

Department of Electronic Engineering Assessments 2018/19

ELE00030I

Digital Design with HDL Final Project

Implementation of a Parameterizable Matrix Multiplication System VHDL_Project_Y3843738-Y3843317.pdf

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Question Answers

Question 1 (Datapath)

What is the maximum width (in terms of bits) of the coefficients of C and which generics are relevant?

The maximum size of the output bus (OutputSize) and width of the RAM will be determined by the largest possible negative number that can be generated from the signed binary numbers within the ROMs. This would come from the maximum negative number being multiplied by the maximum positive number M times.

For example, in with a data width of **4-bit Signed** using matrices of dimensions A = 2x3 and B = 3x2:

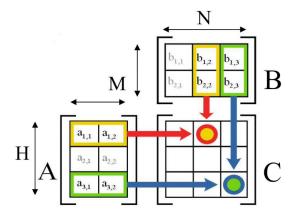


Figure 1 - Multiplying two matrices (Tempesti, 2018)

If A(1,1) and A(1,2) = -8

Along with B(1,2) and B(2,2) = 7

C (Red Circle) would be the largest negative number: -112

If A(3,1), A(3,2), B(1,3) and B(2,3) = -8

C (Blue Circle) would be the largest positive number: 128

The largest number is therefore calculated using this equation:

$$(M\times 2^{2\times (DataSize-1)})$$

The size function is used. Provided in the DigEng package, this returns the number of bits required to express exactly that value. E.g. To express the number 16, 5-bits is necessary. So the equation becomes:

$$Size(M \times 2^{2 \times (DataSize-1)})$$

Then since the output is a signed value an extra bit must be added to account for this:

$$OutputSize = Size(M \times 2^{2 \times (DataSize - 1)}) + 1$$

Question 2 (Datapath)

What is the width and depth of the memories that store A, B, and C, as a function of M, N, H? From Figure 1 we can also work out the depth of the memories.

The depth of A will be: $M \times H$

The depth of B will be: $M \times N$

The depth of C will be: $N \times H$

Given the previous example in Figure 1, A will be: $2 \times 3 = 6$, B will be: $2 \times 3 = 6$ and C will be: $3 \times 3 = 9$.

The width of both A and B will be pre-determined based on the ROMs being used, and the value assigned to dataSize. Output buses from the ROMs will therefore be: (data size - 1 downto 0);

The width of C (the RAM) will be: (output size - 1 downto 0);

What is then the width of the address bus for each of the memories as a function of M, N, H?

The width of the address bus for each memory will be the ceiling of the \log_2 function of their depths.

The address bus for ROM_A: $\log_2(M \times H)$

The address bus for ROM_B: $\log_2(M \times N)$

The address bus for RAM will be: $log_2(H \times N)$

What are the input matrices that you will use to test the system?

The testing of the Matrix Multiplier was done using the following generics M = 3, N = 5, and H = 4 and dataSize = 5.

This tested the maximum positive and negative numbers possible, along with zero output and further values to confirm correct functionality.

The below matrices were generated using MATLAB.

```
>> A = [-16, -16, -16; 4, 5, 6; 7, 8, 9; 10, 11, 12]
A =
       -16
  -16
            -16
    4
        5
             6
    7
         8
              9
        11
             12
   10
>> B = [-16, 15, 0, 4, 5; -16, 15, 0, 9, 10; -16, 15, 0, 14, 15]
B =
                   4
  -16
       15 0
                        5
  -16
        15
             0
                  9
                        10
        15
             0
  -16
                  14
>> A*B
ans =
  768 -720
             0 -432 -480
 -240
      225
              0
                145
                       160
 -384 360
              0 226
                       250
 -528 495
             0
                  307
                       340
```

Figure 2 - MATLAB generated input and output matrices.

First, second and third output are largest positive, largest negative and zero respectively.

Question 3 (Control Logic)

How are the counters used for address generation related to each other?

The M counter will increment up to its maximum value. At this point the N counter will increment and the M counter will count over back to zero. The N counter will continue to do this until it reaches its maximum value. The H counter will then be incremented when both M and N counters reach their maximum value. Both M and N will count over back to zero.

This provides the coordinates for all matrix multiplications. However, this is not how the coefficients are stored in the ROM and combinational logic is needed to address them.

When should each counter reset to 0 (beyond the global reset)?

The counters will reset to zero as they roll over their maximum value.

What are the sizes (widths) of the counters?

The M counter will be a function of M it will count from 0 to M-1

The N counter will be a function of N it will count from 0 to N-1

The H counter will be a function of H it will count from 0 to H-1

How are the addresses computed from the counter values?

Due to storing all the arrays row first in the ROMs, addressing the ROM using only the counters would not work. Combinational logic is therefore used as follows.

Address for ROM A: $Generic_M \times Count_H + Count_M$

This is incrementing through the columns in the Matrix A shown in Figure 1 based on the M Counter and working down the row depending on the H counters value. The H counter value is multiplied by the size of the generic M which increments down H number of rows, or H rows worth of memory locations within the ROM.

Address for ROM B: $Generic_N \times Count_M + Count_N$

This is incrementing through the columns in the Matrix B shown in Figure 1 based on the N Counter and working along the rows depending on the M counters value. The M counter value is multiplied by the size of the generic N which increments down M rows, or M rows worth of memory locations within the ROM.

Address for RAM: $Generic_N \times Count_H + Count_N$

This increments down through the RAM in sequential order but based on the values of the counters H and N. N is only incremented as a full coefficient is calculated and cycles through the columns of the output matrix C in Figure 1. H * N increments the memory location over an H number of rows of the output matrix C.

Question 4 (Control Logic / FSM)

What is the behaviour of the state machine?

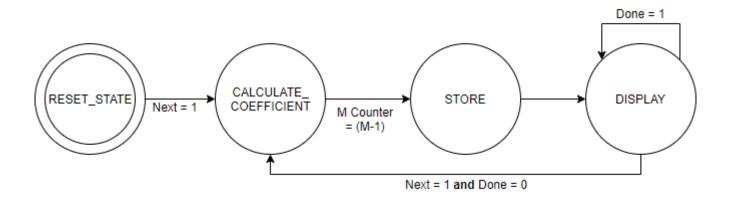


Figure 3 - Mealy state transition diagram

	1			
RESET_STATE	In this state everything is reset, the MACC and counters are disabled.			
	MACC_RST is held high removing any previous value. When the user			
	presses NXT, the state goes to CALCULATE_COEFFICIENT.			
CALCULATE_COEFFICIENT	In this state the M Counter is enabled. This updates the ROM			
	addresses via combinational logic. MACC is enabled. Keeps			
	incrementing counters and generating addresses for ROM's until			
	count_M = Matrix_Common – 1. Then moves to STORE state.			
STORE	In this state only write_EN is high. All other control signals are low.			
	The address of the RAM is calculated via combinational logic. The			
	value of the MACC is stored into this location. Always moves to			
	DISPLAY state.			
DISPLAY	In this state the output is displayed and the circuit waits for an input			
	from the user. The N Counter is enabled when the user presses NXT if			
	the done signal is low. The H counter is enabled based on the user			
	pressing NXT and the done signal being low and the values of N and			
	M counters. Write_EN and MACC_EN are both low. MACC_RST is high			
	to remove the previous value. If done = 0, returns to			
	CALCULATE_COEFFICIENT state, else remains in DISPLAY until RST.			

What are the control signals for the memories, the MACC unit, and the counters as a function of each state?

State	CNT_EN_M	CNT_EN_N	CNT_EN_H	MACC_RST	MACC_EN	Write_EN
RESET_STATE	0	0	0	1	0	0
CALCULATE_COEFFICIENT	Count_M < Matrix_Common- 1	0	0	0	1	0
STORE	0	0	0	0	0	1
DISPLAY	Done = 0 and NXT = 1	Done = 0 and NXT = 1	Done = 0 and NXT = 1 and Count_M = Matrix_ Common - 1 and Count_N = Matrix_B_Width - 1	1	0	0

VHDL Code

Top Level Matrix_Multiplier

```
-- Company: University of York
-- Engineer: James Gardner
-- Create Date: 21/11/2018

-- Design Name: Parameterizable Matrix-Multiplier

-- Module Name: Matrix-Multiplier
-- Project Name: Final Project
-- Tool versions: Any (tested on ISE 2017.4)
-- Description:
-- A fully parameterizable matrix-multiplier, multiplies two pre-defined
-- ROMs and stores the output in a parameterizable RAM.
-- Dependencies:
-- Requires DigEng.vhd package
-- Additional Comments:
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
use work.DigEng.ALL;
-- This is the top-level component of the parameterizable matrix-multiplier.
-- It generates to debouncers for user inputs and connects the control-logic to
-- the datapath.
entity Matrix Multiplier is
    -- The generics state the size of each matrix to be multiplied.
    Generic ( data_size : integer := 5; -- Number of bits per coefficient of the
                                         -- input matrices
          Matrix_A_Height : integer := 4; -- {H} The number of rows within input
                                           -- matrix A
          Matrix B Width : integer := 5; -- {N} The number of columns within input
                                          -- matrix B
          Matrix_Common : integer := 3); -- {M} The number of columns within input
                                          -- matrix A and number of rows within
                                          -- input matrix B
    Port ( CLK : in STD LOGIC; -- Global clock input
           RST : in STD LOGIC; -- User input debounced Reset
           NXT : in STD LOGIC; -- User input debounced Next
           -- The size of the output buss is determined by the maximum value
           -- possible to represent using a binary number of data size wide
           -- multiplied by itself Matrix Common times.
           Output : out SIGNED ((size (Matrix Common *
                               ((2**(data size - 1))**2))) downto 0));
end Matrix Multiplier;
architecture Behavioral of Matrix Multiplier is
signal deb rst, deb nxt : STD LOGIC; -- debounced reset and "next" signals
-- Address sizes of both ROMs determined by the log2 function of generic variables
signal Address ROM A : UNSIGNED (log2 (Matrix A Height*Matrix Common) -1 downto 0);
signal Address ROM B : UNSIGNED (log2 (Matrix B Width*Matrix Common) -1 downto 0);
signal MACC RST: STD LOGIC; -- Reset output of multiply-accumulate unit to zero
signal MACC EN : STD LOGIC; -- Enable of multiply-accumulate unit
-- Address size of RAM determined by the log2 function of generic variables
signal Address RAM : UNSIGNED(log2 (Matrix A Height*Matrix B Width) -1 downto 0);
signal Write EN : STD LOGIC; -- Enabling writing to the RAM
```

```
-- The size of the output bus is determined by the maximum value possible to
-- represent using a binary number of data size wide multiplied by itself
-- Matrix Common times. Here it is declared as a constant to be used throughout
-- other components.
constant output_size : integer := size(Matrix_Common * ((2**(data_size - 1))**2))+1;
begin
-- Debouncer for "RST" signal
Rst_Debouncer: entity work.Debouncer
    PORT MAP ( CLK => CLK,
              Sig => RST,
              Deb Sig => deb_rst);
-- Debouncer for "NXT" signal
Next Debouncer: entity work. Debouncer
    PORT MAP ( CLK => CLK,
              Sig => NXT,
              Deb Sig => deb nxt);
-- Connecting the generics and ports for the control and the datapath.
Control: entity work.Control
    GENERIC MAP ( data size => data size,
                  Matrix A Height => Matrix A Height,
                  Matrix B Width => Matrix B Width,
                  Matrix Common => Matrix Common)
    PORT MAP ( CLK => CLK,
               RST => deb rst,
               NXT => deb nxt,
               Address ROM A => Address ROM A,
               Address ROM B => Address ROM B,
               MACC_RST => MACC RST,
               MACC EN => MACC EN,
               Address RAM => Address RAM,
               Write EN => Write EN);
Datapath: entity work.Datapath
    GENERIC MAP ( data size => data_size,
                  Matrix A Height => Matrix A Height,
                  Matrix B Width => Matrix B Width,
                  Matrix Common => Matrix Common,
                  output size => output size)
    PORT MAP ( CLK => CLK,
               Address ROM A => Address_ROM_A,
               Address ROM B => Address ROM B,
               MACC RST => MACC RST,
               MACC EN => MACC EN,
               Address RAM => Address RAM,
               Write EN => Write EN,
               Output => Output);
end Behavioral;
```

Datapath

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
use work.DigEng.ALL;
-- This is datapath of the parameterizable matrix-multiplier.
-- It connects the ROMs, MACC and RAM together.
-- It contains the combinational logic of the MACC containing:
-- the multiplication, addition and registers.
entity Datapath is -- The generics state the size of each matrix to be multiplied.
    Generic ( data size : integer := 5; -- Number of bits per coefficient of the
                                         -- input matrices
              Matrix A Height: integer:= 4; -- {H} The number of rows within input
                                              -- matrix A
              Matrix B Width : integer := 5; -- {N} The number of columns within
                                             -- input matrix B
              Matrix Common : integer := 3; -- {M} The number of columns within
                                            -- input matrix A and number of rows
                                            -- within input matrix B
              output_size : integer := 7); -- The number of bits per coefficient of
                                           -- the output matrix
    Port ( CLK : in STD LOGIC; -- Global clock input
           -- Address sizes of both ROMs determined by the log2 function of generic
           -- variables
           Address ROM A : in UNSIGNED (log2 (Matrix A Height*Matrix Common) -1
                                        downto 0);
           Address ROM B : in UNSIGNED (log2 (Matrix B Width*Matrix Common) -1
                                        downto ();
           MACC RST : in STD LOGIC; -- Reset output of multiply-accumulate unit to
                                    -- zero
           MACC EN : in STD LOGIC; -- Enable of multiply-accumulate unit
           -- Address size of RAM determined by the log2 function of generic
           -- variables
           Address RAM : in UNSIGNED (log2 (Matrix A Height*Matrix B Width) -1
                                      downto ();
           Write EN : in STD LOGIC; -- Enabling writing to the RAM
           Output : out SIGNED (output size -1 downto 0)); -- The output of the RAM
end Datapath;
architecture Behavioral of Datapath is
-- Internal ROM outputs (data size)-Bit data buses
signal ROM_A_Data_out, ROM_B_Data_out : SIGNED (data_size - 1 downto 0);
-- Internal output of MACC, size of bus is determined by largest
-- possible output of the two signed inputs.
signal MACC_Data_out : SIGNED (output_size - 1 downto 0);
begin
-- Multiply-accumulate unit (MACC) consists of a multiplier coupled
-- with an adder that accumulates the results by adding together the results of
-- the multiplication. Calculates data to be written to RAM.
MACC: process (CLK)
begin
   if (rising edge(CLK)) then
      if (MACC RST = '1') then -- synchronous reset
         MACC Data out <= (others => '0'); -- Sets output to 0
      elsif (MACC EN = '1') then -- Enable signal
        -- Combinational logic for multiply-accumulate unit
        MACC_Data_out <= (ROM_A_Data_out * ROM_B_Data_out) + MACC_Data_out;</pre>
      end if;
   end if;
```

```
end process MACC;
-- Declaring the two ROMs and RAM
ROM_A: entity work.Async_ROM_12x5
    PORT MAP( Address => Address_ROM_A,
              DataOut => ROM_A_Data_out);
ROM_B: entity work.Async_ROM_15x5
    PORT MAP( Address => Address_ROM_B,
              DataOut => ROM_B_Data_out);
RAM: entity work.Param RAM
    GENERIC MAP ( Width => output size,
                 -- The size of the RAM is determined by the generics
                 Depth => Matrix A Height*Matrix B Width)
    PORT MAP ( CLK => CLK,
              Write EN => Write EN,
              Data In => MACC Data out,
              Address => Address RAM,
              Data Out => Output);
end Behavioral;
```

Control

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
use work.DigEng.ALL;
-- This is the control component for a fully parameterizable Matrix-Multiplier.
-- It contains a Mealy finite state machine,
-- combinational logic for the ROM/RAM addresses and counters.
entity Control is -- The generics state the size of each matrix to be multiplied.
    Generic ( data_size : integer := 5; -- Number of bits per coefficient of the
                                         -- input matrices
          Matrix A Height: integer:= 4; -- {H} The number of rows within input
                                          -- matrix A
          Matrix B Width : integer := 5; -- {N} The number of columns within input
                                         -- matrix B
          Matrix_Common : integer := 3); -- {M} The number of columns within input
                                         -- matrix A and number of rows within
                                         -- input matrix B
    Port ( CLK : in STD LOGIC; -- Global clock input
           RST : in STD LOGIC; -- User input debounced Reset
           NXT : in STD LOGIC; -- User input debounced Next
           -- Address sizes of both ROMs determined by the log2 function of generic
           -- variables
           Address ROM A : out UNSIGNED (log2 (Matrix A Height*Matrix Common) -1
                                         downto 0);
           Address ROM B : out UNSIGNED (log2 (Matrix B Width*Matrix Common) -1
                                         downto ();
           MACC RST : out STD LOGIC; -- Reset output of multiply-accumulate unit to
                                      -- zero
           MACC EN: out STD LOGIC; -- Enable of multiply-accumulate unit
           -- Address size of RAM determined by the log2 function of generic
           -- variables
           Address RAM : out UNSIGNED (log2 (Matrix A Height*Matrix B Width) -1
                                      downto 0);
           Write_EN : out STD_LOGIC); -- Enabling writing to the RAM
end Control;
architecture Behavioral of Control is
    -- Defining a new type that contains all possible states of the FSM.
    type fsm states is (RESET STATE, CALCULATE COEFFICIENT, STORE, DISPLAY);
    -- Creating two new signals of newly created 'fsm states' type.
    signal state, next state: fsm states;
    -- Done is set high after final coefficient calculated.
    -- CNT_EM_M/N/H are the enables of each counter.
    signal done, CNT EN M, CNT EN N, CNT EN H : STD LOGIC;
    -- Internal signals of clocks
    signal count M int : UNSIGNED (log2(Matrix Common)-1 downto 0);
    signal count N int : UNSIGNED (log2(Matrix B Width)-1 downto 0);
    signal count H int : UNSIGNED (log2(Matrix A Height)-1 downto 0);
begin
    -- Declaring the three counters of variable sizes used for addressing
    -- RAM and ROM
    M Counter: entity work.Param Counter
    -- M counters size depends on generic Matrix Common
    GENERIC MAP (LIMIT => Matrix Common)
    PORT MAP ( CLK => CLK,
              RST => RST,
              EN \Longrightarrow CNT EN M,
              Count Out => count M int);
```

```
N Counter: entity work.Param Counter
-- N counters size depends on generic Matrix B Width
GENERIC MAP (LIMIT => Matrix B Width)
PORT MAP ( CLK => CLK,
          RST => RST,
          EN => CNT_EN_N,
          Count Out => count N int);
H Counter: entity work.Param Counter
-- H counters size depends on generic Matrix A Height
GENERIC MAP (LIMIT => Matrix A Height)
PORT MAP ( CLK => CLK,
          RST => RST,
          EN => CNT EN H,
          Count Out => count H int);
-- This is the process for the state register
state assignment: process (CLK) is
begin
 if rising edge (CLK) then
    if (RST = '1') then
        -- RESET STATE is the reset state
        state <= RESET STATE;</pre>
    else
        -- If reset is not pressed state gets next state
        state <= next state;</pre>
    end if;
end if;
end process state_assignment;
-- This is the process for the state transitions
transitions: process (state, NXT, done, count M int) is
begin
    case state is
       when RESET STATE =>
       -- STATE DESCRIPTION
       -- Remains idle in this state until NXT is pressed
       -- Everything initially set to 0.
           if NXT = '1' then
                next_state <= CALCULATE_COEFFICIENT;</pre>
           else
               next state <= state;</pre>
           end if;
       when CALCULATE COEFFICIENT =>
       -- STATE DESCRIPTION
       -- Cycles through ROMs, calculating one full
       -- coefficient of the output matrix.
           if count M int = Matrix Common-1 then
               next state <= STORE;</pre>
           else
               next state <= state;</pre>
           end if;
       when STORE =>
       -- STATE DESCRIPTION
       -- Writes the calculated coefficient to the RAM
           next state <= DISPLAY;</pre>
       when DISPLAY =>
       -- STATE DESCRIPTION
       -- Displays the output of current coefficient calculated.
       -- Remains in this state until user presses NXT if not
       -- done. Else remains until RST.
           if NXT = '1' and done = '0' then
```

```
next state <= CALCULATE COEFFICIENT;</pre>
               else
                   next state <= state;</pre>
               end if;
       end case;
   end process transitions;
-- Below is all the combinational logic determining the control signals.
-- They are based on current states, counter outputs and user inputs.
-- Done is the flag for the final coefficient being calculated.
-- Based on when all counters have reached their maximum values.
done <= '1' when count M int = Matrix Common-1</pre>
            and count N int = Matrix B Width-1
            and count H int = Matrix A Height-1
            else '0';
-- Causes M Counter to count to its maximum value every time the state is
-- CALCULATE COEFFICIENT Is then incremented back to start value when NXT is pressed
-- and state is DISPLAY.
CNT EN M <= '1' when state = CALCULATE COEFFICIENT and count M int < Matrix Common-1
                else '1' when state = DISPLAY and done = '0' and NXT = '1'
                else '0';
-- Controlled by the user pressing NXT when in DISPLAY state.
CNT EN N <= '1' when state = DISPLAY and done = '0' and NXT = '1'
                else '0';
-- Controlled by the user pressing NXT when in DISPLAY state and
-- when other two counters are at maximum value.
CNT EN H <= '1' when state = DISPLAY and done = '0' and NXT = '1'
                and count M int = Matrix_Common-1
                and count N int = Matrix B Width-1
                else '0';
-- Used to remove previous data from the MACC output.
-- Needed prior to each new coefficient calculated or in RST.
MACC RST <= '1' when state = RESET_STATE
                else '1' when state = DISPLAY
                else '0';
-- Enabling MACC to calculate values. Only in state CALCULATE COEFFICIENT
MACC EN <= '1' when state = CALCULATE COEFFICIENT
               else '0';
-- Enabling writing of data to RAM, only in STORE state.
Write EN <= '1' when state = STORE
                else '0';
-- All below address buses are calculated through combinational logic.
-- As a function of counters and generic values.
-- Combinational logic of RAM
Address RAM <= RESIZE(((TO_UNSIGNED(Matrix B Width,
log2(Matrix B Width)))*count H int) + count N int,
log2 (Matrix_A_Height*Matrix_B_Width));
-- Combinational logic for addresses of A and B ROM
Address ROM A <= RESIZE(((TO_UNSIGNED(Matrix_Common,
log2(Matrix Common)))*count H int) + count M int,
log2 (Matrix A Height*Matrix Common));
Address ROM B <= RESIZE(((TO_UNSIGNED(Matrix B Width,
log2(Matrix B Width)))*count M int) + count N int,
log2 (Matrix B Width*Matrix Common));
end Behavioral;
```

Asynchronous ROM A – Async_ROM_12x5

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
-- This is a ROM component to be used within the Parameterizable Matrix-Multiplier.
-- It is made up of an array of integers for ease of reading. This is converted
-- to signed binary numbers in synthesis.
entity Async ROM 12x5 is
    Port ( Address : in UNSIGNED (3 downto 0);
           DataOut : out SIGNED (4 downto 0));
end Async ROM 12x5;
architecture Behavioral of Async ROM 12x5 is
type ROM Array is array (0 to 11) of integer;
    constant Content: ROM Array := (
        -- This is used as Matrix A. So to test functionality
        -- of the Matrix-Multiplier the first three numbers
        -- are set to -16. This will correspond to values chosen
        -- in the other ROM to test the limits of the design.
        0 \implies -16,
        1 => -16,
        2 => -16,
        3 => 4,
        4 => 5,
        5 => 6,
        6 = > 7,
        7 => 8,
        8 => 9,
        9 \implies 10,
        10 => 11,
        11 => 12,
        others \Rightarrow 0);
begin
        -- Converting the integers used above to signed binary values.
        DataOut <= TO SIGNED (Content (TO INTEGER (Address)), 5);</pre>
end Behavioral:
```

Asynchronous ROM B – Async_ROM_15x5

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
-- This is a ROM component to be used within the Parameterizable Matrix-Multiplier.
-- It is made up of an array of integers for ease of reading. This is converted
-- to signed binary numbers in synthesis.
entity Async ROM 15x5 is
    Port ( Address : in UNSIGNED (3 downto 0);
           DataOut : out SIGNED (4 downto 0));
end Async ROM 15x5;
architecture Behavioral of Async ROM 15x5 is
type ROM Array is array (0 to 14) of integer;
    constant Content: ROM Array := (
        -- This is used as Matrix B. So to test functionality
        -- of the Matrix-Multiplier locations 0, 5 and 10 contain the value
        -- -16. This will correspond to values chosen in the other ROM to
        -- produce the largest positive number possible. Locations 1, 6 and 11
        -- contain 15 to be multiplied with -16 within the other ROM to produce the
        -- largest negative number.
        0 \implies -16,
        1 => 15,
        2 => 0,
        3 => 4,
        4 = 5,
        5 \implies -16
        6 \implies 15,
        7 = > 0,
        8 => 9,
        9 => 10,
        10 \implies -16,
        11 => 15,
        12 => 0,
        13 => 14,
        14 => 15,
        others => 0);
begin
        -- Converting the integers used above to signed binary values.
        DataOut <= TO SIGNED (Content (TO INTEGER (Address)), 5);</pre>
end Behavioral;
```

Parameterizable RAM

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
use work.DigEng.ALL;
-- This is a Synchronous write / asynchronous read parameterizable single-port RAM
entity Param RAM is
    Generic ( Width : integer := 4; -- Datasize in bits
               Depth: integer := 5); -- Matrix A Height * Matrix B Width
    Port ( CLK : in STD LOGIC;
            Write_EN : in STD_LOGIC;
Data_In : in SIGNED (Width -1 downto 0);
Address : in UNSIGNED (log2(Depth) -1 downto 0);
            Data_Out : out SIGNED (Width -1 downto 0));
end Param RAM;
architecture Behavioral of Param RAM is
type ram type is array (0 to Depth -1) of SIGNED(Width -1 downto 0);
signal ram inst: ram type;
begin
  -- Asynchronous read
  Data_Out <= ram_inst(to_integer(Address));</pre>
  -- Synchronous write (write enable signal)
  process (CLK)
  begin
    if (rising edge(CLK)) then
       if (write en='1') then
          ram inst(to integer(Address)) <= Data In;</pre>
       end if;
    end if;
  end process;
end Behavioral;
```

Self-checking VHDL Testbench

```
library IEEE;
use IEEE.STD LOGIC 1164.ALL;
use IEEE.NUMERIC STD.ALL;
use work.DigEng.ALL;
-- This is the test-bench of the Matrix Multiplier. It is a parameterizable,
-- self checking test-bench. It uses a record containing pre-calculated expected
-- outputs and their corresponding output-matrix locations. The test-bench will
-- report when there are errors and also when the circuit works as expected.
entity Matrix Multiplier tb is
end Matrix Multiplier tb;
architecture Behavioral of Matrix Multiplier tb is
constant CLK PERIOD : time := 10 ns; -- Defines the standard clock time
-- Constants that will be remapped to Matrix Multiplier generics
constant data size : integer := 5; -- Number of bits per coefficient of the input
matrices
constant Matrix A Height: integer := 4; -- {H} The number of rows within input
matrix A
constant Matrix B Width : integer := 5; -- {N} The number of columns within input
matrix B
constant Matrix Common : integer := 3; -- {M} The number of columns within input
                                       -- and number of rows withing input matrix B
-- The size of the output buss is determined by the maximum value possible to
represent using a
-- binary number of data size wide multiplied by itself Matrix Common times. Here it
-- declared as a constant to be used throughout other components.
constant output size : integer := (size(Matrix Common * ((2**(data size - 1))**2)))
+1;
signal CLK : STD_LOGIC; -- Global clock input
signal RST : STD LOGIC; -- User input debounced Reset
signal NXT : STD LOGIC; -- User input debounced Next
signal Output : SIGNED (output size -1 downto 0); -- Output of RAM
-- Record declared that contains Column/Row integers used to identify coefficient
-- position within RAM and Output rcd which is pre-calculated expected output of
RAM.
-- These a grouped together under the name output coefficient
type output coefficient is record
    column : integer;
    row : integer;
    output rcd : SIGNED (output size-1 downto 0);
end record;
-- Declaring a type of array made up of the output coefficient type called
-- results array
type results array is array
    (natural range <>) of output coefficient;
-- Creating a results array called results and filling it
-- with a completed output matrix of correct expected outputs
-- and their corresponding positions within that matrix. These
-- were calculated using MatLab. It contains one erroneous output.
constant results : results array := (
```

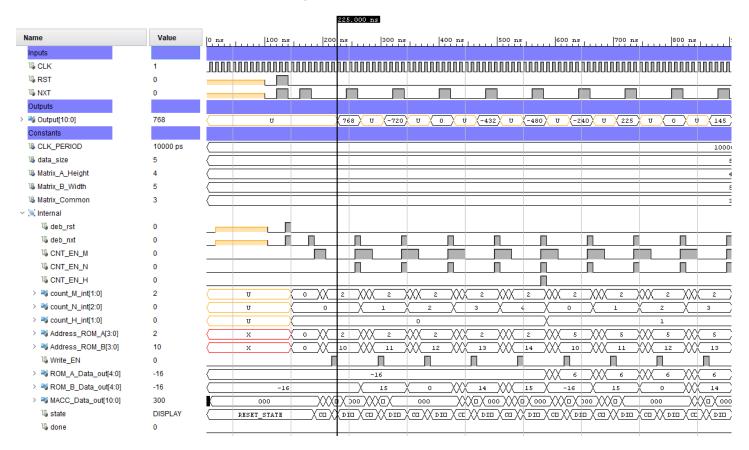
```
-- Column, Row,
                             Output RCD
     -- Testing maximum positive number.
                  0, TO SIGNED (768, output size)),
     -- Testing maximum negative number, uses MSB.
              0, TO SIGNED(-720, output_size)),
     -- Testing 0 output.
                0, TO_SIGNED(0, output size)),
     -- Further sets of inputs to check circuit is operating correctly
              0, TO_SIGNED(-432, output_size)),
     (3,
                    0,
                            TO_SIGNED(-480, output_size)),
     (4,
                           TO_SIGNED(-480, output_size)),
TO_SIGNED(-240, output_size)),
TO_SIGNED(225, output_size)),
TO_SIGNED(0, output_size)),
TO_SIGNED(145, output_size)),
TO_SIGNED(160, output_size)),
TO_SIGNED(-384, output_size)),
TO_SIGNED(360, output_size)),
TO_SIGNED(0, output_size)),
TO_SIGNED(226, output_size)),
TO_SIGNED(250, output_size)),
TO_SIGNED(-528, output_size)),
TO_SIGNED(495, output_size)),
TO_SIGNED(495, output_size)),
TO_SIGNED(0, output_size)),
                    1,
     (0,
                    1,
     (1,
                    1,
     (2,
                   1,
     (3,
                   1,
     (4,
                   2,
     (0,
                   2,
     (1,
                   2,
     (2,
                   2,
     (3,
                   2,
     (4,
                    3,
     (0,
     (1,
     (2,
                             TO SIGNED (0, output size)),
                             TO SIGNED (307, output size)),
     -- The final result is erroneous to test error checking
     -- functionality of test-bench.
                              TO SIGNED (342, output size)));
     (4,
begin
UUT: entity work.Matrix Multiplier
     -- Remapping generic and port maps with testbench constants and signals
     GENERIC MAP ( data size => data size,
                       Matrix A Height => Matrix A Height,
                       Matrix B Width => Matrix B Width,
                       Matrix Common => Matrix Common)
     PORT MAP ( CLK => CLK,
                   RST => RST,
                   NXT => NXT,
                   Output => Output);
-- Clock process
clk process :process
begin
     clk <= '0';
     wait for CLK PERIOD/2;
     clk <= '1';
     wait for CLK PERIOD/2;
end process;
test : process
begin
     wait for 100 ns;
     wait until falling edge(CLK);
     -- Needed for resetting debouncers
     -- All inputs need to last for 2*CLK_PERIOD's
     -- for the debouncer to accept them as inputs
     -- and outputs the signals to the counter.
     RST <= '0';
     NXT <= '0';
     wait for CLK PERIOD*2;
     RST <= '1';
     NXT <= '1';
     wait for CLK_PERIOD*2;
```

```
RST <= '0';
   NXT <= '0';
   wait for CLK PERIOD*2;
    -- Looping through the results_array - results.
   for i in results'range loop
   NXT <= '1'; -- NXT is pressed to begin the calculation of a coefficient
   wait for CLK PERIOD*2;
   NXT <= '0';
   wait for CLK PERIOD★6; -- Waiting 6 Clock cycles between DISPLAY states.
   assert (output = results(i).output rcd) -- comparing expected and actual values
    -- If assert not true report occurs displaying expected and actual values
   report "Test failed for column: {" & integer'image(results(i).column)
           & "} and row: {" & integer'image(results(i).row) &
           "} Expected output = {" &
           integer'image(to_integer(results(i).output rcd)) &
           "} Actual output = {" & integer'image(to_integer(Output)) & "}"
    severity error;
    -- If first report doesn't occur test was successful and this report occurs
    -- displaying expected and actual value.
   assert (output /= results(i).output rcd)
    report "Test, no errors for column: { " & integer'image(results(i).column)
            & "} and row: {" & integer'image(results(i).row) &
           "} Expected output = {" &
           integer'image(to integer(results(i).output rcd)) &
           "} Actual output = {" & integer'image(to integer(Output)) & "}"
   severity note;
   end loop;
    -- Resetting after full matrix calculated
   RST <= '1';
   wait for CLK PERIOD*2;
   RST <= '0';
    -- Running through loop again after reset
   for i in results'range loop
   NXT <= '1'; -- NXT is pressed to begin the calculation of a coefficient
   wait for CLK PERIOD*2;
   NXT <= '0';
   wait for CLK PERIOD*6; -- Waiting 6 Clock cycles between DISPLAY states.
   assert (output = results(i).output rcd) -- comparing expected and actual values
    -- If assert not true report occurs displaying expected and actual values
    report "Test failed for column: {" & integer'image(results(i).column)
            & "} and row: {" & integer'image(results(i).row) &
           "} Expected output = {" &
           integer'image(to_integer(results(i).output rcd)) &
           "} Actual output = {" & integer'image(to integer(Output)) & "}"
   severity error;
    -- If first report doesn't occur test was successful and this report occurs
    -- displaying expected and actual value.
    assert (output /= results(i).output rcd)
    report "Test, no errors for column: { " & integer'image(results(i).column)
           & "} and row: {" & integer'image(results(i).row) &
           "} Expected output = {" &
           integer'image(to_integer(results(i).output rcd)) &
           "} Actual output = {" & integer'image(to_integer(Output)) & "}"
    severity note;
   end loop;
   wait;
end process;
end Behavioral;
```

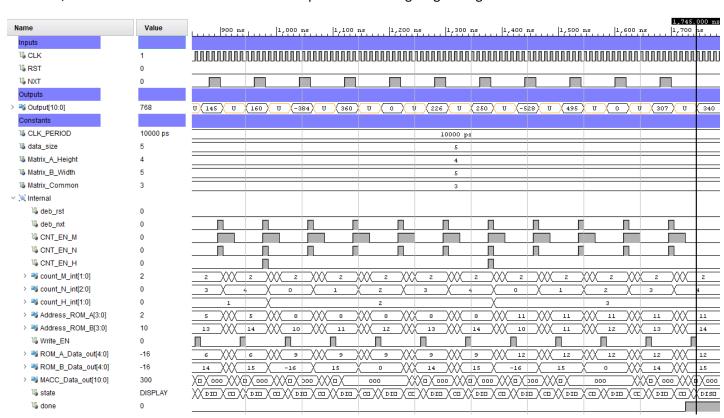
Simulation Output

Final value of every coefficient of the product matrix

Marker 225.000ns - First DISPLAY state with output 768.



Marker 1,745.000ns - Final DISPLAY state with output 340. Done signal goes high.



Full cycle of computation for first and last product matrix coefficients

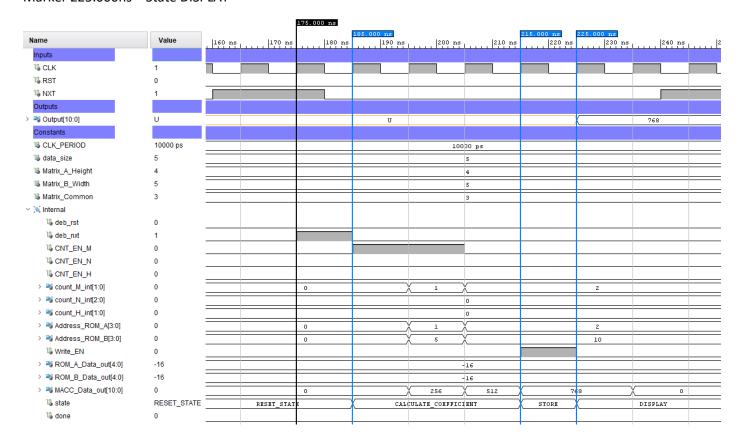
First

Marker 175.000ns - deb_nxt goes high

Marker 185.000ns - State CALCULATE_COEFFICIENT

Marker 215.000ns - State STORE

Marker 225.000ns - State DISPLAY



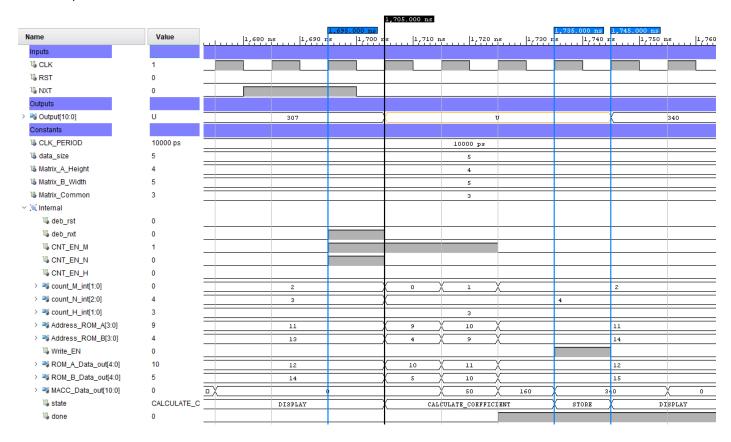
Last

Marker 1,695.00ns – deb_nxt goes high

Marker 1,705.000ns - State CALCULATE_COEFFICIENT

Marker 1,735.000ns - State STORE

Marker 1,745.00ns - State DISPLAY



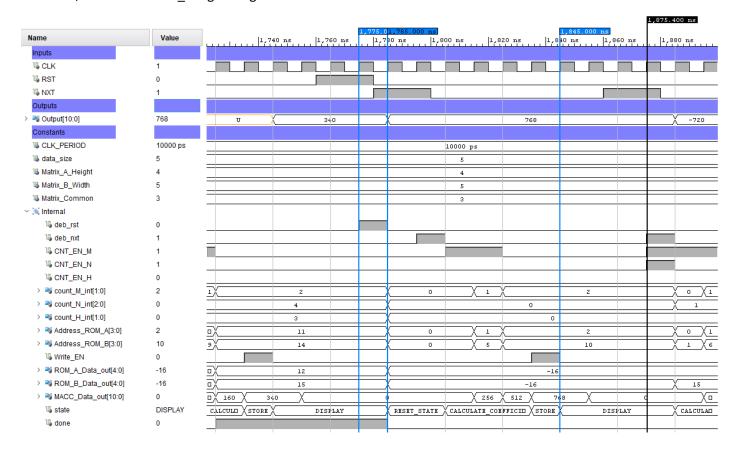
Testing return to RESET_STATE

Marker 1,750.000ns - deb_rst goes high

Marker 1,785.000ns - State RESET_STATE

Marker 1,845.000ns - State DISPLAY

Marker 1,875.400ns - deb_nxt goes high



Console displaying the confirmation messages

Showing two full run cycles separated by a RST. The final output on each cycle has an erroneous expected output to test the error message functionality.

INFO: [Simtcl 6-17] Simulation restarted run 100 us Note: Test, no errors for column: {0} and row: {0} Expected output = {768} Actual output = {768} Time: 240 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd Note: Test, no errors for column: {1} and row: {0} Expected output = {-720} Actual output = {-720} Time: 320 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd Note: Test, no errors for column: {2} and row: {0} Expected output = {0} Actual output = {0} Time: 400 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd Note: Test, no errors for column: {3} and row: {0} Expected output = {-432} Actual output = {-432} Time: 480 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd Note: Test, no errors for column: {4} and row: {0} Expected output = {-480} Actual output = {-480} Time: 560 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File: M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd Note: Test, no errors for column: {0} and row: {1} Expected output = {-240} Actual output = {-240} Time: 640 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd Note: Test, no errors for column: {1} and row: {1} Expected output = {225} Actual output = {225} Time: 720 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd Note: Test, no errors for column: {2} and row: {1} Expected output = {0} Actual output = {0} Time: 800 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File: M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd Note: Test, no errors for column: {3} and row: {1} Expected output = {145} Actual output = {145} Time: 880 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd Note: Test, no errors for column: {4} and row: {1} Expected output = {160} Actual output = {160} Time: 960 ns Iteration: 0 Process: /Matrix Multiplier tb/test File: M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd Note: Test, no errors for column: {0} and row: {2} Expected output = {-384} Actual output = {-384}

```
Time: 1040 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd
Note: Test, no errors for column: {1} and row: {2} Expected output = {360} Actual output = {360}
Time: 1120 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd
Note: Test, no errors for column: {2} and row: {2} Expected output = {0} Actual output = {0}
Time: 1200 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final\_Project/Final\_Project.srcs/sim\_1/new/Matrix\_Multiplier\_tb.vhd
Note: Test, no errors for column: {3} and row: {2} Expected output = {226} Actual output = {226}
Time: 1280 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {4} and row: {2} Expected output = {250} Actual output = {250}
Time: 1360 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {0} and row: {3} Expected output = {-528} Actual output = {-528}
Time: 1440 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {1} and row: {3} Expected output = {495} Actual output = {495}
Time: 1520 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {2} and row: {3} Expected output = {0} Actual output = {0}
Time: 1600 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {3} and row: {3} Expected output = {307} Actual output = {307}
Time: 1680 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Error: Test failed for column: {4} and row: {3} Expected output = {342} Actual output = {340}
Time: 1760 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd
Note: Test, no errors for column: {0} and row: {0} Expected output = {768} Actual output = {768}
Time: 1860 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {1} and row: {0} Expected output = {-720} Actual output = {-720}
Time: 1940 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {2} and row: {0} Expected output = {0} Actual output = {0}
Time: 2020 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {3} and row: {0} Expected output = {-432} Actual output = {-432}
```

```
Time: 2100 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd
Note: Test, no errors for column: {4} and row: {0} Expected output = {-480} Actual output = {-480}
Time: 2180 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {0} and row: {1} Expected output = {-240} Actual output = {-240}
Time: 2260 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {1} and row: {1} Expected output = {225} Actual output = {225}
Time: 2340 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {2} and row: {1} Expected output = {0} Actual output = {0}
Time: 2420 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {3} and row: {1} Expected output = {145} Actual output = {145}
Time: 2500 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {4} and row: {1} Expected output = {160} Actual output = {160}
Time: 2580 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {0} and row: {2} Expected output = {-384} Actual output = {-384}
Time: 2660 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {1} and row: {2} Expected output = {360} Actual output = {360}
Time: 2740 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {2} and row: {2} Expected output = {0} Actual output = {0}
Time: 2820 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:
M:/VivadoProjects/Final Project/Final Project.srcs/sim 1/new/Matrix Multiplier tb.vhd
Note: Test, no errors for column: {3} and row: {2} Expected output = {226} Actual output = {226}
Time: 2900 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {4} and row: {2} Expected output = {250} Actual output = {250}
Time: 2980 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {0} and row: {3} Expected output = {-528} Actual output = {-528}
Time: 3060 ns Iteration: 0 Process: /Matrix Multiplier tb/test File:
M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
Note: Test, no errors for column: {1} and row: {3} Expected output = {495} Actual output = {495}
```

```
Time: 3140 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:

M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd

Note: Test, no errors for column: {2} and row: {3} Expected output = {0} Actual output = {0}

Time: 3220 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:

M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd

Note: Test, no errors for column: {3} and row: {3} Expected output = {307} Actual output = {307}

Time: 3300 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:

M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd

Error: Test failed for column: {4} and row: {3} Expected output = {342} Actual output = {340}

Time: 3380 ns Iteration: 0 Process: /Matrix_Multiplier_tb/test File:

M:/VivadoProjects/Final_Project/Final_Project.srcs/sim_1/new/Matrix_Multiplier_tb.vhd
```

RTL Component Statistics

```
______
Start RTL Component Statistics
______
Detailed RTL Component Info :
+---Adders :
    2 Input 3 Bit Adders := 1
2 Input 2 Bit Adders := 2
+---Registers :
              11 Bit Registers := 1
              3 Bit Registers := 1
              2 Bit Registers := 3
1 Bit Registers := 6
+---Muxes :
    15 Input 5 Bit
2 Input 3 Bit
2 Input 2 Bit
4 Input 2 Bit
5 Input 1 Bit
                        Muxes := 1
                        Muxes := 1
                        Muxes := 2
                        Muxes := 1
                        Muxes := 1
              _ bit
1 Bit
                        Muxes := 1
     3 Input
     2 Input
                        Muxes := 3
Finished RTL Component Statistics
______
```

Bibliography

Tempesti, D. G. (2018). Project Script. Retrieved from https://bit.ly/2S5PmXM