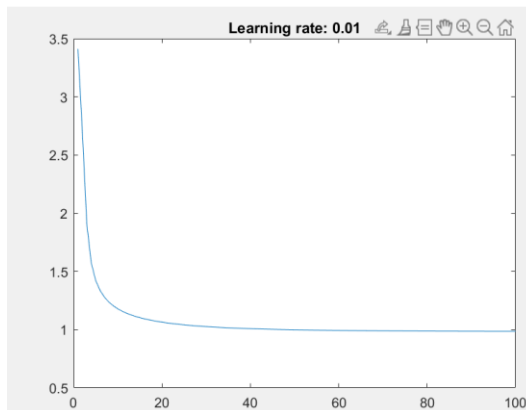


## HW4

## Learning

$$F(U, V) = \frac{1}{2} \sum (M_{ij} - u_i v_j^T)^2 + \frac{\lambda}{2} (\|U\|_F^2 + \|V\|_F^2)$$

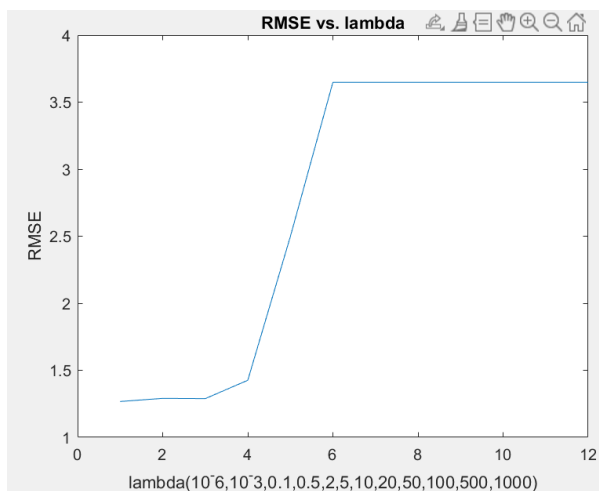
1.  $\frac{dF}{dU} = (M - uv)v^T - \lambda U, \frac{dF}{dV} = (M - uv)u^T - \lambda V$
2. For each non-zero element in the testing dataset, U and V are updated by subtracting its current value by its gradient multiplied by the learning rate. It is updated for 100 iterations in which the error should hopefully gradually approach 0.
- 3.



The average error of our model does decrease as the iterations go on but seems to converge at around 1 and does not quite reach 0.

## Evaluation

1. RMSE for  $\lambda = 1$  was 1.4895
- 2.



The RMSE is lower the smaller value lambda is and increases as lambda gets greater. It seems to even out at 3.65 after lambda is greater than 10.