

2)

47	23		14	15	3	5	7	8	36	10	10
0	1	2	3	4	5	6	7	8	9	10	11

23: $H(23) = 23 \text{ MOD } 11 = 1$

1 int/6

Total: 27

14: $H(14) = 14 \text{ MOD } 11 = 3$

1 int/6

10: $H(10) = 10$

1 int/6

15: $H(15) = 15 \text{ MOD } 11 = 4$

1 int/6

3: $H(3) = 3$

$h_1(3) = 3+1 \text{ MOD } 11 = 4$

3 int/6

$h_2(3) = 3+2 \text{ MOD } 11 = 5$

5: $H(5) = 5$

2 int/6

$h_1(5) = 5+1 \text{ MOD } 11 = 6$

7: $H(7) = 7$

1 int/6

8: $H(8) = 8$

1 int/6

36: $H(36) = 36 \text{ MOD } 11 = 3$

7 int/6

$h_1(36) = 4$

$h_2(36) = 5$

$h_3(36) = 6$

$h_4(36) = 7$

$h_5(36) = 8$

$h_6(36) = 9$

47: $H(47) = 3$

9 int/6

$h_1 = 4$

$h_5 = 8$

$h_2 = 5$

$h_6 = 9$

$h_3 = 6$

$h_7 = 10$

$h_4 = 7$

$h_8 = 0$

47	23	14	15	5	30	3	8	7	10	11	12
0	1	2	3	4	5	6	7	8	9	10	11

b)

Total: 17

$$H(23) = 1 \quad 1 \text{ in}$$

$$H(14) = 3 \quad 1 \text{ in}$$

$$H(10) = 10 \quad 1 \text{ in}$$

$$H(15) = 4 \quad 1 \text{ in}$$

$$H(3) = 3$$

$$H(4) = 3 \text{ MOD } 10 + 1 = 4$$

$$H_1(3) = 3 + 4 \text{ MOD } 11 = 7 \quad 2 \text{ in/out}$$

$$H(5) = 5 \quad 1 \text{ in/out}$$

$$H(7) = 7$$

$$H(7) = 7 \text{ MOD } 10 + 1 = 8$$

$$H_1(7) = 7 + 8 \text{ MOD } 11 = 4$$

$$H_2(7) = 7 + 8 \cdot 2 \text{ MOD } 11 = 23 \text{ MOD } 11 = 1 \quad 4 \text{ in/out}$$

$$H_3(7) = 7 + 8 \cdot 3 = 31 \text{ MOD } 11 = 9$$

$$H(8) = 8 \quad 1 \text{ in/out}$$

$$H(36) = 3$$

$$H(36) = 36 \text{ MOD } 10 + 1 = 7$$

$$H_1(36) = 3 + 7 \cdot 1 \text{ MOD } 11 = 10$$

$$H_2(36) = 3 + 7 \cdot 2 \text{ MOD } 11 = 17 \text{ MOD } 11 = 6$$

$$H(47) = 3$$

$$H(47) = 47 \text{ MOD } 10 + 1 = 8$$

$$H_1(47) = 3 + 8 \text{ MOD } 11 = 0$$

Total: 17

$$H(23) = 1 \quad 1 \text{ in/out}$$

$$H(14) = 3 \quad 1 \text{ in}$$

$$H(10) = 10 \quad 1 \text{ in}$$

$$H(15) = 4 \quad 1 \text{ in}$$

$$H(3) = 3 \quad 2 \text{ in}$$

$$H(5) = 5 \quad 1 \text{ in}$$

$$H(7) = 7 \quad 1 \text{ in}$$

$$H(8) = 8 \quad 1 \text{ in}$$

$$H(36) = 3 \quad 3 \text{ in}$$

$$H(47) = 3 \quad 4 \text{ in}$$

Total: 16

c)

