

Tutorial - 3

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Ans 1.

```
for (i=0 to n)
{
    if (arr[i] == value)
        // element found
}
```

Ans 2.

```
void insertionSort(int arr[], int n)
{
    for (int i=1; i<n; i++)
    {
        j=i-1;
        x=arr[i];
        while (j>-1 && arr[j]>x)
        {
            arr[j+1]=arr[j];
            j--;
        }
        arr[j+1]=x;
    }
}
```

Recursive

```
void insertionSort(int arr[], int n)
{
    if (n <= 1)
        return;
    insertionSort(arr, n-1);
    int last = arr[n-1];
    int j = n-2;
    while (j >= 0 && arr[j] > last)
    {
        arr[j+1] = arr[j];
        j--;
    }
    arr[j+1] = last;
}
```

Insertion sort is called online sorting because it does not need to know anything about what values it will sort and information is requested while algorithm is running.

Other Sorting Algorithm

Bubble sort

Quick sort

Merge sort

Selection sort

Heap sort

Count sort

Ans 3.

Sorting Algorithm	Best	Worst	Average
Selection Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Insertion Sort	$O(n)$	$O(n^2)$	$O(n^2)$
Heap Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quick Sort	$O(n \log n)$	$O(n^2)$	$O(n \log n)$
Merge Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$

Ans 4.

Implace Sorting
Bubble Sort
Selection Sort
Insertion Sort
Quick Sort
Heap Sort

Stable Sorting
Merge Sort
Bubble Sort
Insertion Sort
Count Sort

Online Sorting
Insertion Sort

Ans 5. Iterative \rightarrow

```
int linearsearch (int arr[], int l, int r, int key)
{
    while (l <= r) {
        int m = ((l+r)/2);
        if (arr[m] == key)
            return m;
        else
            if (key < arr[m])
                r = m-1;
            else
                l = m+1;
    }
}
```

```

        l = m + 1;
    }
    return -1;
}

```

Recursive

```

int binarysearch (int arr[], int l, int r, int key)
{
    while (l <= r) {
        int m = (l + r) / 2;
        if (key == arr[m]) {
            return m;
        }
        else if (key < arr[m]) {
            return binarysearch (arr, l, m - 1, key);
        }
        else {
            return binarysearch (arr, m + 1, r, key);
        }
    }
    return -1;
}

```

Time complexity →

Linear search → $O(n)$

Binary search → $O(\log n)$

Ans 6.

$$T(n) = T(n/2) + 1 \quad - (1)$$

$$T(n/2) = T(n/4) + 1 \quad - (2)$$

$$T(n/4) = T(n/8) + 1 \quad - (3)$$

$$\begin{aligned} T(n) &= T(n/2) + 1 \\ &= T(n/4) + 1 + 1 \\ &= T(n/8) + 1 + 1 + 1 \\ &\vdots \\ &= T(n/2^k) + 1 \text{ (k times)} \end{aligned}$$

$$\text{let } 2^k = n$$

$$k = \log n$$

$$T(n) = T(n/n) + \log n$$

$$T(n) = T(1) + \log n$$

$$\boxed{T(n) = O(\log n)} \rightarrow \text{Answer}$$

Ans 7.

```
for (i=0; i<n; i++)  
{  
    for (int j=0; j<n; j++)  
    {  
        if (a[i] + a[j] == k)  
            printf ("%d %d", i, j);  
    }  
}
```

Ans 8.

Quick sort is fastest general purpose sort. In most practical situation quick sort is the method of choice as stability is important and space is available, mergesort might be best.

Ans 9

A pair $(A[i], A[j])$ is said to be inversion if
 $A[i] > A[j]$
 $i < j$

Total no. of inversion in given array are 31 using merge sort.

Ans 10.

Worst case $O(n^2)$ → The worst case occurs when the pivot element is an extreme (smallest / largest) element.

This happens when input array is sorted or reverse sorted and either first or last element is selected as pivot.

Best Case $O(n \log n)$ → The best case occurs when we will select pivot element as a mean element.

Ans 11

Merge Sort

$$\begin{array}{l} \text{Best case} \rightarrow T(n) = 2T(n/2) + O(n) \\ \text{Worst case} \rightarrow T(n) = 2T(n/2) + O(n) \end{array} \left. \vphantom{\begin{array}{l} \text{Best case} \\ \text{Worst case} \end{array}} \right\} O(n \log n)$$

Quick Sort

$$\text{Best case} \rightarrow T(n) = 2T(n/2) + O(n) \rightarrow O(n \log n)$$

$$\text{Worst case} \rightarrow T(n) = T(n-1) + O(n) \rightarrow O(n^2)$$

In quick sort array of element is divided into 2 parts repeatedly until it is not possible to divide it further.

In merge sort the elements are split into 2 subarray $(n/2)$ again and again until only one element is left.

Ans 13

A better version of bubble sort known as m bubble sort includes a flag that is set if an exchange is made after an entire pass over.

