

# SAS® GLOBAL FORUM 2017

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#SASGF

USERS PROGRAM



# Presenter

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Paul Edwards is a senior manager on the Canadian Retail Models & Analytics team. Paul has worked in the financial sector since 2013 holding roles in risk modeling and fraud analytics. Paul has used SAS for 3 years.

# Real AdaBoost

Boosting for Credit Scorecards and Similarity to WOE Logistic Regression

# Objectives

- The need for transparency in models
- The desire for machine learning
- Consumer risk models
  - Scorecards
  - Weight-of-evidence (WOE) Regression
- Boosting
  - How it works
  - Highlights of boosting
  - How it is similar to WOE techniques
- Real AdaBoost macro
  - Example

# Transparency

- Modeling has undergone a renaissance
  - New machine learning algorithms
  - Powerful computers
  - Data-driven decision making has lead to large profits<sup>1</sup>
- Modeling departments at Financial Institutions are at a crossroads
  - Executives want some of the famed value of advanced methods
  - Others want models that are easy to understand & use
    - Regulators & auditors
    - Front line staff
    - Implementation teams (IT)



<sup>1</sup> <https://hbr.org/2016/05/how-companies-are-using-machine-learning-to-get-faster-and-more-efficient>

# Consumer Risk Models

## Introduction

- Risk modelers have developed methodology that is easy to implement and effective
  - The methodology is based on decision trees and regression
- Characteristics are binned and each bin receives a score proportional to risk

| Characteristic        | Bin                                       | Score points |
|-----------------------|---|--------------|
| Past loan delinquency | No past loan delinquency                  | 21           |
|                       | One past loan delinquency event           | 5            |
|                       | More than one past loan delinquency event | 0            |
| Credit utilization    | Low credit utilization (<30%)             | 25           |
|                       | Medium credit utilization (30-80%)        | 10           |
|                       | High credit utilization (>80%)            | 0            |

# Consumer Risk Models

## Scorecards

- This makes the models easy to understand, communicate and implement
- An applicant falls into just one bin per characteristic
  - The applicants gets one score from each characteristic. Total score is summed
  - Applicant proceeds down scorecard summing up a final score

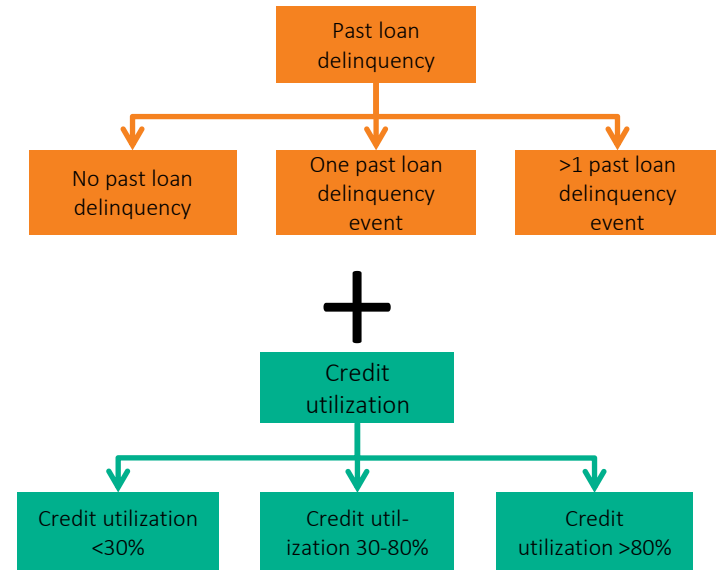
| Characteristic        | Bin                                       | Score points |
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# Consumer Risk Models

## Building Scorecards

- The bins for each characteristic are determined by a decision tree

| Characteristic        | Bin                                       | Score points |
|-----------------------|---|--------------|
| Past loan delinquency | No past loan delinquency                  | 21           |
|                       | One past loan delinquency event           | 5            |
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- The scorecard add the contributions from each tree



# Building Trees for Scorecard

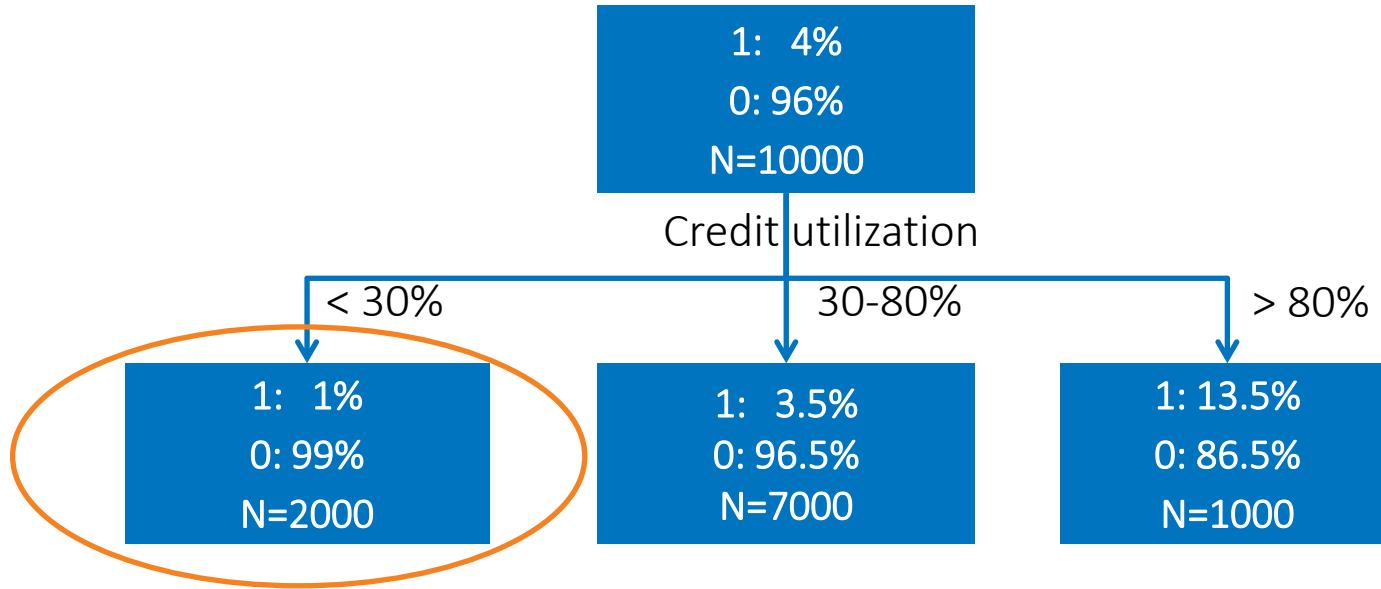
## 1. Gather (binary) training data

- $Y \in \{0,1\}$  : your target variable. In consumer risk,  $Y = 1$  indicates an applicant will become delinquent
- $\mathbf{x}: \{x_1, x_2, \dots, x_j\}$  : predictor variables (characteristics; e.g. credit utilization)

| Applicant | Y | $x_1$ | $x_2$ | ... | $x_j$ |
|-----------|---|-------|-------|-----|-------|
| 111       | 0 | 0.1   | A     |     | .     |
| 112       | 1 | 0.9   | A     |     | 1     |
| 113       | 0 | 0.0   | B     |     | 6     |

# Building Trees for Scorecard

2. Build a decision tree, splitting  $x_i$  into uniform bins of  $Y$ 
  - As an illustration, say  $x_1$  is credit utilization



# Building Trees for Scorecard

## Weight-of-evidence

3. Standardize the avg(Y) in each bin using “weight-of-evidence” (WOE)
- WOE is measures the “purity” of Y in the bin. A bin with most Y=0 events has large value

### General equations

$$F_{G,j}(k) = \frac{N_{j,k}^{Y=0}}{N_k^{Y=0}}$$

$$F_{B,j}(k) = \frac{N_{j,k}^{Y=1}}{N_k^{Y=1}}$$

$$WOE_{j,k} = \log \left( \frac{F_{G,j}(k)}{F_{B,j}(k)} \right)$$

### For credit utilization bin 1

$$F_{G,1}(1) = \frac{1980}{9600}$$

$$F_{B,1}(1) = \frac{20}{400}$$

$$WOE_{1,1} = \log \left( \frac{F_{G,1}(1)}{F_{B,1}(1)} \right) = 0.61$$

Credit utilization <30%

1: 20 (1%)

0: 1980 (99%)

N: 2000

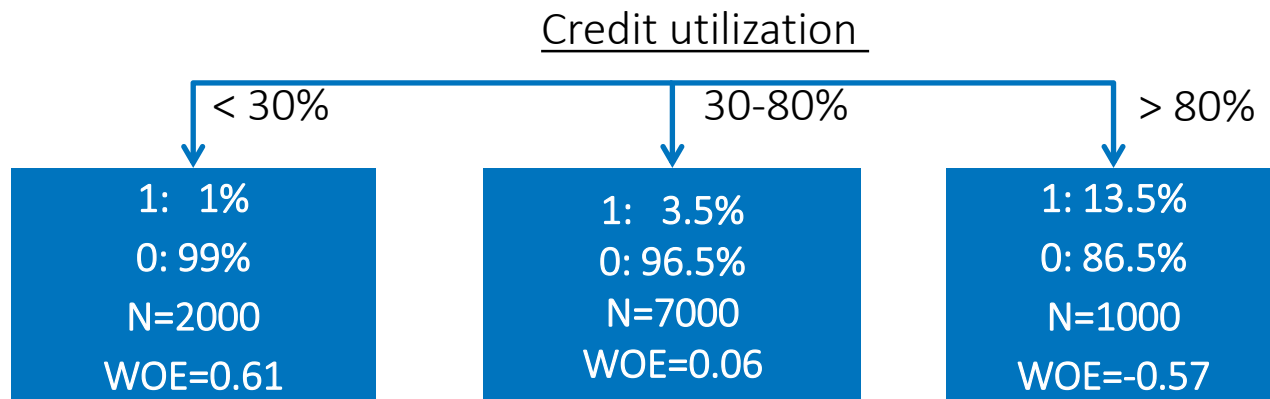
WOE: 0.61



# Building and Weighting Trees

## Weight-of-evidence

- New function  $W_j(x_j)$  - sorts characteristic  $j$  into appropriate bin and outputs the WOE value of that bin
- Examples
  - $W_1(x_1 = 40\%) = 0.06$
  - $W_1(x_1 = 85\%) = -0.57$
  - $W_1(x_1 = 90\%) = -0.57$



# Weighting Trees

## Logistic regression

- Logistic regression

$$\text{logit}(P(Y = 1)) = \beta_0 + \sum_{j=1}^M \beta_j W_j(x_j)$$

- Recall  $W_j(x_j)$  is a WOE tree: One term (one tree) per characteristic
- The  $\beta$  coefficients allow different contribution from each tree/characteristic
- Binning variables and standardizing with WOE allows
  - non-linear relationships to be modelled
  - categorical or missing data to be modelled naturally
- Non-linear version of logistic regression!

# Link to Machine Learning

## Weak learners

- The key to connecting WOE logistic regression with boosting methods is to understand that  $W_j(x_j)$  is itself a predictive model of  $P(Y = 1)$ 
  - A “weak learner” in ML parlance

| Y | $\beta_1$ | $W_1(x_1)$ | $x_1$ |
|---|-----------|------------|-------|
| ? | 0.55      | -0.57      | 0.86  |
| ? | 0.55      | 0.61       | 0.00  |
| ? | 0.55      | 0.61       | 0.04  |

- A record with a negative WOE is more likely Y=1

# Link to Machine Learning

## Weak learners

- Our confidence grows as we add trees
- Record 1 looks even more likely to be  $Y=1$

| $Y$ | $\beta_1$ | $W_1(x_1)$ | $x_1$ | $\beta_2$ | $W_2(x_2)$ | $x_2$ |
|-----|-----------|------------|-------|-----------|------------|-------|
| ?   | 0.55      | -0.57      | 0.86  | 0.65      | -1.2       | 5     |
| ?   | 0.55      | 0.61       | 0.00  | 0.65      | 1.0        | 1     |
| ?   | 0.55      | 0.61       | 0.04  | 0.65      | 2.0        | 0     |

# Link to Machine Learning

## Strong learner

- All three trees agree that the first record is  $Y=1$ 
  - The probability  $P(Y=1)$  is proportional to  $\beta_1 W_1(x_1) + \beta_2 W_2(x_2) + \beta_3 W_3(x_3)$

| Y | $\beta_1$ | $W_1(x_1)$   | $x_1$ | $\beta_2$ | $W_2(x_2)$  | $x_2$ | $\beta_3$ | $W_3(x_3)$  | $x_3$ |
|---|-----------|--------------|-------|-----------|-------------|-------|-----------|-------------|-------|
| ? | 0.55      | <b>-0.57</b> | 0.86  | 0.65      | <b>-1.2</b> | 5     | 0.11      | <b>-0.2</b> | 5.5   |
| ? | 0.55      | <b>0.61</b>  | 0.00  | 0.65      | <b>1.0</b>  | 1     | 0.11      | <b>0.4</b>  | -1.1  |
| ? | 0.55      | <b>0.61</b>  | 0.04  | 0.65      | <b>2.0</b>  | 0     | 0.11      | <b>0.4</b>  | 0.0   |

- Adding weak learners to form a strong one is a motivating principle in ML
  - This is possibly why WOE regression works



# Real AdaBoost

- Real AdaBoost<sup>1</sup> add weak learner trees:  $H_j(x_j)$  just like  $W_j(x_j)$
- But Real AdaBoost builds trees stage wise,
  1. Build  $H_1(x_1)$  (i.e., bin  $x_1$  using a tree)
  2. Estimate residual  $w = Y - H_1(x_1)$
  3. Build  $H_2(x_2)$  weighted by residuals. Two (equivalent) ways to think about this:
    - Resample your training data, proportional to  $w$ , then build  $H_2(x_2)$
    - The second tree tries hard to predict the difficult cases about which the previous tree was wrong
  4. Repeat
- H returns the weighted log odds of the bin, rather than the WOE of the bin

$$G(P(Y = 1)) = \sum_{j=1}^M H_j(x_j); \quad H_j(x_j) = \frac{1}{2} \log \left( \frac{P_w(Y = 1|x_j)}{P_w(Y = 0|x_j)} \right)$$

# Real AdaBoost

## Highlights

- Adaptive binning “wrings out” any variance left in the model
  - SAS EM credit scoring add-on builds all WOE trees first, then does regression.
  - Minimizes multicollinearity & remove need for variable reduction
- Automatic, but modifiable
  - Real AdaBoost can automatically fit a model even automatically detecting variable interactions
  - A business partner may insist on a certain variable, which could be added at from of AdaBoost series
- Established technique
- No fitted Coefficients
  - No regression step. The authors prove that a  $\beta=1$  coefficient will always minimizes error
- Scorecards
  - A Real AdaBoost model is a sum of a series of trees. The model can be expressed as a scorecard
- Extensible
  - Boosting (though not Real AdaBoost) can be done on non-binary targets

Trevor Hastie  
Robert Tibshirani  
Jerome Friedman

## The Elements of Statistical Learning

Data Mining, Inference, and Prediction

They wrote the book on machine learning!

# Real AdaBoost

## Macro

- A brief example of macro usage (synthetic data)

| Original input data |        |        |        |        |        |    |
|---------------------|--------|--------|--------|--------|--------|----|
| ID                  | COL1   | COL2   | COL3   | COL4   | COL5   | DF |
| 1                   | 1.241  | 1.617  | -0.808 | -1.286 | -2.463 | 0  |
| 2                   | -0.535 | 1.200  | -0.969 | -2.597 | 2.085  | 1  |
| 3                   | -1.014 | 0.356  | 1.063  | 0.444  | -0.006 | 1  |
| 4                   | 0.690  | -0.357 | 0.708  | -0.605 | 0.821  | 0  |

```
%adaboost(data=fakepd_t, target=df, var=col1 col2 col3 col4 col5,  
          scoreme=fakepd_v fakepd_o, seed=1234, ntree=10, interaction=0,  
          treedepth=2, outada=outadaboost);
```

# Real AdaBoost

## Macro outputs

### The scored data set

| Original input data |        |       |        |        |        |    | New columns |     |        |          |       |       |                |
|---------------------|--------|-------|--------|--------|--------|----|-------------|-----|--------|----------|-------|-------|----------------|
| ID                  | COL1   | COL2  | COL3   | COL4   | COL5   | DF | f1          | ... | f10    | adascore | p_df1 | p_df0 | ada-predict_df |
| 1                   | 1.241  | 1.617 | -0.808 | -1.286 | -2.463 | 0  | 0.143       |     | -0.085 | 0.350    | 0.587 | 0.413 | 1              |
| 2                   | -0.535 | 1.200 | -0.969 | -2.597 | 2.085  | 1  | 0.143       |     | 0.038  | 0.495    | 0.621 | 0.379 | 1              |
| 3                   | -1.014 | 0.356 | 1.063  | 0.444  | -0.006 | 1  | 0.024       |     | 0.038  | 0.431    | 0.606 | 0.394 | 1              |

### Scorecard

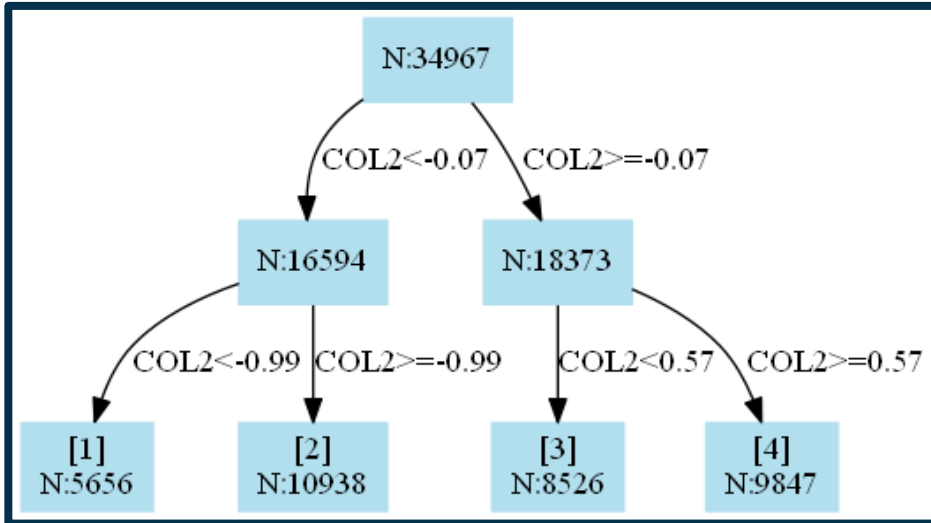
| LEAF | rule                    | score  | ADATREENUMBER |
|------|-------------------------|--------|---------------|
| 1    | ;COL2<-0.99             | -0.183 | 1             |
| 2    | ;COL2>=-0.99;COL2<-0.07 | -0.059 | 1             |
| 3    | ;COL2>=-0.07;COL2<0.57  | 0.024  | 1             |
| 4    | ;COL2>=0.57             | 0.143  | 1             |

# Real AdaBoost

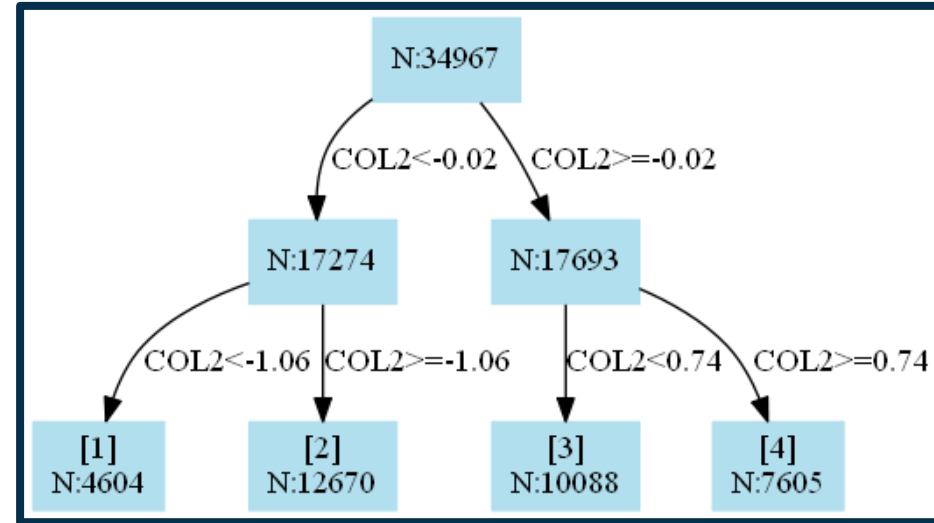
## Macro outputs

- Graphical trees
  - A helper program included in macro can generate graphical trees

Tree #2 in Real AdaBoost model




Tree #1 in Real AdaBoost model



# Questions

- Thanks for your attention!

| Contact  | Try the macro   |
|--|---|
| <a href="mailto:paul.edwards2@scotiabank.com">paul.edwards2@scotiabank.com</a><br><br>Questions & comments welcome | <ul style="list-style-type: none"><li>• The most up-to-date macro will always be on github*</li><li>• <a href="https://github.com/pedwardsada/real_adaboost">https://github.com/pedwardsada/real_adaboost</a></li></ul>  |

\* Pull requests are welcome! Submit your bugs and patches