## Programming Assignment #2 Maximum Planar Subset (Dynamic Programming)

(a) Data structure (2%) How do you store the data of chords and/or other supporting information?

1. data of chord: 用一個一維vector去記錄每個vertics 上chord的另一端的paired vertics

2. other supporting information: 利用二維vector M 跟 S 去分別記錄maximum planar subset number 跟 the case of each M[i,j] is calculated from

```
std::vector<std::vector<int>> S;
std::vector<std::vector<int>> M;
```

- (b) Algorithm (3%)
  - Describe the algorithm of your program, including how your program finds the number of chords and the chords themselves of the maximum planar subset
  - E.g. if you use dynamic programming, you should mention the recurrence equation and how to utilize your data structure to do calculation
- 1. Use Dynamic Programming with recurrence equation:
- 2. Construct table M[i,i] and S[i,i] with both size of 2n x 2n
  - M[i,j]: 用來存放某i,j區間下的 Maximum Planar Subset chord 數(即此區間最大互不交跨的chord的數量)
  - S[i,j]: 用來存放各M[i,j] 是由recurrence equation中的哪個case計算出來的, 以便在 recurrence trace回去找各chord的時候有辦法回朔找subset
- 3. 設定base case: (M[i],[i]對角線皆為0)

```
for(int i=0;i<=2*n-1;i++){
    M[i][i]=0; //initialize 對角線為0
}
```

4. 填滿M[i,j] 與 S[i,j]

```
從I=1 to I-2n (I: i, j間間格)

從i=0 to i=2n-1 (i: 範圍的左界)

j=i+l (j: 範圍的右界)

k=chords[j] (k 為j的chord 另一端的paired_vertics)

利用k 的位置去判斷現在i,j為case 幾, M[i,j]要從哪個subset來

紀錄M[i,j] 為 recurrence equation case1 or 2 or 3

紀錄S[i,j] 為 計算M[i,j]時的case
```

5. 利用recursive 從M[0,11] 一路跟著S[i][j] 紀錄的case, 根據各case 的 recurrence equation 往回回溯, 若為case2 與 case4(case3的第二個情形), 則i,j為其中之一選擇的chord, 並存入 maximumPlanarSubset\_chord中 直到 j<=i 中止

```
void trace maximumPlanarSubset _chord(int i,int j){
    ///cout<<"now i = "<<i<<"now j = "<<j<< endl;
    //+止條件: trace回去到了如果j<=i 左下角形含對角線就停止這個subtree, return 0;
    if(j<=i){
        return;
    }

    if(S[i][j]==1){//case1 //ij上面沒線, 來自M[i][j]=M[i][j-1];
        trace_maximumPlanarSubset_chord(i,j-1);
    }else if(S[i][j]==2){//case2 //ij上面有線, 來自M[i][j]=M[i+1][j-1]+1;
        ///cout<<"push i = "<<i<<"push j = "<<j<< endl;
        trace_maximumPlanarSubset_chord(i+1,j-1);

        maximumPlanarSubset_chord(push_back({i,j}); //放在回call後面, 所以出來的chord還是會照原順序
}else if(S[i][j]==4){//case4 //ij上面有線, 來自M[i][j]=M[i][k-1]+1+M[k+1][j-1];
        int k=chords[j];
        ///cout<<"push i = "<<i<<"push j = "<<j<< endl;
        trace_maximumPlanarSubset_chord(i,k-1);
        trace_maximumPlanarSubset_chord(k+1,j-1);
        maximumPlanarSubset_chord(k+1,j-1);
        maximumPlanarSubset_chord(k+1,j-1);
        maximumPlanarSubset_chord_push_back({k,j}); //<Debug4> 這個case是kj在連線!//放在回call後面,所以出來的chord還是會照原順序
}
return;
}
```

- (c) Time Complexity Analysis (3%)
  - In terms of number of chords *n*
  - Analysis based on your implementation code

Ans:

因

 $T(maximumPlanarSubset()) = \theta(n^2) \& T(trace_maximumPlanarSubset_chord()) = \theta(n^2)$  $\Rightarrow T(n) = \theta(n^2)$ 

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```
(d) README (2%)
           • Clear instruction of how to compile and execute your program
             You may refer to PA#1 README
(also written in file README)
This is README file for Algorithm PA#2
Author: <余佳融 B10611038>
Date: 2024/11/3
=====
SYNOPSIS:
./bin/mps <input_file_name> <output_file_name>
ex: ./bin/mps inputs/12.in outputs/12.out
This program supports finding the maximum planar subset of a 0~2n-1 vertices
=====
DIRECTORY:
bin/
        executable binary
doc/
        reports
inputs/ input data (all chords)
outputs/ output result (maximum planar subset chords)
src/
        source C++ codes
utility/ checker
=====
HOW TO COMPILE:
       Under the root directory of this PA, simply type
       make
=====
```

## HOW TO RUN:

cd PA2/

./bin/mps <input\_file\_name> <output\_file\_name>
For example,

i di example,

under <student\_id>\_pa1

./bin/mps inputs/12.in outputs/12.out

=====

## OTHER NOTICE: