**Topic**: Hyperbolic derivatives

Question: Find the derivative of the hyperbolic function.

$$y = \cosh(x^2 - 1)$$

# **Answer choices:**

$$A y' = -2x \sinh(x^2 - 1)$$

$$B y' = -2x \cosh(x^2 - 1)$$

$$C y' = 2x \sinh(x^2 - 1)$$

$$D y' = 2x \cosh(x^2 - 1)$$

# Solution: C

Make a substitution, letting  $u = x^2 - 1$  and u' = 2x. Then  $y = \cosh u$ , and the derivative is

$$y' = \sinh u \cdot u'$$

$$y' = \sinh(x^2 - 1) \cdot (2x)$$

$$y' = 2x \sinh(x^2 - 1)$$



**Topic**: Hyperbolic derivatives

Question: Find the derivative of the hyperbolic function.

$$y = x^2 \sinh x$$

#### **Answer choices:**

$$A y' = x \cosh x + 2 \sinh x$$

$$B y' = x^2 \cosh x + 2x \sinh x$$

$$C y' = x \cosh x - 2 \sinh x$$

$$D y' = x^2 \cosh x - 2x \sinh x$$

### Solution: B

Use the product rule with

$$f(x) = x^2$$

$$f'(x) = 2x$$

and

$$g(x) = \sinh x$$

$$g'(x) = \cosh x$$

Then the derivative is

$$y' = f(x)g'(x) + f'(x)g(x)$$

$$y' = (x^2)(\cosh x) + (2x)(\sinh x)$$

$$y' = x^2 \cosh x + 2x \sinh x$$

**Topic**: Hyperbolic derivatives

Question: Find the derivative of the hyperbolic function.

$$f(x) = \sinh(\cosh(2x))$$

# **Answer choices:**

$$A f'(x) = 2\sinh(2x)\sinh(\sinh(2x))$$

$$B f'(x) = 2\sinh(2x)\cosh(\sinh(2x))$$

C 
$$f'(x) = 2 \sinh(2x) \cosh(\cosh(2x))$$

$$D f'(x) = 2\cosh(2x)\cosh(\cosh(2x))$$

### **Solution**: C

Use a substitution with  $u = \cosh(2x)$  and  $u' = 2\sinh(2x)$ . Then the function can be rewritten as

$$f(x) = \sinh u$$

and the derivative is

$$f'(x) = \cosh u \cdot u'$$

$$f'(x) = \cosh(\cosh(2x)) \cdot (2\sinh(2x))$$

$$f'(x) = 2\sinh(2x)\cosh(\cosh(2x))$$