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# ASSIGNMENT 6 : CBSE PROBABILITY CLASS-12

## **AI21BTECH11016**

### **EXAMPLE - 25**

# **Question:**

Find the probability distribution of number of doublets in three throws of a pair of dice.

#### **Solution:**

Let  $X = \{0, 1, 2, 3\}$  be a random variable representing the number of doublets.

Event	Description		
X = 0	no dublet in three throws		
X = 1	one dublet in three throws		
X = 2	two doublets in three throws		
X = 3	all three throws are doublets		

TABLE I

For a single throw the possible doublets are:

$$(1,1)$$
,  $(2,2)$ ,  $(3,3)$ ,  $(4,4)$ ,  $(5,5)$ ,  $(6,6)$ 

 $\Rightarrow$  Probability of getting a doublet =  $\frac{1}{6}$ 

From the binomial distribution:

(i)

$$\Pr\left\{X = 0\right\} = {3 \choose 0} \times \left[\frac{1}{6}\right]^0 \times \left[\frac{5}{6}\right]^3 \qquad (1)$$
$$= \frac{125}{216} \qquad (2)$$

(ii)

$$\Pr\left\{X = 1\right\} = {3 \choose 1} \times \left[\frac{1}{6}\right]^1 \times \left[\frac{5}{6}\right]^2 \qquad (3)$$
$$= 3 \times \frac{25}{216} \qquad (4)$$
$$= \frac{75}{216} \qquad (5)$$

(iii)

$$\Pr\left\{X = 2\right\} = {3 \choose 2} \times \left[\frac{1}{6}\right]^2 \times \left[\frac{5}{6}\right]^1 \qquad (6)$$

$$= 3 \times \frac{5}{216} \qquad (7)$$

$$= \frac{15}{216} \qquad (8)$$

$$\Pr\left\{X = 3\right\} = {3 \choose 3} \times \left[\frac{1}{6}\right]^3 \times \left[\frac{5}{6}\right]^0 \qquad (9)$$
$$= \frac{1}{216} \qquad (10)$$

⇒ The Probability distribution of number of doublets in three throws of a pair of dice is :

X	0	1	2	3
P(X)	$\frac{125}{216}$	$\frac{75}{216}$	$\frac{15}{216}$	$\frac{1}{216}$

TABLE II