

# ParaStream: A parallel streaming Delaunay triangulation algorithm for LiDAR points on multicore architectures

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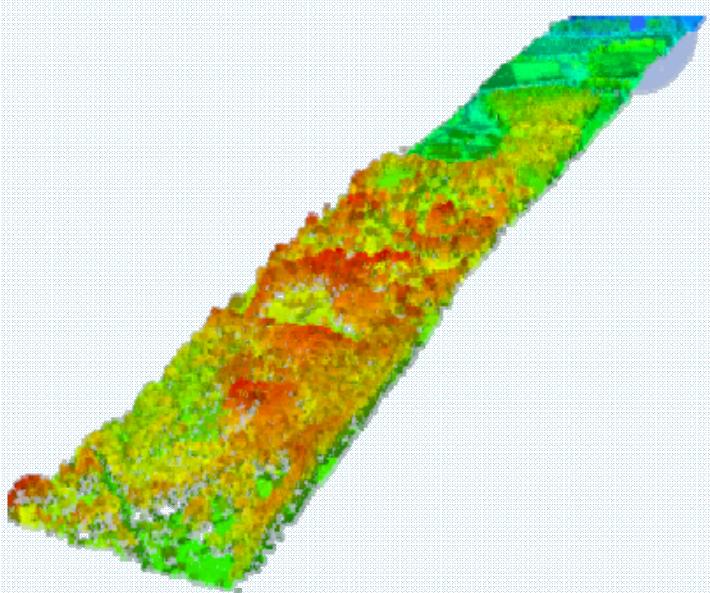
Wuhan University & TU Delft

Management of massive point cloud, December 8, 2015

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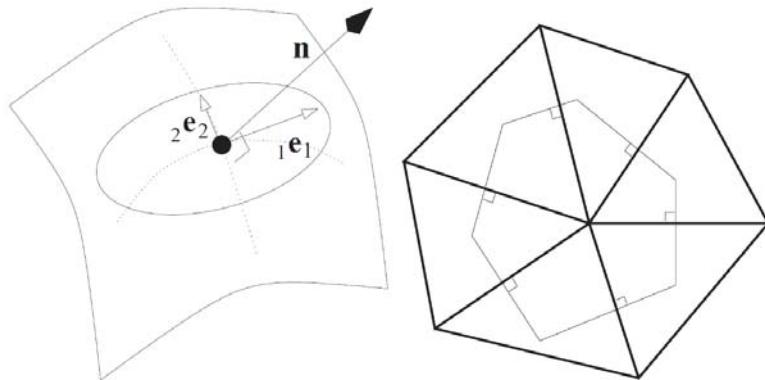
- Background & Research Objective
- Parallel Streaming Delaunay Triangulation
- Performance Evaluation
- Conclusion & Future work

# Background



LiDAR Point Cloud

DT and its dual Voronoi can be used to derive point geometry attributes for the further continuous LOD research.

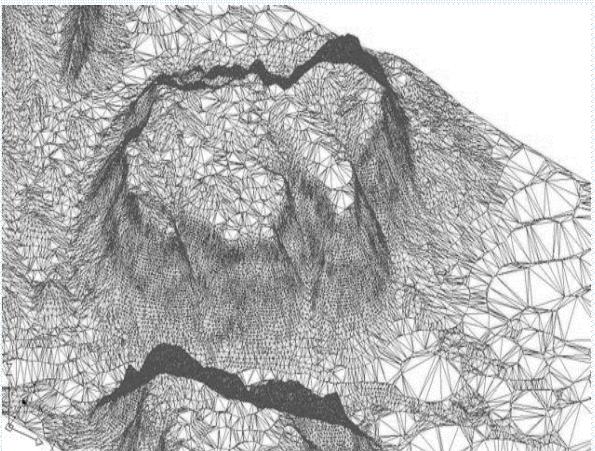


Normal, Gradient, Curvature, ...

# Challenges

## Challenge 1:

During the process massive point cloud can not be fitting in the main memory of commodity computers.



## Challenge 2:

Processing such massive point cloud, e.g. Delaunay Triangulation, are usually time-consuming.

## Research Objective

To address these challenges, a parallel Delaunay triangulation algorithm will be proposed for processing billions of points from discrete LiDAR LAS files.

- Integrate the idea of streaming computation
- Exploit the parallelism of the multi-core platform

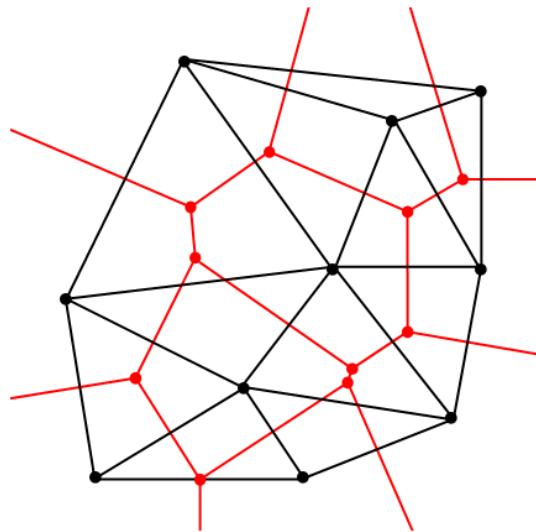
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- Background & Research Objective
- Parallel Streaming Delaunay Triangulation
  - Transformation from sequential D&C DT to parallel DT
  - Transformation from batch execution to streaming execution
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- Conclusion & Future work

# Delaunay Triangulation

A 2D Delaunay triangulation for a set  $P$  of points in a plane is a triangulation  $DT(P)$  such that no point in  $P$  is inside the circumcircle of any triangle in  $DT(P)$ .

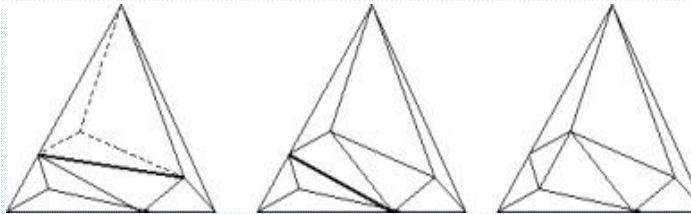
- DT & Voronoi diagram  
dual graph



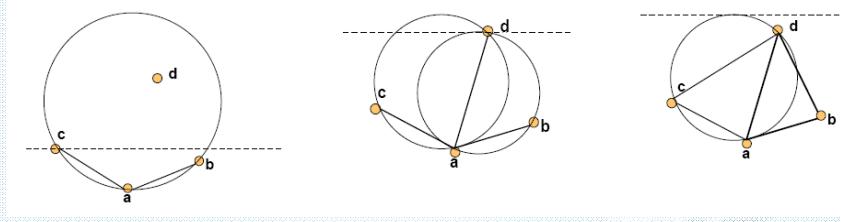
$$V(p) = \{x \in R^d : \|x - p\| \leq \|x - q\|, \forall q \in P, p \neq q\}$$

# Delaunay Triangulation Methods

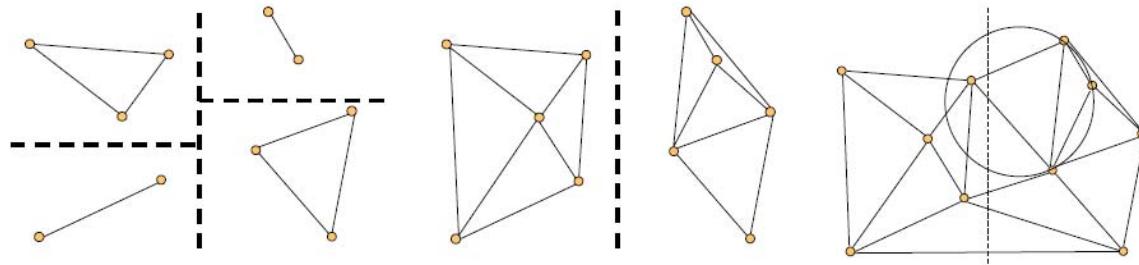
- Incremental Insertion



- Sweepline



- Divide & Conquer (D&C)



Triangle : Jonathan Shewchuk, UC Berkley

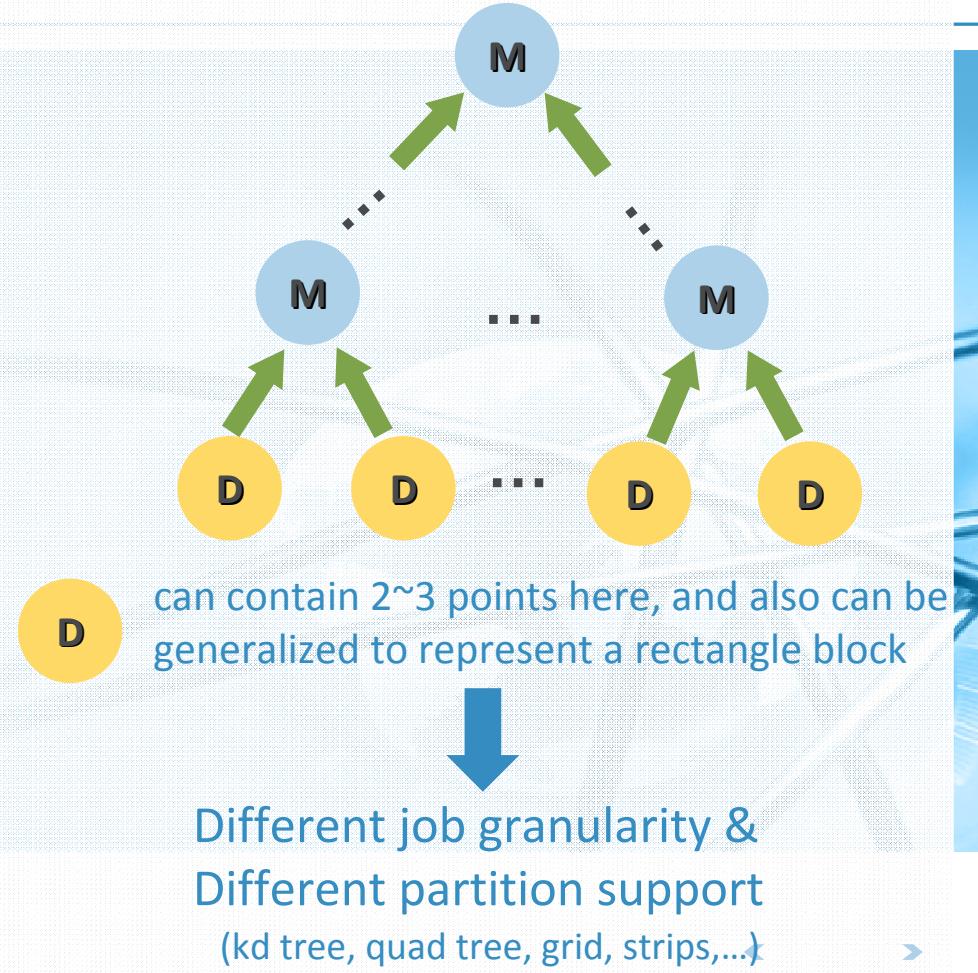
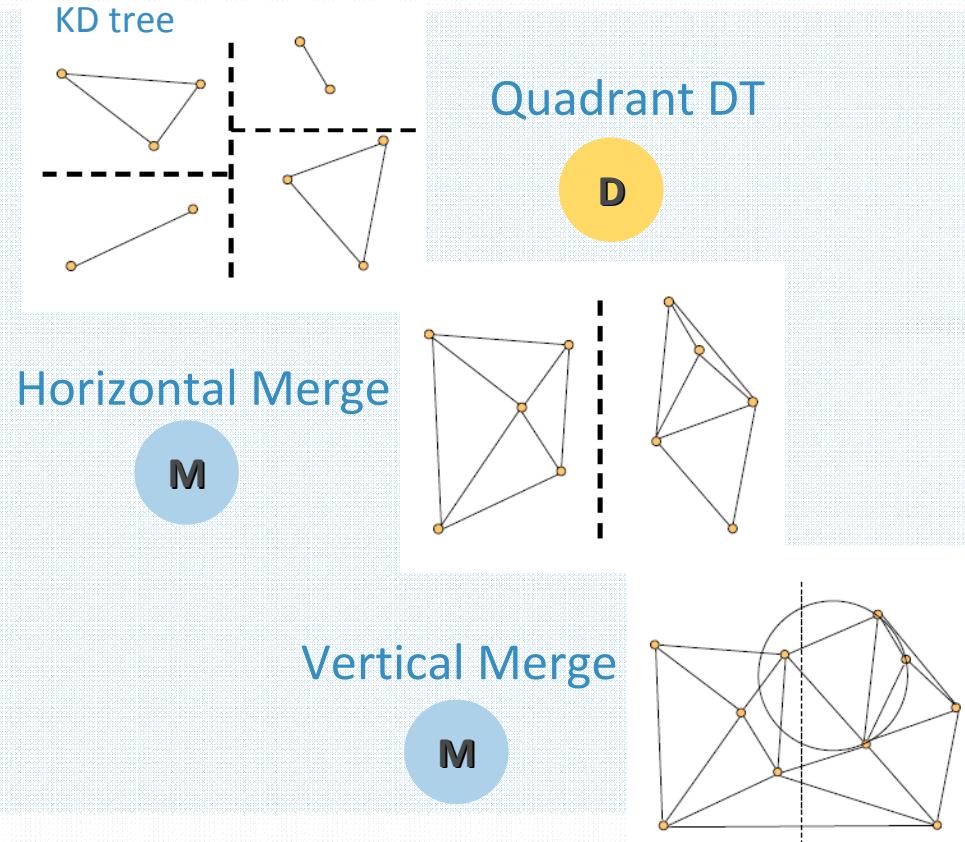
<http://www.cs.cmu.edu/~quake/triangle.html>

(a)

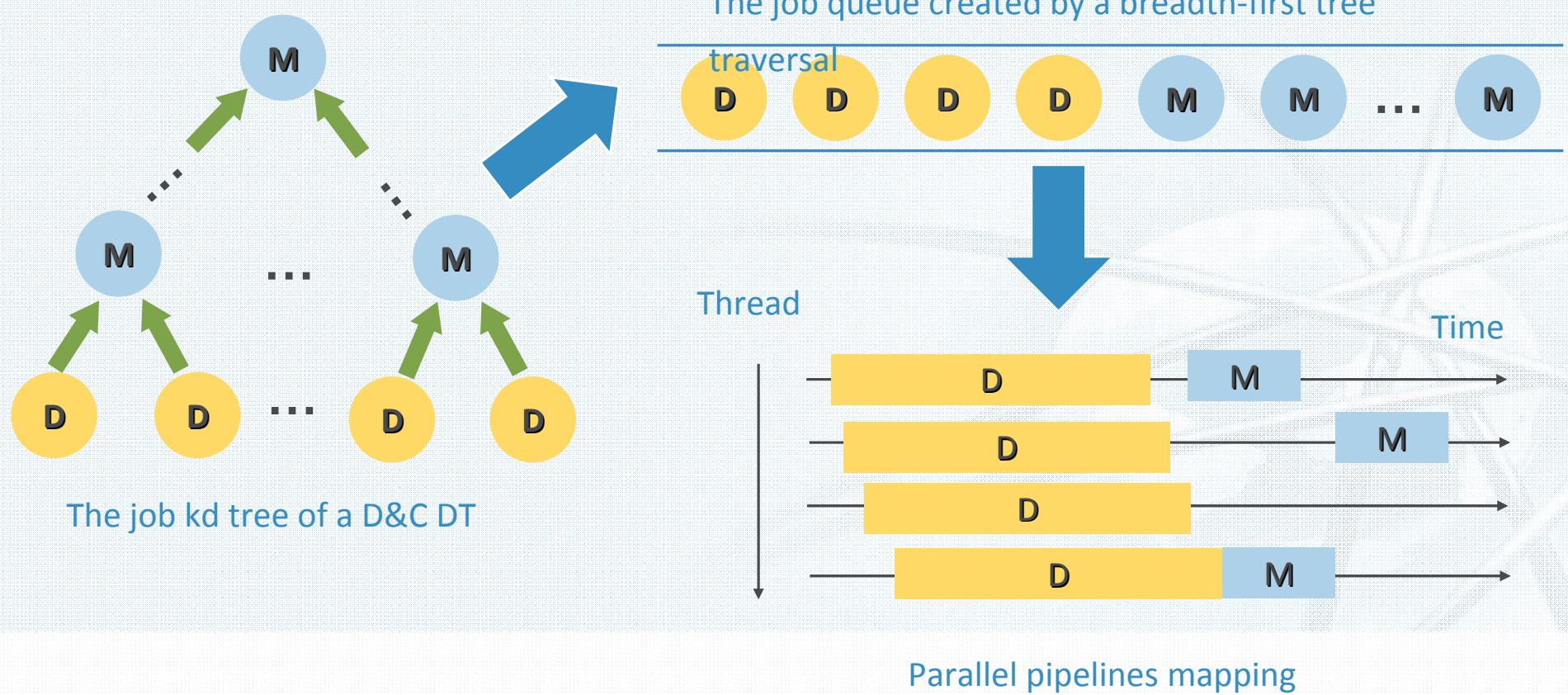
(b)

(c)

# D&C Delaunay Triangulation



# Parallel Streaming DT----Parallel pipelines



# Streaming Computation

Streaming computation has **four** requirements:

- **Sequential data access:** in the streaming model, the input data that are operated upon should not be randomly accessed from disk or memory
- **Linear execution:** the operations on elements of the input streams are orderly chained and work together as a pipeline.
- **Data locality:** when discrete elements of input streams pass through the pipeline of operations, each kernel operation on a given element does not involve too far away elements of streams.
- **Memory recycling:** streaming computation loads the input data sequentially, processes elements of input using a small memory buffer, outputs results immediately and frees partial or entire occupied memory space for later use.

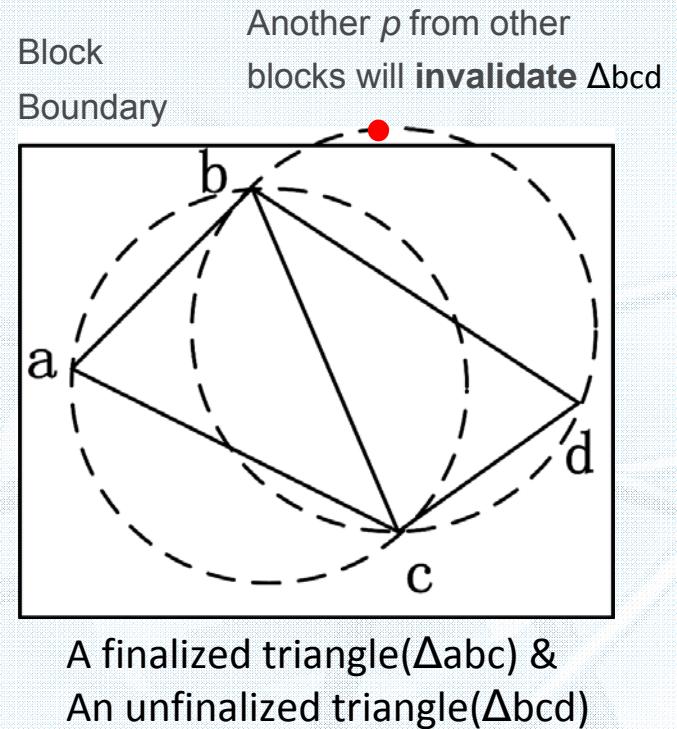
Spatial  
Sort



## Parallel Streaming DT---- Finalized triangles

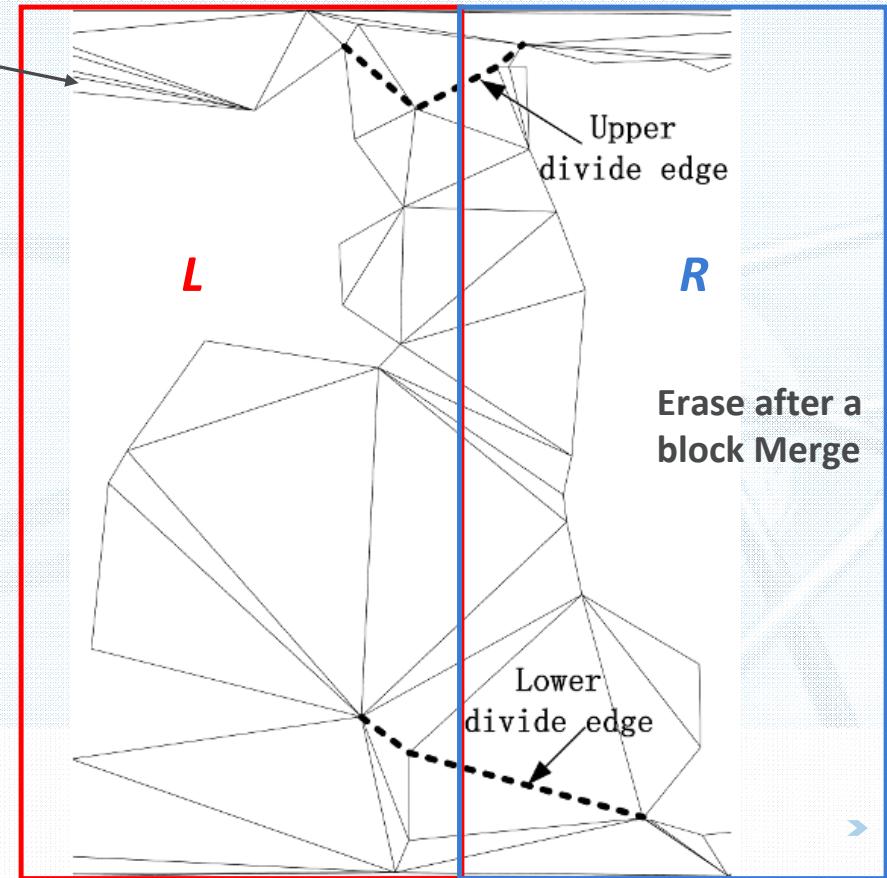
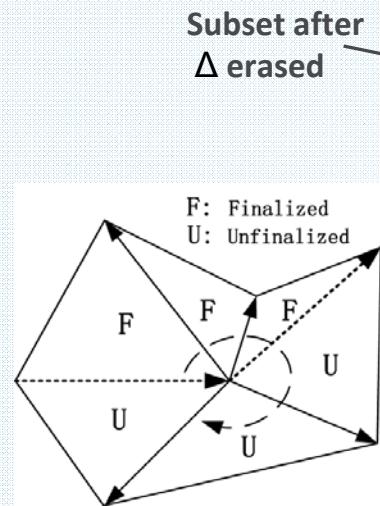
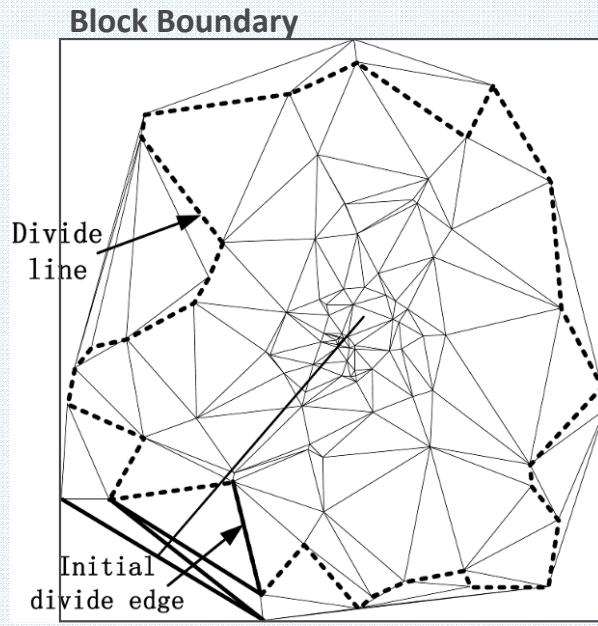
At any given time during the 2D Delaunay triangulation, the triangles in the mesh can be divided into two categories: *finalized* and *unfinalized*. The triangle, which has already been guaranteed to be part of the final output, is called the finalized triangle. Any triangle that will be eliminated and thus not appear in the final output, is called an unfinalized triangle (Isenburg et al. 2006)

Roughly determined by  $\bigcirc$  and  $\square$  Intersection



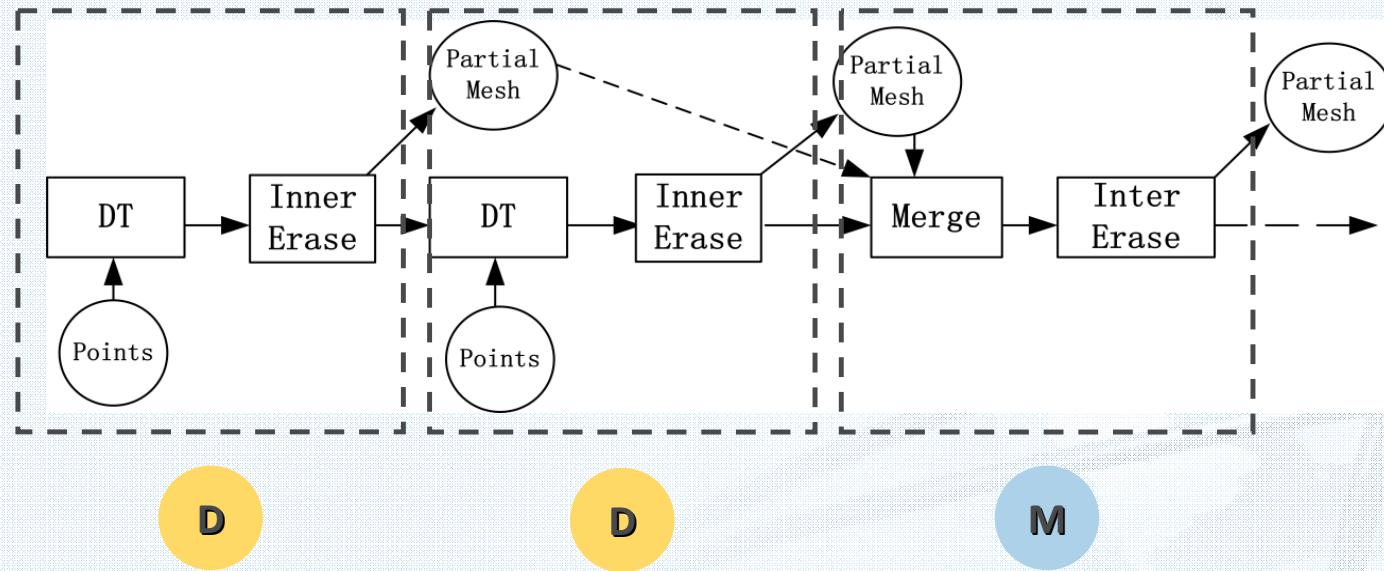
# Parallel Streaming DT---- Erase of finalized triangles

Erase finalized triangles after the DT & Merge steps to realize memory reuse.



Erase after each block DT

# Parallel Streaming DT---- The final version of one DT pipeline



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# Experimental Configuration

- Three performance evaluations
  - InnerErase* performance in the block DT
  - Sequential performance compared with other open-source DT methods
  - Parallel performance and scalability
- Experimental Data
  - Synthetic point datasets with different distribution patterns (*for test1*)
  - real-world LAS files(0.883 billion points; 16.4GB; 2173 LAS files) (*for test2 and 3*)
- Hardware
  - Two quad-core Intel Xeon E5405(2GHz each core), 8GB DDR2-667 ECC SDRAM, and 1TB SATA hard disk(7200rpm, 32MB cache)

# Evaluation of finalized triangle erase

Line

Normal

Uniform

Points (x10 <sup>6</sup> )	Line Distribution			Normal Distribution			Uniform Distribution		
	T <sub>dt</sub>	T <sub>e</sub>	Pct.	T <sub>dt</sub>	T <sub>e</sub>	Pct.	T <sub>dt</sub>	T <sub>e</sub>	Pct.
0.1	0.241	0.005	2.20%	0.175	5.91E-05	0.034%	0.177	0.001	0.49%
0.5	1.336	0.009	0.71%	1.122	9.21E-05	0.008%	1.109	0.003	0.23%
1	2.684	0.011	0.42%	2.476	1.02E-04	0.004%	2.421	0.004	0.16%
2	5.171	0.014	0.27%	5.384	1.18E-04	0.002%	5.284	0.006	0.11%
4	9.629	0.016	0.17%	11.685	1.20E-04	0.001%	11.292	0.009	0.08%

More

Less

$T_{dt}$  is the time spent on Delaunay triangulation;  $T_e$  is the time spent on the *Inner Erase* step.  
Pct. is the ratio of  $T_e$  to  $T_{dt}$ . (Time in seconds)

Trivial and nearly negligible < >

# Performance comparison between different DT methods

Blocks (LAS files)	Points (million)	ParaStream		Triangle(D&C)		Streaming TIN		
		Time(s.)	Memory	Time	Memory	Level	Time	Memory (MB)
1	0.53	1.30	44.08	1.36	39.94	4	1.53	7.42
2	0.87	2.09	36.85	2.07	64.46	4	2.48	7.85
4	1.79	4.37	43.87	4.39	131.94	6	5.56	7.88
16	6.85	16.36	50.45	15.97	499.60	6	20.08	13.19
32	15.25	36.50	57.39	35.74	1110.29	8	51.70	26.13

**Execution Time:**

- 1.Triangle
- 2.ParaStream
- 3.Streaming TIN

**Memory Usage:**

- 1.Streaming TIN
- 2.ParaStream
- 3.Triangle

Streaming TIN uses an internal multilevel quadtree in each block. This means a much smaller granularity.

**Triangle** : Jonathan Shewchuk, UC Berkley, 1996

**Streaming TIN( LAStools)**: Martin Isenburg, UNC, 2006 (The owner of Rapidlasso GmbH )

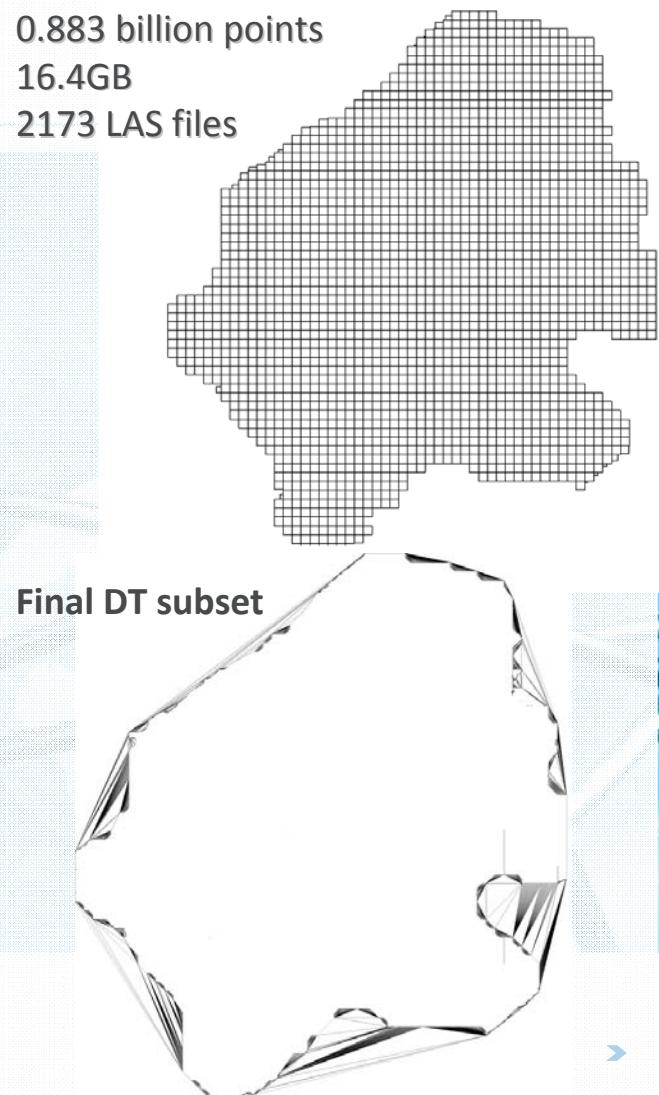


# Evaluation of parallel streaming DT

Threads	Direct output		Compression on output		
	Time(s.)	Speedup	Time	Speedup	Memory(MB)
1	2584.01		6195.94		313.17
2	1623.03	1.59	3207.84	1.93	365.41
4	1269.79	2.03	1624.04	3.82	456.80
6	1255.62	2.06	1144.17	5.42	506.16
8	1280.79	2.02	965.17	6.42	590.49

Less I/O, Faster DT, Better Speedup

0.883 billion points  
16.4GB  
2173 LAS files



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# Conclusion

A robust parallel D&C Delaunay triangulation scheme called *ParaStream* is proposed particularly for shared-memory multicore architectures to process billions of LiDAR points.

- Scalable for billions of points
- Scalable for tens of CPU cores
- Very efficient memory usage

## Future work

- 2D TIN → 3D Delaunay Triangulation;
- Evaluation with much larger datasets (e.g. ahn2, 640 billion);
- Implementation on top of database(e.g. MongoDB);
- Hybrid computing support (CPU plus GPU tasks);
- Applied in the discrete/continuous LoD point clouds.



# Thanks for your attention!

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