

Skewness

Skewness can be determined using a formula:

$$\text{Skewness} = \frac{3(\text{Mean} - \text{Median})}{\text{Standard Deviation}}$$

Consider the following data list for days of absences in a class of 10 students:

Days of absences = { 1, 2, 2, 3, 3, 3, 3, 4, 4, 5 }

Median is the middle number which is 3.

Mean is the sum of all numbers divided by 10:

$$1 + 2 + 2 + 3 + 3 + 3 + 3 + 4 + 4 + 5 = 30$$

$$\text{Mean} = 30/10 = 3$$

$$\text{Sample standard deviation} = s = \sqrt{\frac{(x_1 - \bar{x})^2 + (x_2 - \bar{x})^2 + \dots + (x_n - \bar{x})^2}{n-1}} = 1.155$$

$$\text{Skewness} = 3(\text{Mean} - \text{Median})/\text{Standard Deviation} = 3(3 - 3)/1.155 = 0$$

This skewness example has zero skewness, meaning it has symmetry and is shaped like a bell curve.

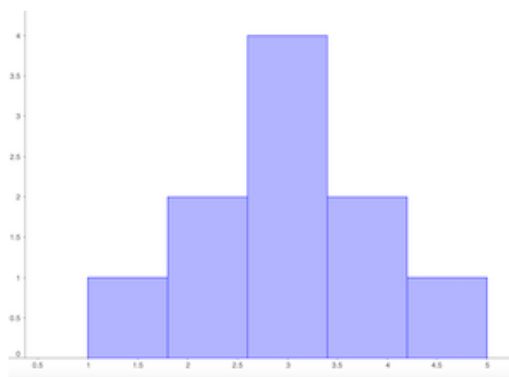


Fig. 2 Histogram showing zero skewness from example 1 data set.

The value for skewness can range from negative infinity to positive infinity.

A **negative value for skewness** indicates that the tail is on the left side of the distribution, which extends towards more negative values.

A **positive value for skewness** indicates that the tail is on the right side of the distribution, which extends towards more positive values.

A **value of zero** indicates that there is no skewness in the distribution at all, meaning the distribution is perfectly symmetrical.