

2019140032

Waw

Q1.

a) i) Infix to prefix:

$$(i) ((a+b)^* (c/d^* e))$$

$$\star + ab \mid c \star de$$

$$(ii) ((a+b-c)^* (d/e))$$

$$\star + ab - c \mid de$$

$$\star + a - bc \mid dc$$

2) Application of queue:

→ Eg. CPU scheduling or Disk scheduling

where a resource is shared among multiple consumers

→ Scheduling jobs can use priority queue.

→ breadth first tree traversal makes use of a queue.

→ Path finding algorithms.

→ When data is asynchronously transferred between two processes, eg I/O buffers, pipes, etc.

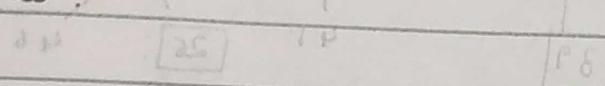
3) Algo:

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- Take a count variable and initialize it to zero
- traverse the linked list and increment count variable
- When a node points to null, it means we reached the end and we return the value of ^{count} count variable.

Code :



Wieder wo

```
int no_of_nodes()
```

```
struct node * temp = head;
```

```
int count = 0;
```

```
while (temp != NULL)
```

L

```
temp = temp -> next;
```

add after loop

```
count++;
```

now at last 15

J

```
printf("The number of nodes is %d", count);
```

done

```
return count;
```

J

15

Q1

1) Balance factor : The balance factor of a binary tree is the difference in heights of its two subtrees ($h_R - h_L$) .

The balance factor of a height balanced binary tree may take one of the value -1, 0, +1

If it is not among them then that node is unbalanced and rotation is needed.

2) To find balance factor :

Code :

```
void updatefactor (tree * root)
```

L

```
if (root == NULL)  
    return;
```

```
root -> bf = height (root -> left) - height (root -> right);
```

}

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// Height

int height (tree * root)

L

(if (root == NULL) { if (root is valid) return 0; }

return (1 + max (height (root -> left), height (root -> right));

})

// max

int max (int a, int b)

L

if (a > b)

return a;

else

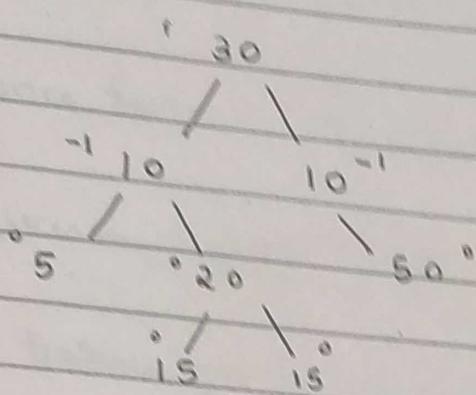
return b;

>

Q1

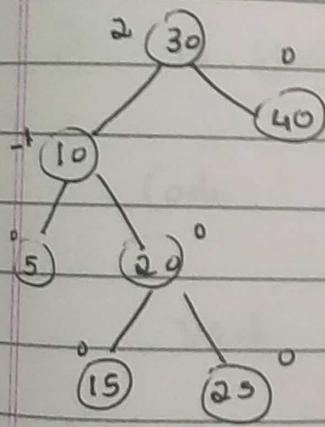
(B) OR

3)



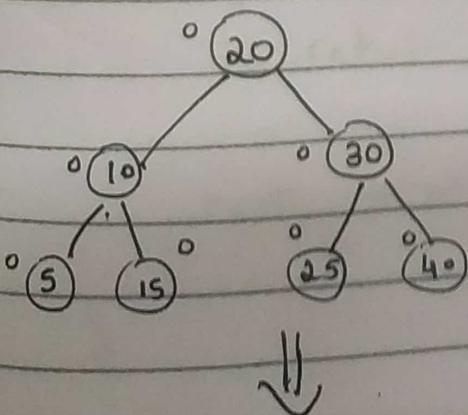
deleting 50:

As 50 has 0 children, we will directly delete 50 and then update the balance factor of the tree.



\Rightarrow Here the balance factor of node 30 is 2, hence we perform rotation.

We perform LR rotation to get this final tree which is height balanced.



Final tree

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Q2

(A) We maintain two arrays visited and stack, we enter starting element and push the adjacents and mark it visited.

Stack: D 4/5 E 10/11 F 12/13

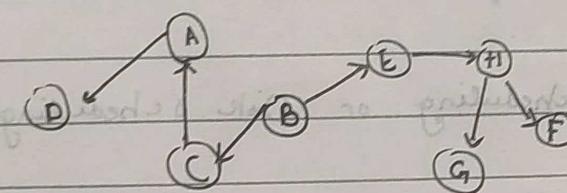
A 3/6 C 2/3 H 9 G 9/14

C 2/7 E 8 F 8/15

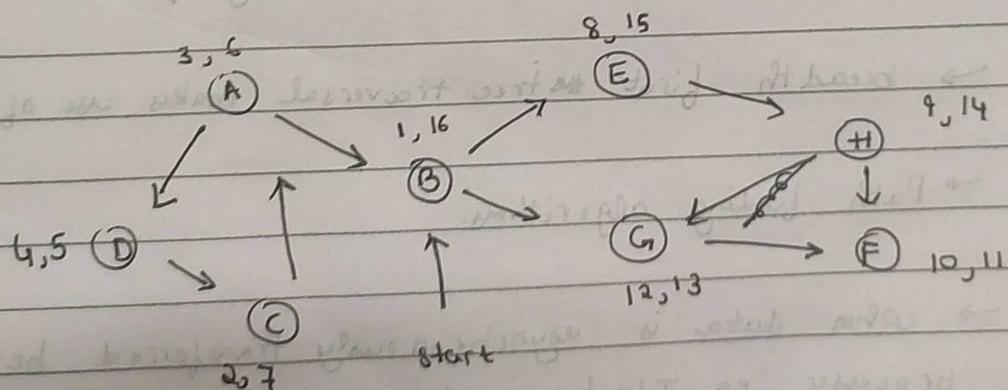
B 1 (C, B), (C - d + b) 1/16

If all the neighbours have been visited then we backtrack and pop

DFS graph:



With start time, end time:



DFS order :

B → C → A → D → E → H → F → G

↓

start

↓

Finish.

Q2

(B)

OR

Extract Min is the most important operation on a Fibonacci heap.

Here we remove the node with minimum value and the tree is re-adjusted.

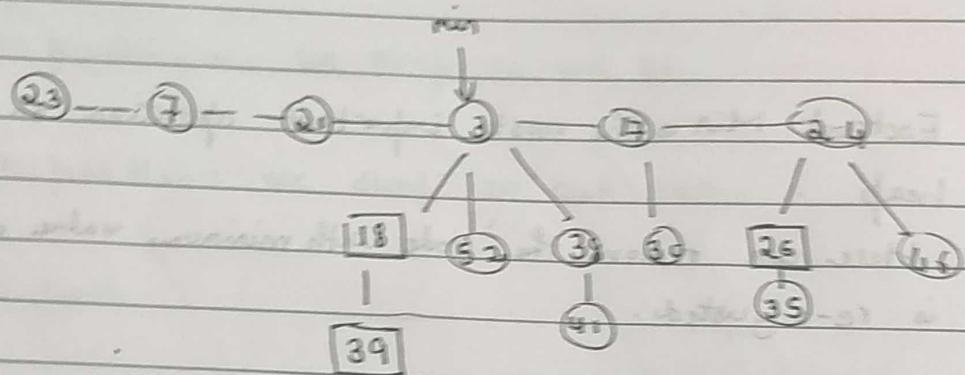
Alg. Algo.:

1. Delete the min node.
2. Set the min pointer to the next root in the root list.
3. Create an array of size equal to maximum degree of the trees in the heap before deletion.
4. Do the following steps (5 to 7) until there is no multiple roots with same degree.
5. Map the degree of the current root (min-pointer) to the degree in array.
6. Map the degree of next root to the degree in array.
7. If there are more than two mappings for the same degree, then apply union operation to those roots such that the min heap property is maintained.

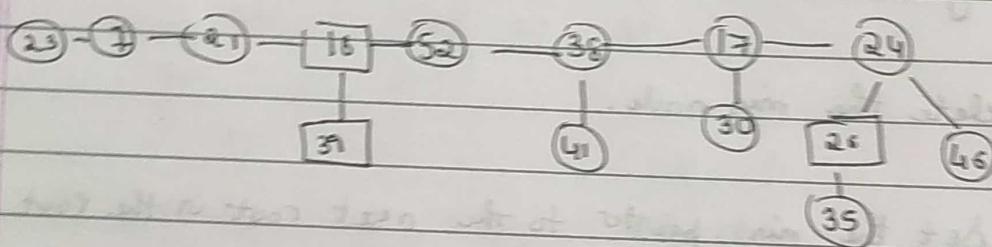
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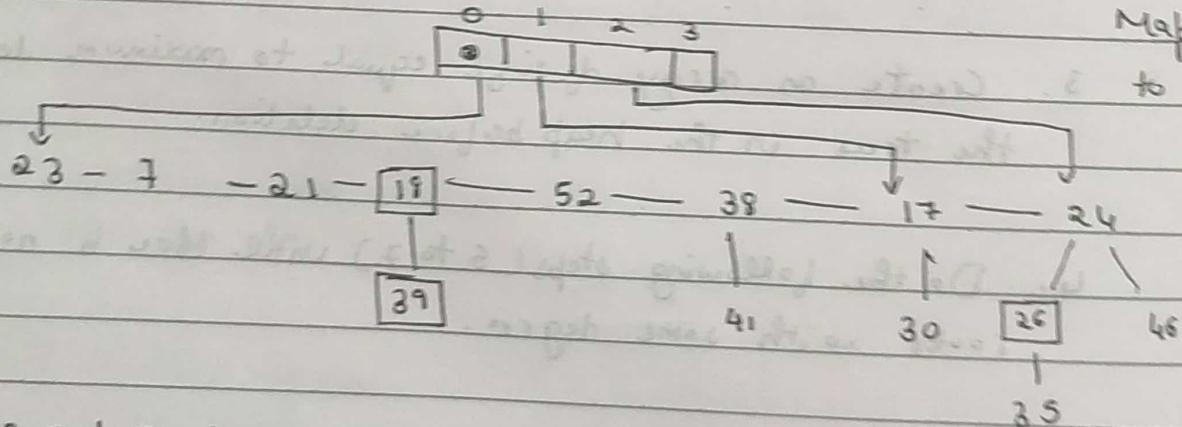
Eg.



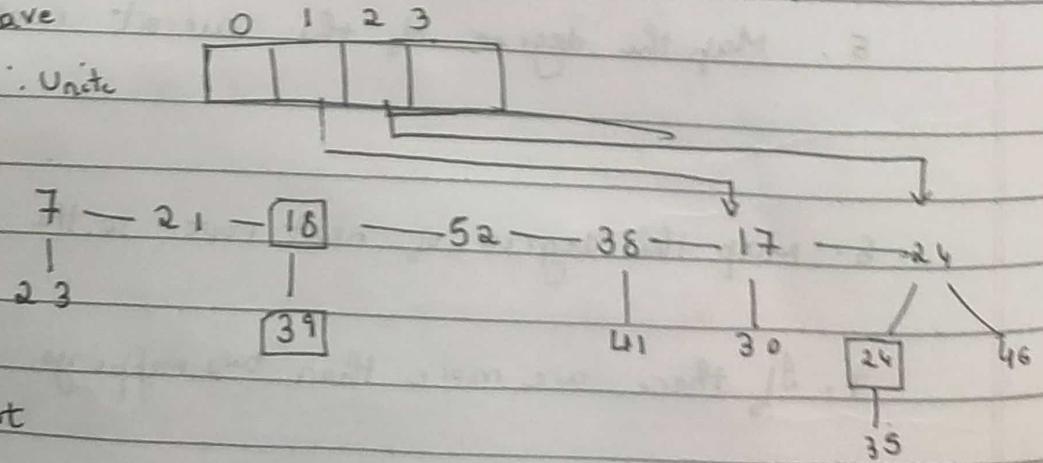
delete



Map degree
to array



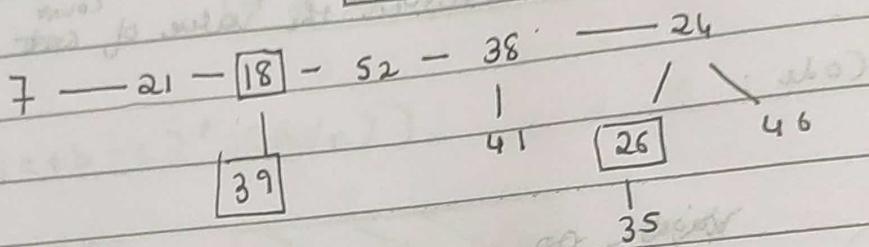
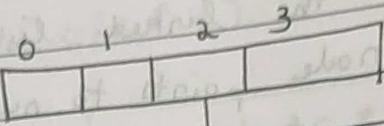
23 and 7 have
same degree, ∴ Unit



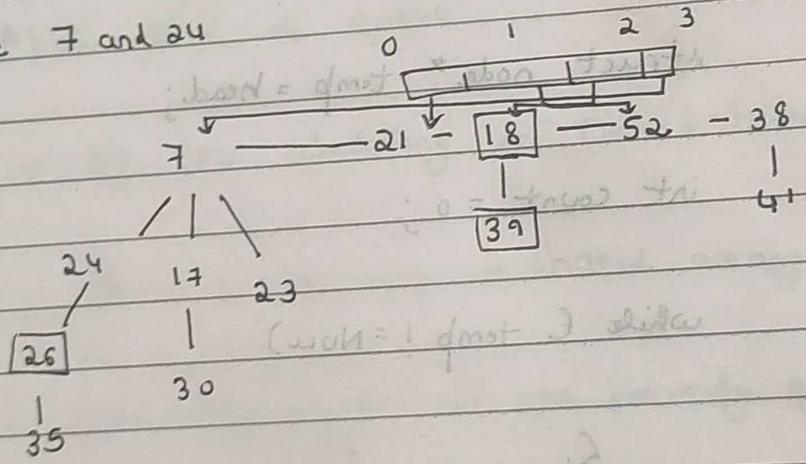
Min 7 ∴ root

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7 and 17 have
same degree



Unite 7 and 24



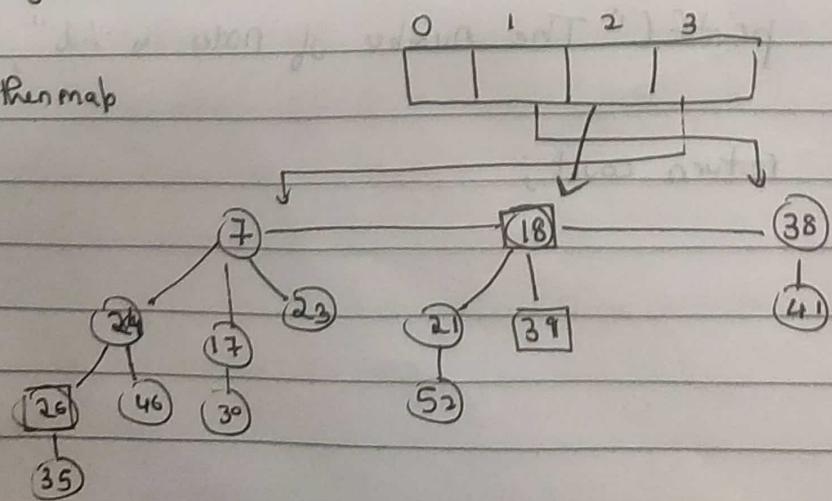
52 and 21 same down + first = first

degree unite them

21 and 18 same

degree unite

Then map



Q3

(A). Properties of B-tree:

1. All leaves are at the same level.
2. A B-tree is defined by the term minimum degree 't'.
The value of t depends upon disk block size.
3. Every node except root must contain at least $(\lceil t/2 \rceil)$ keys. The root may contain minimum 1 key.
4. All nodes (including root) may contain at most $t-1$ keys.
5. No. of children of a node equals no. of keys in it plus one.
6. All keys of a node are sorted in increasing order. The child between two keys k_1 and k_2 contains all keys in the range from k_1 and k_2 .
7. B-tree grows and shrinks from root which is unlike binary search tree. BST grow downward and also shrink from downward.
8. Like other balanced BSTs, time complexity to search, insert and delete is $O(\log n)$.

9. It is optimized for systems that read and write large blocks of data. It is common in database and file systems.

10. It is used for insertion, deletion and searching operations.

~~Insert operation is based on the above steps~~

Case (a) Odd degree No splitting: If the number of keys are less than or equal to $m-2$ then we directly add it in that node.

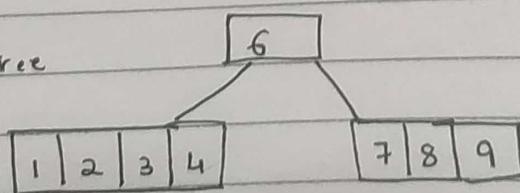
Case (b) If odd degree and more than $m-1$ keys in that node:

We divide that node into two nodes (with min no. of keys) and the middle key is promoted to parent.

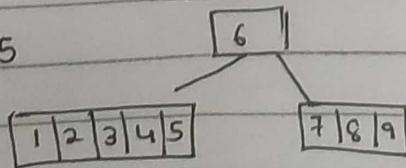
If the parent overflows then repeat [recursion]

If root overflows then make a new node and make that the root.

Eg. order 5 b tree



Insert 5

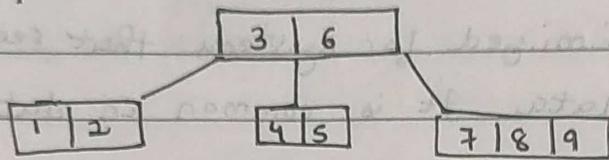


→ this node overflows

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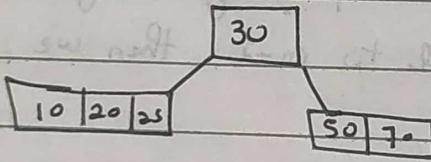
WCUW

split



Case (C) : If order is even then according to the question we do either right or left biased splitting. (to treat

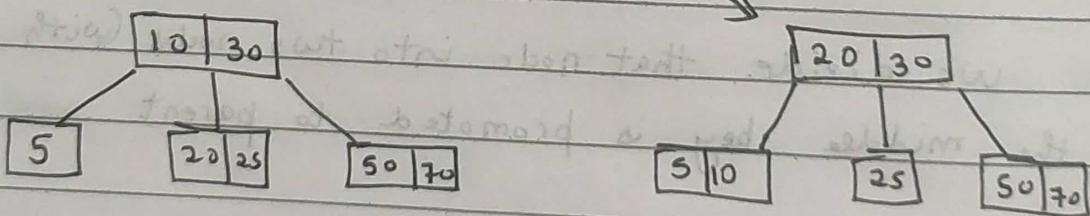
Eg. order 4 if 30 is at root then left biased splitting : (03 and)



Insert 5

right
biased

Left
biased



ADS

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Date

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Desired properties of hash function:

- The hash function should uniformly distribute the data across the entire set of possible hash values. This reduces the number of collisions and thus increasing efficiency.
- The hash function should generate very different hash values for similar strings. This allows distribution of data over the hash table.
- The hash function should be computed with efficiency.
- The hash value is fully determined by the data being hashed.
- The hash function uses all the input data.

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c) Linear probing :

$$m = 13$$

formula : $(k + i) \bmod m = h(k; i)$

$$\rightarrow 26 \bmod 13 = 0 \quad \checkmark$$

$$T[0] = 26 \text{ because } 26 \bmod 13 = 0$$

$$\bullet h(52; 0) = (52+0) \bmod 13 = 0 \quad \times$$

1st probe :

$$h(52; 1) = (52+1) \bmod 13 = 1 \quad \checkmark$$

$$T[1] = 52$$

$$\bullet h(12; 0) = (12+0) \bmod 13 = 12 \quad \checkmark$$

$$\bullet h(24; 0) = (24+0) \bmod 13 = 11 \quad \checkmark$$

$$\bullet h(77; 0) = (77+0) \bmod 13 = 12 \quad \times$$

1st probe :

$$\bullet h(77; 1) = 78 \bmod 13 = 0 \quad \times$$

2nd probe :

$$h(77; 2) = 79 \bmod 13 = 1 \quad \times$$

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3rd probe:

$$h(77; 3) = 80 \cdot 1 \cdot 13 = 2 \checkmark$$

~~$$\text{then } T[2] = 77.625 \text{ d}$$~~

$$h(80; 0) = (80+0) \cdot 1 \cdot 13 = 2 \times$$

Collision

1st probe $\circ + \bullet$

$$h(80; 1) = (80+1) \cdot 1 \cdot 13 = 3 \checkmark$$

~~$$\therefore \sqrt{T[3]} = 80.25 \text{ d} = (0; 25) \text{ d}$$~~

$$h(75; 0) = (75+0) \cdot 1 \cdot 13 = 10 \checkmark$$

$$T[10] = 75 \cdot 1.58 = 10.58 \text{ d}$$

$$h(30; 0) = (30+0) \cdot 1 \cdot 13 = 4 \checkmark$$

$$T[4] = 30 \text{ d}$$

Final table $a_1 = 81 \cdot 1.510$

$$T \Rightarrow a_1 = [26] \text{ d}$$

2 77

3 80

4 30

5 -

6 75

7 -

8 - d

9 -

10 75

11 24

12

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(iii) Quadratic:

formula: $h(k, i) = [h_1(k) + c_1 i + c_2 i^2] \bmod m$

where $c_1 = 0$, and $h_1(k) = k$; $c_2 = 1$

$$= (k + 0 \cdot i^2) \bmod m$$

$\checkmark h(26; 0) = 26 \cdot 1 \cdot 13 = 0 \quad \checkmark$

$\checkmark T[0] = 26 \quad \checkmark$

$\checkmark h(52; 0) = 52 \cdot 1 \cdot 13 = 0 \quad \times$

$h(52; 1) = (52 + 1) \cdot 1 \cdot 13 = (0; 08) \quad \checkmark$

 $= 1 \quad \checkmark$

$T[1] = 52$

$\checkmark h(12; 0) = 12 \cdot 1 \cdot 13 = 12 \quad \checkmark$

$T[12] = 12$

$\checkmark h(24; 0) = 24 \cdot 1 \cdot 13 = 11 \quad \checkmark$

$T[11] = 24$

$\checkmark h(77; 0) = 77 \cdot 1 \cdot 13 = 12 \quad \times$

$h(77; 1) = 78 \cdot 1 \cdot 13 = 0 \quad \times$

$h(77; 4) = 81 \cdot 1 \cdot 13 = 3 \quad \checkmark$

$T[3] = 77$

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$$\cdot h(80; 0) = 80 \cdot 1 \cdot 13 \\ = 2 \checkmark$$

$$T[2] = 80$$

$$\cdot h(75; 0) = 75 \cdot 1 \cdot 13 \rightarrow 20 \text{ small off } \checkmark \\ = 10 \checkmark$$

$$\cdot h(30; 0) = 30 \cdot 1 \cdot 13$$

Final table:

$T \rightarrow$	0	26
1	52	
2	80	
3	77	
4	30	
5	-	
6	-	
7	-	
8	-	
9	-	
10	75	
11	24	
12	12	