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In [3]:
       from sympv.interactive import printing
       printing.init printing(use latex=True)
       from sympy import Eq,solve linear system,Matrix,det,transpose,Transpose,symbols,trace,Trace
       from sympy.solvers import solve
       from sympy import simplify, sqrt
       from sympy.physics.quantum import Bra, Ket
       from time import time
       import numpy as np
       import sympy as sp
       print(' ----Welcome to Linear Algebra Calculator Material---- ')
       print('\n\n\n')
       print('1 -- UNIT-I -- SOLVING SYSTEM OF LINEAR EQUATIONS')
       print('2 -- UNIT-II -- LINEAR DEPENDANCY AND BASIS FORMATION CHECKING')
       print('3 -- UNIT-III -- FINDING EIGEN VALUE AND EIGEN VECTOR')
       print('4 -- UNIT-IV -- ORTHOGONALIZATION')
       print('5 -- UNIT-V -- OR DECOMPOSITION')
       inum=int(input('Enter Your Choice of Chapter : '))
       if inum==1:
           print("-----Welcome! To Solving system Of Linear Equations-----")
           print("2.2X2 Matrix")
           print("3.3X3 Matrix")
           print("4.4X4 Matrix")
           u=int(input("which nXn matrix you want : "))
           display("Using Sympy Module")
           if u==2:
              display("-----")
              eq1=sp.Function("eq1")
              eq2=sp.Function("eq2")
              x,y=sp.symbols("x y")
              x1=int(input("Enter your X1 coefficient : "))
              v1=int(input("Enter your Y1 coefficient : "))
              display("-----")
              x2=int(input("Enter your X2 coefficient : "))
              y2=int(input("Enter your Y2 coefficient : "))
              display("-----")
              c1=int(input("Enter your constant 1 : "))
              c2=int(input("Enter your constant 2 : "))
              display("-----")
              eq1=sp.Function("eq1")
```

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eq2=sp.Function("eq2")
   x,y=sp.symbols('x y')
   eq1=Eq(x1*x+y1*y,c1)
   eq2=Eq(x2*x+y2*y,c2)
   display(eq1)
   display(eq2)
   row1=[x1,y1,c1]
   row2=[x2,y2,c2]
   system=Matrix((row1,row2))
   display(system)
   start=time()
   if(solve linear system(system,x,y)==None):
      display("System is Inconsistent")
   else:
      display("System is Consistent")
      display(solve linear system(system,x,y))
   end=time()
   display("Execution Time : ",end-start)
if u==3:
   display("-----")
   x1=int(input("Enter your X1 coefficient : "))
   y1=int(input("Enter your Y1 coefficient : "))
   z1=int(input("Enter your z1 coefficient : "))
   display("-----")
   x2=int(input("Enter your X2 coefficient : "))
   y2=int(input("Enter your Y2 coefficient : "))
   z2=int(input("Enter your z2 coefficient : "))
   display("-----")
   x3=int(input("Enter your X3 coefficient : "))
   y3=int(input("Enter your Y3 coefficient : "))
   z3=int(input("Enter your z3 coefficient : "))
   display("-----")
   c1=int(input("Enter your constant 1 : "))
   c2=int(input("Enter your constant 2 : "))
   c3=int(input("Enter your constant 3 : "))
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```
display("-----")
   eq1=sp.Function("eq1")
   eq2=sp.Function("eq2")
   eq3=sp.Function("eq3")
   x,y,z=sp.symbols('x y z')
   eq1=Eq(x1*x+y1*y+z1*z,c1)
   eq2=Eq(x2*x+y2*y+z2*z,c2)
   eq3=Eq(x3*x+y3*y+z3*z,c3)
   display(eq1)
   display(eq2)
   display(eq3)
   row1=[x1,y1,z1,c1]
   row2=[x2,y2,z2,c2]
   row3=[x3,y3,z3,c3]
   system=Matrix((row1,row2,row3))
   display(system)
   start=time()
   if(solve linear system(system,x,y,z)==None):
      display("System is Inconsistent")
   else:
      display("System is Consistent")
      display(solve linear system(system,x,y,z))
   end=time()
   display("Execution Time : ",end-start)
if u==4:
   display("-----")
   w1=int(input("Enter your w1 coefficient : "))
   x1=int(input("Enter your X1 coefficient : "))
   y1=int(input("Enter your Y1 coefficient : "))
   z1=int(input("Enter your z1 coefficient : "))
   display("-----")
   w2=int(input("Enter your w2 coefficient : "))
   x2=int(input("Enter your X2 coefficient : "))
   y2=int(input("Enter your Y2 coefficient : "))
   z2=int(input("Enter your z2 coefficient : "))
   display("----")
   w3=int(input("Enter your w3 coefficient : "))
   x3=int(input("Enter your X3 coefficient : "))
   y3=int(input("Enter your Y3 coefficient : "))
```

```
z3=int(input("Enter your z3 coefficient : "))
display("-----")
w4=int(input("Enter your w4 coefficient : "))
x4=int(input("Enter your X4 coefficient : "))
y4=int(input("Enter your Y4 coefficient : "))
z4=int(input("Enter your z4 coefficient : "))
display("-----")
c1=int(input("Enter your constant 1 : "))
c2=int(input("Enter your constant 2 : "))
c3=int(input("Enter your constant 3 : "))
c4=int(input("Enter your constant 4 : "))
display("-----")
eq1=sp.Function("eq1")
eq2=sp.Function("eq2")
eq3=sp.Function("eq3")
eq4=sp.Function("eq4")
w,x,y,z=sp.symbols('w x y z')
eq1=Eq(w1*w+x1*x+y1*y+z1*z,c1)
eq2=Eq(w2*w+x2*x+y2*y+z2*z,c2)
eq3=Eq(w3*w+x3*x+y3*y+z3*z,c3)
eq4=Eq(w4*w+x4*x+y4*y+z4*z,c4)
display(eq1)
display(eq2)
display(eq3)
display(eq4)
row1=[w1,x1,y1,z1,c1]
row2=[w2,x2,y2,z2,c2]
row3=[w3,x3,y3,z3,c3]
row4=[w4, x4, y4, z4, c4]
system=Matrix((row1,row2,row3,row4))
display(system)
start=time()
if(solve_linear_system(system,w,x,y,z)==None):
   display("System is Inconsistent")
else:
```

```
display("System is Consistent")
      display(solve linear system(system,w,x,y,z))
   end=time()
   display("Execution Time : ",end-start)
print("Using Numpy module")
print("-----")
if u==2:
   nrow1=[x1,y1]
  nrow2=[x2,y2]
   nmat=np.array([nrow1,nrow2])
   cons=np.array([c1,c2])
   display(nmat,cons)
   start1=time()
   answer=linalg.solve(nmat,cons)
   end1=time()
   xval=answer[0]
   yval=answer[1]
   print("-----")
   display("x= ",float(xval))
   display("y= ",float(yval))
   display("-----")
   display("Execution time : ",end1-start1)
   display("-----")
if u==3:
  nrow1=[x1,y1,z1]
  nrow2=[x2,y2,z2]
   nrow3=[x3,y3,z3]
   nmat=np.array([nrow1,nrow2,nrow3])
   cons=np.array([c1,c2,c3])
   display(nmat,cons)
   start1=time()
   answer=linalg.solve(nmat,cons)
   end1=time()
   xval=answer[0]
   yval=answer[1]
   zval=answer[2]
```

```
display("x= ",float(xval))
     display("y= ",float(yval))
      display("z= ",float(zval))
      print("-----")
      display("Execution time : ",end1-start1)
      print("-----")
  if u==4:
      nrow1=[w1,x1,y1,z1]
      nrow2=[w2,x2,y2,z2]
      nrow3=[w3,x3,v3,z3]
      nrow4 = [w4, x4, y4, z4]
      nmat=np.array([nrow1,nrow2,nrow3,nrow4])
      cons=np.array([c1,c2,c3,c4])
      display(nmat,cons)
      start1=time()
      answer=linalg.solve(nmat,cons)
      end1=time()
      wval=answer[0]
      xval=answer[1]
      vval=answer[2]
      zval=answer[3]
      print("-----")
      display("w= ",int(wval))
     display("x= ",int(xval))
      display("y= ",int(yval))
      display("z= ",int(zval))
      print("-----")
      display("Execution time : ",end1-start1)
      print("-----")
elif inum==2:
   print("----- Welcome! To Find linear combination dependancy and basis formation checking -----")
   no=int(input("No of Times you going to execute the program : "))
  for j in range(0,no):
     n=int(input('Number of vectors : '))
     m,a,e,g=sp.symbols('* + = -->')
      if n==2:
            x,y,m,a,e,g=sp.symbols("x1 x2 * + = -->")
            a11,a12=map(int,input("Enter 1st row : ").split())
            a21,a22=map(int,input("Enter 2nd row : ").split())
            vect1, vect2=[a11,a12], [a21,a22]
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```
amat=Matrix((vect1, vect2))
                  print("Given Matrix")
                  display(amat)
                  print('now')
                  display(((x,m,vect1),a,(y,m,vect2),e,(0,0),g))
                  r1,r2=[a11,a21,0],[a12,a22,0]
                  eq1,eq2,eqn,eqm=sp.Function("eq1"),sp.Function("eq2"),sp.Function("eqn"),sp.Function("eqm")
                  eqm = (a11*x, a12*x)
                  eqn=(a21*v,a22*v)
                  display((eqm,a,eqn,e,(0,0)))
                  eq1,eq2=Eq(a11*x+a21*y,0),Eq(a12*x+a22*y,0)
                  display(eq1,eq2)
                  print("arranged matrix")
                 display((transpose(amat),Matrix((x,y)),e,Matrix((0,0))))
                  system=Matrix((r1,r2))
                  print("augmented form")
                  display(system)
                  print("\n\n\nThe two vectors are ")
                  if(det(amat)==0):
                           print("linearly dependant")
                          display(solve linear system(system,x,y))
                           print("dim R2 != 2, The given vectors NOT form a basis of R^2")
                  else:
                           print("linearly independent")
                          display(solve linear system(system,x,y))
                          print("The given vectors does form a basis of R^2")
if n==3:
                  x,y,z=sp.symbols("x1 x2 x3")
                  a11,a12,a13=map(int,input("Enter 1st row : ").split())
                  a21,a22,a23=map(int,input("Enter 2nd row: ").split())
                  a31,a32,a33=map(int,input("Enter 3rd row: ").split())
                  vect1, vect2, vect3=[a11,a12,a13], [a21,a22,a23], [a31,a32,a33]
                  amat=Matrix((vect1, vect2, vect3))
                  print("Given Matrix")
                  display(amat)
                  print('now')
                  display(((x,m,vect1),a,(y,m,vect2),a,(z,m,vect3),e,(0,0,0),g))
                  r1,r2,r3=[a11,a21,a31,0],[a12,a22,a32,0],[a13,a23,a33,0]
                  eq1,eq2,eq3,eqn,eqm,eqo=sp.Function("eq1"),sp.Function("eq2"),sp.Function("eq3"),sp.Function("eqn"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Function("eq1"),sp.Funct
                  eqm=(a11*x,a12*x,a13*x)
                  eqn=(a21*y,a22*y,a23*y)
                  eqo=(a31*z,a32*z,a33*z)
                  display((eqm,a,eqn,a,eqo,e,(0,0,0),g))
                  eq1, eq2, eq3 = Eq(a11*x+a21*y+a31*z, 0), Eq(a12*x+a22*y+a32*z, 0), Eq(a13*x+a23*y+a33*z, 0)
                  display(eq1,eq2,eq3)
```

```
print("arranged matrix")
                display((transpose(amat), Matrix((x,y,z)), e, Matrix((0,0,0))))
                system=Matrix((r1,r2,r3))
                print("augmented form")
                display(system)
                print("\n\nThe two vectors are ")
                if(det(transpose(amat))==0):
                         print("linearly dependant")
                         display(solve linear system(system,x,v,z))
                         print("dim R3 != 3, The given vectors NOT form a basis of R^3")
                else:
                         print("linearly independent")
                         display(solve linear system(system,x,v,z))
                         print("The given vectors does form a basis of R^3")
if n==4:
                x,y,z,w=sp.symbols("x1 x2 x3 x4")
                a11,a12,a13,a14=map(int,input("Enter 1st row: ").split())
                a21,a22,a23,a24=map(int,input("Enter 2nd row : ").split())
                a31,a32,a33,a34=map(int,input("Enter 3rd row: ").split())
                a41,a42,a43,a44=map(int,input("Enter 4th row: ").split())
                vect1, vect2, vect3, vect4=[a11,a12,a13,a14], [a21,a22,a23,a24], [a31,a32,a33,a34], [a41,a42,a43,a44]
                amat=Matrix((vect1, vect2, vect3, vect4))
                print("Given Matrix")
                display(amat)
                print('now')
                display(((x,m,vect1),a,(y,m,vect2),a,(z,m,vect3),a,(w,m,vect4),e,(0,0,0,0),g))
                r1,r2,r3,r4=[a11,a21,a31,a41,0],[a12,a22,a32,a42,0],[a13,a23,a33,a43,0],[a14,a24,a34,a44,0]
                eq1,eq2,eq3,eq4=sp.Function("eq1"),sp.Function("eq2"),sp.Function("eq3"),sp.Function("eq4")
                eqm=(a11*x,a12*x,a13*x,a14*x)
                eqn=(a21*y,a22*y,a23*y,a24*y)
                eqo=(a31*z,a32*z,a33*z,a34*z)
                eqp=(a41*w,a42*w,a43*w,a44*w)
                display((eqm,a,eqn,a,eqo,a,eqp,e,(0,0,0,0),g))
                eq1, eq2, eq3, eq4 = Eq(a11*x + a21*y + a31*z + a41*w, 0), Eq(a12*x + a22*y + a32*z + a42*w, 0), Eq(a13*x + a23*y + a33*z + a43*w, 0), Eq(a14*x + a24*y + a34*y + a34*z + a43*w, 0), Eq(a14*x + a24*y + a34*x + a24*y + a34*x + a24*w, 0), Eq(a14*x + a24*y + a34*x + a24*x 
                display(eq1,eq2,eq3,eq4)
                system=Matrix((r1,r2,r3,r4))
                print('rearranged matrix')
                display((transpose(amat),Matrix((x,y,z,w)),e,Matrix((0,0,0,0))))
                print("augmented form")
                display(system)
                print("\n\nThe two vectors are ")
                if(det(amat)==0):
                         print("linearly dependant")
                        display(solve linear system(system,x,y,z,w))
                         print("dim R4 != 4, The given vectors NOT form a basis of R^4")
```

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else:
                    print("linearly independent")
                    display(solve linear system(system,x,y,z,w))
                    print("The given vectors form a basis of R^4")
    print('
elif inum==3:
    a11,a12,a13,a21,a22,a23,a31,a32,a33=map(int,input("Enter the matrix coefficients: ").split())
    r1=[a11,a12,a13]
    r2=[a21,a22,a23]
    r3=[a31,a32,a33]
    amat=sp.Matrix((r1,r2,r3))
    print("Input matrix")
    display(amat)
    s1=a11+a22+a33
    display('S1={0}+{1}+{2}'.format(a11,a22,a33))
    display('s1={0}'.format(s1))
    s2=(((a22*a33)-(a32*a23))+((a11*a33)-(a31*a13))+((a11*a22)-(a21*a12)))
    display('s2=((({0}*{1})-({2}*{3}))+(({4}*{5})-({6}*{7}))+(({8}*{9})-({10}*{11}))'.format(a22,a33,a32,a23,a11,a33,a31,a13,a11,a22,a21,a12)
    display('s2=({0}+{1}+{2})'.format(((a22*a33)-(a32*a23)),((a11*a33)-(a31*a13)),((a11*a22)-(a21*a12))))
    s3=det(amat)
    display('s3=det(amat)')
    display("s3={0}".format(s3))
    display(s1=\{0\} s2=\{1\} s3=\{2\}'.format(\{s1, s2, s3\})
    x=sp.symbols('\lambda')
    eq1=sp.Function("eq1")
    eq1=Eq((x**3 - (s1)*x**2 + (s2)*x - s3))
    display(eq1)
    k=sp.factor(eq1)
    display(k)
    K=solve(k)
    print("Eigen values are : ",K)
    a,b,c,d,e,f=sp.symbols('a b c * = ->')
    b1=[a11-x,a12,a13]
    b2=[a21,a22-x,a23]
   b3=[a31,a32,a33-x]
    bmat=sp.Matrix((b1,b2,b3))
    xmat=sp.Matrix((a,b,c))
    print("To find eigen vector")
    display(bmat,d,xmat)
    cmat=sp.Matrix((0,0,0))
    if(len(K)==2):
        print("If \lambda = \{0\}".format(K[0]))
        b1=[a11-K[0],a12,a13]
        b2=[a21,a22-K[0],a23]
        b3=[a31,a32,a33-K[0]]
        bmat=sp.Matrix((b1,b2,b3))
        display((bmat,d,xmat,e,cmat,f))
```

```
bm1=[a11-K[0],a12,a13,0]
    bm2=[a21,a22-K[0],a23,0]
    bm3=[a31,a32,a33-K[0],0]
    eq2=sp.Function("eq2")
    eq3=sp.Function("eq3")
    eq4=sp.Function("eq4")
    eq2=Eq((a11-K[0])*a+a12*b+a13*c)
    eq3=Eq(a21*a+(a22-K[0])*b+a23*c)
    eq4=Eq(a31*a+a32*b+(a33-K[0])*c)
    display(eq2,eq3,eq4)
    system=Matrix((bm1,bm2,bm3))
    n=sp.solve linear system(system,a,b,c)
    display(n)
    print("If \lambda = \{0\}".format(K[1]))
    b1=[a11-K[1],a12,a13]
    b2=[a21,a22-K[1],a23]
    b3=[a31,a32,a33-K[1]]
    bmat=sp.Matrix((b1,b2,b3))
    display((bmat,d,xmat,e,cmat,f))
    bm1=[a11-K[1],a12,a13,0]
    bm2=[a21,a22-K[1],a23,0]
   bm3=[a31,a32,a33-K[1],0]
    eq2=sp.Function("eq2")
    eq3=sp.Function("eq3")
    eq4=sp.Function("eq4")
    eq2=Eq((a11-K[1])*a+a12*b+a13*c)
    eq3=Eq(a21*a+(a22-K[1])*b+a23*c)
    eq4=Eq(a31*a+a32*b+(a33-K[1])*c)
    display(eq2,eq3,eq4)
    system=Matrix((bm1,bm2,bm3))
   n=sp.solve linear system(system,a,b,c)
    display(n)
    print("Eigen vector")
   j=amat.eigenvects()
   display(j)
if(len(K)==3):
    print("If \lambda = \{0\}".format(K[0]))
    b1=[a11-K[0],a12,a13]
    b2=[a21,a22-K[0],a23]
    b3=[a31,a32,a33-K[0]]
    bmat=sp.Matrix((b1,b2,b3))
    display((bmat,d,xmat,e,cmat,f))
   bm1=[a11-K[0],a12,a13,0]
    bm2=[a21,a22-K[0],a23,0]
```

```
bm3=[a31,a32,a33-K[0],0]
eq2=sp.Function("eq2")
eq3=sp.Function("eq3")
eq4=sp.Function("eq4")
eq2=Eq((a11-K[0])*a+a12*b+a13*c)
eq3=Eq(a21*a+(a22-K[0])*b+a23*c)
eq4=Eq(a31*a+a32*b+(a33-K[0])*c)
display(eq2,eq3,eq4)
system=Matrix((bm1,bm2,bm3))
n=sp.solve linear system(system,a,b,c)
display(n)
print("If \lambda = \{0\}".format(K[1]))
b1=[a11-K[1],a12,a13]
b2=[a21,a22-K[1],a23]
b3=[a31,a32,a33-K[1]]
bmat=sp.Matrix((b1,b2,b3))
display((bmat,d,xmat,e,cmat,f))
bm1=[a11-K[1],a12,a13,0]
bm2=[a21,a22-K[1],a23,0]
bm3=[a31,a32,a33-K[1],0]
eq2=sp.Function("eq2")
eq3=sp.Function("eq3")
eq4=sp.Function("eq4")
eq2=Eq((a11-K[1])*a+a12*b+a13*c)
eq3=Eq(a21*a+(a22-K[1])*b+a23*c)
eq4=Eq(a31*a+a32*b+(a33-K[1])*c)
display(eq2,eq3,eq4)
system=Matrix((bm1,bm2,bm3))
n=sp.solve linear system(system,a,b,c)
display(n)
print("If \lambda = \{0\}".format(K[2]))
b1=[a11-K[2],a12,a13]
b2=[a21,a22-K[2],a23]
b3=[a31,a32,a33-K[2]]
bmat=sp.Matrix((b1,b2,b3))
display((bmat,d,xmat,e,cmat,f))
bm1=[a11-K[2],a12,a13,0]
bm2=[a21,a22-K[2],a23,0]
bm3=[a31,a32,a33-K[2],0]
eq2=sp.Function("eq2")
eq3=sp.Function("eq3")
eq4=sp.Function("eq4")
eq2=Eq((a11-K[2])*a+a12*b+a13*c)
eq3=Eq(a21*a+(a22-K[2])*b+a23*c)
eq4=Eq(a31*a+a32*b+(a33-K[2])*c)
display(eq2,eq3,eq4)
system=Matrix((bm1,bm2,bm3))
```

```
n=sp.solve linear system(system,a,b,c)
       display(n)
       print("Eigen vector")
       j=amat.eigenvects()
       display(j)
elif inum==4:
              ----Welcome to Eigen value and Eigen vector Calculation---- ')
    print('
    print('1. Vector method\n2. Matrix method')
   ornum=int(input('Enter method to do Orthogonalization'))
   if ornum==1:
       mv1, mv2, mv3, eq=sp.symbols('||V1|| ||V2|| ||V3|| =')
       su1, su2, su3, sv1, sv2, sv3=sp.symbols('U1 U2 U3 V1 V2 V3')
       bu1,bu2,bu3=Bra('U1'),Bra('U2'),Bra('U3')
       bv1,bv2,bv3=Bra('V1'),Bra('V2'),Bra('V3')
       ku1,ku2,ku3=Ket('U1'),Ket('U2'),Ket('U3')
       kv1,kv2,kv3=Ket('V1'),Ket('V2'),Ket('V3')
       u1=Matrix(list(map(int,input('Vector 1 :').split())))
       u2=Matrix(list(map(int,input('Vector 2 :').split())))
       u3=Matrix(list(map(int,input('Vector 3 :').split())))
       print('Let the given vectors be {u1,u2,u3}')
       display((u1,u2,u3))
       eq1=Eq(su1,sv1)
       display(eq1)
       display((sv1,eq,u1))
       v1=u1
       print('For our convinience we first find self inner products of v1')
       v1s=v1.dot(v1)
       ev1s=Bra(v1)*Ket(v1)
       display((mv1**2,eq,bv1*kv1,eq,ev1s,eq,v1s))
       eq2=(((su2-((bu2*kv1)/(mv1**2))*su1)))
       display((sv2,eq,eq2))
       u2v1=u2.dot(v1)
       display((bu2*kv1,eq,Bra(u2)*Ket(v1),eq,u2v1))
       div1=u2v1/v1s
       v2=u2-(div1*v1)
       display((sv2,eq,v2))
       v2s=v2.dot(v2)
       display((bv2*kv2,eq,Bra(v2)*Ket(v2),eq,v2s))
       eq3=((su3-(((bu3*kv1/(mv1**2))*sv1)-((bu3*kv2)/(mv2**2))*sv2)))
       display((sv3,eq,eq3))
       u3v1=u3.dot(v1)
```

```
u3v2=u3.dot(v2)
    display((bu3*kv1,eq,Bra(u3)*Ket(v1),eq,u3v1))
   display((bu3*kv2,eq,Bra(u3)*Ket(v2),eq,u3v2))
    v2s=v2.dot(v2)
    ev2s=Bra(v2)*Ket(v2)
    display((mv2**2,eq,bv2*kv2,eq,ev2s,eq,v2s))
    div2=u3v1/v1s
    div3=u2v1/v2s
   v3=u3-(div2*v1)-(div3*v2)
   display((sv3,eq,v3))
   v3s=v3.dot(v3)
    ev3s=Bra(v3)*Ket(v3)
    display((mv3**2,eq,bv3*kv3,eq,ev3s,eq,v3s))
    print('Orthogonal Vectors We Got')
    display((v1,v2,v3))
    print('Orthonormal Basis')
    w1, w2, w3, mul, div=sp.symbols('w1 w2 w3 * /')
    display((w1,eq,(sv1/mv1)))
    display((w2,eq,(sv2/mv2)))
    display((w3,eq,(sv3/mv3)))
   W1=v1/sqrt(v1s)
   W2=v2/sqrt(v2s)
   W3=v3/sqrt(v3s)
    display((w1,eq,v1,div,sqrt(v1s)))
    display((w1,eq,W1))
    display((w2,eq,v2,div,sqrt(v2s)))
    display((w2,eq,W2))
   display((w3,eq,v3,div,sqrt(v3s)))
    display((w3,eq,W3))
   print('The obtained Orthonormal Basis is ')
    display((W1,W2,W3))
    quit()
elif ornum==2:
   mv1, mv2, mv3, eq=sp.symbols('||V1|| ||V2|| ||V3|| =')
   su1, su2, su3, sv1, sv2, sv3=sp.symbols('U1 U2 U3 V1 V2 V3')
    bv1,bv2,bv3=Bra('V1'),Bra('V2'),Bra('V3')
    bu1, bu2, bu3=Bra('U1'), Bra('U2'), Bra('U3')
    ku1,ku2,ku3=Ket('U1'),Ket('U2'),Ket('U3')
   kv1,kv2,kv3=Ket('V1'),Ket('V2'),Ket('V3')
    w1, w2, w3, mul, div=sp.symbols('w1 w2 w3 * /')
   all,al2,a21,a22=map(int,input('Enter the matrix elements of A : ').split())
    b11,b12,b21,b22=map(int,input('Enter the matrix elements of A : ').split())
   c11,c12,c21,c22=map(int,input('Enter the matrix elements of A : ').split())
    ar1,ar2=[a11,a12],[a21,a22]
    br1,br2=[b11,b12],[b21,b22]
```

```
cr1,cr2=[c11,c12],[c21,c22]
print('Let u1 , u2 and u3 be given basis')
matu1=Matrix((ar1,ar2))
display(matu1)
matu2=Matrix((br1,br2))
display(matu2)
matu3=Matrix((cr1,cr2))
display(matu3)
matv1=matu1
display((sv1,eq,su1))
display((sv1,eq,matv1))
mev1s=Bra(Transpose(matv1))*Ket(Transpose(Transpose(matv1)))
mv1s=trace(Transpose(matv1)*matv1)
display((mv1**2,eq,bv1*kv1,eq,mev1s,eq,Trace(Transpose(matv1)*matv1),eq,mv1s))
eq2=Eq(((su2-((bu2*kv1)/(mv1**2))*su1)),sv2)
display(eq2)
mu2mv1=trace(Transpose(matu2)*matv1)
display((bu2*kv1,eq,Bra(Transpose(matv1))*Ket(Transpose(Transpose(matu2))),eq,Trace(Transpose(matv1)*matu2),eq,mu2mv1))
mdiv1=mu2mv1/mv1s
matv2=matu2-(matu1*mdiv1)
display((sv2,eq,matv2))
mev2s=Bra(Transpose(matv2))*Ket(Transpose(Transpose(matv2)))
mv2s=trace(Transpose(matv2)*matv2)
display((mv2**2,eg,bv2*kv2,eg,mev2s,eg,Trace(Transpose(matv2)*matv2),eg,mv2s))
eq3=((su3-(((bu3*kv1)/(mv1**2))*sv1)-((bu3*kv2)/(mv2**2))*sv2))
display((eq3,eq,sv3))
mu3mv1=trace(Transpose(matv1)*matu3)
mu3mv2=trace(Transpose(matv2)*matu3)
display((bu3*kv1,eq,Bra(Transpose(matv1))*Ket(Transpose(Transpose(matu3))),eq,Trace(Transpose(matv1)*matu3),eq,mu3mv1))
display((bu3*kv2,eq,Bra(Transpose(matv2))*Ket(Transpose(Transpose(matu3))),eq,Trace(Transpose(matv2)*matu3),eq,mu3mv2))
mdiv2=mu3mv1/mv1s
mdiv3=mu3mv2/mv2s
matv3=matu3-(mdiv2*matv1)-(mdiv3*matv2)
display((sv3,eq,matv3))
mev3s=Bra(Transpose(matv3))*Ket(Transpose(Transpose(matv3)))
mv3s=trace(transpose(matv3)*matv3)
display((mv3**2,eq,bv3*kv3,eq,mev3s,eq,Trace(Transpose(matv3)*matv3),eq,mv3s))
print('Orthogonal basis We Got')
display((matv1, matv2, matv3))
print('Orthonormal Basis')
display((w1,eq,(sv1/mv1)))
display((w2,eq,(sv2/mv2)))
display((w3,eq,(sv3/mv3)))
matW1=matv1/sqrt(mv1s)
matW2=matv2/sqrt(mv2s)
matW3=matv3/sqrt(mv3s)
display((w1,eq,matv1,div,sqrt(mv1s)))
```

```
display((w1,eq,matW1))
       display((w2,eq,matv2,div,sqrt(mv2s)))
        display((w2,eq,matW2))
       display((w3,eq,matv3,div,sqrt(mv3s)))
       display((w3,eq,matW3))
        print('The obtained Orthonormal Basis is ')
        display((matW1,matW2,matW3))
        quit()
elif inum==5:
   print('
                               ----Welcome To Calculate OR decomposition----
   mv1, mv2, mv3, eq=sp.symbols('||u1|| ||u2|| ||u3|| =')
    su1, su2, su3, sv1, sv2, sv3=sp.symbols('a1 a2 a3 u1 u2 u3')
    bv1,bv2,bv3=Bra('u1'),Bra('u2'),Bra('u3')
    ku1,ku2,ku3=Ket('a1'),Ket('a2'),Ket('a3')
    kv1,kv2,kv3=Ket('u1'),Ket('u2'),Ket('u3')
   u1=list(map(int,input('coloumn 1 :').split()))
    u2=list(map(int,input('coloumn 2 :').split()))
    u3=list(map(int,input('coloumn 3 :').split()))
    amat=transpose(Matrix((u1,u2,u3)))
    display(amat)
    miu1,miu2,miu3=Matrix(u1),Matrix(u2),Matrix(u3)
    print('Let the given vectors be {a1,a2,a3}')
    display((u1,u2,u3))
    eq1=Eq(su1,sv1)
    display(eq1)
    display((sv1,eq,miu1))
    v1=miu1
    print('For our convinience we first find self inner products of v1')
    v1s=simplify(v1.dot(v1))
    ev1s=Bra(v1)*Ket(v1)
    display((mv1**2,eq,bv1*kv1,eq,ev1s,eq,v1s))
   eq2=Eq(((su2-((bv2*ku1)/(mv1**2))*su1)),sv2)
    display(eq2)
   u2v1=simplify(miu2.dot(v1))
    display((bv1*ku2,eq,Bra(u2)*Ket(v1),eq,u2v1))
    div1=simplify((u2v1/v1s))
   v2=simplify(miu2-(div1*v1))
   display((sv2,eq,v2))
   v2s=simplify(v2.dot(v2))
   display((bv2*kv2,eq,Bra(v2)*Ket(v2),eq,v2s))
   eq3=((su3-(((bv3*ku1)/(mv1**2))*sv1)-((bv3*ku2)/(mv2**2))*sv2))
    display((eq3,eq,sv3))
    u3v1=simplify(miu3.dot(v1))
    u3v2=simplify(miu3.dot(v2))
```

```
display((bv3*ku1,eq,Bra(u3)*Ket(v1),eq,u3v1))
display((bv3*ku2,eq,Bra(u3)*Ket(v2),eq,u3v2))
v2s=simplify(v2.dot(v2))
ev2s=Bra(v2)*Ket(v2)
display((mv2**2,eq,bv2*kv2,eq,ev2s,eq,v2s))
div2=simplify((u3v1/v1s))
div3=simplify((u3v2/v2s))
v3=simplify((miu3-(div2*v1)-(div3*v2)))
display((sv3,eq,v3))
v3s=simplify(v3.dot(v3))
ev3s=Bra(v3)*Ket(v3)
display((mv3**2,eq,bv3*kv3,eq,ev3s,eq,v3s))
print('Orthogonal Vectors We Got')
display((v1,v2,v3))
print('Orthonormal Basis')
w1, w2, w3, mul, div=sp.symbols('w1 w2 w3 * /')
display((w1,eq,(sv1/mv1)))
display((w2,eq,(sv2/mv2)))
display((w3,eq,(sv3/mv3)))
W1=simplify(v1/sqrt(v1s))
W2=simplify(v2/sqrt(v2s))
W3=simplify(v3/sqrt(v3s))
display((w1,eq,v1,div,simplify(sqrt(v1s))))
display((w1,eq,W1))
display((w2,eq,v2,div,simplify(sqrt(v2s))))
display((w2,eq,W2))
display((w3,eq,v3,div,simplify(sqrt(v3s))))
display((w3,eq,W3))
display((W1,W2,W3))
sq,sr,sa,st=symbols('Q R A T')
display((sq,eq,(((sv1/mv1)),((sv2/mv2)),((sv3/mv3)))))
display((sq,eq,transpose(Matrix((list(W1),list(W2),list(W3))))))
bw1,bw2,bw3=Bra('w1'),Bra('w2'),Bra('w3')
rmmat=Matrix(([bw1*ku1,bw1*ku2,bw1*ku3],[0,bw2*ku2,bw2*ku3],[0,0,bw3*ku3]))
display((sr,eq,rmmat))
a1w1=simplify(miu1.dot(W1))
display((bw1*ku1,eq,Bra(W1)*Ket(miu1),eq,a1w1))
a2w1=simplify(miu2.dot(W1))
display((bw1*ku2,eq,Bra(W1)*Ket(miu2),eq,a2w1))
a3w1=simplify(miu3.dot(W1))
display((bw1*ku3,eq,Bra(W1)*Ket(miu3),eq,a3w1))
a2w2=simplify(miu2.dot(W2))
display((bw2*ku2,eq,Bra(W2)*Ket(miu2),eq,a2w2))
a3w2=simplify(miu3.dot(W2))
display((bw2*ku3,eq,Bra(W2)*Ket(miu3),eq,a3w2))
a3w3=simplify(miu3.dot(W3))
```

```
display((bw3*ku3,eq,Bra(miu3)*Ket(W3),eq,a3w3))
     rmat=Matrix(([a1w1,a2w1,a3w1],[0,a2w2,a3w2],[0,0,a3w3]))
     print('One Last Check')
     display((sa,eq,sq*sr,eq,transpose(Matrix((list(W1),list(W2),list(W3)))),mul,rmat,eq,transpose(Matrix((list(W1),list(W2),list(W3))))*rmat)
     quit()
                         ----Welcome to Linear Algebra Calculator Material----
1 -- UNIT-I -- SOLVING SYSTEM OF LINEAR EQUATIONS
2 -- UNIT-II -- LINEAR DEPENDANCY AND BASIS FORMATION CHECKING
3 -- UNIT-III -- FINDING EIGEN VALUE AND EIGEN VECTOR
4 -- UNIT-IV -- ORTHOGONALIZATION
5 -- UNIT-V -- OR DECOMPOSITION
Enter Your Choice of Chapter: 3
Enter the matrix coefficients : 2 2 1 1 3 1 1 2 2
Input matrix
    2 \quad 1
     3 1
 \begin{bmatrix} 1 & 2 & 2 \end{bmatrix}
'S1=2+3+2'
's1=7'
's2=(((3*2)-(2*1))+((2*2)-(1*1))+((2*3)-(1*2))'
's2=(4+3+4)'
's3=det(amat)'
's3=5'
's1=7 s2=11 s3=5'
c:\users\elcot\appdata\local\programs\python\python39\lib\site-packages\sympy\core\relational.py:495: SymPyDeprecationWarning:
Eq(expr) with rhs default to 0 has been deprecated since SymPy 1.5.
Use Eq(expr, 0) instead. See
https://github.com/sympy/sympy/issues/16587 for more info.
 SymPyDeprecationWarning(
\lambda^3 - 7\lambda^2 + 11\lambda - 5 = 0
(\lambda - 5) \left(\lambda - 1\right)^2 = 0
Eigen values are : [1, 5]
To find eigen vector
```

$$\begin{bmatrix} 2-\lambda & 2 & 1 \\ 1 & 3-\lambda & 1 \\ 1 & 2 & 2-\lambda \end{bmatrix}$$

*

$$\begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

If
$$\lambda=1$$

$$\left(\begin{bmatrix}1&2&1\\1&2&1\\1&2&1\end{bmatrix}, *, \begin{bmatrix}a\\b\\c\end{bmatrix}, =, \begin{bmatrix}0\\0\\0\end{bmatrix}, ->\right)$$

$$a + 2b + c = 0$$

$$a + 2b + c = 0$$

$$a + 2b + c = 0$$

$$\{a:-2b-c\}$$

If $\lambda=5$

$$\left(\begin{bmatrix} -3 & 2 & 1 \\ 1 & -2 & 1 \\ 1 & 2 & -3 \end{bmatrix}, *, \begin{bmatrix} a \\ b \\ c \end{bmatrix}, =, \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}, -> \right)$$

$$-3a + 2b + c = 0$$

$$a - 2b + c = 0$$

$$a + 2b - 3c = 0$$

$${a:c, b:c}$$

Eigen vector

$$\left[\left(1, \ 2, \ \left[\begin{bmatrix} -2 \\ 1 \\ 0 \end{bmatrix}, \ \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} \right] \right), \ \left(5, \ 1, \ \left[\begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \right) \right) \right]$$