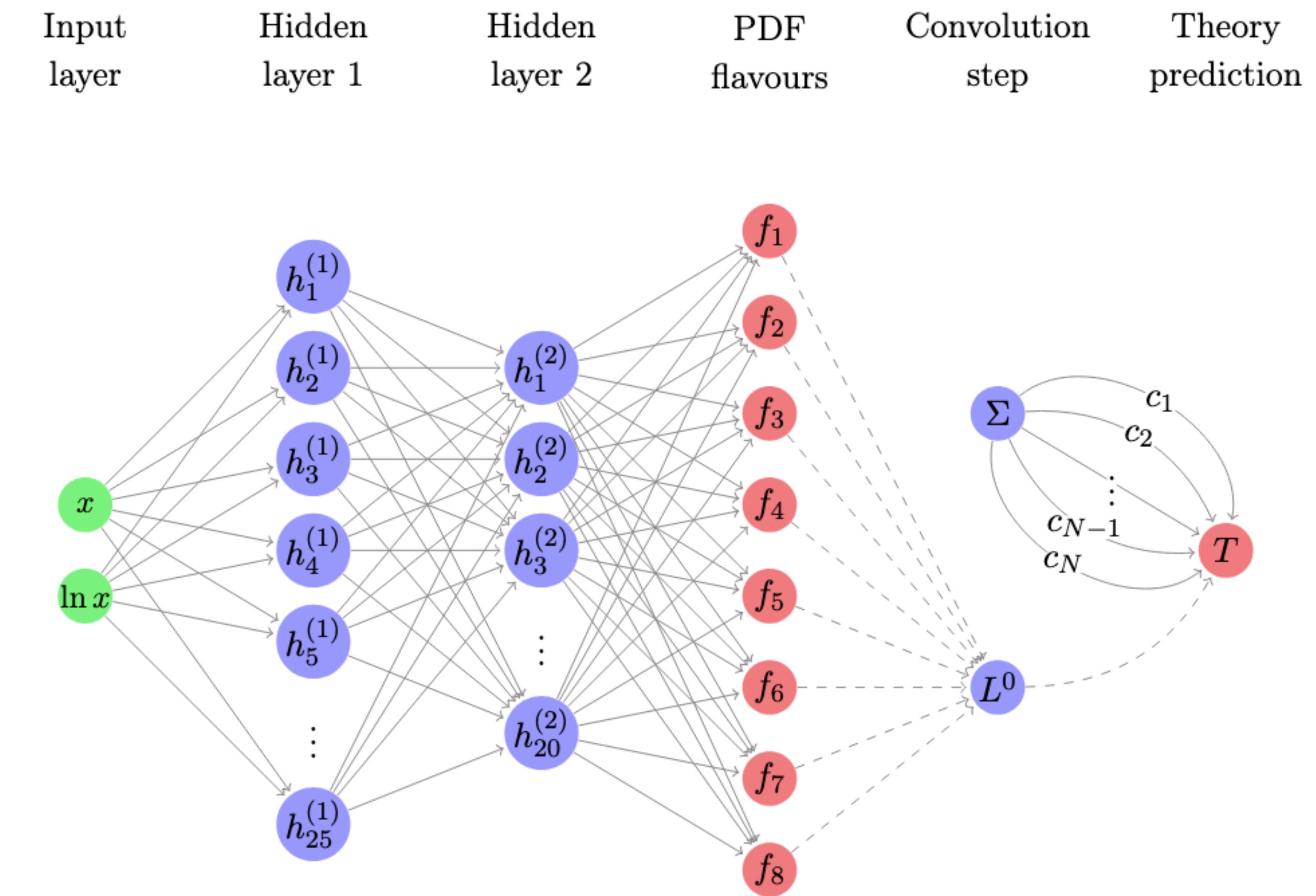
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  - Can include **quadratic\*** SMEFT corrections through **non-trainable edges**.
  - Can easily include **PDF-independent observables**.
  - Can perform **fixed PDF fits** by **freezing the PDF part of the network**.



# **3. - The top quark legacy of the LHC Run II for PDF and SMEFT analyses**

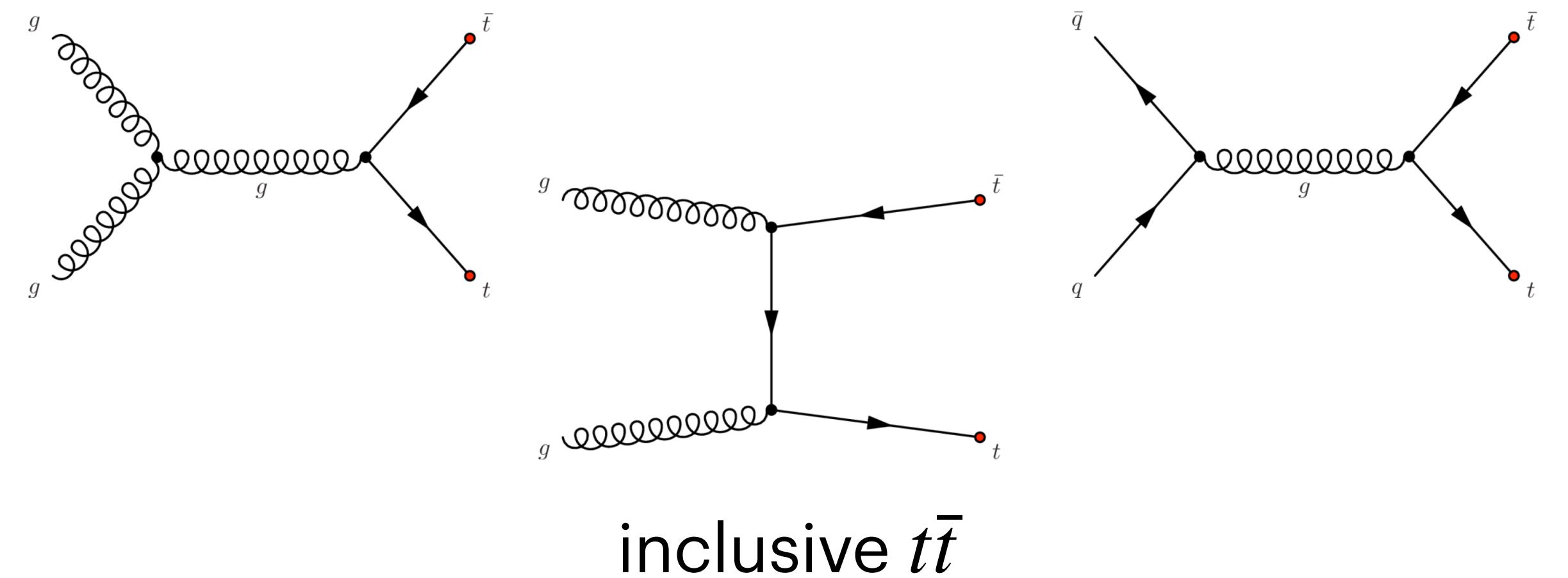
***Based on 2303.06159***

# Run II top quark data

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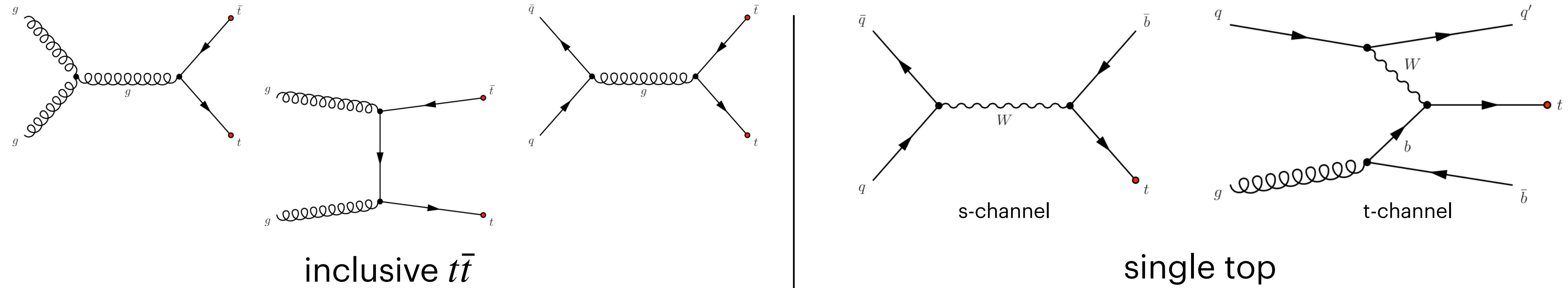
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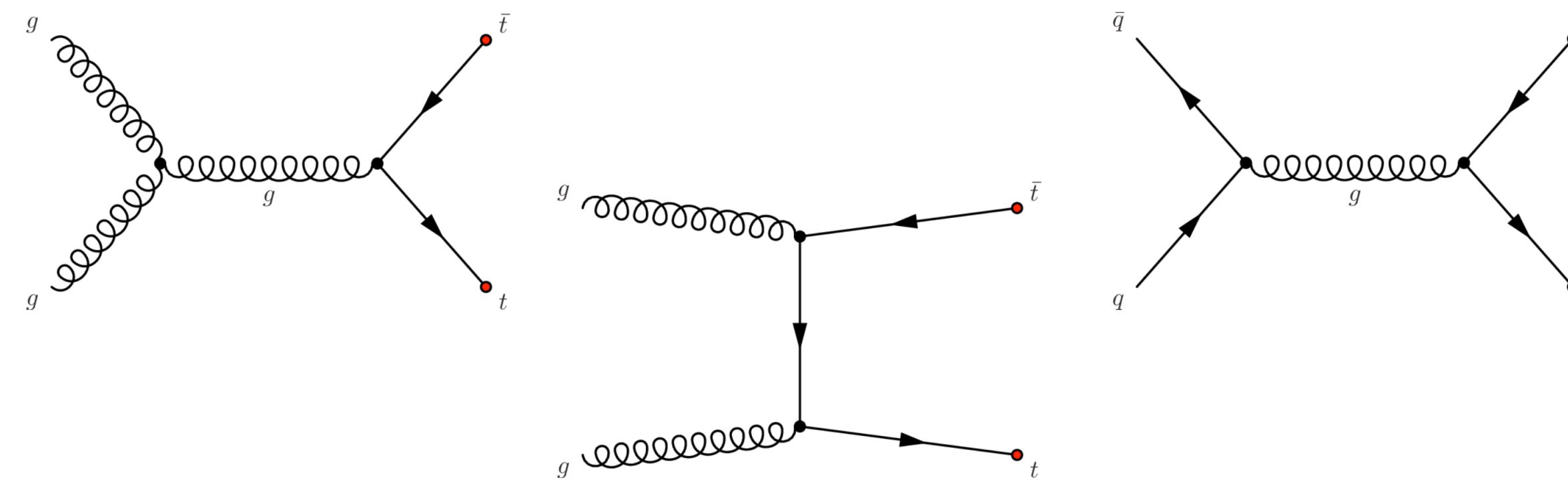
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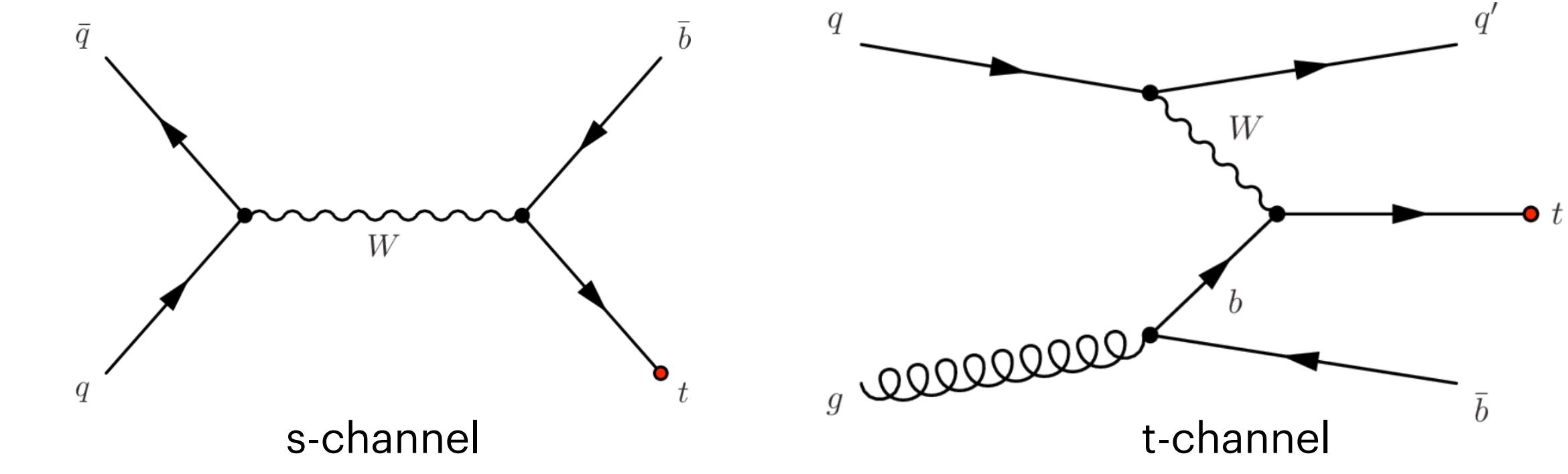


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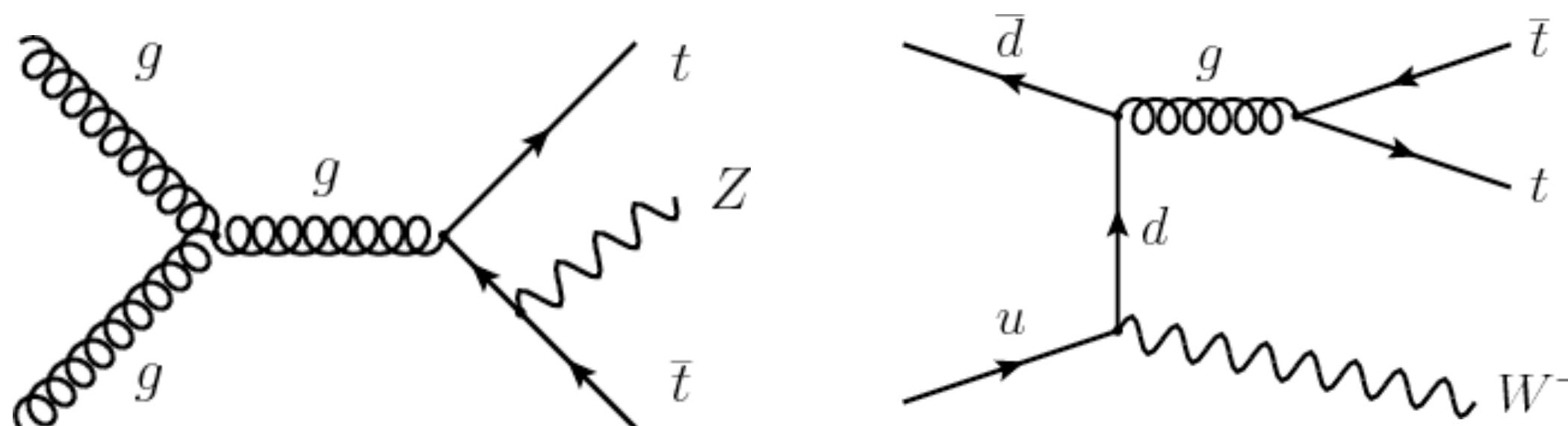
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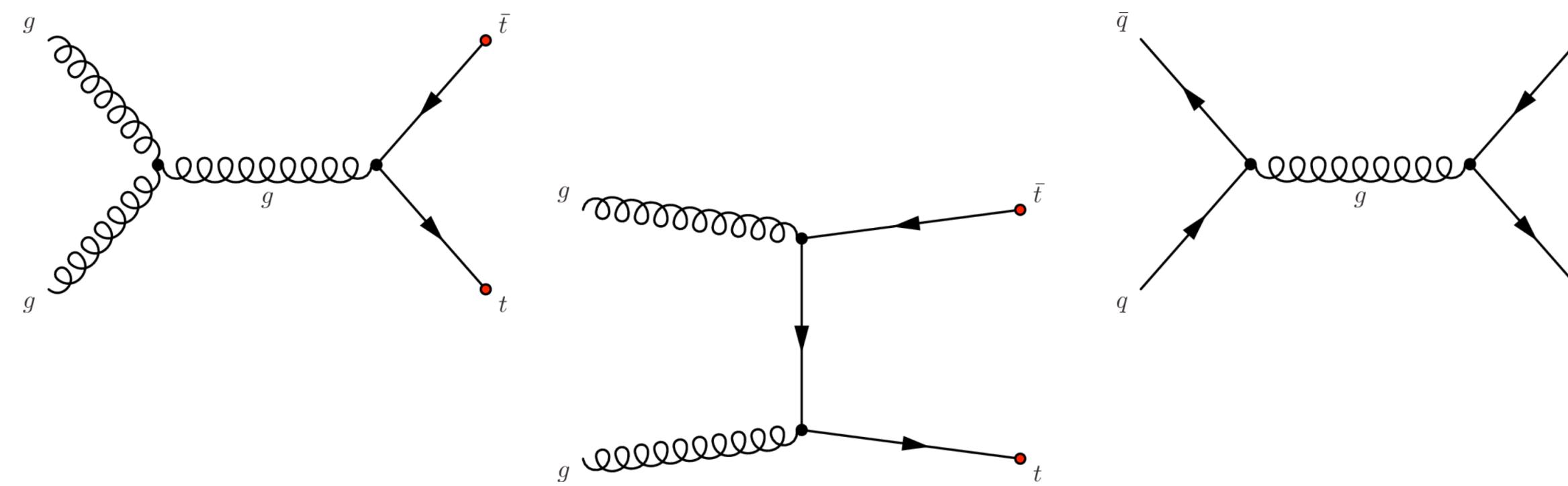
single top



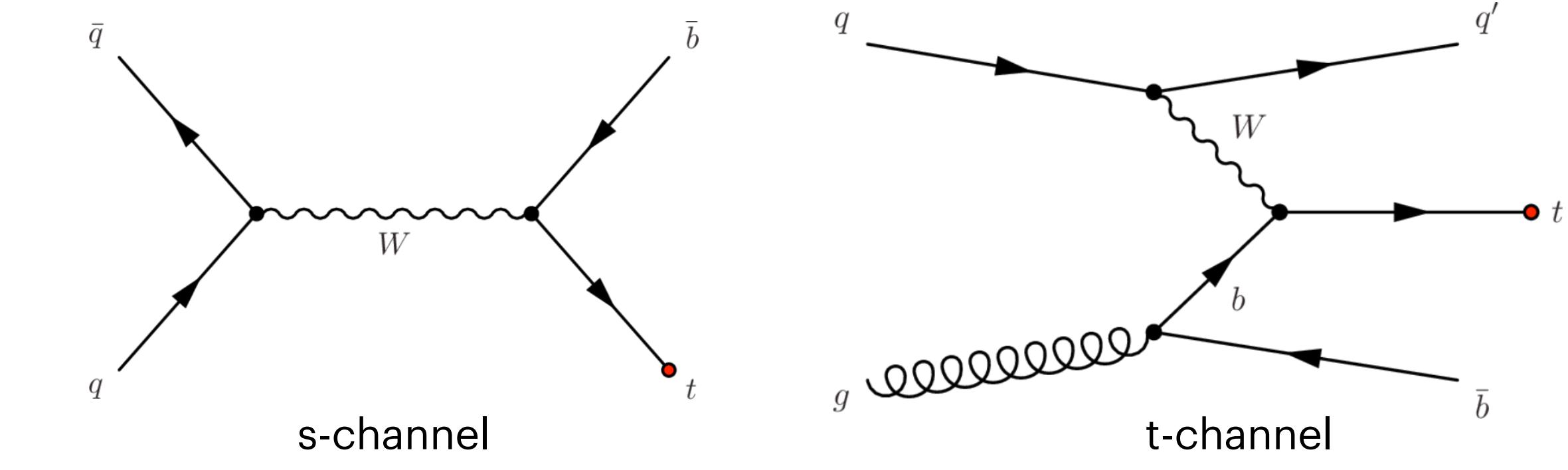
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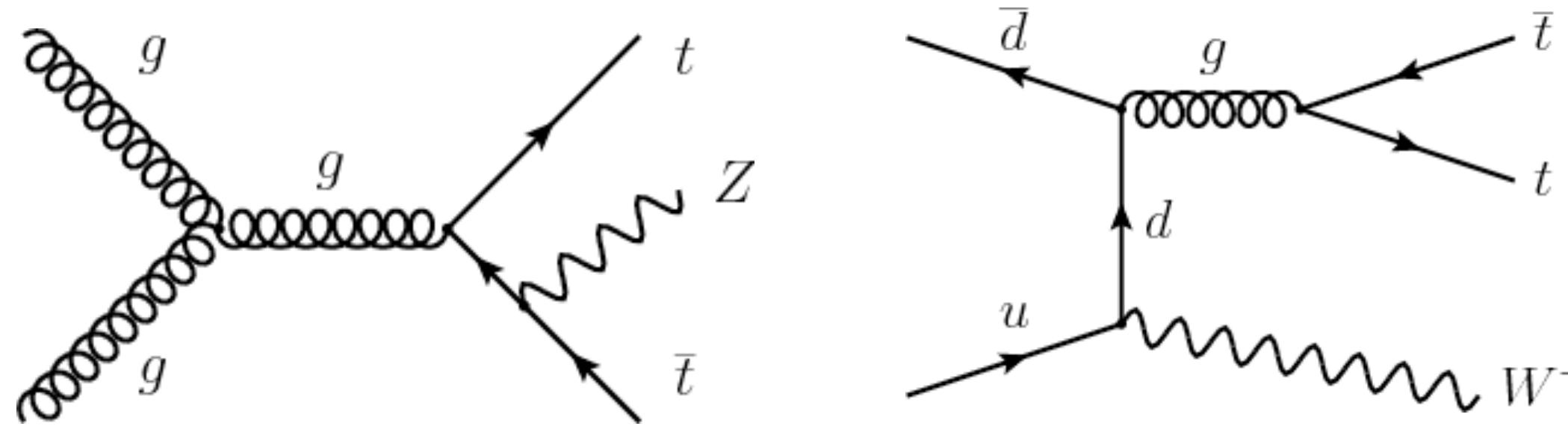
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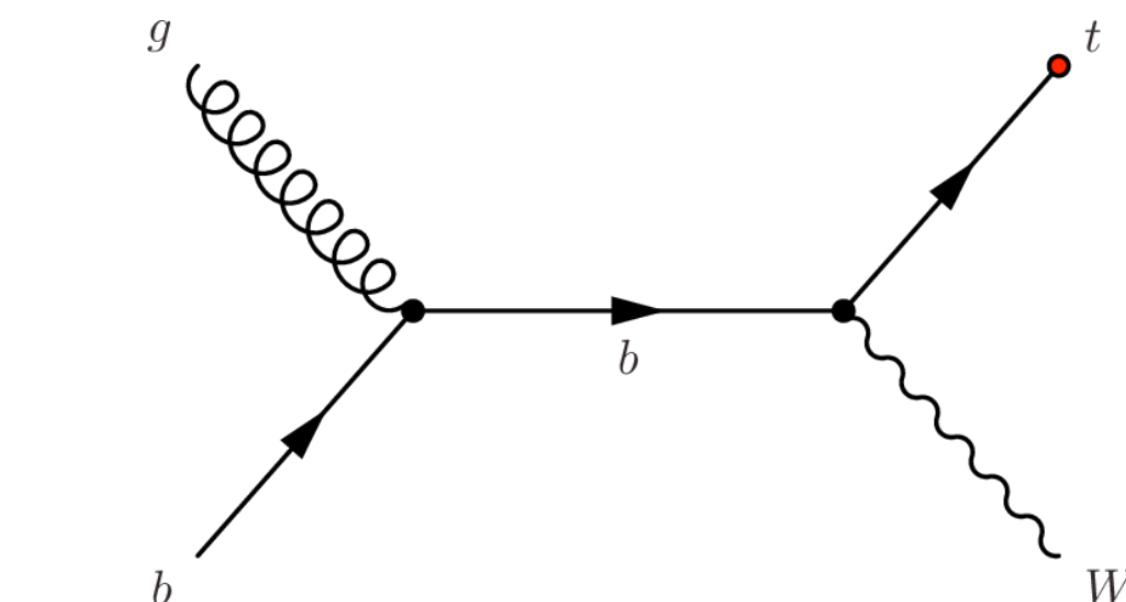
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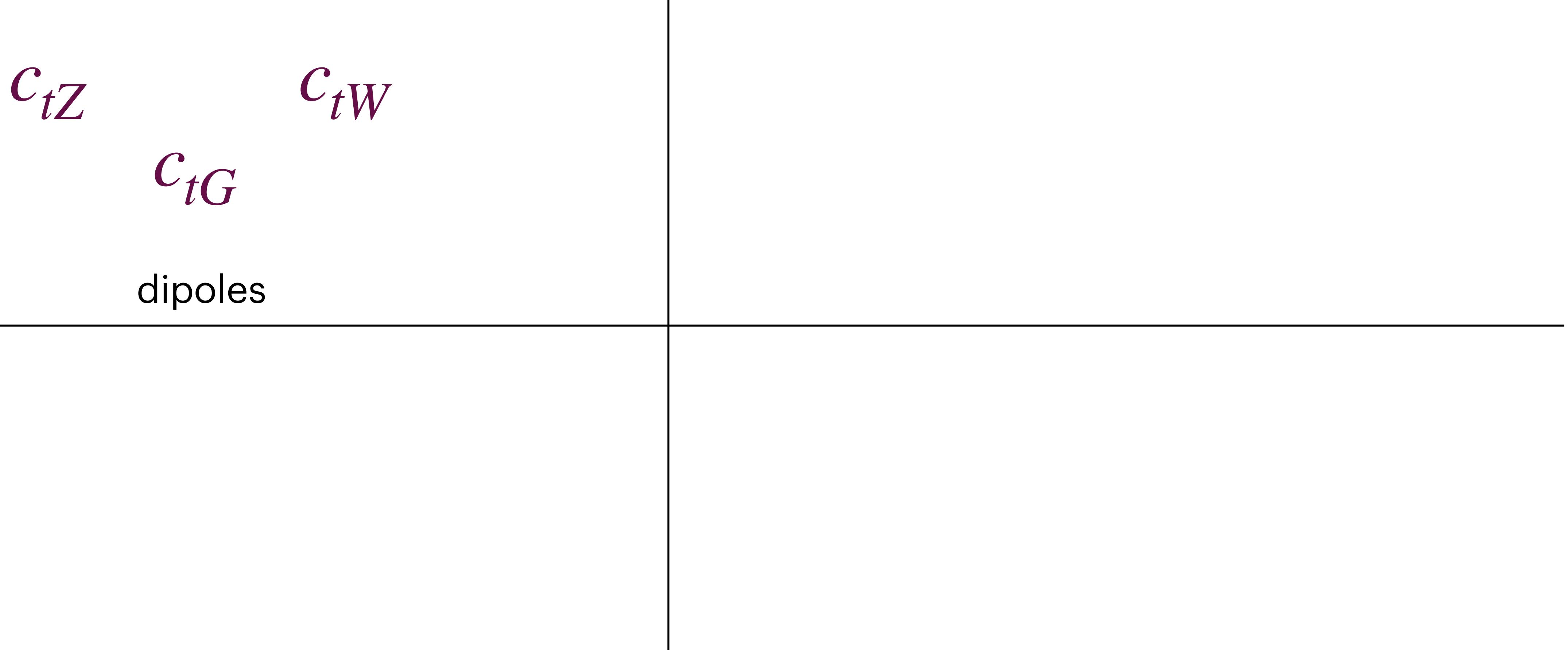
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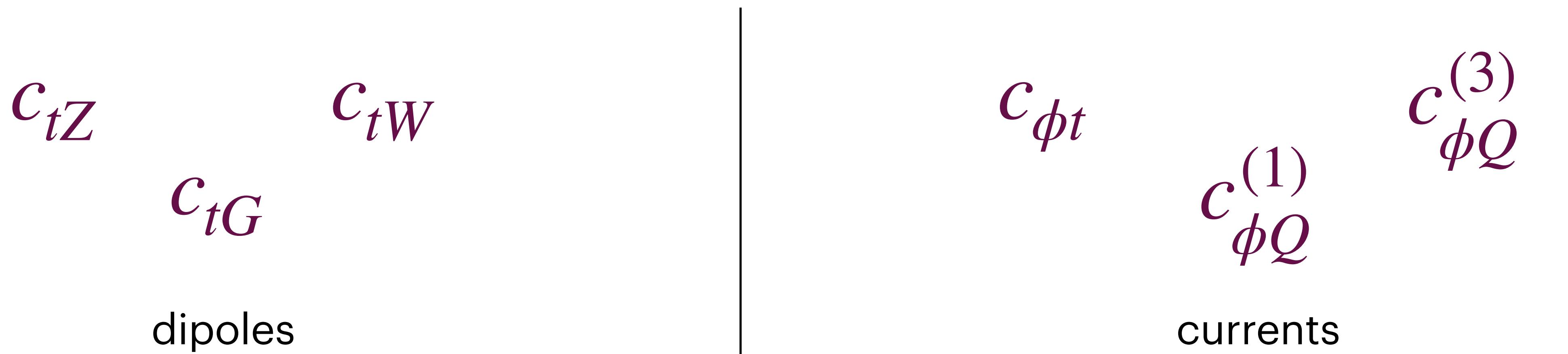
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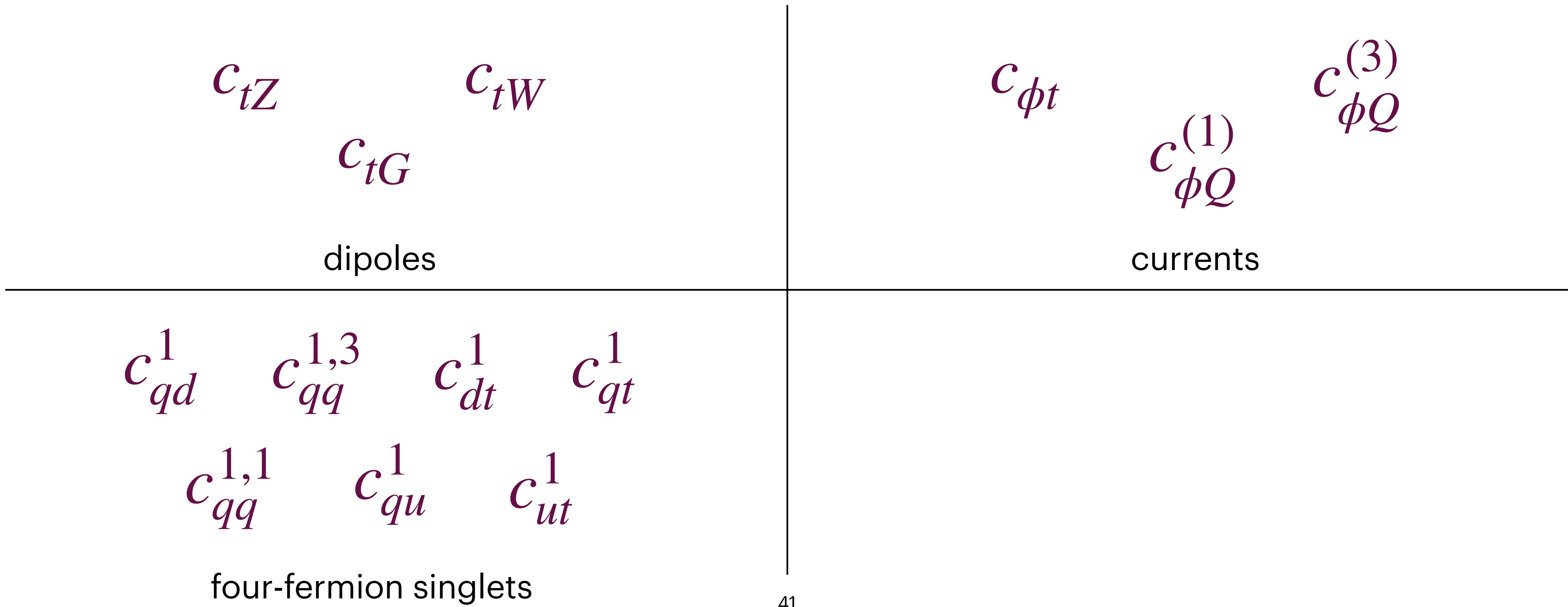
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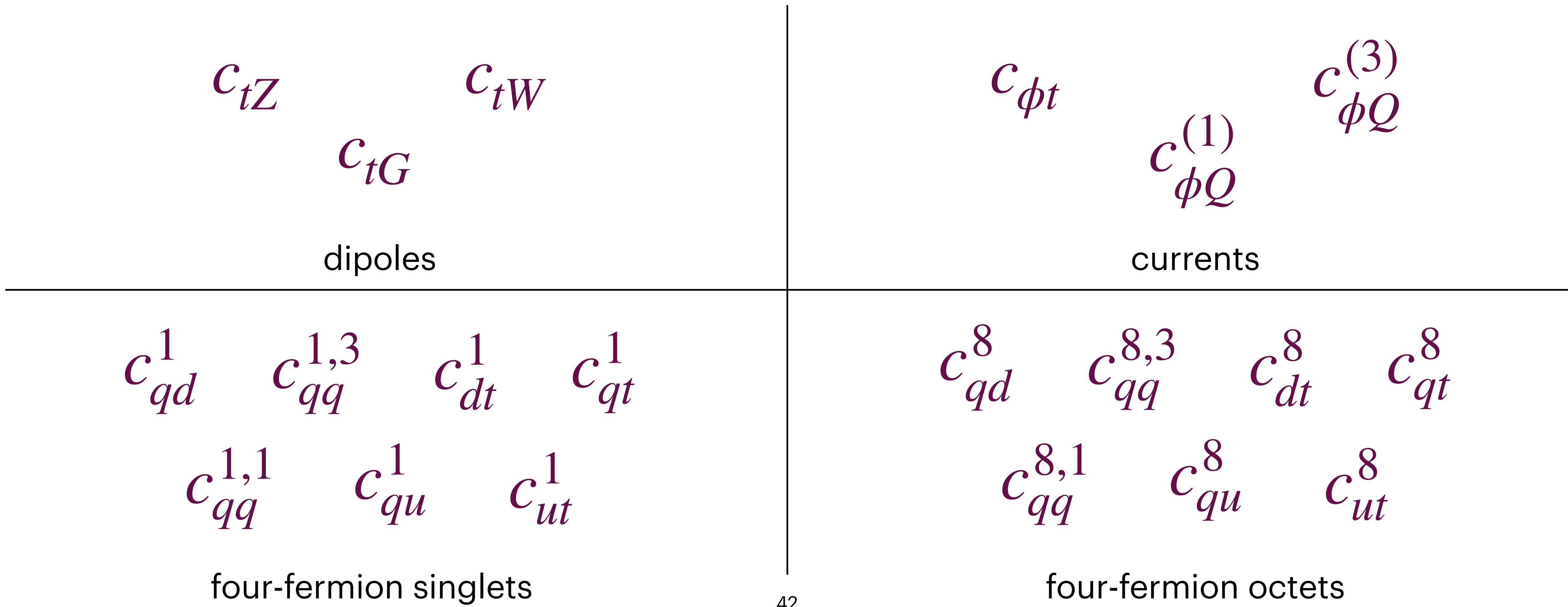
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- 2. How do PDFs compare between SM PDF fits and simultaneous PDF-EFT fits?**

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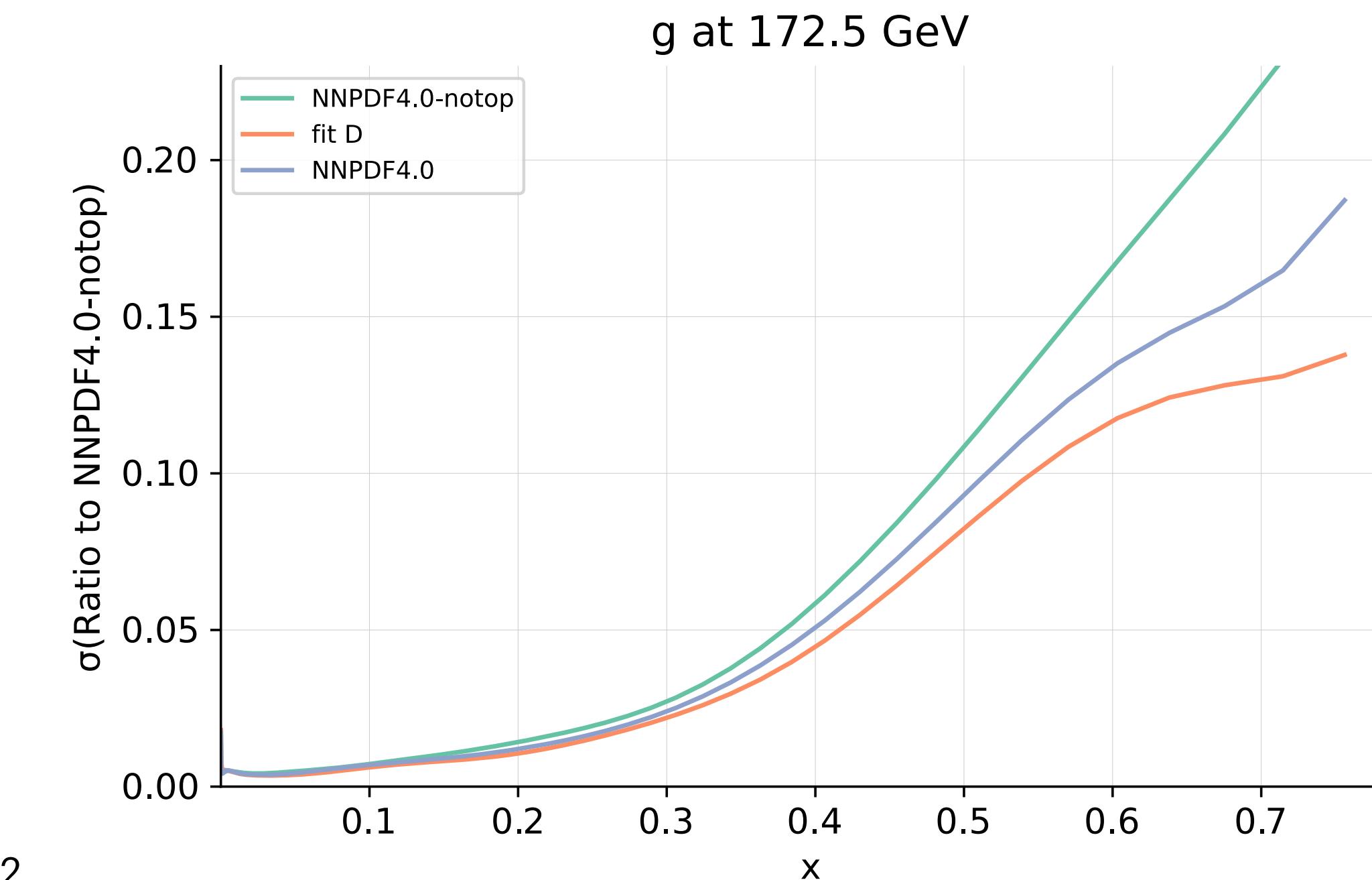
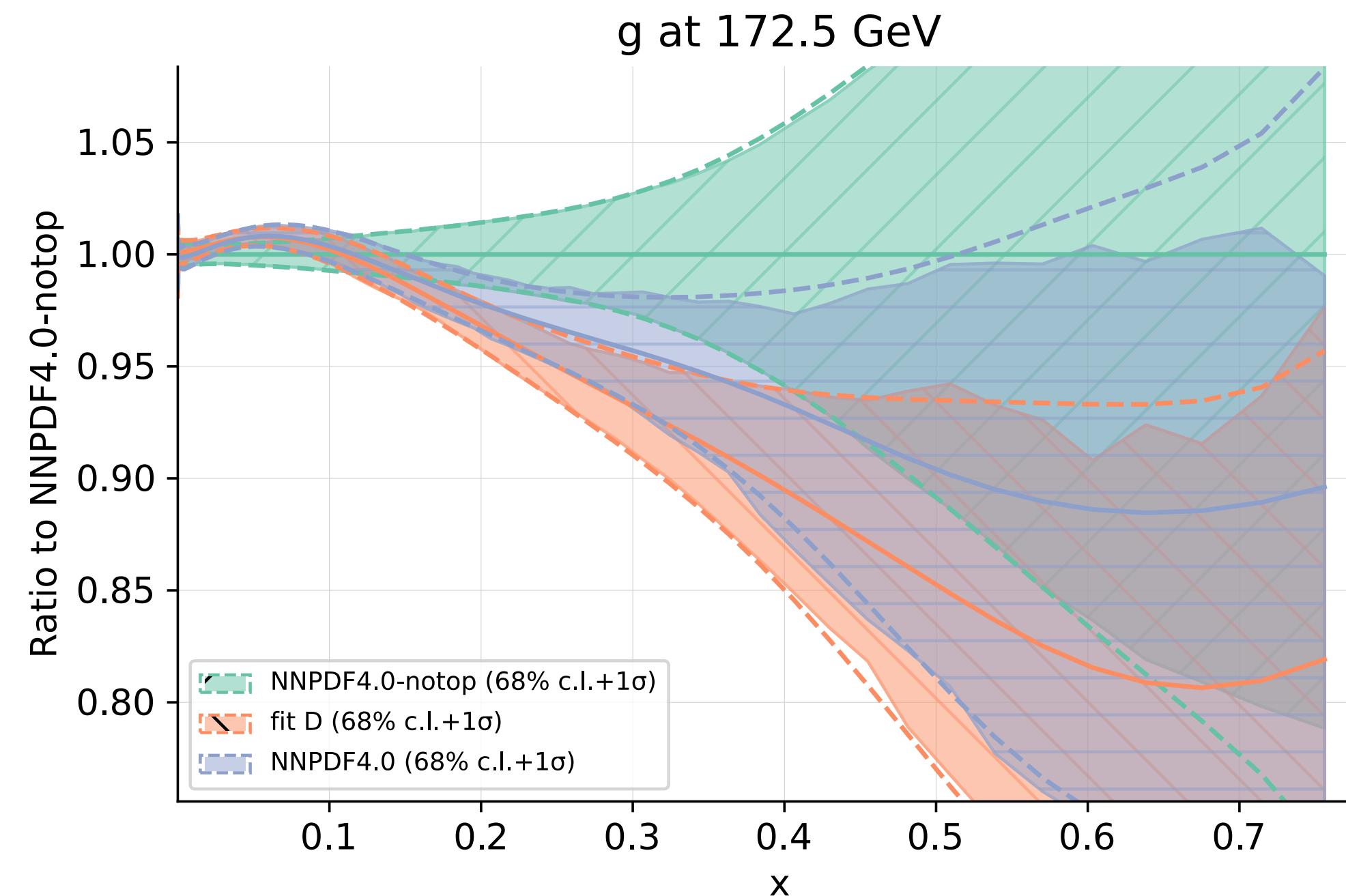
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- We work with theory predictions accurate to **NNLO in QCD in the SM**, and include **NLO QCD in the SMEFT**. Some fits are **linear in the SMEFT**, some are **quadratic** - a point we will return to.

**Let's start the results with the PDF-only fits...**

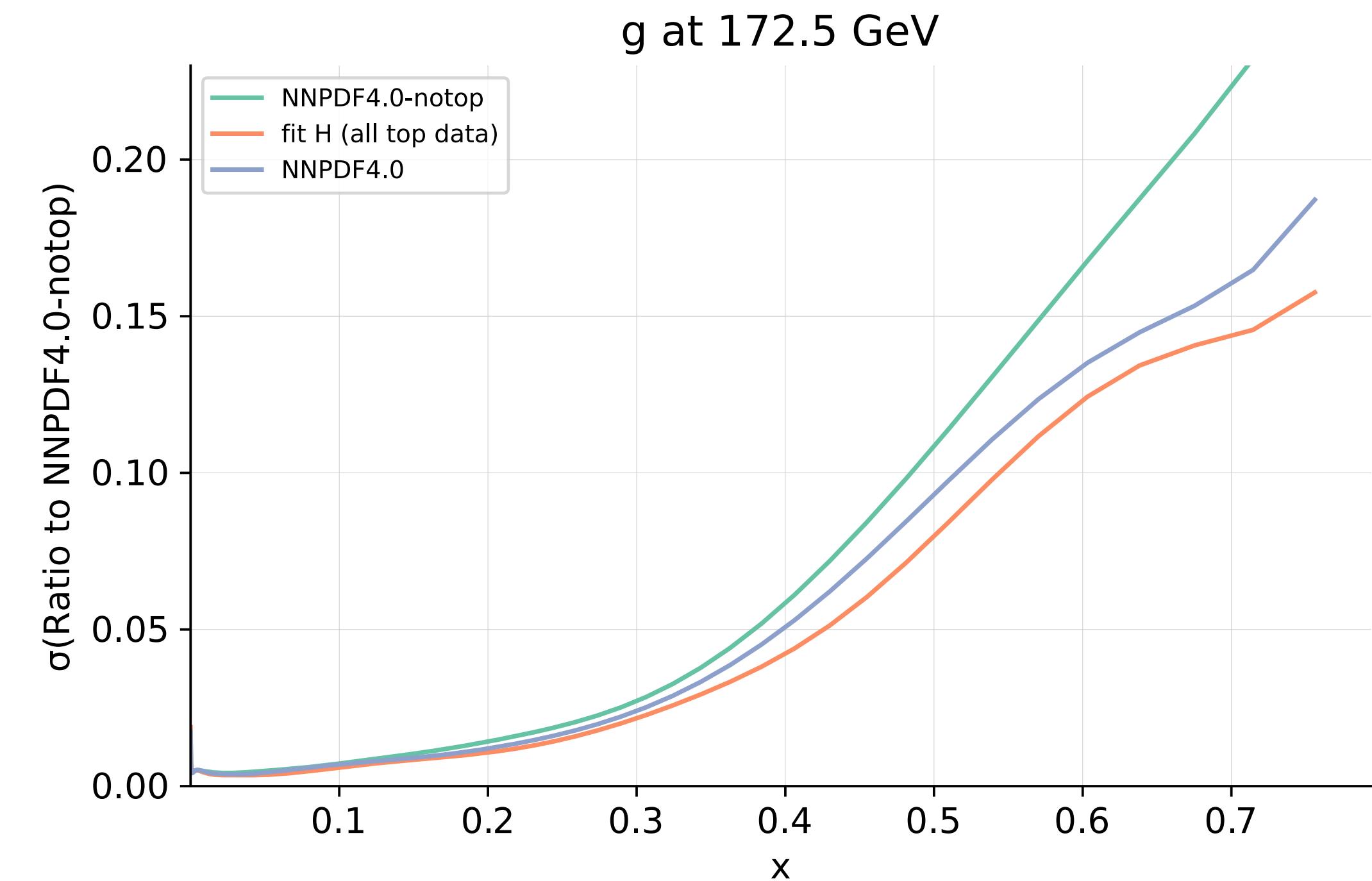
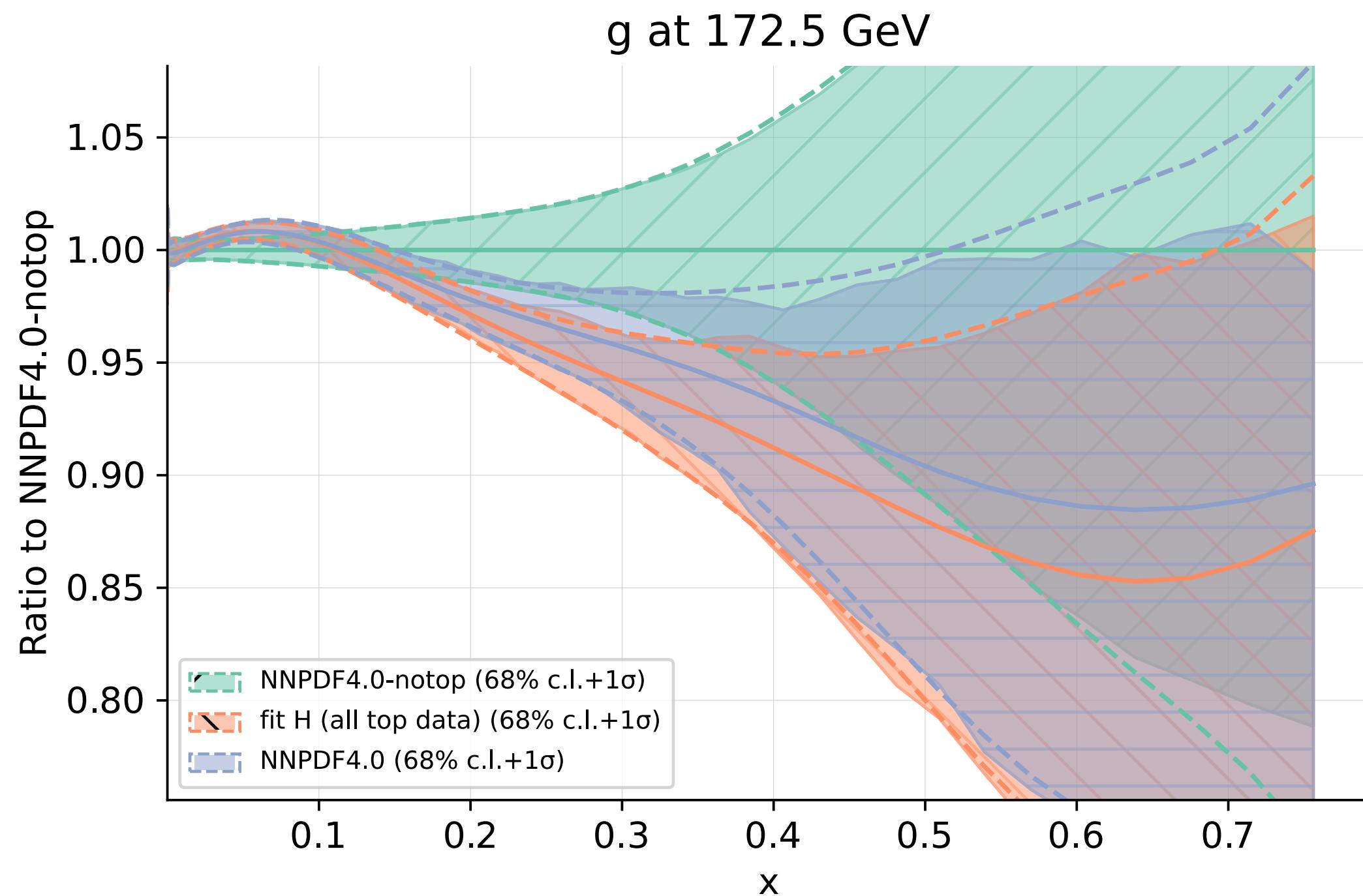
# PDFs in the SM - impact of inclusive $t\bar{t}$ and single-top

- First, we consider the impact of our dataset on PDFs **in the SM**.
- Begin by considering the updates to the **inclusive  $t\bar{t}$**  and **single-top** dataset relative to NNPDF4.0. If we perform a SM PDF fit using only our new inclusive  $t\bar{t}$  and single-top data, we see a more pronounced effect on the **large- $x$  gluon** relative to NNPDF4.0. The **uncertainty** is also **further reduced**.



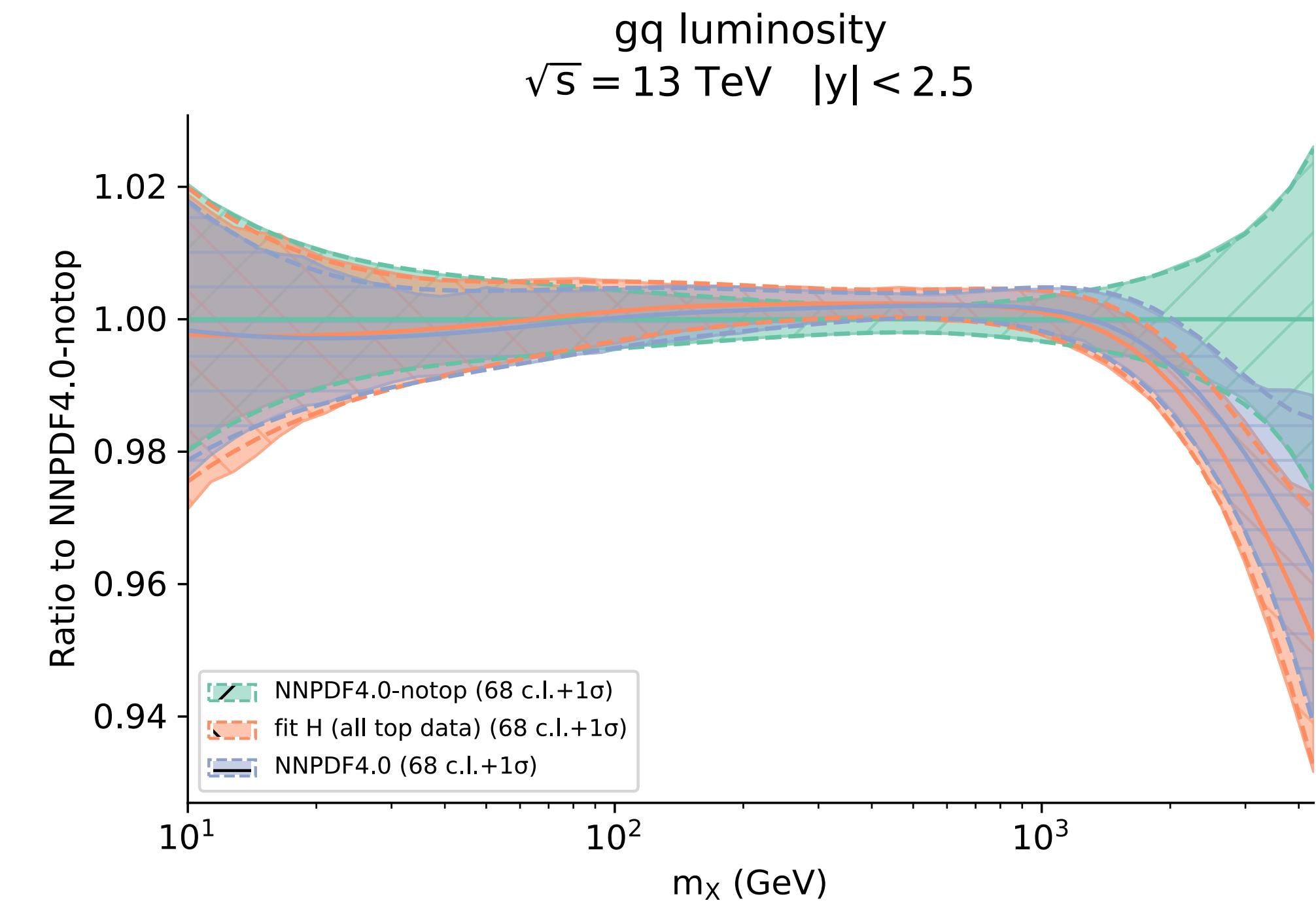
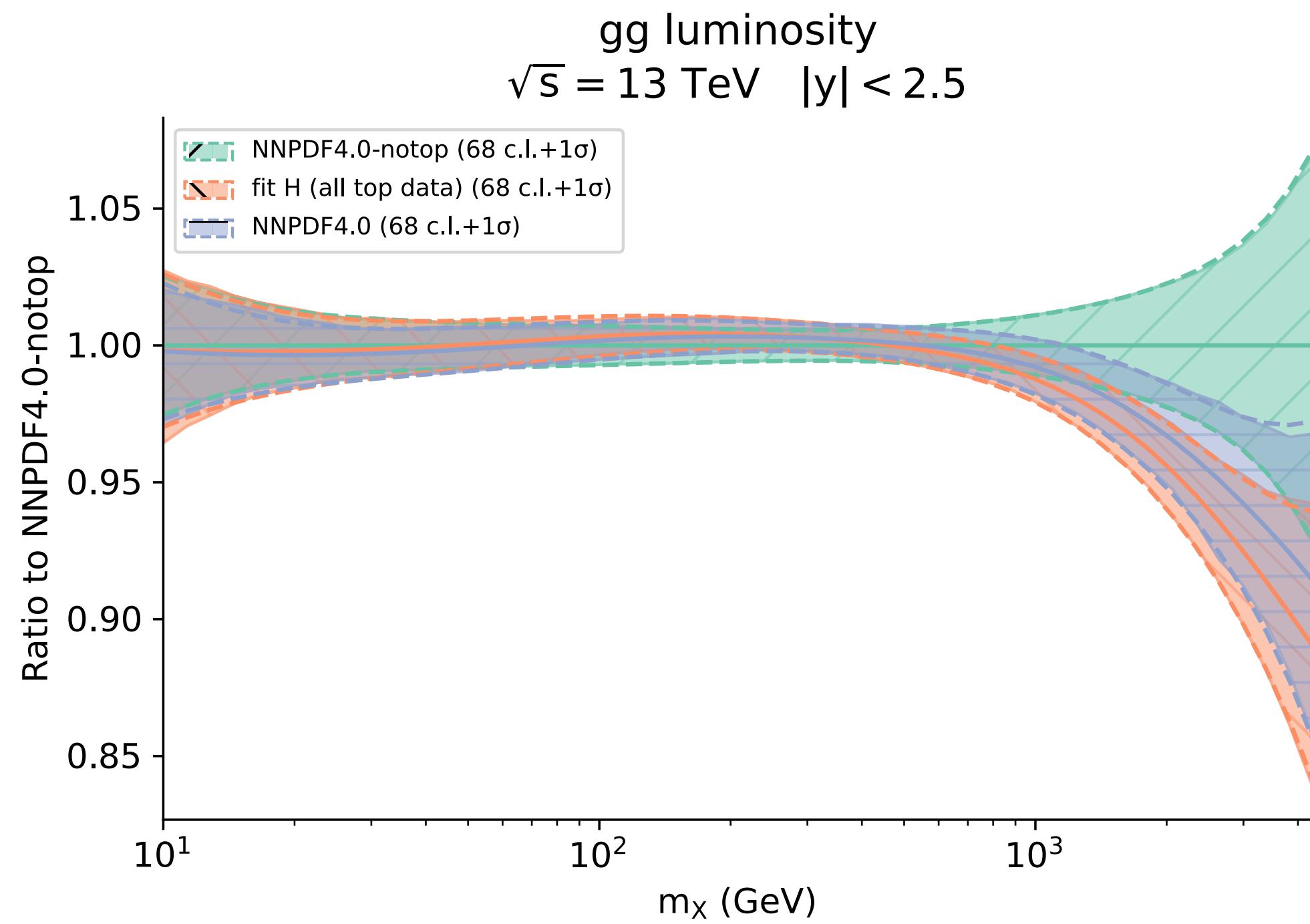
# PDFs in the SM - impact of all new top data

- Finally, we present the results of a **complete PDF fit** including **all our new top data**. As expected, the effect on the large- $x$  gluon is broadly the same as the effect of just including the inclusive  $t\bar{t}$  and single-top data, but is mildly tempered by the associated top data.



# PDFs in the SM - impact of all new top data

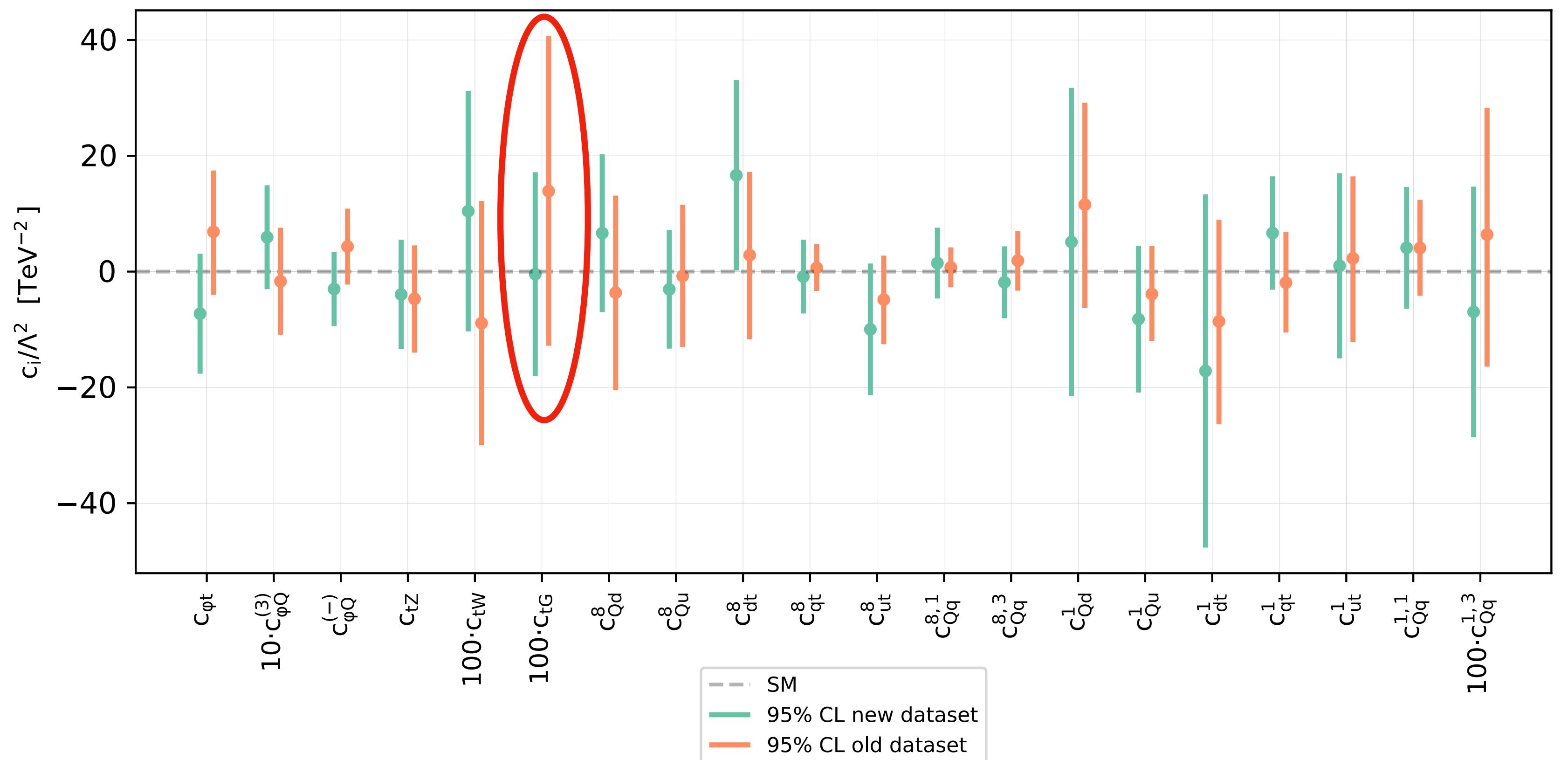
- A similar trend holds for the **PDF luminosities**, with our new updated fit compatible with NNPDF4.0, but with the central luminosity reduced relative to NNPDF4.0 at very large invariant mass.



**Now let's see the SMEFT-only fits...**

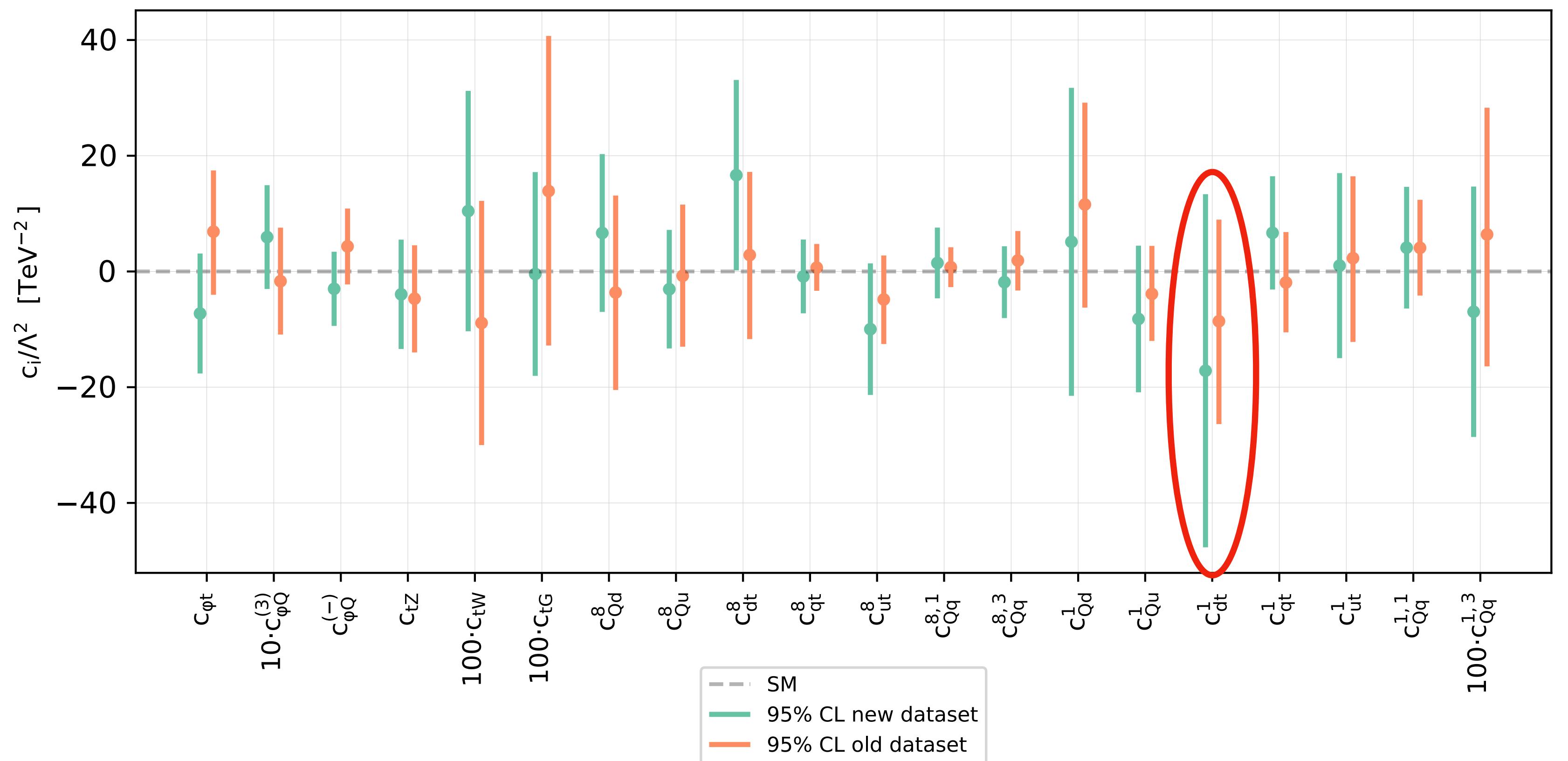
# SMEFT-only fits: linear SMEFT

- We have also performed SMEFT-only fits to see the impact of our new dataset relative to previous SMEFT-fits, namely **SMEFiT**.
- At the **linear level** in the SMEFT, best improvement is seen in  $c_{tG}$ , whose bound undergoes a 35% tightening - this is traced to more precise total  $t\bar{t}$  measurements.



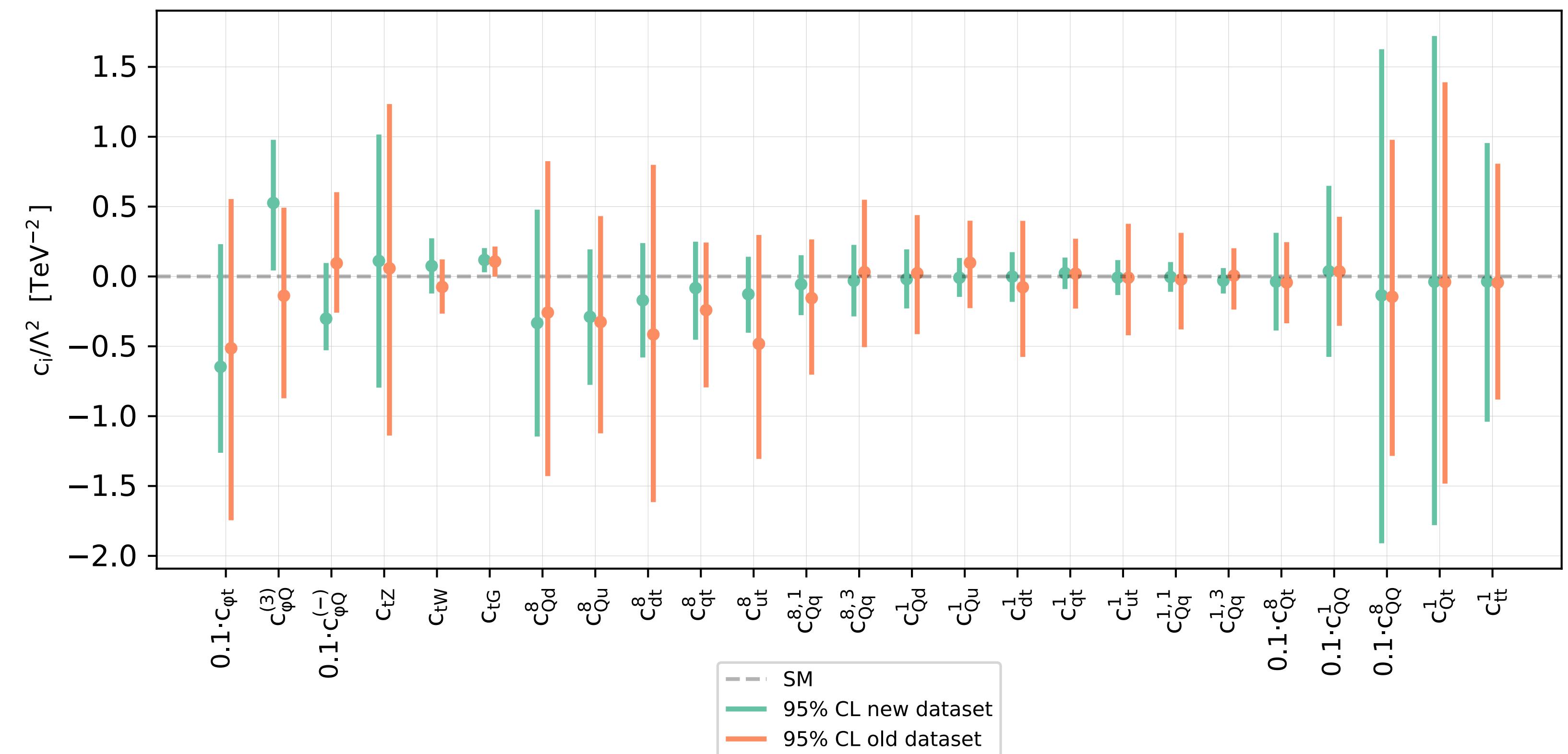
# SMEFT-only fits: linear SMEFT

- Some other coefficients undergo a **shift in the central value**, but no tightening or broadening of the constraint.
- Some coefficients have **broader bounds** than previously obtained, in particular some of the four-fermion operators.
- However, bounds are very weak here anyway, and likely challenge EFT validity.



# SMEFT-only fits: quadratic SMEFT

- Results are **much more promising** when **quadratic SMEFT effects** are included. A **significant tightening** of bounds is seen for most operators.
  - Only the five **four-heavy operators** experience broadening relative to the old dataset. This could point to some inconsistency in the  $t\bar{t}t\bar{t}$  and  $t\bar{t}b\bar{b}$  data, but with such large uncertainties, it is difficult to be precise.



# PDF-SMEFT correlation

- We can try to get intuition for the result of the **joint PDF-SMEFT** fit by considering the **PDF-SMEFT correlation** in the SMEFT-only fits.

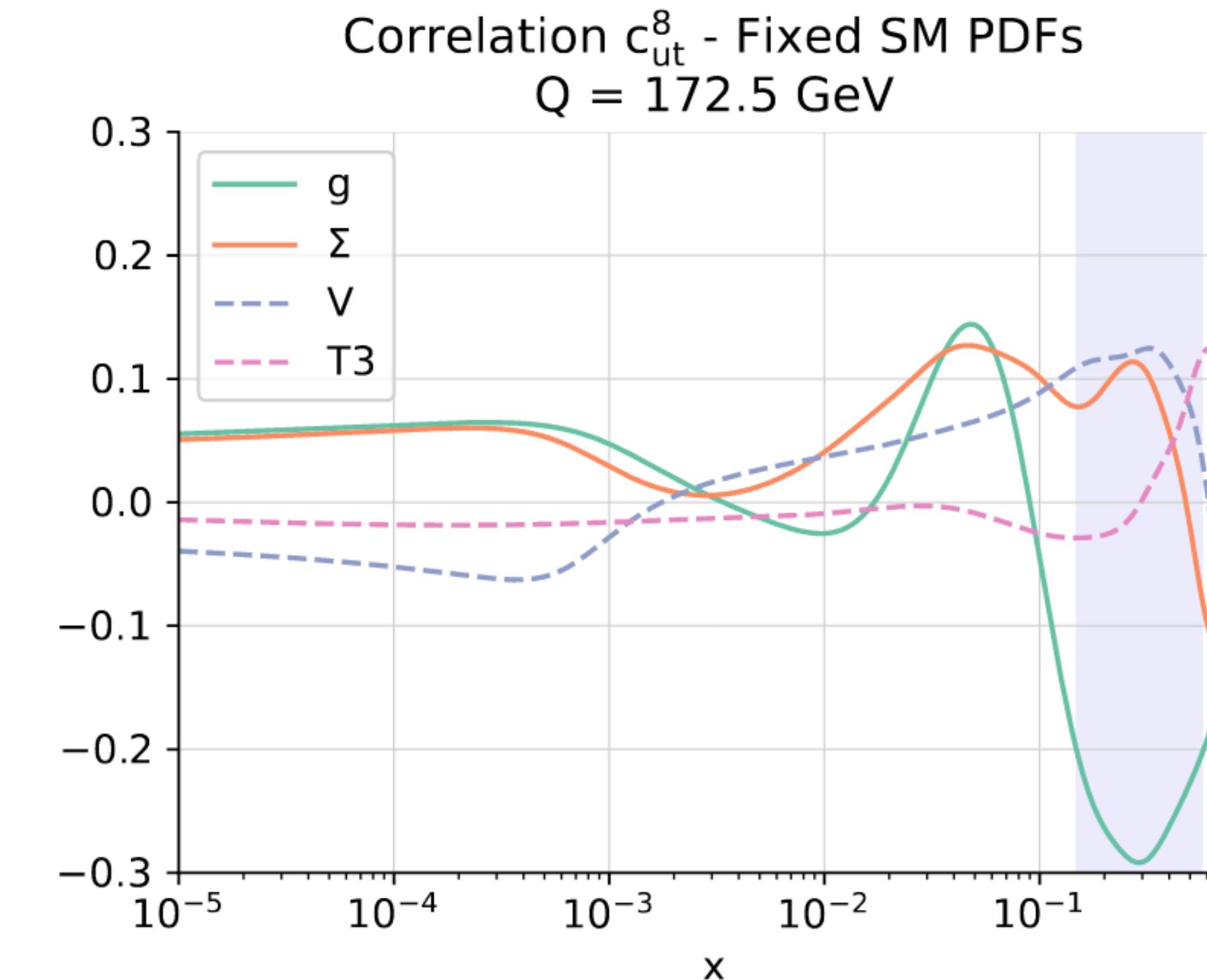
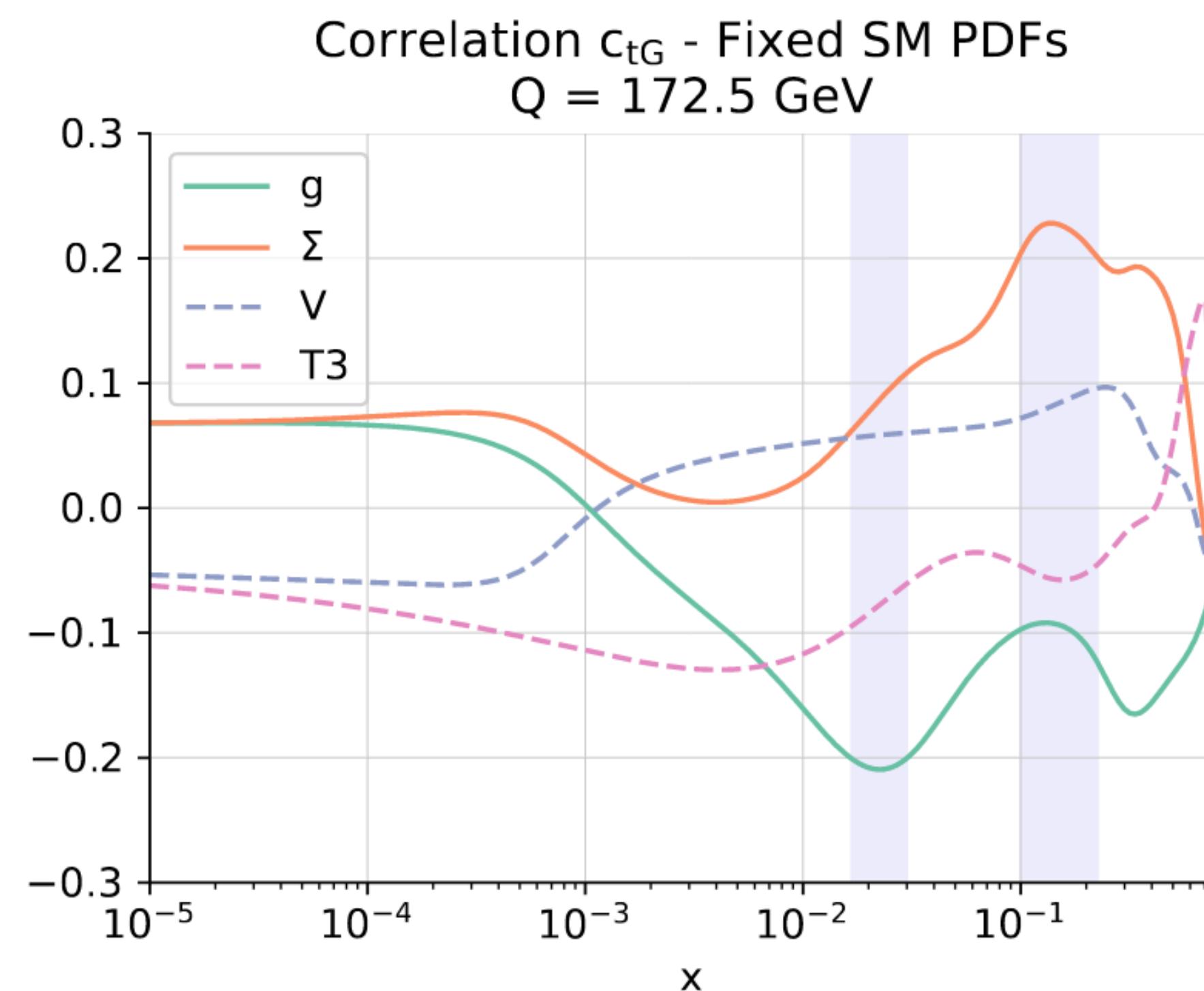
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- This is defined for each Wilson coefficient and each PDF flavour by:

$$\rho(c, f(x, Q^2)) = \frac{\langle c^{(k)} f^{(k)}(x, Q^2) \rangle_k - \langle c^{(k)} \rangle_k \langle f^{(k)}(x, Q^2) \rangle_k}{\sqrt{\langle (c^{(k)})^2 \rangle_k - \langle c^{(k)} \rangle_k^2} \sqrt{\langle (f^{(k)}(x, Q^2))^2 \rangle_k - \langle f^{(k)}(x, Q^2) \rangle_k^2}}$$

# PDF-SMEFT correlation

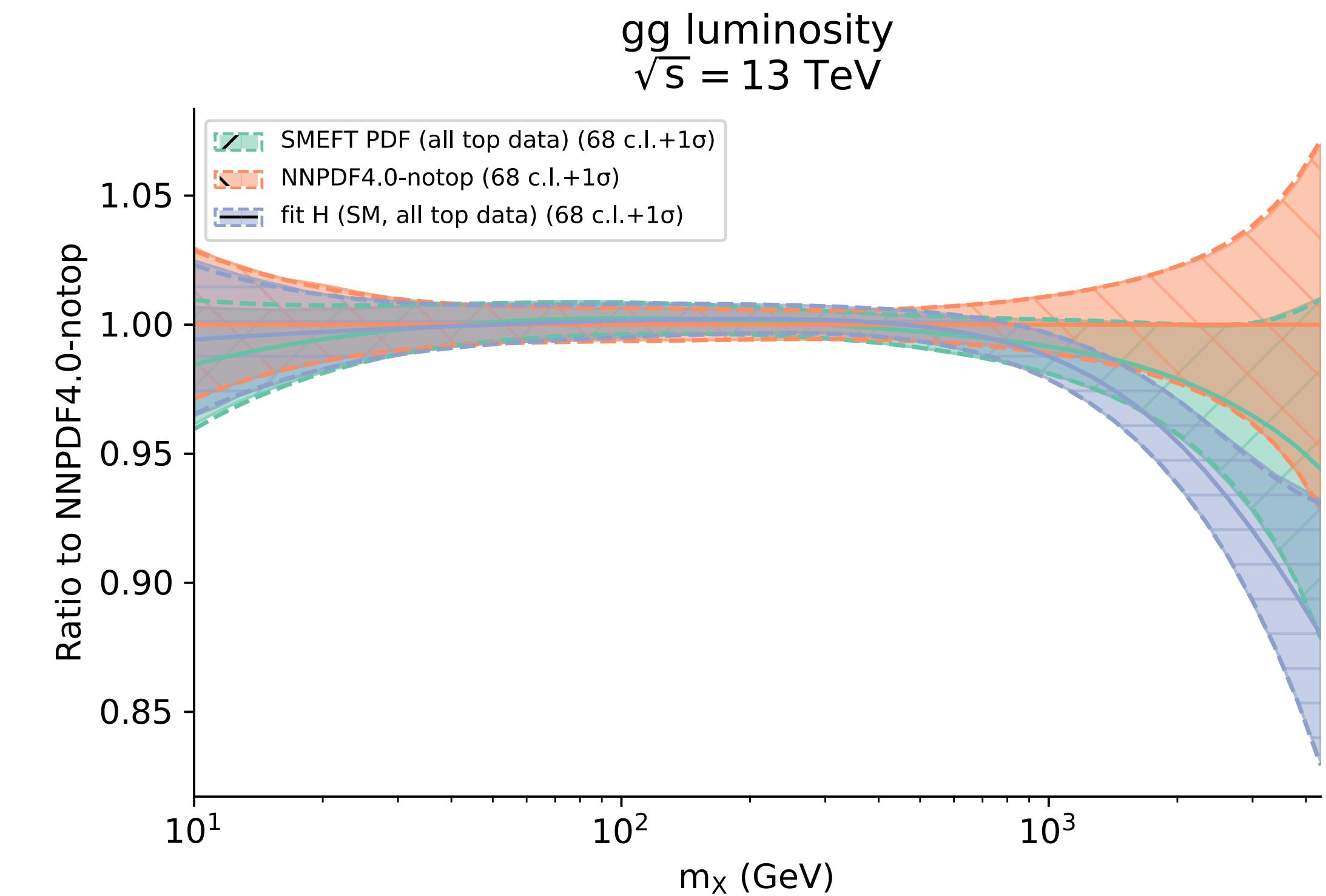
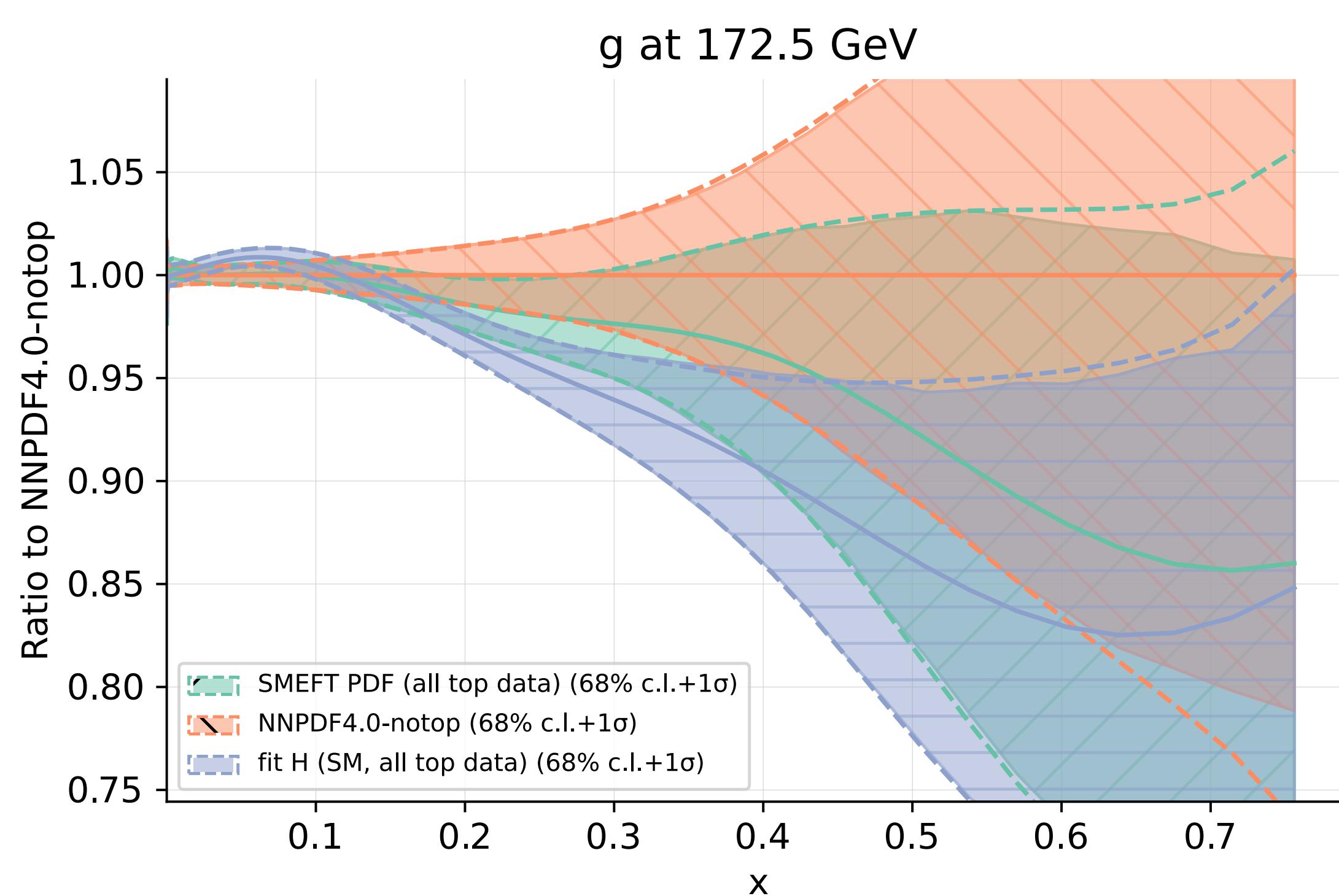
- We see the **strongest correlation** between the Wilson coefficients and the gluon PDF at high- $x$ , as to be expected. The correlation is still **mild** though, suggesting that the interplay will also be **relatively mild**.



**Now, let's do the joint fit...**

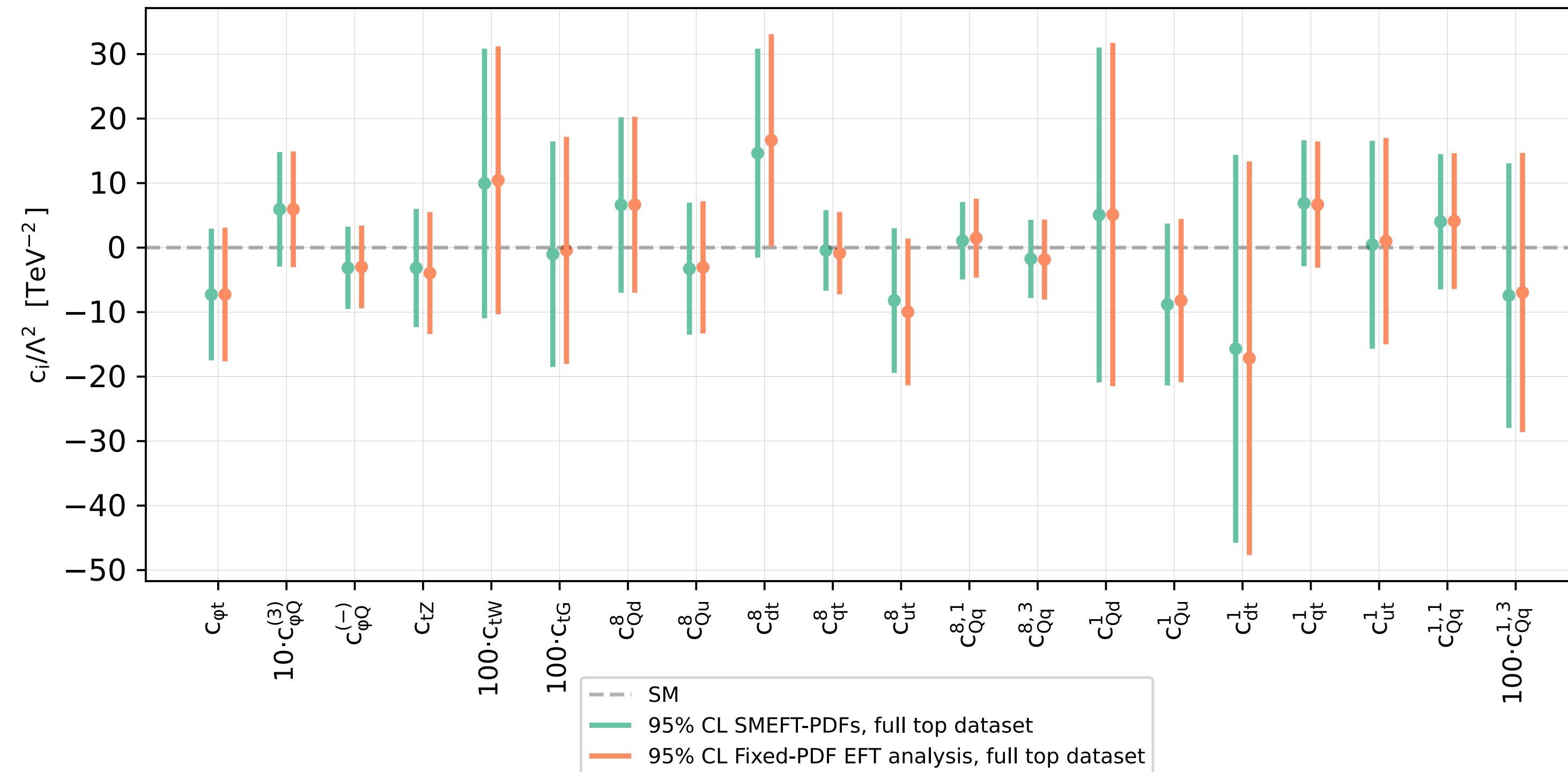
# Joint PDF-SMEFT fits: linear SMEFT

- Finally, we present the key result of the work: a **simultaneous** determination of PDFs and SMEFT Wilson coefficients. We start assuming **linear SMEFT**.
- In terms of the gluon PDFs and luminosities, we find that a simultaneous determination **reduces the pull** of the top data from the **non-top baseline**.



# Joint PDF-SMEFT fits: linear SMEFT

- On the other hand, we find that the bounds on the Wilson coefficients are **very stable** between a simultaneous PDF-SMEFT fit and a SMEFT-only fit.



- This indicates that within a **linear EFT interpretation** of the top data, the PDF effects are **currently subdominant**.

# Joint PDF-SMEFT fits: quadratic SMEFT

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- However... during the course of our study, we discovered an important problem with the **Monte Carlo replica method** used to propagate uncertainties in the SIMUnet methodology.
- The issue is such that quadratic results with the SIMUnet methodology (and indeed with any methodology that uses the Monte Carlo replica method) are **currently unreliable**.

# Joint PDF-SMEFT fits: quadratic SMEFT

- **Next obvious fit...** joint PDF-SMEFT fit using **quadratic SMEFT contributions?** Could interplay be more pronounced there ... ?
- However... during the course of our study, we discovered an important problem with the **Monte Carlo replica method** used to propagate uncertainties in the SIMUnet methodology.
- The issue is such that quadratic results with the SIMUnet methodology (and indeed with any methodology that uses the Monte Carlo replica method) are **currently unreliable**.
- An **upcoming publication** will describe the issue in more detail; for now, here's the basics...

# Pitfalls of the Monte-Carlo replica method

- For simplicity, consider a single data point  $d$  with experimental variance  $\sigma^2$ , which we attempt to describe using the **quadratic** theory, involving a single theory parameter  $c$ :

$$t(c) = t^{\text{SM}} + t^{\text{lin}}_c + t^{\text{quad}}_c c^2$$

- The Monte-Carlo replica method propagates the uncertainty from the data to the theory parameter by fitting to **pseudodata**. We sample lots of pseudodata replicas from a normal distribution based on the data,  $d_p \sim N(d, \sigma^2)$ , and define the corresponding **parameter replicas** to be a random function of the pseudodata given by minimising the  $\chi^2$ -statistic:

$$c_p(d_p) = \arg \min_c \left( \frac{(t(c) - d_p)^2}{\sigma^2} \right)$$

# Pitfalls of the Monte-Carlo replica method

- In this very simple example, one can compute the distribution function of the parameter replicas analytically; it is given by:

$$P_{c^{(i)}}(c) \propto \delta\left(c + \frac{t^{\text{lin}}}{2t^{\text{quad}}}\right) \int_{-\infty}^{t_{\min}} dx \exp\left(-\frac{1}{2\sigma^2}(x - d)^2\right) + \frac{2}{|2ct^{\text{quad}} + t^{\text{lin}}|} \exp\left(-\frac{1}{2\sigma^2}(d - t(c))^2\right)$$

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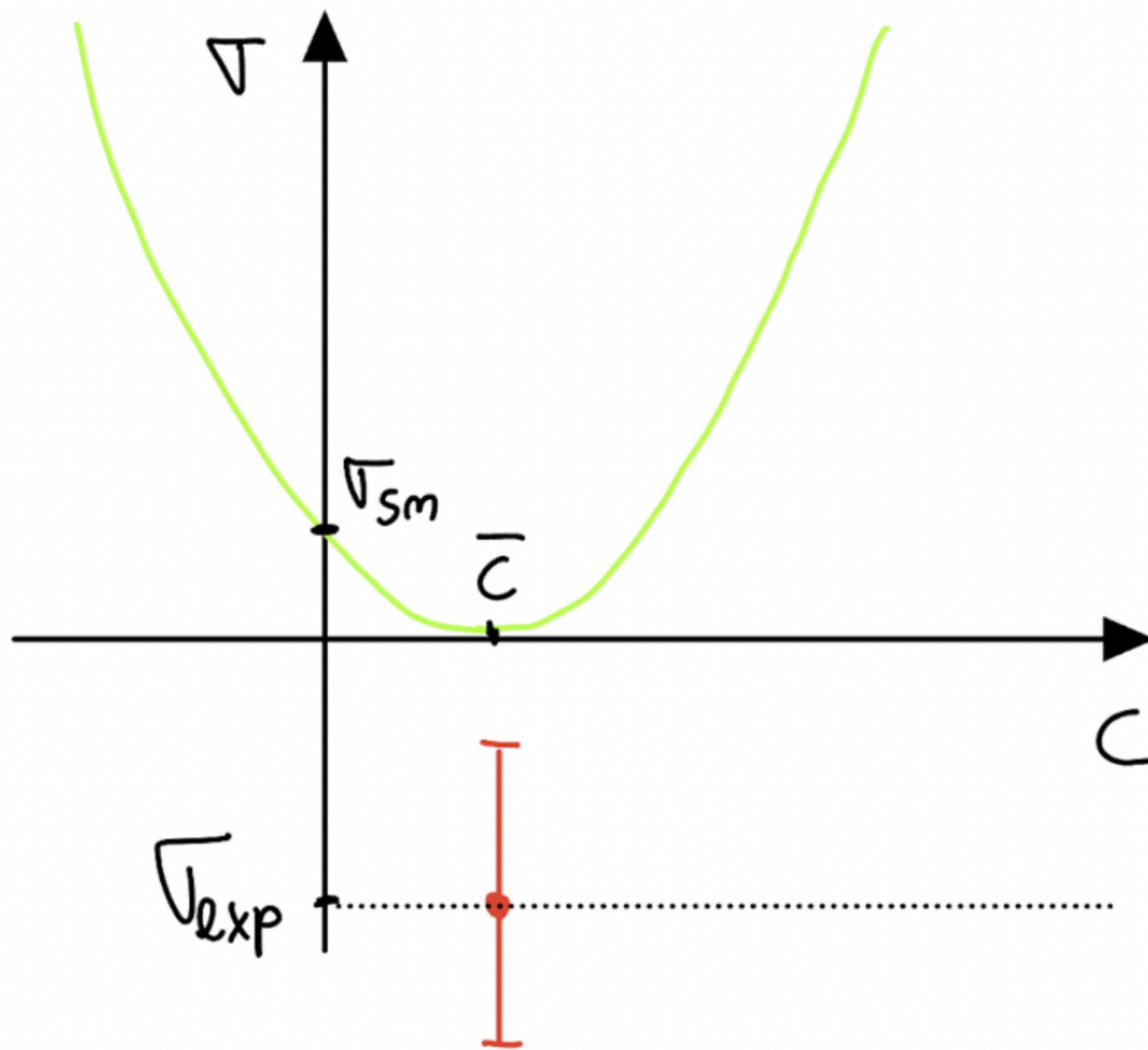
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- **Key features to note:**
  - Part of the distribution looks like a **scaled version** of what we would expect from a **Bayesian method with uniform prior**.
  - There is also a **delta function spike** in the distribution - interesting to ask: why...?

# Pitfalls of the Monte-Carlo replica method

- The **minimum of the theory** can result in many pseudodata replicas falling **below the range of the theory**.

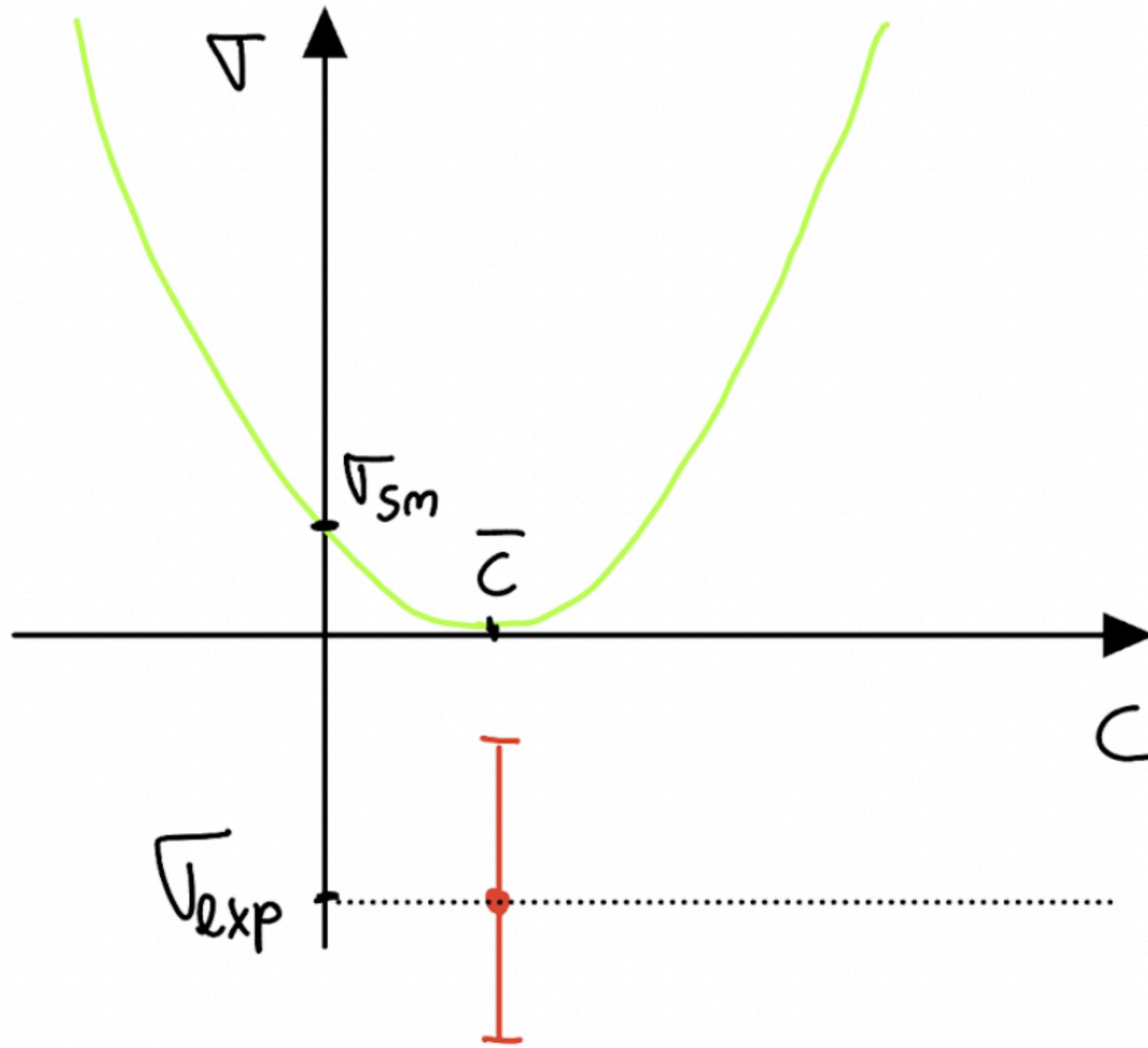
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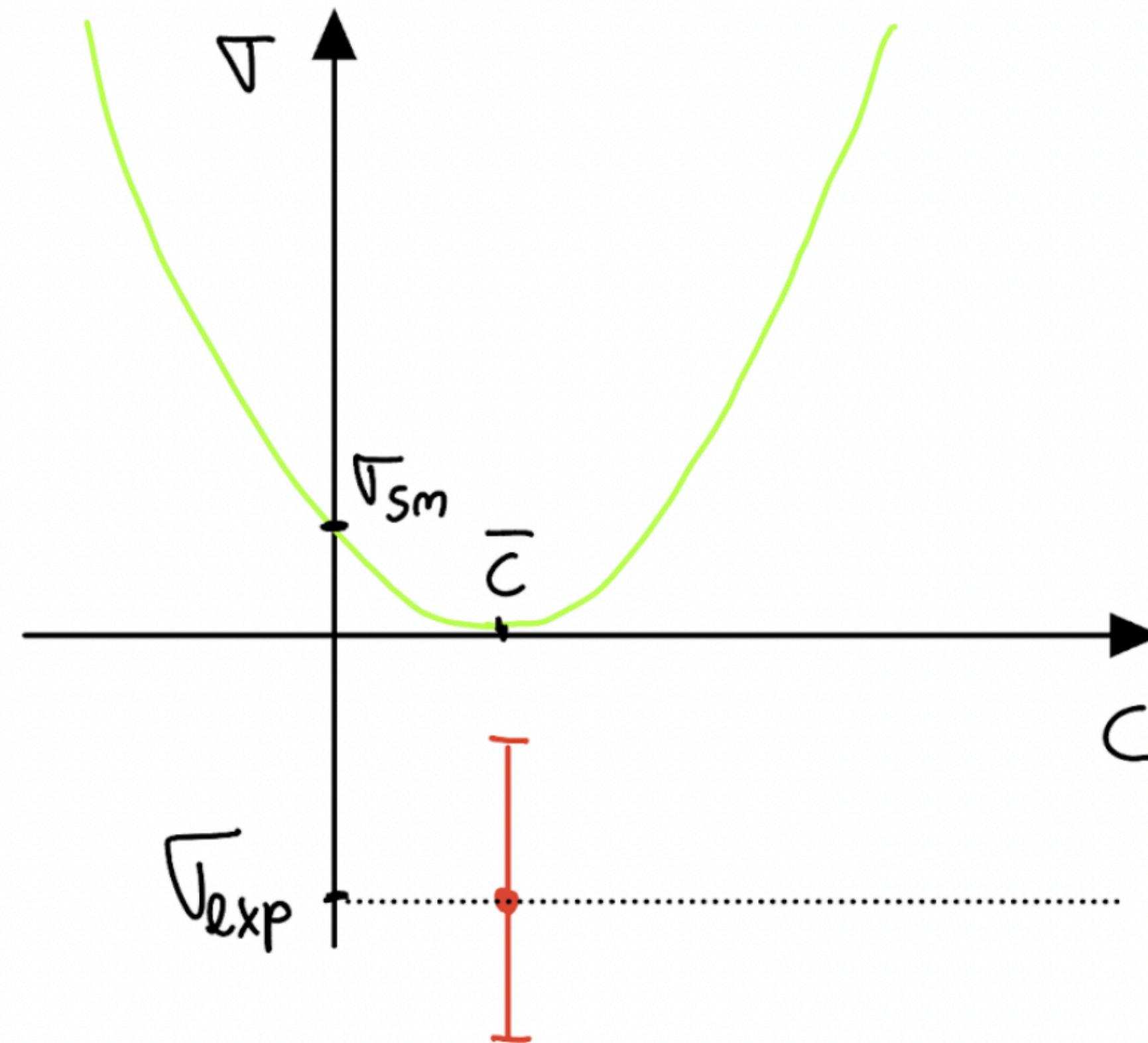
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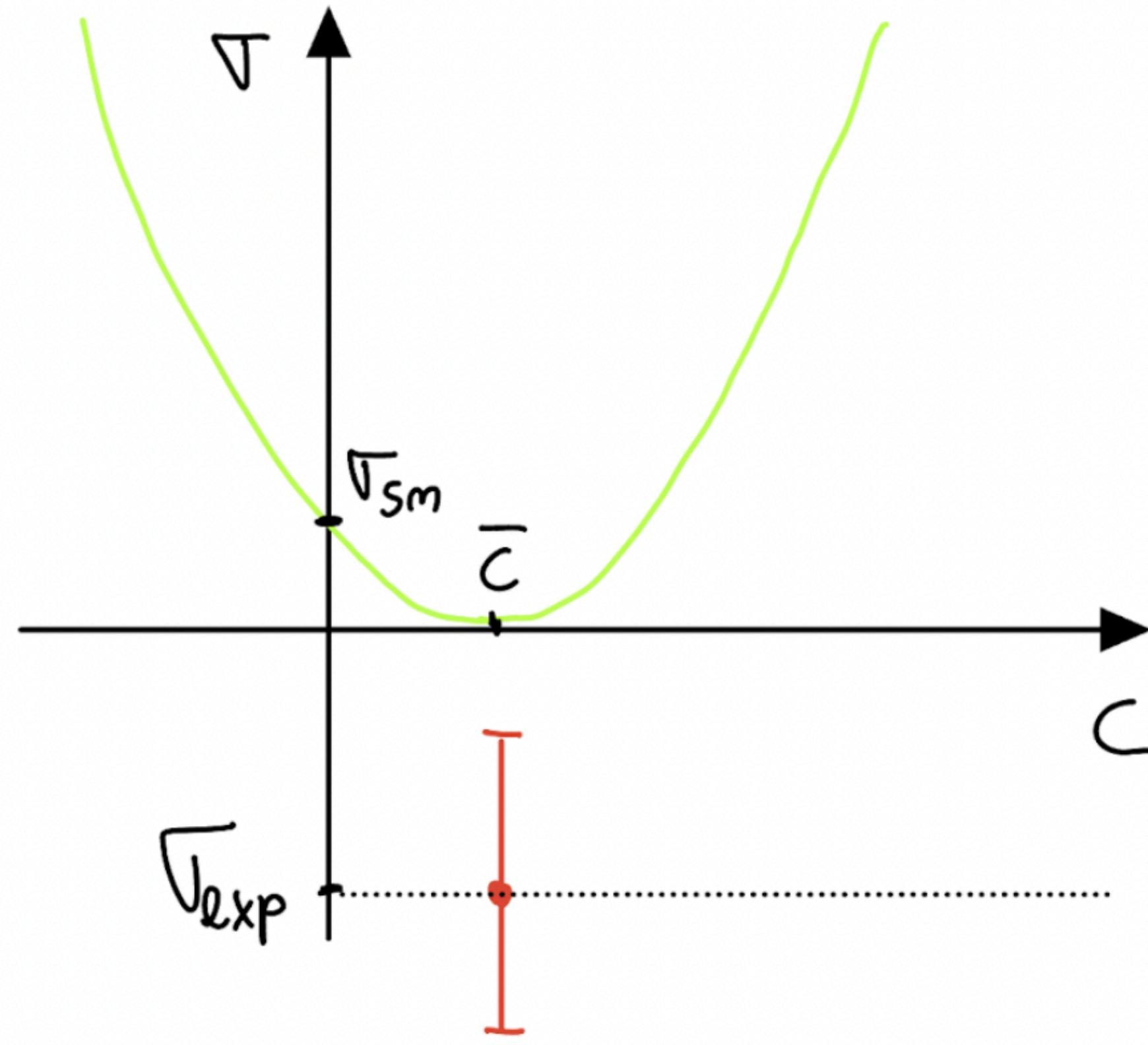
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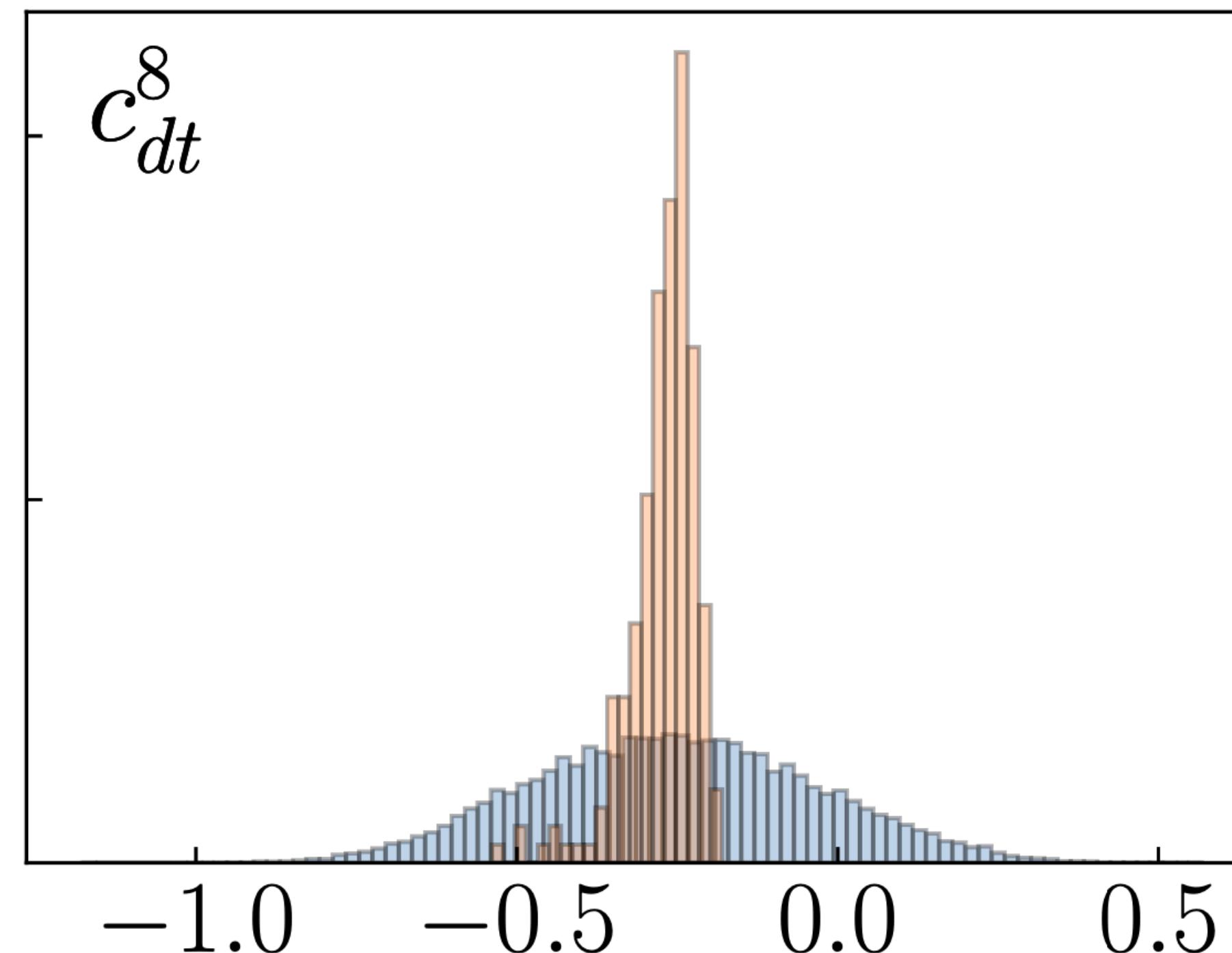
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    - This gives rise to the spike in the distribution at  $c = -t^{\text{lin}}/2t^{\text{quad}}$ .
- 

# Pitfalls of the Monte-Carlo replica method

- These problems extend to our top fit... for example in a **realistic quadratic fit** of one operator  $c_{dt}^8$ , we get the following comparison between the Monte-Carlo method (**orange**) and a Bayesian method with uniform prior (**blue**).
- We see that **Monte-Carlo massively underestimates uncertainties.**



## **Key questions for the future:**

**Can the MC replica method be modified to agree with Bayesian methods?**

**To what extent do existing fits (in the SMEFT world, PDF world, and beyond) that use the MC replica method underestimate uncertainties?**

# Conclusions

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- **Simultaneous determination of PDFs and BSM parameters**, will be **very important in future analyses** (especially as we enter Run III).
- Members of the **PBSP team** have already produced three works in the direction of simultaneous PDF-SMEFT fits: (i) a **phenomenological study** 2104.02723 showing the need for simultaneous extraction; (ii) a **methodology** (SimuNET, 2201.07240) capable of **fast simultaneous fitting**; (iii) a **comprehensive simultaneous extraction** of PDFs and SMEFT couplings from the **full LHC Run II top dataset**, 2303.06159.

**Thanks for listening!**  
**Questions?**