

The foundations blah blah blah

$$|f(y) - f(x)| < \epsilon.$$

Question 1:

a)

b)

1. Prove that  $\text{rank}(A) \leq m$

Since the definition of  $\text{rank}(A)$  is the number of nonzero rows, and  $A \in \mathbb{R}^{m \times m}$  then the maximum number of nonzero rows that can exist is all of them, or  $m$ . ■

2. Prove that if  $\text{rank}(A) = m$ , then  $Ax = b$  has a solution for every  $b$ .
3. Prove that if  $\text{rank}(A) < m$ , then there exists a  $b$  such that  $Ax = b$  has no solution.