MATHEMATICS FOR SCIENCE STUDENTS

An open-source book

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$$a^{b} = e^{b \log(a)}$$

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$T(\alpha \vec{u} + \beta \vec{v}) = \alpha T(\vec{u}) + \beta T(\vec{v})$$

$$A = Q\Lambda Q^{-1}$$

$$Cos(\theta) = \cos(\theta) \cos(\theta)$$

$$\sin(\theta) \cos(\theta)$$

$$e^{\pi i} + 1 = 0$$

$$T(\alpha \vec{u} + \beta \vec{v}) = \alpha T(\vec{u}) + \beta T(\vec{v})$$

$$df = \lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

$$\vec{v} = \sum_{i=1}^{n} \alpha_{i} \hat{e}_{i}$$

$$cos(x) = \sum_{n=0}^{\infty} \frac{(-1)^{n}}{(2n)!} x^{2n}$$

PUBLISHED IN THE WILD

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HERE BE TABLE



INTRODUCTION

In this chapter we introduce key concepts that will be used in later chapters. For this reason, unlike other chapters it contains many statements, sometimes given without thorough explanations or reasoning. While all of these statements are grounded in deep ideas and can be formulated in a rigorous manner, it is advised to first get an intuitive understanding of the ideas before diving into their more formal construction.

Note 0.1 In case you are already familiar with the topics

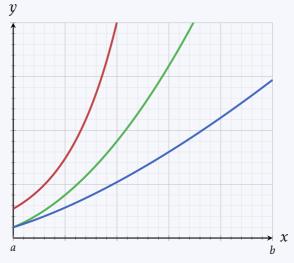
It is recommended for readers who are familiar with the topics to at least gloss over this chapter and make sure they know and understand all the concepts presented here.

0.1 DERIVATIVES

One of the most important tool in analyzing a function $f : \mathbb{R} \to \mathbb{R}$ is the ability to quantitatively describe the way it behaves as we change its argument x. At any given point a function can either increase in its value, decrease in its value, or stay constant. We would like to develop a method that is able to tell us exactly how such function changes at any given point.

Example 0.1 Quantitative measure of change

Compare the following three functions on the domain $x \in [a, b]$:



While all three functions are increasing on [a,b], it is clear that the rate of increase between the functions is different: the red function increases faster than the green one, which in turn increases faster than the blue one. In fact, even within each function the increase is not uniform: the more x increases so does the rate of increase of the function.

To start developing a method to quantitatively measure the rate of increase of a function, we can first consider one of the simplest functions: $f(x) = x^2$. If we "zoom in" on any point of the function we would see that it "straightens out" - the more we zoom in, the more it looks like a straight line (??).

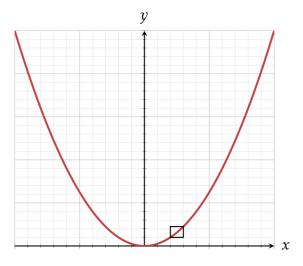


Figure 0.1