

Stepwise Selection

The REG Procedure

Model: MODEL1

Dependent Variable: quality

Adjusted R-Square Selection Method

| | |
|-----------------------------|------|
| Number of Observations Read | 1599 |
| Number of Observations Used | 1599 |

| Number in Model | Adjusted R-Square | R-Square | AIC | Variables in Model |
|-----------------|-------------------|----------|------------|---------------------------------------------------------------------|
| 7 | 0.3572 | 0.3600 | -1382.2341 | vol_acidity chlorides free_sulfur total_sulfur pH sulphates alcohol |
| 6 | 0.3554 | 0.3578 | -1378.5568 | vol_acidity chlorides total_sulfur pH sulphates alcohol |
| 6 | 0.3507 | 0.3532 | -1367.1591 | vol_acidity chlorides free_sulfur total_sulfur sulphates alcohol |
| 5 | 0.3500 | 0.3520 | -1366.2685 | vol_acidity chlorides total_sulfur sulphates alcohol |

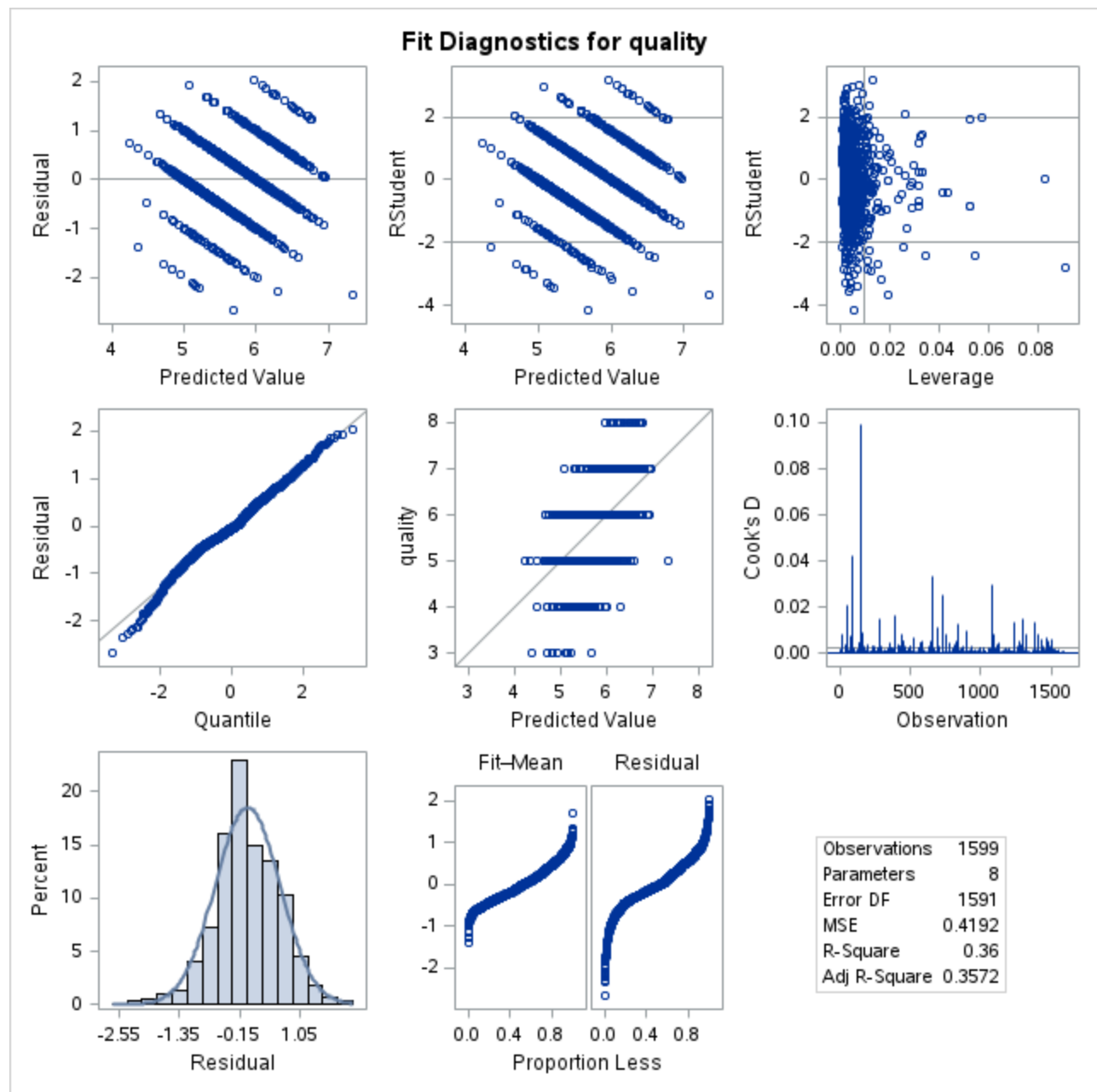
| Number in Model | Adjusted R-Square | R-Square | AIC | Variables in Model |
|-----------------|-------------------|----------|------------|-----------------------------------------------------------|
| 6 | 0.3472 | 0.3497 | -1358.4932 | vol_acidity chlorides free_sulfur pH sulphates alcohol |
| 5 | 0.3468 | 0.3488 | -1358.4479 | vol_acidity chlorides pH sulphates alcohol |
| 6 | 0.3467 | 0.3491 | -1357.1258 | vol_acidity free_sulfur total_sulfur pH sulphates alcohol |
| 5 | 0.3449 | 0.3470 | -1353.8915 | vol_acidity total_sulfur pH sulphates alcohol |
| 5 | 0.3430 | 0.3451 | -1349.2612 | vol_acidity free_sulfur total_sulfur sulphates alcohol |
| 5 | 0.3428 | 0.3448 | -1348.6744 | vol_acidity chlorides free_sulfur sulphates alcohol |
| 4 | 0.3421 | 0.3438 | -1348.1049 | vol_acidity total_sulfur sulphates alcohol |
| 4 | 0.3419 | 0.3435 | -1347.4780 | vol_acidity chlorides sulphates alcohol |
| 5 | 0.3375 | 0.3396 | -1335.8198 | vol_acidity free_sulfur pH sulphates alcohol |
| 4 | 0.3372 | 0.3388 | -1336.0432 | vol_acidity pH sulphates alcohol |
| 4 | 0.3353 | 0.3370 | -1331.5566 | vol_acidity free_sulfur sulphates alcohol |
| 3 | 0.3346 | 0.3359 | -1330.9611 | vol_acidity sulphates alcohol |
| 6 | 0.3312 | 0.3338 | -1319.8471 | vol_acidity chlorides free_sulfur total_sulfur pH alcohol |
| 5 | 0.3297 | 0.3318 | -1317.2506 | vol_acidity free_sulfur total_sulfur pH alcohol |
| 5 | 0.3290 | 0.3311 | -1315.4782 | vol_acidity chlorides total_sulfur pH alcohol |
| 4 | 0.3276 | 0.3293 | -1313.1734 | vol_acidity total_sulfur pH alcohol |
| 5 | 0.3228 | 0.3249 | -1300.7357 | vol_acidity chlorides free_sulfur total_sulfur alcohol |
| 4 | 0.3227 | 0.3244 | -1301.6547 | vol_acidity free_sulfur total_sulfur alcohol |
| 4 | 0.3227 | 0.3244 | -1301.6296 | vol_acidity chlorides pH alcohol |
| 5 | 0.3226 | 0.3247 | -1300.3548 | vol_acidity chlorides free_sulfur pH alcohol |
| 4 | 0.3219 | 0.3236 | -1299.6167 | vol_acidity chlorides total_sulfur alcohol |
| 3 | 0.3218 | 0.3231 | -1300.4790 | vol_acidity total_sulfur alcohol |
| 3 | 0.3214 | 0.3227 | -1299.5345 | vol_acidity pH alcohol |
| 4 | 0.3213 | 0.3230 | -1298.3000 | vol_acidity free_sulfur pH alcohol |
| 6 | 0.3171 | 0.3197 | -1286.3578 | chlorides free_sulfur total_sulfur pH sulphates alcohol |
| 4 | 0.3164 | 0.3181 | -1286.7162 | vol_acidity chlorides free_sulfur alcohol |
| 3 | 0.3163 | 0.3176 | -1287.5629 | vol_acidity free_sulfur alcohol |
| 3 | 0.3162 | 0.3174 | -1287.1765 | vol_acidity chlorides alcohol |
| 2 | 0.3161 | 0.3170 | -1288.0566 | vol_acidity alcohol |
| 5 | 0.3127 | 0.3148 | -1277.1042 | chlorides total_sulfur pH sulphates alcohol |
| 5 | 0.3014 | 0.3036 | -1251.0644 | chlorides free_sulfur pH sulphates alcohol |
| 4 | 0.3014 | 0.3031 | -1252.0049 | chlorides pH sulphates alcohol |
| 5 | 0.2968 | 0.2990 | -1240.5742 | free_sulfur total_sulfur pH sulphates alcohol |
| 5 | 0.2959 | 0.2981 | -1238.4988 | chlorides free_sulfur total_sulfur sulphates alcohol |
| 4 | 0.2940 | 0.2958 | -1235.1502 | chlorides total_sulfur sulphates alcohol |
| 4 | 0.2923 | 0.2941 | -1231.4306 | total_sulfur pH sulphates alcohol |
| 4 | 0.2839 | 0.2857 | -1212.5257 | chlorides free_sulfur sulphates alcohol |
| 3 | 0.2832 | 0.2845 | -1211.8348 | chlorides sulphates alcohol |
| 3 | 0.2820 | 0.2833 | -1209.1681 | pH sulphates alcohol |
| 4 | 0.2819 | 0.2836 | -1207.8988 | free_sulfur pH sulphates alcohol |
| 4 | 0.2813 | 0.2831 | -1206.6831 | free_sulfur total_sulfur sulphates alcohol |
| 3 | 0.2791 | 0.2804 | -1202.6789 | total_sulfur sulphates alcohol |
| 3 | 0.2694 | 0.2708 | -1181.4323 | free_sulfur sulphates alcohol |
| 5 | 0.2693 | 0.2716 | -1179.2671 | chlorides free_sulfur total_sulfur pH alcohol |
| 2 | 0.2690 | 0.2699 | -1181.4774 | sulphates alcohol |
| 4 | 0.2652 | 0.2671 | -1171.3068 | free_sulfur total_sulfur pH alcohol |
| 4 | 0.2632 | 0.2651 | -1166.9959 | chlorides total_sulfur pH alcohol |
| 3 | 0.2593 | 0.2607 | -1159.4823 | total_sulfur pH alcohol |
| 3 | 0.2549 | 0.2563 | -1150.0701 | chlorides pH alcohol |

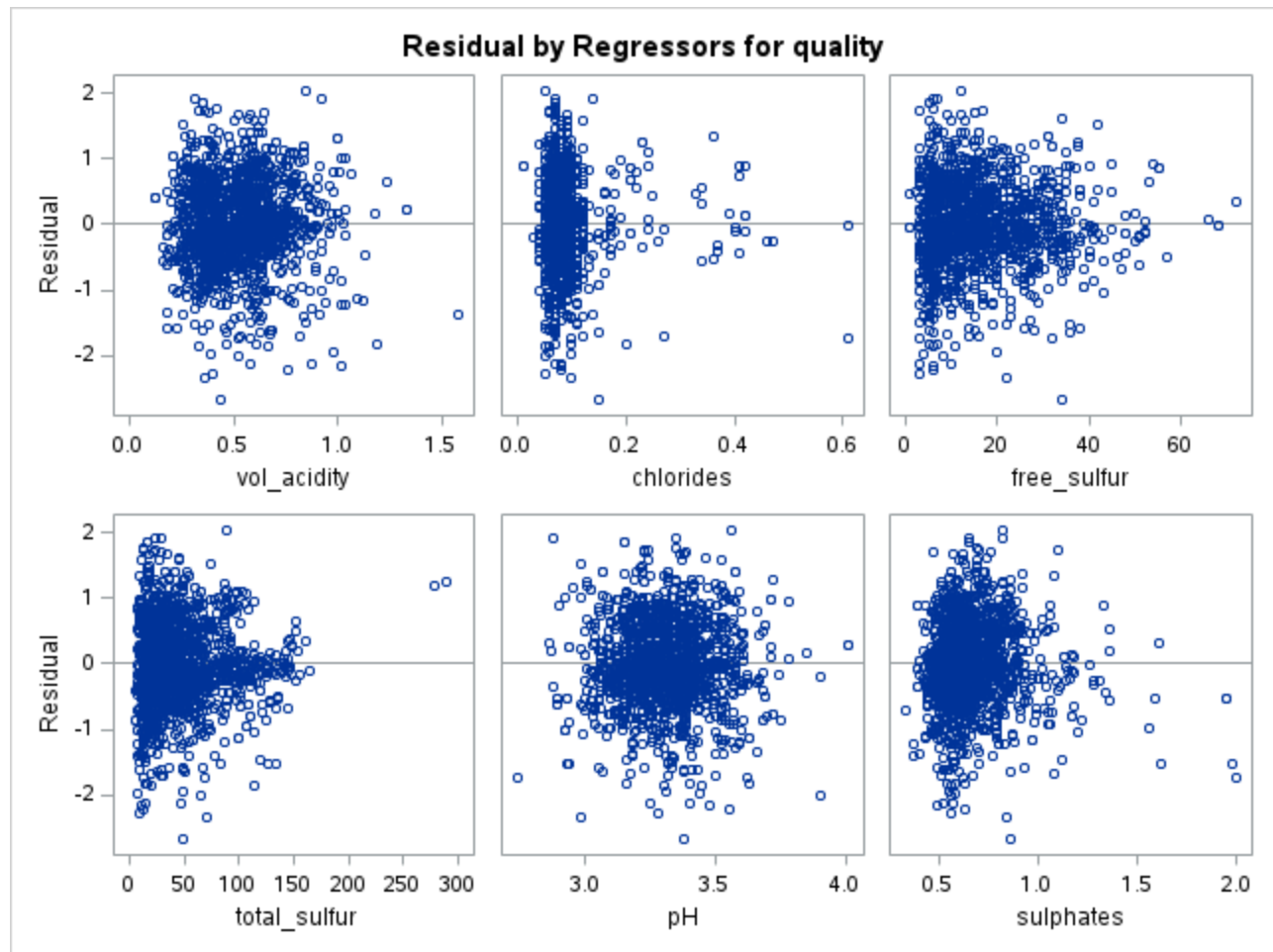
| Number in Model | Adjusted R-Square | R-Square | AIC | Variables in Model |
|-----------------|-------------------|----------|------------|-------------------------------------------------------------|
| 4 | 0.2545 | 0.2563 | -1148.0950 | chlorides free_sulfur pH alcohol |
| 2 | 0.2511 | 0.2520 | -1142.8308 | pH alcohol |
| 3 | 0.2506 | 0.2520 | -1140.8630 | free_sulfur pH alcohol |
| 5 | 0.2383 | 0.2407 | -1112.7962 | vol_acidity chlorides free_sulfur total_sulfur sulphates |
| 6 | 0.2380 | 0.2408 | -1111.0843 | vol_acidity chlorides free_sulfur total_sulfur pH sulphates |
| 4 | 0.2367 | 0.2386 | -1110.3158 | chlorides free_sulfur total_sulfur alcohol |
| 3 | 0.2364 | 0.2379 | -1110.8238 | free_sulfur total_sulfur alcohol |
| 4 | 0.2354 | 0.2373 | -1107.6702 | vol_acidity chlorides total_sulfur sulphates |
| 5 | 0.2349 | 0.2373 | -1105.6724 | vol_acidity chlorides total_sulfur pH sulphates |
| 3 | 0.2340 | 0.2354 | -1105.7378 | chlorides total_sulfur alcohol |
| 2 | 0.2337 | 0.2347 | -1106.1436 | total_sulfur alcohol |
| 2 | 0.2265 | 0.2275 | -1091.2236 | chlorides alcohol |
| 3 | 0.2264 | 0.2278 | -1089.8948 | chlorides free_sulfur alcohol |
| 1 | 0.2262 | 0.2267 | -1091.6482 | alcohol |
| 2 | 0.2261 | 0.2270 | -1090.2927 | free_sulfur alcohol |
| 4 | 0.2130 | 0.2150 | -1061.5644 | vol_acidity chlorides free_sulfur sulphates |
| 5 | 0.2128 | 0.2153 | -1060.1542 | vol_acidity chlorides free_sulfur pH sulphates |
| 3 | 0.2091 | 0.2106 | -1054.6534 | vol_acidity chlorides sulphates |
| 4 | 0.2088 | 0.2107 | -1052.9245 | vol_acidity chlorides pH sulphates |
| 5 | 0.2070 | 0.2095 | -1048.4508 | vol_acidity free_sulfur total_sulfur pH sulphates |
| 4 | 0.2064 | 0.2084 | -1048.1889 | vol_acidity free_sulfur total_sulfur sulphates |
| 4 | 0.2042 | 0.2062 | -1043.6641 | vol_acidity total_sulfur pH sulphates |
| 3 | 0.2027 | 0.2041 | -1041.6161 | vol_acidity total_sulfur sulphates |
| 4 | 0.1890 | 0.1911 | -1013.5477 | vol_acidity chlorides free_sulfur total_sulfur |
| 5 | 0.1889 | 0.1914 | -1012.2958 | vol_acidity chlorides free_sulfur total_sulfur pH |
| 3 | 0.1855 | 0.1870 | -1007.5819 | vol_acidity chlorides total_sulfur |
| 4 | 0.1850 | 0.1871 | -1005.7005 | vol_acidity chlorides total_sulfur pH |
| 4 | 0.1824 | 0.1844 | -1000.5201 | vol_acidity free_sulfur pH sulphates |
| 3 | 0.1797 | 0.1812 | -996.2278 | vol_acidity free_sulfur total_sulfur |
| 4 | 0.1793 | 0.1813 | -994.4020 | vol_acidity free_sulfur total_sulfur pH |
| 3 | 0.1789 | 0.1804 | -994.6967 | vol_acidity free_sulfur sulphates |
| 3 | 0.1783 | 0.1798 | -993.5018 | vol_acidity pH sulphates |
| 2 | 0.1757 | 0.1768 | -989.5499 | vol_acidity total_sulfur |
| 3 | 0.1757 | 0.1772 | -988.4344 | vol_acidity total_sulfur pH |
| 2 | 0.1755 | 0.1765 | -989.0045 | vol_acidity sulphates |
| 5 | 0.1675 | 0.1701 | -970.6644 | chlorides free_sulfur total_sulfur pH sulphates |
| 3 | 0.1655 | 0.1670 | -968.7129 | vol_acidity chlorides free_sulfur |
| 4 | 0.1650 | 0.1671 | -966.8536 | vol_acidity chlorides free_sulfur pH |
| 2 | 0.1630 | 0.1640 | -965.0056 | vol_acidity chlorides |
| 3 | 0.1625 | 0.1641 | -963.0394 | vol_acidity chlorides pH |
| 4 | 0.1610 | 0.1631 | -959.1814 | chlorides free_sulfur total_sulfur sulphates |
| 4 | 0.1599 | 0.1620 | -957.0932 | chlorides total_sulfur pH sulphates |
| 3 | 0.1555 | 0.1570 | -949.6675 | vol_acidity free_sulfur pH |
| 3 | 0.1554 | 0.1570 | -949.6145 | chlorides total_sulfur sulphates |
| 2 | 0.1545 | 0.1555 | -948.7776 | vol_acidity free_sulfur |
| 2 | 0.1526 | 0.1537 | -945.3579 | vol_acidity pH |
| 1 | 0.1520 | 0.1525 | -945.0694 | vol_acidity |
| 4 | 0.1269 | 0.1291 | -895.5201 | chlorides free_sulfur pH sulphates |
| 3 | 0.1244 | 0.1261 | -891.9686 | chlorides free_sulfur sulphates |

| Number in Model | Adjusted R-Square | R-Square | AIC | Variables in Model |
|-----------------|-------------------|----------|-----------|---------------------------------------|
| 3 | 0.1234 | 0.1251 | -890.1796 | chlorides pH sulphates |
| 2 | 0.1204 | 0.1215 | -885.5437 | chlorides sulphates |
| 4 | 0.1088 | 0.1110 | -862.6175 | free_sulfur total_sulfur pH sulphates |
| 3 | 0.1081 | 0.1097 | -862.3748 | free_sulfur total_sulfur sulphates |
| 2 | 0.1005 | 0.1016 | -849.8972 | total_sulfur sulphates |
| 3 | 0.1004 | 0.1021 | -848.6175 | total_sulfur pH sulphates |
| 4 | 0.0707 | 0.0730 | -795.7828 | chlorides free_sulfur total_sulfur pH |
| 2 | 0.0661 | 0.0673 | -789.8362 | free_sulfur sulphates |
| 3 | 0.0655 | 0.0673 | -787.8541 | free_sulfur pH sulphates |
| 1 | 0.0626 | 0.0632 | -784.8891 | sulphates |
| 2 | 0.0621 | 0.0633 | -783.0113 | pH sulphates |
| 3 | 0.0590 | 0.0608 | -776.7798 | chlorides total_sulfur pH |
| 3 | 0.0565 | 0.0583 | -772.4918 | chlorides free_sulfur total_sulfur |
| 3 | 0.0495 | 0.0513 | -760.7352 | free_sulfur total_sulfur pH |
| 2 | 0.0483 | 0.0495 | -759.7160 | chlorides total_sulfur |
| 2 | 0.0427 | 0.0439 | -750.2114 | free_sulfur total_sulfur |
| 2 | 0.0380 | 0.0392 | -742.4217 | total_sulfur pH |
| 1 | 0.0337 | 0.0343 | -736.2425 | total_sulfur |
| 3 | 0.0266 | 0.0284 | -722.5899 | chlorides free_sulfur pH |
| 2 | 0.0253 | 0.0265 | -721.5020 | chlorides pH |
| 2 | 0.0187 | 0.0199 | -710.6181 | chlorides free_sulfur |
| 1 | 0.0167 | 0.0174 | -708.4987 | chlorides |
| 2 | 0.0043 | 0.0055 | -687.3391 | free_sulfur pH |
| 1 | 0.0027 | 0.0033 | -685.8350 | pH |
| 1 | 0.0019 | 0.0026 | -684.6052 | free_sulfur |

Stepwise Selection

The REG Procedure
Model: MODEL1
Dependent Variable: quality







Forward Selection

The REG Procedure
Model: MODEL1
Dependent Variable: quality

| | |
|-----------------------------|------|
| Number of Observations Read | 1599 |
| Number of Observations Used | 1599 |

Forward Selection: Step 1

Variable alcohol Entered: R-Square = 0.2267 and C(p) = 327.4438

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 1 | 236.29279 | 236.29279 | 468.26 | <.0001 |
| Error | 1597 | 805.87231 | 0.50462 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-----------|--------------------|----------------|------------|---------|--------|
| Intercept | 1.87502 | 0.17471 | 58.12245 | 115.18 | <.0001 |
| alcohol | 0.36084 | 0.01668 | 236.29279 | 468.26 | <.0001 |

Bounds on condition number: 1, 1

Forward Selection: Step 2

Variable vol_acidity Entered: R-Square = 0.3170 and C(p) = 105.1076

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 2 | 330.33266 | 165.16633 | 370.32 | <.0001 |
| Error | 1596 | 711.83245 | 0.44601 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-------------|--------------------|----------------|------------|---------|--------|
| Intercept | 3.09370 | 0.18445 | 125.47003 | 281.32 | <.0001 |
| vol_acidity | -1.37875 | 0.09495 | 94.03987 | 210.85 | <.0001 |
| alcohol | 0.31381 | 0.01601 | 171.40529 | 384.31 | <.0001 |

Bounds on condition number: 1.0427, 4.1707

Forward Selection: Step 3

Variable sulphates Entered: R-Square = 0.3359 and C(p) = 60.0833

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 3 | 350.04487 | 116.68162 | 268.89 | <.0001 |
| Error | 1595 | 692.12024 | 0.43393 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-------------|--------------------|----------------|------------|---------|--------|
| Intercept | 2.60914 | 0.19563 | 77.19066 | 177.89 | <.0001 |
| vol_acidity | -1.21712 | 0.09668 | 68.77538 | 158.49 | <.0001 |
| sulphates | 0.67935 | 0.10079 | 19.71221 | 45.43 | <.0001 |
| alcohol | 0.30921 | 0.01580 | 166.10533 | 382.79 | <.0001 |

Bounds on condition number: 1.111, 9.6919

Forward Selection: Step 4

Variable total_sulfur Entered: R-Square = 0.3438 and C(p) = 42.4337

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 4 | 358.28179 | 89.57045 | 208.77 | <.0001 |
| Error | 1594 | 683.88331 | 0.42904 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|--------------|--------------------|----------------|------------|---------|--------|
| Intercept | 2.82456 | 0.20064 | 85.03112 | 198.19 | <.0001 |
| vol_acidity | -1.19449 | 0.09627 | 66.05144 | 153.95 | <.0001 |
| total_sulfur | -0.00224 | 0.00051076 | 8.23693 | 19.20 | <.0001 |
| sulphates | 0.71245 | 0.10051 | 21.55750 | 50.25 | <.0001 |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|----------|--------------------|----------------|------------|---------|--------|
| alcohol | 0.29529 | 0.01603 | 145.52567 | 339.19 | <.0001 |

Bounds on condition number: 1.1142, 17.337

Forward Selection: Step 5

Variable chlorides Entered: R-Square = 0.3520 and C(p) = 23.9903

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 5 | 366.85151 | 73.37030 | 173.07 | <.0001 |
| Error | 1593 | 675.31359 | 0.42393 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|--------------|--------------------|----------------|------------|---------|--------|
| Intercept | 3.00981 | 0.20365 | 92.59849 | 218.43 | <.0001 |
| vol_acidity | -1.13579 | 0.09658 | 58.62706 | 138.30 | <.0001 |
| chlorides | -1.75580 | 0.39051 | 8.56972 | 20.22 | <.0001 |
| total_sulfur | -0.00232 | 0.00050804 | 8.83789 | 20.85 | <.0001 |
| sulphates | 0.92016 | 0.11007 | 29.62549 | 69.88 | <.0001 |
| alcohol | 0.27659 | 0.01647 | 119.53606 | 281.97 | <.0001 |

Bounds on condition number: 1.3123, 29.688

Forward Selection: Step 6

Variable pH Entered: R-Square = 0.3578 and C(p) = 11.6590

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 6 | 372.85906 | 62.14318 | 147.81 | <.0001 |
| Error | 1592 | 669.30605 | 0.42042 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|--------------|--------------------|----------------|------------|---------|--------|
| Intercept | 4.30995 | 0.39928 | 48.98620 | 116.52 | <.0001 |
| vol_acidity | -1.03187 | 0.10003 | 44.73448 | 106.40 | <.0001 |
| chlorides | -2.05284 | 0.39675 | 11.25507 | 26.77 | <.0001 |
| total_sulfur | -0.00238 | 0.00050621 | 9.31856 | 22.16 | <.0001 |
| pH | -0.43827 | 0.11594 | 6.00755 | 14.29 | 0.0002 |
| sulphates | 0.89328 | 0.10985 | 27.80237 | 66.13 | <.0001 |
| alcohol | 0.29029 | 0.01680 | 125.54249 | 298.61 | <.0001 |

Bounds on condition number: 1.3282, 44.182

Forward Selection: Step 7

Variable free_sulfur Entered: R-Square = 0.3600 and C(p) = 8.0000

| Analysis of Variance | | | | | |
|----------------------|----|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 7 | 375.23126 | 53.60447 | 127.88 | <.0001 |

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Error | 1591 | 666.93384 | 0.41919 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|--------------|--------------------|----------------|------------|---------|--------|
| Intercept | 4.44319 | 0.40261 | 51.05423 | 121.79 | <.0001 |
| vol_acidity | -1.00664 | 0.10045 | 42.09899 | 100.43 | <.0001 |
| chlorides | -2.06652 | 0.39622 | 11.40313 | 27.20 | <.0001 |
| free_sulfur | 0.00505 | 0.00212 | 2.37220 | 5.66 | 0.0175 |
| total_sulfur | -0.00349 | 0.00068647 | 10.82327 | 25.82 | <.0001 |
| pH | -0.48543 | 0.11746 | 7.16007 | 17.08 | <.0001 |
| sulphates | 0.88709 | 0.10972 | 27.40348 | 65.37 | <.0001 |
| alcohol | 0.28894 | 0.01678 | 124.23885 | 296.38 | <.0001 |

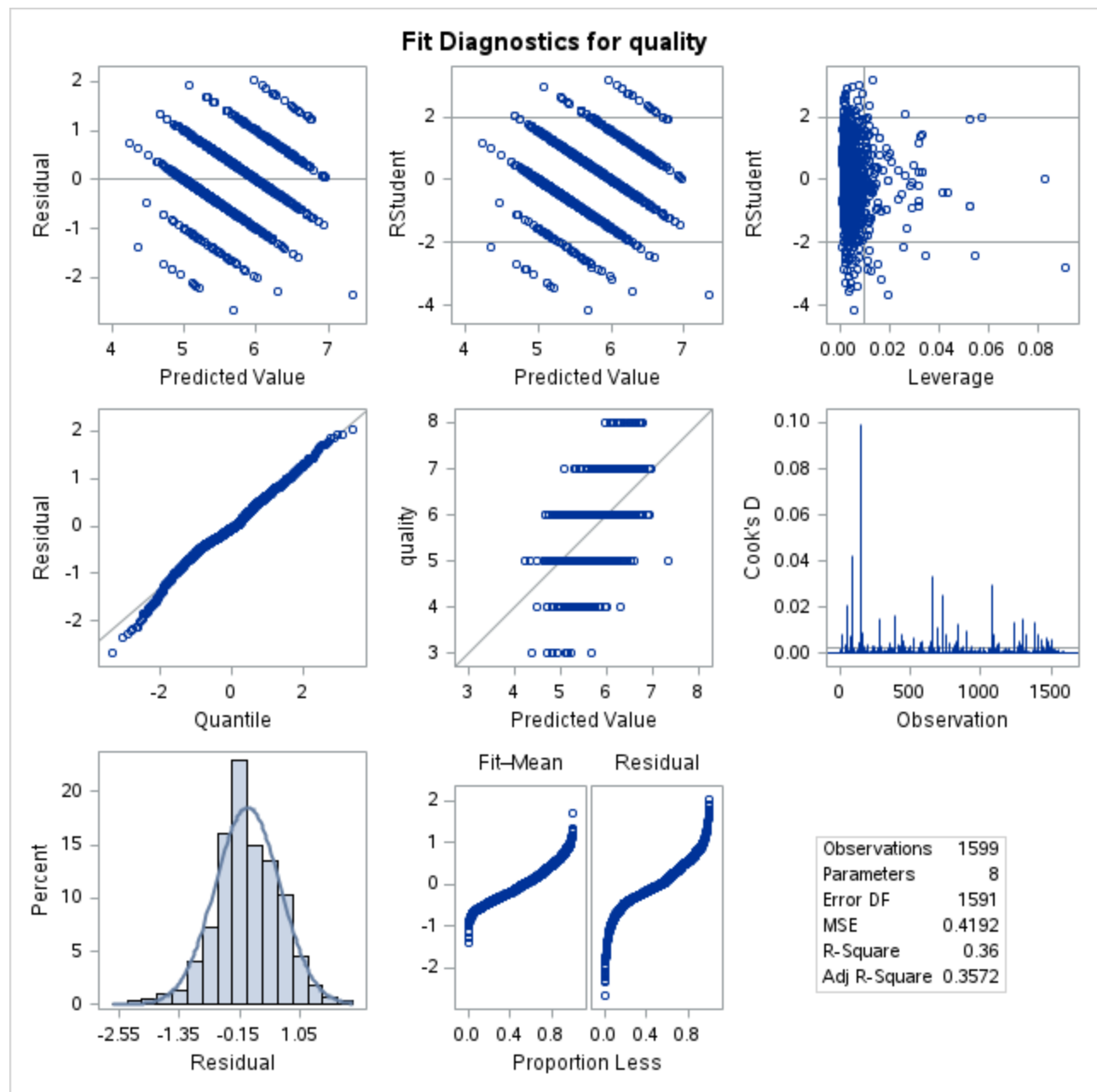
Bounds on condition number: 1.9439, 71.318

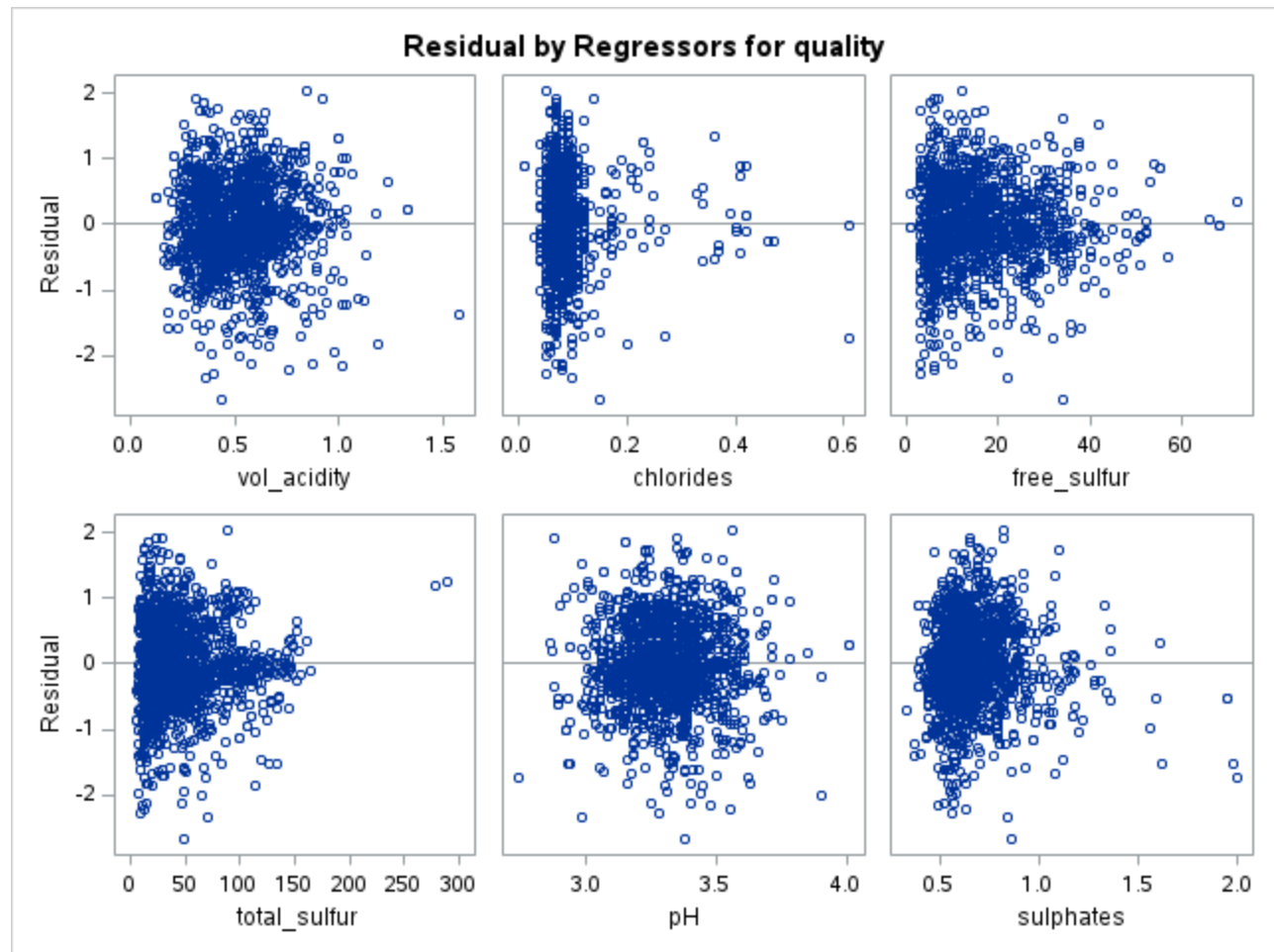
All variables have been entered into the model.

| Summary of Forward Selection | | | | | | | |
|------------------------------|------------------|----------------|------------------|----------------|---------|---------|--------|
| Step | Variable Entered | Number Vars In | Partial R-Square | Model R-Square | C(p) | F Value | Pr > F |
| 1 | alcohol | 1 | 0.2267 | 0.2267 | 327.444 | 468.26 | <.0001 |
| 2 | vol_acidity | 2 | 0.0902 | 0.3170 | 105.108 | 210.85 | <.0001 |
| 3 | sulphates | 3 | 0.0189 | 0.3359 | 60.0833 | 45.43 | <.0001 |
| 4 | total_sulfur | 4 | 0.0079 | 0.3438 | 42.4337 | 19.20 | <.0001 |
| 5 | chlorides | 5 | 0.0082 | 0.3520 | 23.9903 | 20.22 | <.0001 |
| 6 | pH | 6 | 0.0058 | 0.3578 | 11.6590 | 14.29 | 0.0002 |
| 7 | free_sulfur | 7 | 0.0023 | 0.3600 | 8.0000 | 5.66 | 0.0175 |

Forward Selection

The REG Procedure
Model: MODEL1
Dependent Variable: quality







Backward Selection

The REG Procedure
Model: MODEL1
Dependent Variable: quality

| | |
|-----------------------------|------|
| Number of Observations Read | 1599 |
| Number of Observations Used | 1599 |

Backward Elimination: Step 0

All Variables Entered: R-Square = 0.3600 and C(p) = 8.0000

| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 7 | 375.23126 | 53.60447 | 127.88 | <.0001 |
| Error | 1591 | 666.93384 | 0.41919 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|-------------|--------------------|----------------|------------|---------|--------|
| Intercept | 4.44319 | 0.40261 | 51.05423 | 121.79 | <.0001 |
| vol_acidity | -1.00664 | 0.10045 | 42.09899 | 100.43 | <.0001 |
| chlorides | -2.06652 | 0.39622 | 11.40313 | 27.20 | <.0001 |
| free_sulfur | 0.00505 | 0.00212 | 2.37220 | 5.66 | 0.0175 |

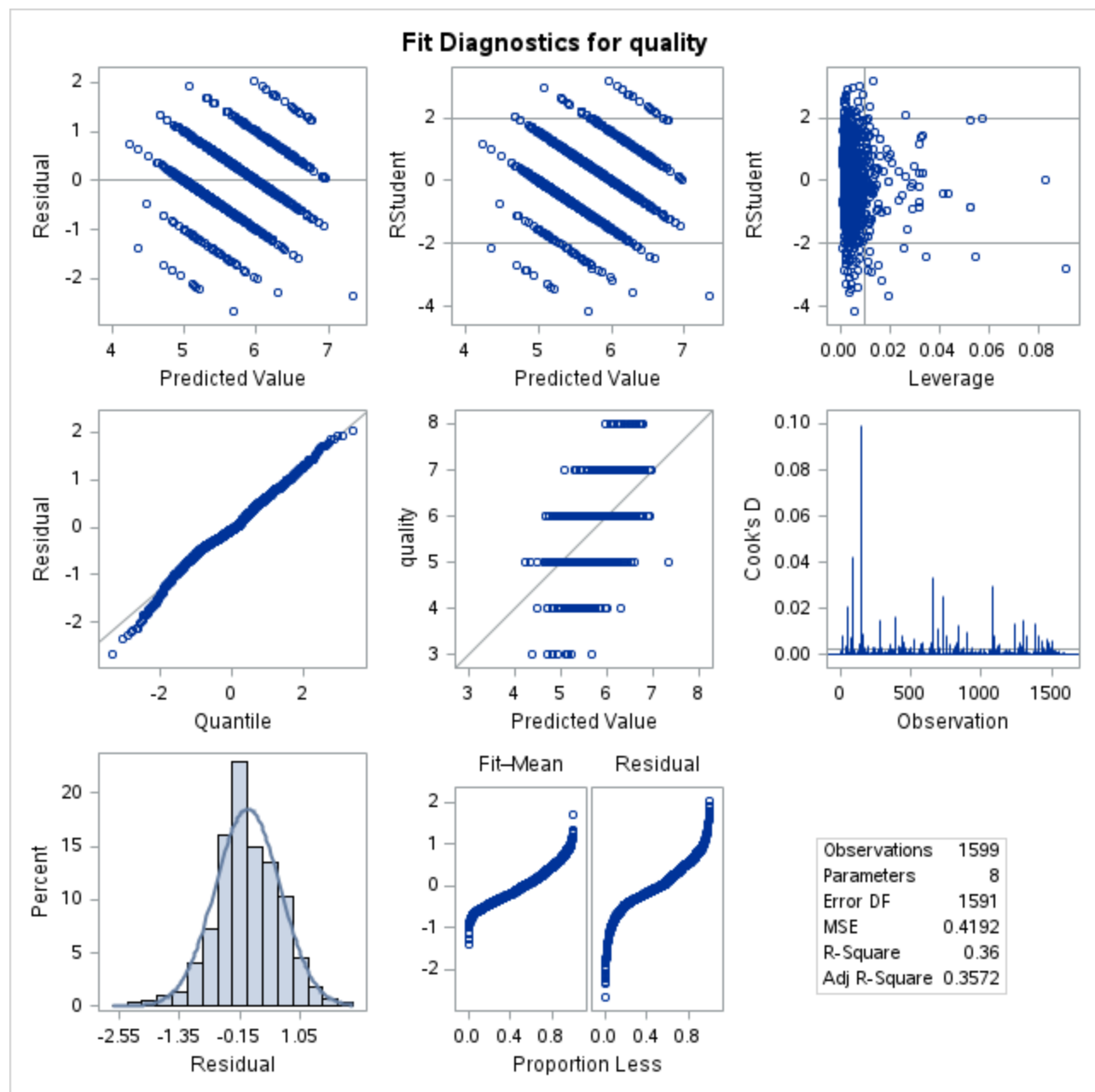
| Variable | Parameter Estimate | Standard Error | Type II SS | F Value | Pr > F |
|--------------|--------------------|----------------|------------|---------|--------|
| total_sulfur | -0.00349 | 0.00068647 | 10.82327 | 25.82 | <.0001 |
| pH | -0.48543 | 0.11746 | 7.16007 | 17.08 | <.0001 |
| sulphates | 0.88709 | 0.10972 | 27.40348 | 65.37 | <.0001 |
| alcohol | 0.28894 | 0.01678 | 124.23885 | 296.38 | <.0001 |

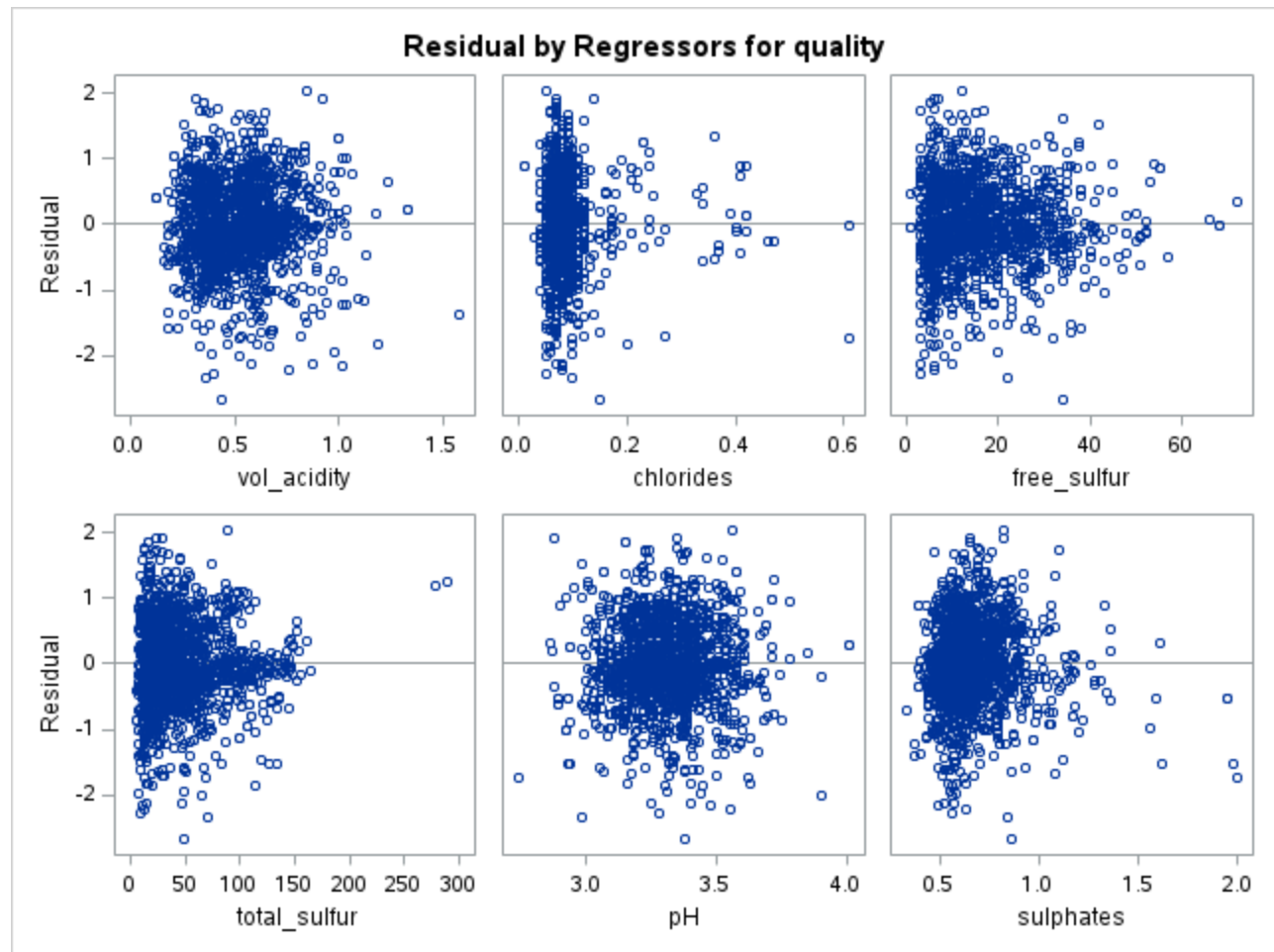
Bounds on condition number: 1.9439, 71.318

All variables left in the model are significant at the 0.1000 level.

Backward Selection

The REG Procedure
Model: MODEL1
Dependent Variable: quality







Lasso procedure

The GLMSELECT Procedure

| | |
|----------------------------------|-----------|
| Data Set | WORK.WINE |
| Dependent Variable | quality |
| Selection Method | LASSO |
| Stop Criterion | SBC |
| Effect Hierarchy Enforced | None |

| | |
|------------------------------------|------|
| Number of Observations Read | 1599 |
| Number of Observations Used | 1599 |

| Dimensions | |
|-----------------------------|---|
| Number of Effects | 8 |
| Number of Parameters | 8 |

Lasso procedure

The GLMSELECT Procedure

| LASSO Selection Summary | | | | |
|-------------------------|----------------|----------------|-------------------|-----|
| Step | Effect Entered | Effect Removed | Number Effects In | SBC |

| LASSO Selection Summary | | | | |
|------------------------------|----------------|----------------|-------------------|-------------|
| Step | Effect Entered | Effect Removed | Number Effects In | SBC |
| 0 | Intercept | | 1 | -677.1197 |
| 1 | alcohol | | 2 | -821.8272 |
| 2 | vol_acidity | | 3 | -1139.7754 |
| 3 | sulphates | | 4 | -1251.2703 |
| 4 | total_sulfur | | 5 | -1283.2733 |
| 5 | chlorides | | 6 | -1292.6707 |
| 6 | pH | | 7 | -1334.7959 |
| 7 | free_sulfur | | 8 | -1339.2171* |
| * Optimal Value of Criterion | | | | |

Selection stopped because all effects are in the final model.

Lasso procedure

The GLMSELECT Procedure Selected Model

The selected model is the model at the last step (Step 7).

Effects: Intercept vol_acidity chlorides free_sulfur total_sulfur pH sulphates alcohol

| Analysis of Variance | | | | |
|----------------------|------|----------------|-------------|---------|
| Source | DF | Sum of Squares | Mean Square | F Value |
| Model | 7 | 375.23126 | 53.60447 | 127.88 |
| Error | 1591 | 666.93384 | 0.41919 | |
| Corrected Total | 1598 | 1042.16510 | | |

| | |
|----------------|-------------|
| Root MSE | 0.64745 |
| Dependent Mean | 5.63602 |
| R-Square | 0.3600 |
| Adj R-Sq | 0.3572 |
| AIC | 218.76587 |
| AICC | 218.87915 |
| SBC | -1339.21706 |

| Parameter Estimates | | |
|---------------------|----|-----------|
| Parameter | DF | Estimate |
| Intercept | 1 | 4.443192 |
| vol_acidity | 1 | -1.006636 |
| chlorides | 1 | -2.066517 |
| free_sulfur | 1 | 0.005054 |
| total_sulfur | 1 | -0.003488 |
| pH | 1 | -0.485430 |
| sulphates | 1 | 0.887095 |
| alcohol | 1 | 0.288944 |

Ridge procedure

The REG Procedure
 Model: MODEL1
 Dependent Variable: quality

| | |
|-----------------------------|------|
| Number of Observations Read | 1599 |
| Number of Observations Used | 1599 |

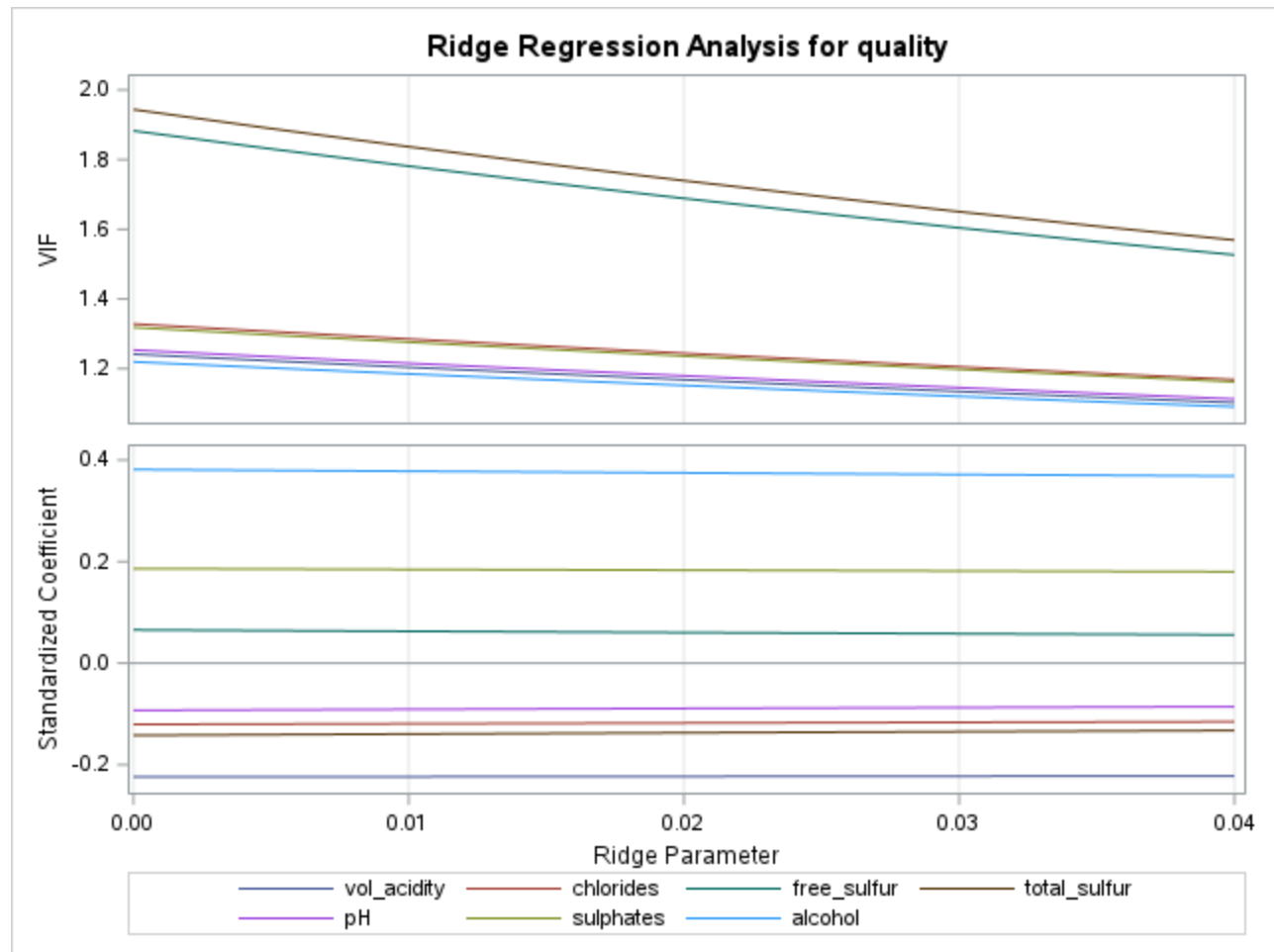
| Analysis of Variance | | | | | |
|----------------------|------|----------------|-------------|---------|--------|
| Source | DF | Sum of Squares | Mean Square | F Value | Pr > F |
| Model | 7 | 375.23126 | 53.60447 | 127.88 | <.0001 |
| Error | 1591 | 666.93384 | 0.41919 | | |
| Corrected Total | 1598 | 1042.16510 | | | |

| | | | |
|----------------|----------|----------|--------|
| Root MSE | 0.64745 | R-Square | 0.3600 |
| Dependent Mean | 5.63602 | Adj R-Sq | 0.3572 |
| Coeff Var | 11.48771 | | |

| Parameter Estimates | | | | | |
|---------------------|----|--------------------|----------------|---------|---------|
| Variable | DF | Parameter Estimate | Standard Error | t Value | Pr > t |
| Intercept | 1 | 4.44319 | 0.40261 | 11.04 | <.0001 |
| vol_acidity | 1 | -1.00664 | 0.10045 | -10.02 | <.0001 |
| chlorides | 1 | -2.06652 | 0.39622 | -5.22 | <.0001 |
| free_sulfur | 1 | 0.00505 | 0.00212 | 2.38 | 0.0175 |
| total_sulfur | 1 | -0.00349 | 0.00068647 | -5.08 | <.0001 |
| pH | 1 | -0.48543 | 0.11746 | -4.13 | <.0001 |
| sulphates | 1 | 0.88709 | 0.10972 | 8.09 | <.0001 |
| alcohol | 1 | 0.28894 | 0.01678 | 17.22 | <.0001 |

Ridge procedure

The REG Procedure
 Model: MODEL1
 Dependent Variable: quality



Ridge procedure

The REG Procedure
Model: MODEL1
Dependent Variable: quality

