

Synchronized Consensus

CONSTANTS N , $FAILNUM$
$$Nodes \triangleq 1 \dots N$$

$counter \triangleq 0$	record the <i>FailNum</i>
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variables	$FailNum = FAILNUM;$	Initialization block
	$up = [n \in Nodes \mapsto \text{TRUE}];$	Nodes are up
	$pt = [n \in Nodes \mapsto 0];$	Nodes are at round 0
	$t = [n \in Nodes \mapsto \text{FALSE}];$	Nodes are not terminated
	$d = [n \in Nodes \mapsto -1];$	Nodes are not decided
	$mb = [n \in Nodes \mapsto \{\}];$	Nodes have mailbox as emptyset

Initialization block

Nodes are up

Nodes are at round 0

Nodes are not terminated

Nodes are not decided

Nodes have mailbox as emptyset

$$SetMin(S) \stackrel{\Delta}{=} \text{CHOOSE } i \in S : \forall j \in S : i \leq j$$

```
macro MaybeFail( ) {
```

$$\{ \textbf{either } \{ up[self] := \text{FALSE}; FailNum := FailNum - 1; counter := counter + 1 \}$$

```
if fail, counter =
```

or skip ;

fair process ($n \in Nodes$)

$$\{$$
$$v := self ;$$

PS: **while** (*pt*[*self*] \leq *counter*) {

$$Q := Nodes;$$
$$L1: \text{while } (up[self] \wedge Q \neq \{\}) \{$$

with $(p \in Q) \{$

MaybeFail(); the node can crash when sending message

if ($\neg up[self]$) { if the node crash, it's terminated

$$t[self] := \text{TRUE};$$

goto PR ;

}

```

else {
    mb[p] := mb[p] ∪ {v};      put value v into the node's mailbox
    Q := Q \ {p};             delete p out of the set Q
}
} ;
}
else {
    await (∀ i ∈ Nodes : pt[i] ≥ 1 ∨ ¬up[i]);    for all nodes, if not at round 0, or up[i] = False
    Q := Nodes;
    L2: while ( up[self] ∧ Q ≠ {} ) {
        with ( p ∈ Q ) {
            MaybeFail();
            if ( ¬up[self] ) {
                t[self] := TRUE;
                goto PR;
            }
            else {
                mb[p] := mb[p] ∪ mb[self];
                Q := Q \ {p};
            }
        } ;
    } ;
    L3: pt[self] := pt[self] + 1;
} ;

PR: await (∀ n ∈ Nodes : (pt[n] = counter + 1 ∨ up[n] = FALSE));    await for all nodes at rounds counter + 1
    if ( up[self] ) d[self] := SetMin(mb[self]);
    t[self] := TRUE;
}
}
}

```

BEGIN TRANSLATION

VARIABLES *FailNum*, *up*, *pt*, *t*, *d*, *mb*, *pc*

define statement

$SetMin(S) \triangleq \text{CHOOSE } i \in S : \forall j \in S : i \leq j$

VARIABLES *v*, *Q*

$vars \triangleq \langle FailNum, up, pt, t, d, mb, pc, v, Q \rangle$

$ProcSet \triangleq (Nodes)$

$Init \triangleq \text{Global variables}$
 $\wedge FailNum = FAILNUM$

$$\begin{aligned}
& \wedge up = [n \in Nodes \mapsto \text{TRUE}] \\
& \wedge pt = [n \in Nodes \mapsto 0] \\
& \wedge t = [n \in Nodes \mapsto \text{FALSE}] \\
& \wedge d = [n \in Nodes \mapsto -1] \\
& \wedge mb = [n \in Nodes \mapsto \{\}] \\
& \text{Process } n \\
& \wedge v = [self \in Nodes \mapsto 0] \\
& \wedge Q = [self \in Nodes \mapsto \{\}] \\
& \wedge pc = [self \in ProcSet \mapsto \text{"P"}] \\
\\
P(self) & \triangleq \wedge pc[self] = \text{"P"} \\
& \wedge \text{IF } up[self] \\
& \quad \text{THEN } \wedge v' = [v \text{ EXCEPT } ![self] = self] \\
& \quad \quad \wedge Q' = [Q \text{ EXCEPT } ![self] = Nodes] \\
& \quad \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"PS"}] \\
& \quad \text{ELSE } \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Done"}] \\
& \quad \quad \wedge \text{UNCHANGED } \langle v, Q \rangle \\
& \quad \wedge \text{UNCHANGED } \langle FailNum, up, pt, t, d, mb \rangle \\
\\
PS(self) & \triangleq \wedge pc[self] = \text{"PS"} \\
& \wedge \text{IF } pt[self] \leq counter \\
& \quad \text{THEN } \wedge \text{IF } pt[self] = 0 \\
& \quad \quad \text{THEN } \wedge Q' = [Q \text{ EXCEPT } ![self] = Nodes] \\
& \quad \quad \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L1"}] \\
& \quad \quad \text{ELSE } \wedge (\forall i \in Nodes : pt[i] \geq 1 \vee \neg up[i]) \\
& \quad \quad \quad \wedge Q' = [Q \text{ EXCEPT } ![self] = Nodes] \\
& \quad \quad \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L2"}] \\
& \quad \text{ELSE } \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"PR"}] \\
& \quad \quad \wedge Q' = Q \\
& \quad \wedge \text{UNCHANGED } \langle FailNum, up, pt, t, d, mb, v \rangle \\
\\
L3(self) & \triangleq \wedge pc[self] = \text{"L3"} \\
& \wedge pt' = [pt \text{ EXCEPT } ![self] = pt[self] + 1] \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"PS"}] \\
& \wedge \text{UNCHANGED } \langle FailNum, up, t, d, mb, v, Q \rangle \\
\\
L1(self) & \triangleq \wedge pc[self] = \text{"L1"} \\
& \wedge \text{IF } up[self] \wedge Q[self] \neq \{\} \\
& \quad \text{THEN } \wedge \exists p \in Q[self] : \\
& \quad \quad \wedge \text{IF } FailNum > 0 \wedge up[self] \\
& \quad \quad \quad \text{THEN } \wedge \vee \wedge up' = [up \text{ EXCEPT } ![self] = \text{FALSE}] \\
& \quad \quad \quad \quad \wedge FailNum' = FailNum - 1 \\
& \quad \quad \quad \quad \wedge counter' = counter + 1 \\
& \quad \quad \quad \vee \wedge \text{TRUE} \\
& \quad \quad \quad \wedge \text{UNCHANGED } \langle FailNum, up \rangle \\
& \quad \text{ELSE } \wedge \text{TRUE}
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{UNCHANGED } \langle \text{FailNum}, up \rangle \\
& \wedge \text{IF } \neg up'[self] \\
& \quad \text{THEN } \wedge t' = [t \text{ EXCEPT } ![self] = \text{TRUE}] \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"PR"}] \\
& \quad \wedge \text{UNCHANGED } \langle mb, Q \rangle \\
& \quad \text{ELSE } \wedge mb' = [mb \text{ EXCEPT } ![p] = mb[p] \cup \{v[self]\}] \\
& \quad \wedge Q' = [Q \text{ EXCEPT } ![self] = Q[self] \setminus \{p\}] \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L1"}] \\
& \quad \wedge t' = t \\
& \quad \text{ELSE } \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L3"}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{FailNum}, up, t, mb, Q \rangle \\
& \wedge \text{UNCHANGED } \langle pt, d, v \rangle \\
L2(self) & \triangleq \wedge pc[self] = \text{"L2"} \\
& \wedge \text{IF } up[self] \wedge Q[self] \neq \{\} \\
& \quad \text{THEN } \wedge \exists p \in Q[self] : \\
& \quad \quad \wedge \text{IF } \text{FailNum} > 0 \wedge up[self] \\
& \quad \quad \quad \text{THEN } \wedge \vee \wedge up' = [up \text{ EXCEPT } ![self] = \text{FALSE}] \\
& \quad \quad \quad \wedge \text{FailNum}' = \text{FailNum} - 1 \\
& \quad \quad \quad \wedge counter' = counter + 1 \\
& \quad \quad \quad \vee \wedge \text{TRUE} \\
& \quad \quad \quad \wedge \text{UNCHANGED } \langle \text{FailNum}, up \rangle \\
& \quad \quad \text{ELSE } \wedge \text{TRUE} \\
& \quad \quad \wedge \text{UNCHANGED } \langle \text{FailNum}, up \rangle \\
& \wedge \text{IF } \neg up'[self] \\
& \quad \text{THEN } \wedge t' = [t \text{ EXCEPT } ![self] = \text{TRUE}] \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"PR"}] \\
& \quad \wedge \text{UNCHANGED } \langle mb, Q \rangle \\
& \quad \text{ELSE } \wedge mb' = [mb \text{ EXCEPT } ![p] = mb[p] \cup mb[self]] \\
& \quad \wedge Q' = [Q \text{ EXCEPT } ![self] = Q[self] \setminus \{p\}] \\
& \quad \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L2"}] \\
& \quad \wedge t' = t \\
& \quad \text{ELSE } \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"L3"}] \\
& \quad \wedge \text{UNCHANGED } \langle \text{FailNum}, up, t, mb, Q \rangle \\
& \wedge \text{UNCHANGED } \langle pt, d, v \rangle \\
PR(self) & \triangleq \wedge pc[self] = \text{"PR"} \\
& \wedge (\forall n \in \text{Nodes} : (pt[n] = counter + 1 \vee up[n] = \text{FALSE})) \\
& \wedge \text{IF } up[self] \\
& \quad \text{THEN } \wedge d' = [d \text{ EXCEPT } ![self] = \text{SetMin}(mb[self])] \\
& \quad \text{ELSE } \wedge \text{TRUE} \\
& \quad \wedge d' = d \\
& \wedge t' = [t \text{ EXCEPT } ![self] = \text{TRUE}] \\
& \wedge pc' = [pc \text{ EXCEPT } ![self] = \text{"Done"}] \\
& \wedge \text{UNCHANGED } \langle \text{FailNum}, up, pt, mb, v, Q \rangle
\end{aligned}$$

$$n(self) \triangleq P(self) \vee PS(self) \vee L3(self) \vee L1(self) \vee L2(self) \\ \vee PR(self)$$

$$Next \triangleq (\exists self \in Nodes : n(self)) \\ \vee \text{Disjunct to prevent deadlock on termination} \\ ((\forall self \in ProcSet : pc[self] = \text{"Done"}) \wedge \text{UNCHANGED } vars)$$

$$Spec \triangleq \wedge Init \wedge \Box [Next]_{vars} \\ \wedge \forall self \in Nodes : WF_{vars}(n(self))$$

$$Termination \triangleq \Diamond (\forall self \in ProcSet : pc[self] = \text{"Done"})$$

END TRANSLATION

$$Inv \triangleq (\exists i \in Nodes : \neg t[i]) \vee (\forall l, m \in Nodes : \neg up[l] \vee \neg up[m] \vee d[l] = d[m])$$

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