

Week - 8

Design an algorithm which will find maximum cost required to connect cities (Prim's Algorithm).

Algorithm: →

- 1) START
- 2) Input n
- 3) if $i \geq n$ goto step 8
- 4) if $j \geq n$ goto step 7
- 5) input $a[i][j]$
- 6) if $j < n$ goto step 4
- 7) if $i < n$ goto step 3
- 8) primus(a, n)
- 9) STOP

```
primus (int ** arr, int n) {  
    vector<bool> visited (n, false);  
    vector<int> weight (n, INF);  
    priority-queue<pair<int, int>>, vector<pair<int, int>>;  
        greater<pair<int, int>> min-heap;  
    int src = 0;  
    weight[src] = 0;  
    min-heap.push(make_pair(weight[src], src));  
    while(!min-heap.empty()) {  
        u = min-heap.top().second;  
        min-heap.pop();  
        if(!visited[u]) {  
            visited[u] = true;  
            for(int v = 0; v < u; ++v) {  
                if(!visited[v] && arr[u][v] != 0 && arr[u][v] < weight[v])  
                {  
                    weight[v] = arr[u][v];  
                    min-heap.push(make_pair(weight[v], v));  
                }  
            }  
        }  
    }  
}
```

```
int sum = 0;  
for (auto i : weight)  
    sum += i;  
return sum;  
}
```

on
min cost (Kruskal Algorithm) minimum cost required

Algorithm: →

- 1) START
- 2) Input n
- 3) if $i \geq n$ goto step 8
- 4) if $j \geq n$ goto step 7
- 5) input graph[i][j]
- 6) if $j < n$ goto step 4
- 7) if $i < n$ goto step 5
- 8) Kruskal (graph, n)
- 9) Stop

Kruskal (graph, n) {

vector <pair <int, pair <int, int>>> G;

for (i=0; i<n; i++)

for (j=0; j<n; j++)

if (graph[i][j] != 0)

G.push_back(make_pair(graph[i][j], make_pair(i, j)));

sort(G.begin(), G.end());

vector <int> parent (n, NIL);

S=0;

for (auto i : G) {

u = i.second.first;

v = i.second.second;

w = i.first;

if (UnionByWeight (parent, u, v))

S += w;

}

return S;

}

③ Design an algorithm and find the maximum budget required for a project.

Algorithm \rightarrow

- 1) START
- 2) input n
- 3) if $i \geq n$ goto step 8
- 4) if $j \geq n$ goto step 7
- 5) input $graph[i][j]$
- 6) if $j < n$ goto step 4
- 7) if $i < n$ goto step 3
- 8) Kruskals($graph, n$)
- 9) STOP

```
Kruskals( $graph, n$ ) {  
    for ( $i=0; i < n; i++$ )  
        for ( $j=0; j < n; j++$ )  
            if ( $graph[i][j] \neq 0$ )  
                G.push_back(make_pair( $graph[i][j]$ , make_pair( $i, j$ )));  
    sort(G.begin(), G.end(), greater<pair<int, int>());  
  
    vector<int> parent( $n, NIL$ );  
    int s = 0;  
    for (auto i : G) {  
        u = i.second.first;  
        v = i.second.second;  
        w = i.first;  
        if (UnionByWeight(parent, u, v))  
            s += w;  
    }  
    return s;  
}
```