Model

Parameters

卡车相关参数

- α : fixed cost per day per truck
- β : transportation cost per package per unit distance
- s: a sequence of index of different capacities
- C_s : capacity of sth type of truck
- ullet L: max number of legs allowed to be traveled by a truck
- ullet D: max distance allowed to be traveled by a truck
- **Speed**: average speed of trucks, if necessary it can be truck specific
- *DrivingTimePerDay*: driving time per day allowed for trucks
- $b_{ij}^{\tau} = 1$ if τ contains arc(i,j)
- ullet $L_{so}:$ the number of trucks available starting from origin o with capacity of C_s

节点相关参数

- q^p : quantity of pickup and delivery demand p
- $l_{i,j}$: distance of arc(i,j)

Auxiliary graph $G^{'}(V^{'},A^{'})$

- ullet $V^{'}:$ for each $u\in V$, associate T vertices: u_{1},u_{2},\ldots,u_{T}
- $ullet A_T = ig\{(u_t, u_{(t+1)modT}) | u \in V, t \in \{1, 2, \ldots, T\}ig\}$
- $\bullet \ \ \tilde{A} = \left\{(u_t, (w_{(t+t(u,w))modT})) | (u,w) \in A, t \in \{1,2,\ldots,T\}\right\}$
- $\bullet \ \ A^{'}=A_{T}\cup \tilde{A}$
- ullet cost: $A_T=0$ $ilde{A}=l(u,w)$

Decision variables

- $z_{ au}$: the number of trucks choose to run in cycle au
- $x_{i,j}^p$: a split of demand q^p shipped on arc $(i,j) \in ilde{A} \cup A_T$

Sets

- V: set of nodes
- A: set of arcs
- P: set of demand O-D pairs
- S: set of index of different capacities of trucks

Indices

- *i*, *j*: index of nodes
- (i, j): index of arcs
- **p**: index of O-D pairs

Const

$$b_i^p = \left\{egin{array}{ll} q^p & i = o(p) \ -q^p & i = d(p) \ 0 & ext{otherwise} \end{array}
ight.$$

Minimize

$$\textstyle \sum_{\tau \in \theta} \sum_{(i,j) \in \tilde{A} \cup A_T} \frac{\alpha l_{ij} b_{ij}^{\tau} z_{\tau}}{Speed*DrivingTimePerDay} + \sum_{s \in S} \sum_{o \in O} \sum_{\tau \in \theta_{so}} \gamma_{so} z_{\tau} + \sum_{p \in P} \sum_{(i,j) \in \tilde{A} \cup A_T} \beta l_{ij} x_{ij}^{p}$$

Subject to:

$$\sum_{(i,j)\in\delta^{+}(i)}x_{ij}^{p}-\sum_{(j,i)\in\delta^{-}(i)}x_{ji}^{p}=b_{i}^{p} \qquad \forall p\in P, i\in V^{'}$$
 (1)

$$\sum_{p \in P} x_{ij}^p \leqslant \sum_{s \in S} \sum_{ au \in heta_s} C_s b_{ij}^ au z_ au \qquad orall (i,j) \in ilde{A}$$

$$\sum_{\tau \in \theta_{so}} z_{\tau} + q_{so} \leqslant L_{so} \qquad \forall s \in S, \forall o \in O$$
 (3)

$$x_{ij}^p\geqslant 0 \qquad orall p\in P, (i,j)\in ilde A\cup A_T \qquad (4)$$

$$z_{ au} \in Z \qquad \forall au \in heta \qquad (5)$$

$$egin{array}{ll} z_{ au} \in Z & orall au \in heta & (5) \ q_{so} \geqslant 0 & orall s \in S, o \in O \end{array}$$

$$\sum_{ au \in heta} b_{ij}^ au z_ au \leqslant 1 \qquad orall (i,j) \in ilde{A}$$