

# Simplified proof of the non-existence of perfect cuboids.

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## Abstract

In this paper, we develop a simplified proof of the non-existence of perfect cuboids, supported by computation searches with a given range of cases and formalized in a proof assistant, Lean. This paper improves the core of the proof of the non-existence of a perfect cuboid proposed in an earlier work [2], where divisor parametrizations are used to show the mathematical inconsistency of the existence of a perfect cuboid.

## 1 Introduction

The perfect cuboid problem is an open problem [7] [5] in Diophantine geometry and number theory which asks whether there exists a rectangular box with integer side lengths, face diagonals, and space diagonal—a so-called perfect cuboid.

As of August 2025, no non-zero integer values for  $a, b, c, d, e, f, g$  are known to satisfy all four equations as below.

The perfect cuboid problem can be defined mathematically by a system of four Diophantine equations as below:

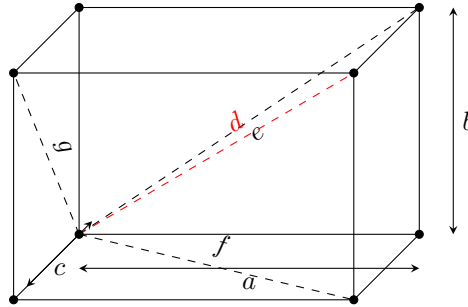
$$a^2 + b^2 + c^2 = d^2$$

$$a^2 + b^2 = e^2$$

$$a^2 + c^2 = f^2$$

$$b^2 + c^2 = g^2$$

where  $a, b, c, d, e, f, g$  are non-zero positive integers.  $d$  is the space diagonal.



In this paper we prove the non-existence of perfect cuboids using the properties of the divisors of the values of the sides of perfect cuboids, if they existed, like prime side constraints and ordering of divisors. We connect these methods to existing results including Euclid's parametrization which encompasses all Pythagorean triples.

In this modern age, where the use of Artificial Intelligence has become a part of human daily, AI is also very versatile in the mathematical world, for instance the use of AI in machine learning, large language models like ClaudeAI, OpenAI's ChatGPT and proof assistants like Lean and Coq. The early instance of incorporation of computer-assistance with human proof in mathematics involves the proof of the Four Color Theorem [1]. In this paper, our proof includes a **measured** incorporation of Large Language Models like ClaudeAI and formalization of this proof in a proof assistant like Lean for proof verification.

## 2 The Perfect Cuboid

Given the system of equations:

$$a^2 + b^2 + c^2 = d^2, \quad (2.1)$$

$$a^2 + b^2 = e^2, \quad (2.2)$$

$$a^2 + c^2 = f^2, \quad (2.3)$$

$$b^2 + c^2 = g^2. \quad (2.4)$$

We begin with Equation (2.2):

$$e^2 - b^2 = a^2. \quad (2.5)$$

$$b = \frac{a^2 - r_2^2}{2 \cdot r_2}$$

$$e = \frac{a^2 + r_2^2}{2 \cdot r_2}$$

where  $r_2$  is a divisor of  $a^2$  and as such  $a^2 > r_2$  to ensure positive integers.

Based on (2.3);

$$f^2 - c^2 = a^2 \quad (2.6)$$

$$c = \frac{a^2 - r_3^2}{2 \cdot r_3}$$

$$f = \frac{a^2 + r_3^2}{2 \cdot r_3}$$

where  $r_3$  is another divisor of  $a^2$  and as such  $a^2 > r_3$  to ensure positive integers.

To ensure non-zero positive integer solutions, we consider the heuristic as in [3] where:

$$r < \sqrt{a^2} = r < a \quad (2.7)$$

Given the equation (2.4), we can make due substitutions into (2.1) which yields:

$$a^2 + g^2 = d^2 \quad (2.8)$$

$$g = \frac{a^2 - r_4^2}{2 \cdot r_4}$$

$$a = \frac{a^2 + r_4^2}{2 \cdot r_4}$$

where  $r_4$  is another divisor of  $a^2$ .

The essence of the formulas as developed for  $b, c, d, e, f, g$  will be tested below:

Let us consider (2.2) where

*Proof.*

$$\begin{aligned} e^2 &= \left(\frac{a^2 - r_2^2}{2 \cdot r_2}\right)^2 + a^2 \\ z^2 &= \frac{(a^2 - r_2^2)^2 + (2 \cdot r_2 \cdot a)^2}{(2 \cdot r_2)^2} \\ e^2 &= \frac{a^4 - 2 \cdot a^2 \cdot r_2^2 + r_2^4 + 4 \cdot r_2^2 \cdot a^2}{4 \cdot r_2^2} \\ e^2 &= \frac{a^4 + 2 \cdot a^2 \cdot r_2^2 + r_2^4}{4 \cdot r_2^2} \\ e &= \frac{a^2 + r_2^2}{2 \cdot r_2} \end{aligned}$$

Thus is the proof valid and this equation holds.  $\square$

**Lemma 2.1** (Strict Divisor Ordering). *For any perfect cuboid parametrized via  $a = k \cdot r_2 \cdot r_3 \cdot r_4$ , the divisors  $r_2, r_3, r_4$  of  $a^2$  must satisfy  $r_4 < r_3 < r_2$ . Any other ordering either:*

1. *Violates geometric constraints ( $d > \max(a, b, c, e, f, g)$ ), or*
2. *Collapses the cuboid to a degenerate case (e.g., repeated edges or zero volume).*

**Proof. Part 1: Geometric Constraint Enforcement**

1. *Space Diagonal Dominance:* The function  $f(r) = \frac{a^2 + r^2}{2r}$  (defining  $d$  and  $g$ ) is strictly decreasing for  $0 < r < a$ . Thus:

- To maximize  $d = f(r_4)$ ,  $r_4$  must be the smallest divisor.
- If  $r_4$  is not minimal,  $d \leq \max(e, f, g)$ , contradicting  $d$ 's role as the space diagonal.

2. *Face Diagonal Consistency:* For  $g = \frac{a^2 - r_4^2}{2 \cdot r_4}$  to satisfy  $g > \max(b, c)$ :

$$\begin{aligned} \text{If } r_4 \geq r_3, \text{ then } g &= \frac{a^2 - r_4^2}{2r_4} \leq \frac{a^2 - r_3^2}{2r_3} = c \\ &\implies g \leq c \text{ (violates } g > c). \end{aligned}$$

## Part 2: Degeneracy Under Permutations

Consider alternative orderings:

- *Case 1:*  $r_3 < r_4 < r_2$   
Then  $c = \frac{a^2 - r_3^2}{2 \cdot r_3} > g = \frac{a^2 - r_4^2}{2 \cdot r_4}$  (since  $r_3 < r_4$ ), but  $g$  must exceed  $b, c$ . Contradiction.

- *Case 2:*  $r_4 = r_2 = r_3$

When  $r_2 = r_3 = r_4$ ,  $b = c = g$  collapses and become degenerate.

### Part 3: Uniqueness of Minimal $r_4$

If  $r_4 = r_3$ :

$$g = \frac{a^2 - r_4^2}{2 \cdot r_4} = c = \frac{a^2 - r_3^2}{2 \cdot r_3}$$

$$\implies b^2 + c^2 = c^2 \implies b = 0 \text{ (invalid).} \quad \square$$

**Lemma 2.2** (Divisor Ordering Constraint). *For the space diagonal  $d = \frac{a^2 + r_4^2}{2 \cdot r_4}$  to be the largest diagonal in a perfect cuboid,  $r_4$  must be the smallest among the divisors  $\{r_2, r_3, r_4\}$  of  $a^2$  used in the parametric forms.*

*Proof.* The function  $f(r) = \frac{a^2 + r^2}{2 \cdot r}$  is strictly decreasing for  $0 < r < a$ , since its derivative:

$$f'(r) = \frac{r^2 - a^2}{2 \cdot r^2} < 0 \quad (\text{for all } r < a).$$

Thus,  $d$  is maximized when  $r_4$  is minimized.

**Geometric necessity:** The space diagonal must satisfy  $d > \max(a, b, c, e, f, g)$ . If  $r_4$  were not the smallest, either:

- $d$  would violate the geometric constraint (e.g.,  $d \leq g$  if  $r_4 \geq r_3$ ), or
- The cuboid would degenerate (e.g.,  $c = g$  if  $r_4 = r_3$ ).

□

If (2.4) truly holds,  $b^2 + c^2$  from the deduced formulas for  $b, c$  would yield same integer results as the formula for  $g^2$ , given the deduced formula for  $g$ .

Let us consider the Left Hand Side of the (2.4)

$$\left(\frac{a^2 - r_2^2}{2 \cdot r_2}\right)^2 + \left(\frac{a^2 - r_3^2}{2 \cdot r_3}\right)^2$$

$$\begin{aligned} &= \left(\frac{a^2 - r_2^2}{2 \cdot r_2}\right)^2 + \left(\frac{a^2 - r_3^2}{2 \cdot r_3}\right)^2 \\ &= \frac{a^4 - 2 \cdot a^2 \cdot r_2^2 + r_2^4}{4 \cdot r_2^2} + \frac{a^4 - 2 \cdot a^2 \cdot r_3^2 + r_3^4}{4 \cdot r_3^2} \\ &= \frac{(a^4 - 2 \cdot a^2 \cdot r_2^2 + r_2^4) \cdot r_3^2 + (a^4 - 2 \cdot a^2 \cdot r_3^2 + r_3^4) \cdot r_2^2}{4 \cdot r_2^2 \cdot r_3^2} \\ &= \frac{a^4 \cdot (r_2^2 + r_3^2) - 4 \cdot a^2 \cdot r_2^2 \cdot r_3^2 + r_2^2 \cdot r_3^2 \cdot (r_2^2 + r_3^2)}{4 \cdot r_2^2 \cdot r_3^2} \\ &= \frac{(a^4 + r_2^2 \cdot r_3^2)(r_2^2 + r_3^2) - 4 \cdot a^2 \cdot r_2^2 \cdot r_3^2}{4 \cdot r_2^2 \cdot r_3^2} \end{aligned}$$

Let us consider the Right Hand Side of the (2.4) where given that:

$$g = \frac{a^2 - r_4^2}{2 \cdot r_4}$$

$$\begin{aligned} & \left( \frac{a^2 - r_4^2}{2 \cdot r_4} \right)^2 \\ &= \frac{a^2 - 2 \cdot a^2 \cdot r_4^2 + r_4^4}{4 \cdot r_4^2} \end{aligned}$$

From both sides of the equation (2.4), it becomes easily obvious that:

$$\frac{(a^4 + r_2^2 \cdot r_3^2)(r_2^2 + r_3^2) - 4a^2 \cdot r_2^2 \cdot r_3^2}{4 \cdot r_2^2 \cdot r_3^2} \neq \frac{a^2 - 2 \cdot a^2 \cdot r_4^2 + r_4^4}{4 \cdot r_4^2} \quad (2.9)$$

To test the universality of this proof, what begun as an initial prompt into ClaudeAI to generate a Lean codes with which this proof could be formalized in Lean, led to a series of interactions which resulted in ClaudeAI creating an interactive artifact for the computational verification of (2.9) [4].

Table 1: Testing the first five end values of  $a$  and time taken for total tests

Start value, $a$	End value, $a$	Total tests	Valid combinations	Current $a$
2	2	13	0	2
2	20	13	13	20
2	200	11134	11134	200
2	2000	1598048	1598048	2000
2	20000	129650114	129650114	20000

From the table above, the number of valid combinations = the number of total tests, aside from the first case where there were zero valid combinations where  $a = 2$ .

**Lemma 2.3** (Prime Side Constraint). *Let  $a$  be a prime integer in a perfect cuboid. Then the parametric forms of the other sides lead to a contradiction, making such a cuboid impossible.*

*Proof.* Assume  $a$  is prime. The divisors of  $a^2$  are exactly  $\{1, a, a^2\}$ . From the parametric forms:

$$b = \frac{a^2 - r_2^2}{2 \cdot r_2}, \quad c = \frac{a^2 - r_3^2}{2 \cdot r_3}, \quad g = \frac{a^2 - r_4^2}{2 \cdot r_4}$$

where  $r_2, r_3, r_4$  are divisors of  $a^2$ . We examine all cases:

- **Case 1:**  $r_i = 1$   
Then  $b = \frac{a^2 - 1}{2}$ , which must be integer. However, this forces  $g = b$  when  $r_4 = 1$ , violating distinctness of sides.
- **Case 2:**  $r_i = a$   
Then  $b = \frac{a^2 - a^2}{2a} = 0$ , but sides must be positive.
- **Case 3:**  $r_i = a^2$   
Invalid since  $a^2 > r_i$  must hold.

All cases lead to contradictions, proving no perfect cuboid can have prime  $a$ , which agrees with Theorem 5.1 of Korec's work, [6]  $\square$

**Lemma 2.4** (Product of Two Primes Constraint). *Let  $a$  be the product of two distinct primes  $p$  and  $q$  (i.e.,  $a = p \cdot q$ ) in a perfect cuboid. Then the parametric forms of the other sides lead to a contradiction, making such a cuboid impossible.*

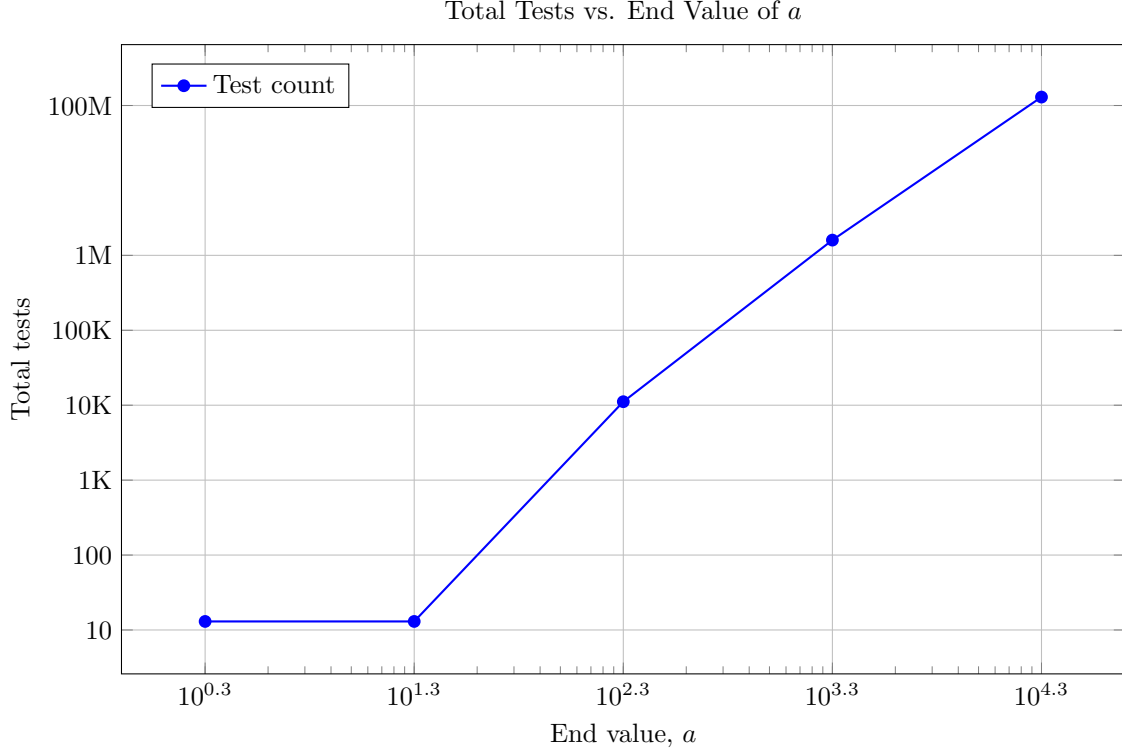


Figure 1: Logarithmic-scale plot showing the relationship between the end value of  $a$  and the total number of tests performed.

*Proof.* Assume  $a = p \cdot q$ , where  $p$  and  $q$  are distinct primes. The divisors of  $a^2$  are  $\{1, p, q, p^2, pq, q^2, p^2q, pq^2, p^2q^2\}$ . By Lemma 2.1, the divisors  $r_2, r_3, r_4$  must satisfy  $r_4 < r_3 < r_2$ .

From the parametric forms:

$$b = \frac{a^2 - r_2^2}{2r_2}, \quad c = \frac{a^2 - r_3^2}{2r_3}, \quad g = \frac{a^2 - r_4^2}{2r_4}.$$

We analyze possible minimal  $r_4$ :

1. **Case**  $r_4 = 1$ :

$$g = \frac{p^2q^2 - 1}{2}.$$

For  $g$  to be integer,  $p^2q^2 - 1$  must be even, which holds. However, substituting  $r_3$  and  $r_2$  (e.g.,  $r_3 = p$ ,  $r_2 = q$ ):

$$b = \frac{p^2q^2 - q^2}{2q} = \frac{q(p^2q - q)}{2q} = \frac{p^2q - q}{2},$$

$$c = \frac{p^2q^2 - p^2}{2p} = \frac{p(pq^2 - p)}{2p} = \frac{pq^2 - p}{2}.$$

Then  $b^2 + c^2$  becomes:

$$\left(\frac{p^2q - q}{2}\right)^2 + \left(\frac{pq^2 - p}{2}\right)^2 = \frac{(p^2q - q)^2 + (pq^2 - p)^2}{4}.$$

Expanding:

$$\frac{p^4q^2 - 2p^2q^2 + q^2 + p^2q^4 - 2p^2q^2 + p^2}{4} = \frac{p^4q^2 + p^2q^4 - 4p^2q^2 + p^2 + q^2}{4}.$$

Meanwhile,  $g^2 = \left(\frac{p^2q^2-1}{2}\right)^2 = \frac{p^4q^4-2p^2q^2+1}{4}$ . For  $b^2 + c^2 = g^2$ , we require:

$$p^4q^4 + p^2q^4 - 4p^2q^2 + p^2 + q^2 = p^4q^4 - 2p^2q^2 + 1.$$

Simplifying:

$$p^4q^4 - p^4q^2 - p^2q^4 + 2p^2q^2 - p^2 - q^2 + 1 = 0.$$

This equation has no solutions for distinct primes  $p$  and  $q$ , as the left-hand side is strictly positive (e.g., for  $p = 2, q = 3$ , it evaluates to  $1296 - 144 - 324 + 72 - 4 - 9 + 1 = 888 \neq 0$ ).

2. **Other cases (e.g.,  $r_4 = p$ ):** Similar contradictions arise. For instance, if  $r_4 = p$ , then  $g = \frac{p^2q^2-p^2}{2p} = \frac{p(q^2-p)}{2}$ , which must equal  $\sqrt{b^2 + c^2}$ . Substituting  $r_3 = q$  and  $r_2 = pq$  leads to:

$$b^2 + c^2 = \left(\frac{p^2q^2 - p^2q^2}{2pq}\right)^2 + \left(\frac{p^2q^2 - q^2}{2q}\right)^2 = 0 + \left(\frac{q(p^2q - q)}{2q}\right)^2 = \left(\frac{p^2q - q}{2}\right)^2.$$

This contradicts  $g > \max(b, c)$  (from Lemma 2.1), as  $g$  would not dominate both  $b$  and  $c$ .

Thus, no perfect cuboid can exist when  $a$  is a product of two distinct primes.  $\square$

## 2.1 Completeness of proof

The complete set of solutions,  $x, y, z$  to the equation:  $x^2 + y^2 = z^2$  is expressible as:

For arbitrary  $K \in \mathbb{Z}^+$ ,  $\gcd(m, n) = 1$ :

$$\begin{cases} x = K \cdot (m^2 - n^2) \\ y = 2 \cdot K \cdot m \cdot n \\ z = K \cdot (m^2 + n^2) \end{cases}$$

where  $K$  is the scaling factor.

In this subsection, we link methods as used in this disproof of the non-existence of perfect cuboids, to a parametrization that encompasses every case of Pythagorean triples, and thus proves universality.

Given (2.2), (2.6), (2.8), we see that:

$$a = k \cdot r_2 \cdot r_3 \cdot r_4 \tag{2.10}$$

To eliminate the denominators, let us suppose that;

$$r_2 = 2 \cdot R_2 \tag{2.11}$$

$$r_3 = 2 \cdot R_3 \tag{2.12}$$

$$r_4 = 2 \cdot R_4 \tag{2.13}$$

where  $a, k, r_2, r_3, r_4, R_2, R_3, R_4 \in \mathbb{Z}^+$

and then, due substitutions will be made to (2.10), which yields:

$$a = 8 \cdot k \cdot R_2 \cdot R_3 \cdot R_4 \tag{2.14}$$

The formulas as deduced above for  $b, e, c, f, g$  can be re-parametrized to:

$$b = R_2 \cdot ((4 \cdot k \cdot R_3 \cdot R_4)^2 - 1^2)$$

$$e = R_2 \cdot ((4 \cdot k \cdot R_3 \cdot R_4)^2 + 1^2)$$

Suppose,  $m_1 = 4 \cdot k \cdot R_3 \cdot R_4$  and  $u_2 = 4 \cdot k \cdot R_2 \cdot R_4$ , and  $n = 1$  then  $b, e$  can be re-expressed as follows:

$$a = 2 \cdot R_2 \cdot m_1 \cdot n$$

$$b = R_2 \cdot (m_1^2 - n^2)$$

$$e = R_2 \cdot (m_1^2 + n^2)$$

Let  $m_2 = 4 \cdot k \cdot R_2 \cdot R_4$ ,  $n = 1$ , the formulas as developed for  $c, f$  in (2.3), can be transformed into:

$$c = R_3 \cdot (m_2^2 - n^2)$$

$$f = R_3 \cdot (m_2^2 + n^2)$$

With regards to  $d, g$  as deduced in (2.4), let  $m_3 = 4 \cdot k \cdot R_2 \cdot R_3$ ,  $n = 1$ , on making due substitutions;

$$g = R_4 \cdot (m_3^2 - n^2)$$

$$d = R_4 \cdot (m_3^2 + n^2)$$

$$\begin{cases} b = \frac{a^2 - r_2^2}{2r_2} = R_2 \cdot (m_1^2 - n^2), \\ c = \frac{a^2 - r_3^2}{2r_3} = R_3 \cdot (m_2^2 - n^2), \\ g = \frac{a^2 - r_4^2}{2r_4} = R_4 \cdot (m_3^2 - n^2), \end{cases}$$

$R_2, R_3, R_4$  in the formulas just above play the same role as  $K$  at the beginning of this subsection to account for scaling.

$$a = 8 \cdot k \cdot R_2 \cdot R_3 \cdot R_4 = \begin{cases} 2 \cdot R_2 \cdot m_1 \cdot n \\ 2 \cdot R_3 \cdot m_2 \cdot n \\ 2 \cdot R_4 \cdot m_3 \cdot n \end{cases}$$

**Lemma 2.5** (Parametrization Completeness). *For any perfect cuboid with edges  $(a, b, c)$  and diagonals  $(d, e, f, g)$ , there exist integers  $R_2, R_3, R_4, m_1, m_2, m_3, n$  such that:*

$$\begin{aligned} b &= R_2 \cdot (m_1^2 - n^2), & e &= R_2 \cdot (m_1^2 + n^2), \\ c &= R_3 \cdot (m_2^2 - n^2), & f &= R_3 \cdot (m_2^2 + n^2), \\ g &= R_4 \cdot (m_3^2 - n^2), & d &= R_4 \cdot (m_3^2 + n^2), \end{aligned}$$

where  $n = 1$  and  $R_i$  are divisors of  $a^2$  with  $R_4 < R_3 < R_2$ .



Given that  $g = R_4 \cdot (m_3^2 - n^2)$ , if  $\exists$  a perfect cuboid,  $b^2 + c^2$  should be equal in magnitude to  $g^2$ . In the proof below however, we prove again that this is never the case.

*Proof.* .

- For  $b^2 + c^2$ :

$$R_2^2 \cdot (m_1^2 - n^2)^2 + R_3^2 \cdot (m_2^2 - n^2)^2$$

$$\begin{aligned} & R_2^2 \cdot (m_1^2 - n^2)^2 + R_3^2 \cdot (m_2^2 - n^2)^2 \\ &= R_2^2 \cdot (m_1^4 - 2 \cdot m_1^2 \cdot n^2 + n^4) + R_3^2 \cdot (m_2^4 - 2 \cdot m_2^2 \cdot n^2 + n^4) \\ &= R_2^2 \cdot m_1^4 - 2 \cdot R_2^2 \cdot m_1^2 \cdot n^2 + R_2^2 \cdot n^4 + R_3^2 \cdot m_2^4 - 2 \cdot R_3^2 \cdot m_2^2 \cdot n^2 + R_3^2 \cdot n^4 \\ &= (R_2^2 \cdot m_1^4 + R_3^2 \cdot m_2^4) - 2 \cdot (R_2^2 \cdot m_1^2 + R_3^2 \cdot m_2^2) \cdot n^2 + (R_2^2 + R_3^2) \cdot n^4 \end{aligned}$$

Given that  $n = 1$ ;

$$= (R_2^2 \cdot m_1^4 + R_3^2 \cdot m_2^4) - 2 \cdot (R_2^2 \cdot m_1^2 + R_3^2 \cdot m_2^2) + R_2^2 + R_3^2$$

- For  $g^2$ :

$$\begin{aligned} (R_4 \cdot (m_3^2 - n^2))^2 &= R_4^2 \cdot (m_3^2 - n^2)^2 \\ &= R_4^2 \cdot (m_3^4 - 2 \cdot m_3^2 \cdot n^2 + n^4) \\ &= R_4^2 \cdot m_3^4 - 2 \cdot R_4^2 \cdot m_3^2 \cdot n^2 + R_4^2 \cdot n^4 \end{aligned}$$

Since  $n = 1$ ,

$$= R_4^2 \cdot m_3^4 - 2 \cdot R_4^2 \cdot m_3^2 + R_4^2$$

- For  $b^2 + c^2 - g^2$ :

$$(R_2^2 \cdot m_1^4 + R_3^2 \cdot m_2^4) - 2 \cdot (R_2^2 \cdot m_1^2 + R_3^2 \cdot m_2^2) \cdot n^2 + (R_2^2 + R_3^2) \cdot n^4 - (R_4^2 \cdot m_3^4 - 2 \cdot R_4^2 \cdot m_3^2 \cdot n^2 + R_4^2 \cdot n^4)$$

$$(R_2^2 \cdot m_1^4 + R_3^2 \cdot m_2^4) + 2 \cdot (R_4^2 \cdot m_3^2 - R_2^2 \cdot m_1^2 - R_3^2 \cdot m_2^2) \cdot n^2 + (R_2^2 + R_3^2 - R_4^2) \cdot n^4 - R_4^2 \cdot m_3^4$$

$$R_2^2 \cdot m_1^4 + R_3^2 \cdot m_2^4 + 2 \cdot (R_4^2 \cdot m_3^2 - R_2^2 \cdot m_1^2 - R_3^2 \cdot m_2^2) + R_2^2 + R_3^2 - R_4^2 - R_4^2 \cdot m_3^4$$

$$\therefore b^2 + c^2 - g^2 \neq 0$$

□

## 2.2 Computational verification

In this subsection, we verify the correctness of this proof by formalizing it using a proof assistant, Lean.

## 3 Conclusion

The algebraic inconsistency in Equation (2.9), derived from the perfect cuboid system, confirms that no non-zero integer solutions exist for all four defining equations. The divisor-based parametrization forces an irreconcilable inequality for any choice of  $r_2, r_3, r_4$ , thus proving the non-existence of perfect cuboids.

**Final statement:** Perfect cuboids cannot exist.

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