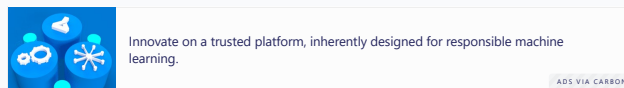


|  |   |
|--|---|
| DSA Introduction   | > |
| Data Structures (I)  | > |
| Data Structures (II)   | > |
| Tree based DSA (I)   | > |
| Tree based DSA (II)  | > |
| Graph based DSA  | > |
| Sorting and Searching Algorithms   | ^ |
| <ul style="list-style-type: none"> <li>Bubble Sort</li> <li>Selection Sort</li> <li>Insertion Sort</li> <li><b>Merge Sort</b></li> <li>Quicksort</li> <li>Counting Sort</li> <li>Radix Sort</li> <li>Bucket Sort</li> <li>Heap Sort</li> <li>Shell Sort</li> <li>Linear Search</li> <li>Binary Search</li> </ul> |   |
| Greedy Algorithms  | > |
| Dynamic Programming  | > |
| Other Algorithms   | > |

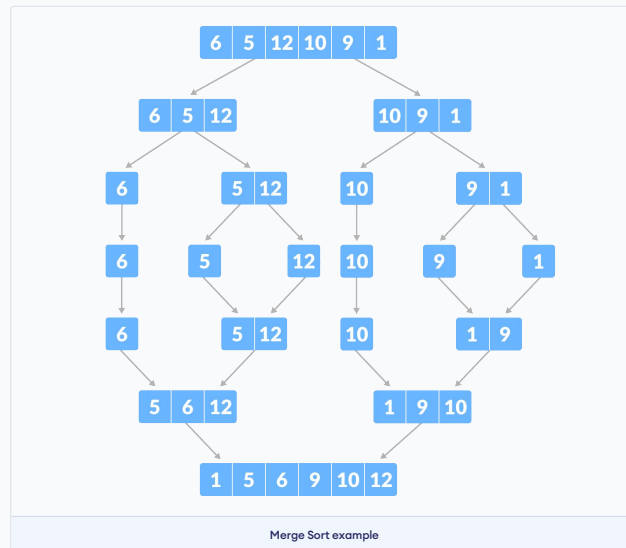


## Merge Sort Algorithm

In this tutorial, you will learn about merge sort algorithm and its implementation in C, C++, Java and Python.

Merge Sort is one of the most popular [sorting algorithms](#) that is based on the principle of [Divide and Conquer Algorithm](#).

Here, a problem is divided into multiple sub-problems. Each sub-problem is solved individually. Finally, sub-problems are combined to form the final solution.



### Divide and Conquer Strategy

Using the **Divide and Conquer** technique, we divide a problem into subproblems. When the solution to each subproblem is ready, we 'combine' the results from the subproblems to solve the main problem.

Suppose we had to sort an array  $A$ . A subproblem would be to sort a sub-section of this array starting at index  $p$  and ending at index  $r$ , denoted as  $A[p..r]$ .

#### Divide

If  $q$  is the half-way point between  $p$  and  $r$ , then we can split the subarray  $A[p..r]$  into two arrays  $A[p..q]$  and  $A[q+1, r]$ .

#### Conquer

In the conquer step, we try to sort both the subarrays  $A[p..q]$  and  $A[q+1, r]$ . If we haven't yet reached the base case, we again divide both these subarrays and try to sort them.

#### Combine

When the conquer step reaches the base step and we get two sorted subarrays  $A[p..q]$  and  $A[q+1, r]$  for array  $A[p..r]$ , we combine the results by creating a sorted array  $A[p..r]$  from two sorted subarrays  $A[p..q]$  and  $A[q+1, r]$ .

### MergeSort Algorithm

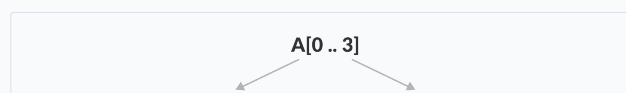
The MergeSort function repeatedly divides the array into two halves until we reach a stage where we try to perform MergeSort on a subarray of size 1 i.e.  $p == r$ .

After that, the merge function comes into play and combines the sorted arrays into larger arrays until the whole array is merged.

```
MergeSort(A, p, r):
    if p > r
        return
    q = (p+r)/2
    mergeSort(A, p, q)
    mergeSort(A, q+1, r)
    merge(A, p, q, r)
```

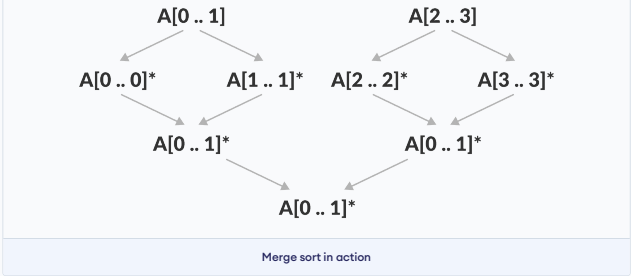
To sort an entire array, we need to call `MergeSort(A, 0, length(A)-1)`.

As shown in the image below, the merge sort algorithm recursively divides the array into halves until we reach the base case of array with 1 element. After that, the merge function picks up the sorted sub-arrays and merges them to gradually sort the entire array.



#### Related Topics

- Divide and Conquer Algorithm
- Insertion Sort Algorithm
- Counting Sort Algorithm
- Selection Sort Algorithm
- Radix Sort Algorithm
- Quicksort Algorithm



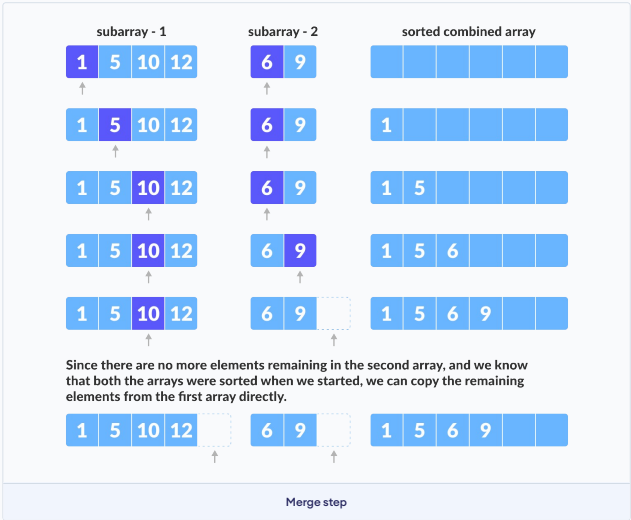
### The merge Step of Merge Sort

Every recursive algorithm is dependent on a base case and the ability to combine the results from base cases. Merge sort is no different. The most important part of the merge sort algorithm is, you guessed it, `merge` step.

The merge step is the solution to the simple problem of merging two sorted lists(arrays) to build one large sorted list(array).

The algorithm maintains three pointers, one for each of the two arrays and one for maintaining the current index of the final sorted array.

```
Have we reached the end of any of the arrays?
No:
    Compare current elements of both arrays
    Copy smaller element into sorted array
    Move pointer of element containing smaller element
Yes:
    Copy all remaining elements of non-empty array
```



### Writing the Code for Merge Algorithm

A noticeable difference between the merging step we described above and the one we use for merge sort is that we only perform the merge function on consecutive sub-arrays.

This is why we only need the array, the first position, the last index of the first subarray(we can calculate the first index of the second subarray) and the last index of the second subarray.

Our task is to merge two subarrays `A[p..q]` and `A[q+1..r]` to create a sorted array `A[p..r]`. So the inputs to the function are `A`, `p`, `q` and `r`

The merge function works as follows:

1. Create copies of the subarrays `L ← A[p..q]` and `M ← A[q+1..r]`.
2. Create three pointers `i`, `j` and `k`
  - a. `i` maintains current index of `L`, starting at 1
  - b. `j` maintains current index of `M`, starting at 1
  - c. `k` maintains the current index of `A[p..q]`, starting at `p`.
3. Until we reach the end of either `L` or `M`, pick the larger among the elements from `L` and `M` and place them in the correct position at `A[p..q]`
4. When we run out of elements in either `L` or `M`, pick up the remaining elements and put in `A[p..q]`

In code, this would look like:

```
// Merge two subarrays L and M into arr
void merge(int arr[], int p, int q, int r) {

    // Create L ← A[p..q] and M ← A[q+1..r]
    int n1 = q - p + 1;
    int n2 = r - q;

    int L[n1], M[n2];
```

```

for (int i = 0; i < n1; i++)
    L[i] = arr[p + i];
for (int j = 0; j < n2; j++)
    M[j] = arr[q + 1 + j];

// Maintain current index of sub-arrays and main array
int i, j, k;
i = 0;
j = 0;
k = p;

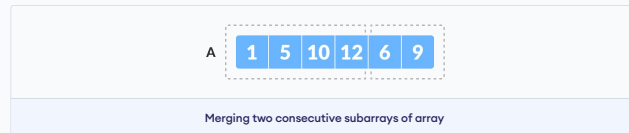
// Until we reach either end of either L or M, pick larger among
// elements L and M and place them in the correct position at A[p..r]
while (i < n1 && j < n2) {
    if (L[i] <= M[j]) {
        arr[k] = L[i];
        i++;
    } else {
        arr[k] = M[j];
        j++;
    }
}

```

## Merge() Function Explained Step-By-Step

A lot is happening in this function, so let's take an example to see how this would work.

As usual, a picture speaks a thousand words.



The array `A[0..5]` contains two sorted subarrays `A[0..3]` and `A[4..5]`. Let us see how the merge function will merge the two arrays.

```

void merge(int arr[], int p, int q, int r) {
    // Here, p = 0, q = 4, r = 6 (size of array)
}

```

### Step 1: Create duplicate copies of sub-arrays to be sorted

```

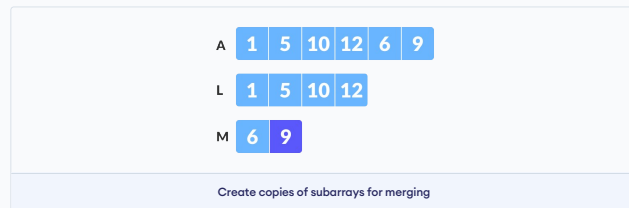
// Create L = A[p..q] and M = A[q+1..r]
int n1 = q - p + 1 = 3 - 0 + 1 = 4;
int n2 = r - q = 5 - 3 = 2;

int L[4], M[2];

for (int i = 0; i < 4; i++)
    L[i] = arr[p + i];
// L[0,1,2,3] = A[0,1,2,3] = [1,5,10,12]

for (int j = 0; j < 2; j++)
    M[j] = arr[q + 1 + j];
// M[0,1] = A[4,5] = [6,9]

```

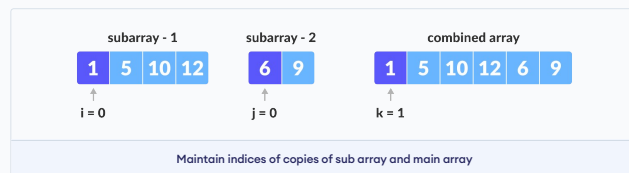


### Step 2: Maintain current index of sub-arrays and main array

```

int i, j, k;
i = 0;
j = 0;
k = p;

```

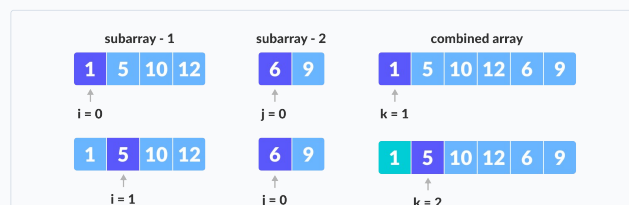


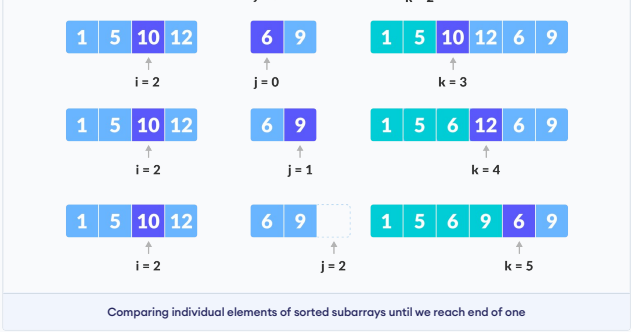
### Step 3: Until we reach the end of either L or M, pick larger among elements L and M and place them in the correct position at A[p..r]

```

while (i < n1 && j < n2) {
    if (L[i] <= M[j]) {
        arr[k] = L[i]; i++;
    }
    else {
        arr[k] = M[j];
        j++;
    }
    k++;
}

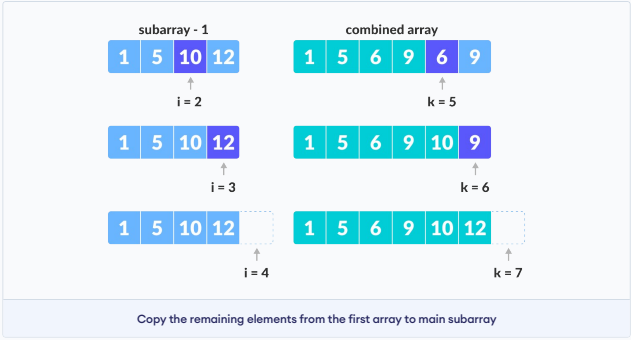
```



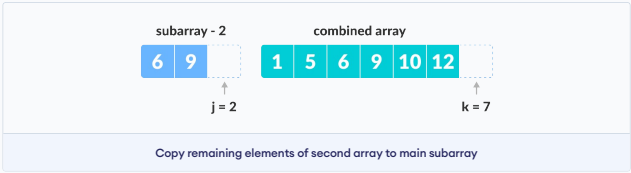


**Step 4: When we run out of elements in either L or M, pick up the remaining elements and put in A[p..r]**

```
// We exited the earlier loop because j < n2 doesn't hold
while (i < n1)
{
    arr[k] = L[i];
    i++;
    k++;
}
```



```
// We exited the earlier loop because i < n1 doesn't hold
while (j < n2)
{
    arr[k] = M[j];
    j++;
    k++;
}
```



This step would have been needed if the size of M was greater than L.  
At the end of the merge function, the subarray `A[p..r]` is sorted.

### Merge Sort Code in Python, Java, and C/C++

```
Python  Java  C  C++

// Merge sort in Java

class MergeSort {

    // Merge two subarrays L and M into arr
    void merge(int arr[], int p, int q, int r) {

        // Create L ← A[p..q] and M ← A[q+1..r]
        int n1 = q - p + 1;
        int n2 = r - q;

        int L[] = new int[n1];
        int M[] = new int[n2];

        for (int i = 0; i < n1; i++)
            L[i] = arr[p + i];
        for (int j = 0; j < n2; j++)
            M[j] = arr[q + 1 + j];

        // Maintain current index of sub-arrays and main array
        int i, j, k;
        i = 0;
        j = 0;
        k = p;

        // Until we reach either end of either L or M, pick larger among
        // elements L and M and place them in the correct position at A[p..r]
        while (i < n1 && j < n2) {
            if (L[i] <= M[j]) {
                arr[k] = L[i];
                i++;
            } else {
                arr[k] = M[j];
                j++;
            }
            k++;
        }

        // Copy the remaining elements of L and M into the array
        while (i < n1)
            arr[k] = L[i];
            i++;
            k++;
        while (j < n2)
            arr[k] = M[j];
            j++;
            k++;
    }
}
```

### Merge Sort Complexity

| Time Complexity |
|-----------------|
|-----------------|

|                         |                     |
|-------------------------|---------------------|
| Best                    | $O(n \cdot \log n)$ |
| Worst                   | $O(n \cdot \log n)$ |
| Average                 | $O(n \cdot \log n)$ |
| <b>Space Complexity</b> | $O(n)$              |
| <b>Stability</b>        | Yes                 |

### Time Complexity

Best Case Complexity:  $O(n \cdot \log n)$

Worst Case Complexity:  $O(n \cdot \log n)$

Average Case Complexity:  $O(n \cdot \log n)$

### Space Complexity

The space complexity of merge sort is  $O(n)$ .

## Merge Sort Applications

- Inversion count problem
- External sorting
- E-commerce applications

## Similar Sorting Algorithms

1. [Quicksort](#)
2. [Insertion Sort](#)
3. [Selection Sort](#)
4. [Bucket Sort](#)

Previous Tutorial:  
[Insertion Sort](#)

Next Tutorial:  
[Quicksort](#)

Share on:



Did you find this article helpful?



## Related Tutorials

DS & Algorithms

**Divide and Conquer Algorithm**

DS & Algorithms

**Insertion Sort Algorithm**

DS & Algorithms

**Counting Sort Algorithm**

DS & Algorithms

**Quicksort Algorithm**



Join our newsletter for the latest updates.

Join



### Tutorials

[Python 3 Tutorial](#)  
[JavaScript Tutorial](#)  
[SQL Tutorial](#)  
[C Tutorial](#)  
[Java Tutorial](#)  
[Kotlin Tutorial](#)  
[C++ Tutorial](#)  
[Swift Tutorial](#)  
[C# Tutorial](#)  
[Go Tutorial](#)  
[DSA Tutorial](#)

### Examples

[Python Examples](#)  
[JavaScript Examples](#)  
[C Examples](#)  
[Java Examples](#)  
[Kotlin Examples](#)  
[C++ Examples](#)

### Company

[About](#)  
[Advertising](#)  
[Privacy Policy](#)  
[Terms & Conditions](#)  
[Contact](#)  
[Blog](#)  
[Youtube](#)

### Apps

[Learn Python](#)  
[Learn C Programming](#)  
[Learn Java](#)

