The fusion categories $package^*$

Jacob C. Bridgeman jcbridgeman.github.iojcbridgeman1@gmail.com

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Abstract

The fusion categories package is a package for type setting fusion category data, including ${\cal F}\text{-}$ and ${\cal R}\text{-}{\rm symbols}.$

This document provides a brief overview of the pacakge and its features.

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^{*}This document corresponds to fusion categories v0.1.3, dated 2024-07-31.

The fusioncategories package

1 Options

```
\frac{\text{delimiter}}{\text{default:}} \ \frac{\{\langle delimiter \rangle\}}{\text{default:}}
```

Sets the delimiter for the subscripts, superscripts, left indices, and right indices.

$$\verb|style| = \langle style \rangle - \{ \texttt{graphical}, \texttt{traditional}, \texttt{compact} \} \\$$

Sets the style for symbol indices. This option sets the default global style, which can be overridden for individual symbols.

The default style is <u>graphical</u>, which places the indices in a style mimiciking their location on a string diagram. The traditional style places the indices in a more traditional style, and the compact style places the indices with left indices at the bottom and right indices at the top.

$$\begin{split} & \text{graphical} - \frac{\beta}{\alpha} \Big[F_{abc}^{\ d} \Big]_{\mu}^{\nu} \\ & \text{traditional} - \Big[F_{abc}^{\ d} \Big]_{(\alpha e \beta)(\mu f \nu)} \\ & \text{compact} - \Big[F_{abc}^{\ d} \Big]_{\alpha e \beta}^{\mu f \nu} \end{split}$$

2 Commands

\NewSymbol
\RenewSymbol
\ProvideSymbol
\DeclareSymbol

Creates a new symbol (and matrix if $\langle left\ indices? \rangle = true\ or\ \langle right\ indices? \rangle = true)$ command with the specified argument types.

For example:

\NSymbol, which can be used as follows: \NSymbol{a,b}{c} produces: N_{ab}^{c} .

\tXSymbol, which can be used as follows:

\tXSymbol{a,b}{\mu} produces: $\left[\tilde{X}_{ab} \right]_{\mu}$.

In addition, the command $\texttt{\txMatrix}$, which can be used as follows:

\tXMatrix{a,b} produces: \tilde{X}_{ab} .

\GammaSymbol, which can be used as follows:

\GammaSymbol{a,b} produces: Γ_{ab} .

\NewSymbol[text=F, style=traditional] {tradF}{1}{1}{1}{creates the command:

\tradfSymbol, which can be used as follows:

 $$$ \left(\mathbf{x}_{abc} \right) = \left(\mathbf{x}_{abc} \right)_{\mu\nu}.$

Arguments that are wanted should marked with 1 or true, and arguments that are not wanted must be left blank or marked with false.

All commands created with \NewSymbol also accept an optional star argument to place an overline over the symbol.

If the symbol has left or right indices, the command will also create a matrix command with the same name as the symbol command.

\NewSymbol will only create a new symbol command if the command does not already exist, otherwise it will throw an error.

\RenewSymbol will overwrite an existing symbol command with the same name. If the command does not exist, it will throw an error.

\ProvideSymbol will create a new symbol command if the command does not already exist, otherwise it will do nothing.

\DeclareSymbol will create a new symbol regardless of whether the command already exists. If the command already exists, it will overwrite the existing command without warning.

Any text in the text option will be used as the symbol text in the output.

The style option can be used to set the style of the symbol. This option will override the global style option for the symbol. The same styles are available as for the global style option.

 $\label{eq:local_norm} $$\NSymbol *{\langle subscripts \rangle} {\langle superscripts \rangle} $$$

Produces a symbol with the specified subscripts and superscripts.

\NSymbol{a,b}{c} produces: N_{ab}^{c}

 $\label{eq:continuous} $$XSymbol \xspace{0.05cm} (subscripts)}{\langle superscripts \rangle}{\langle right\ indices \rangle}$$$

Produces a symbol with the specified subscripts, superscripts, and right indices.

\XSymbol{a,b}{c}{\alpha} produces: $\left[X_{ab}^{c}\right]_{\alpha}$.

 $XMatrix{a,b}{c}$ produces: X_{ab}^{c} .

 $\label{eq:continuous} $$ \Symbol *{\subscripts}}{\arraycolsep} {\arraycolsep} {\arraycolsep}$

Produces a symbol with the specified subscripts, superscripts, left indices, and right indices.

\FSymbol{a,b,c}{d}{\alpha,e,\beta}{\mu,f,\nu} produces: $\int_{c}^{\beta} \left[F_{abc}\right]_{n}^{\nu}$.

\FSymbol*{a,b,c}{d}{\alpha,e,\beta}{\mu,f,\nu} produces: $\int_{c}^{\beta} \left[\overline{F_{abc}}\right]_{f}^{\nu}$.

\FMatrix{a,b,c}{d} produces: F_{abc}^{d}

\FMatrix*{a,b,c}{d} produces: \overline{F}_{abc}^{d}

 $\label{eq:linear_loss} $$\Symbol *{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}}{\subscripts}{\subscripts}}{\subscripts}}{\subscripts}{\subscripts}}{\subscripts}{\subscripts}}{\subscripts}{\subscripts}}{\subscripts}{\subscripts}{\subscripts}}{\subscripts}{\subscri$

 $\verb|\RMatrix| & \RMatrix| & \Subscripts| & \Superscripts| \\$

Produces a symbol with the specified subscripts, superscripts, left indices, and right

\RSymbol{a,b}{c}{\alpha}{\beta} produces: $\left[R_{ab}^{c}\right]_{\beta}$.

\RMatrix{a,b}{c} produces: R_{ab}^{c} .

 $\verb|\PentagonEquation \PentagonEquation| (*) [\langle a \rangle] [\langle b \rangle] [\langle c \rangle] [\langle a \rangle] [\langle \beta \rangle] [\langle \gamma \rangle]$

Typesets the pentagon equation for a fusion category. If the optional * argument is used, the equation is typeset for the multiplicity free case.

The optional arguments a, b, c, α, β , and γ are used to specify the symbols used in the equation. If these arguments are left blank, the default symbols are used.

\PentagonEquation* produces:

$${}_{a_5} \Big[F_{a_0 a_1 c_0}^{\ a_4} \Big]_{c_1 \ a_6} \Big[F_{a_5 a_2 a_3}^{\ a_4} \Big]_{c_0} = \sum_{b_0 \ a_5} \Big[F_{a_0 a_1 a_2}^{\ a_6} \Big]_{b_0 \ a_6} \Big[F_{a_0 b_0 a_3}^{\ a_4} \Big]_{c_1 \ b_0} \Big[F_{a_1 a_2 a_3}^{\ c_1} \Big]_{c_0}.$$

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The italic numbers denote the pages where the corresponding entry is described, numbers underlined point to the definition, all others indicate the places where it is used.

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TO.	$\verb \RenewSymbol 3$
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Change History

v0.1.0	v0.1.2	
General: Initial version 1	General: Restyled the index locations .	
	v0.1.3	
v0.1.1	General: Added Matrix commands	
General: Added support for Greek	and minor tweaks to layout.	
letters and command names being	Added optional style to the symbol	
different from the symbol text 1	creation commands. $\dots 1$	