

ICSE 10,2019

AI21BTECH11016

1 PROBLEM 4-C

1.1. Draw a circle of radius 4cm . Take a point P outside the circle at a distance of 7cm from the centre of the circle and construct a pair of tangents to the circle from that point. Measure and write down the length of any one tangent.

Solution: The input parameters for this construction are available in TABLE 1.1.1.

Symbol	Value	Description
r	4	Radius
d	7	Distance of P from the origin
$\sin\theta$	$\frac{r}{d}$	Angle between the tangent from P and d
P	0	Origin
O	$\begin{pmatrix} d \\ 0 \end{pmatrix}$	Center of circle
Q_i	$r \cot \theta \begin{pmatrix} \cos \theta \\ \pm \sin \theta \end{pmatrix}$	Points of Contact

TABLE 1.1.1

$$\begin{aligned}
 &\text{Consider } \triangle OQ_2P, \\
 &\angle OQ_2P = \pi/2, \\
 &\text{From Pythagorean Theorem,} \\
 &\Rightarrow OP^2 = OQ_2^2 + PQ_2^2 \\
 &OP = 7 \text{ and } OQ_2 = 4 \\
 &\Rightarrow PQ_2 = \sqrt{33}
 \end{aligned}$$

Therefore, the length of tangent is $\sqrt{33}$.

1.2. Generating the figure using Python.

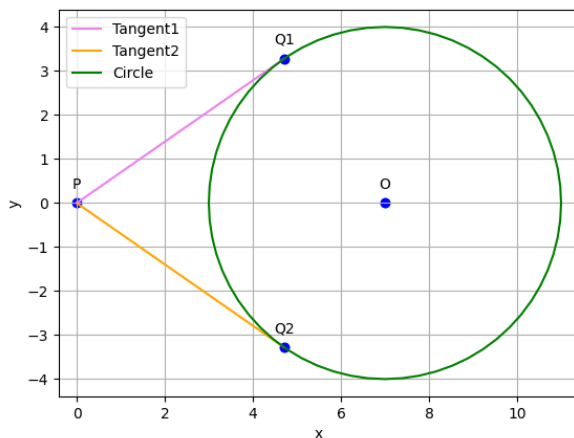


Fig. 1.2.1.