

DEPARTMENT OF  COLORADO SCHOOL OF MINES
EARTH • ENERGY • ENVIRONMENT

COMPUTER SCIENCE

CSCI 341: Computer Organization
WS 2: Floating Point Numbers

1	<p>Given a 32 bit register, show where each part of a floating point number will be. Fill out the table below.</p> <table border="1" data-bbox="269 559 1501 739"> <tr> <td>3</td><td>3</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>2</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>1</td><td>9</td><td>8</td><td>7</td><td>6</td><td>5</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td> </tr> <tr> <td>1</td><td>0</td><td>9</td><td>8</td><td>7</td><td>6</td><td>5</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td><td>9</td><td>8</td><td>7</td><td>6</td><td>5</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td><td>9</td><td>8</td><td>7</td><td>6</td><td>5</td><td>4</td><td>3</td><td>2</td><td>1</td><td>0</td> </tr> <tr> <td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td> </tr> </table>	3	3	2	2	2	2	2	2	2	2	2	2	1	1	1	1	1	1	1	1	9	8	7	6	5	4	3	2	1	0	1	0	9	8	7	6	5	4	3	2	1	0	9	8	7	6	5	4	3	2	1	0	9	8	7	6	5	4	3	2	1	0																																						
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2	<p>Write down the formula for converting a binary floating point number to decimal.</p>																																																																																																				
	<p>Solution: $(-1)^S(1 + F)(2^{E-b})$</p>																																																																																																				
3	<p>Write down the formula for converting a denormal binary floating point number to decimal.</p>																																																																																																				
	<p>Solution: $(-1)^S(0 + F)(2^{1-b})$</p>																																																																																																				
4	<p>Convert the following floating point numbers to decimal</p>																																																																																																				
	<p>1. 1001 0010 0100 1000 0000 0000 0000 0000</p>																																																																																																				
	<p>2. 0111 1011 0100 1000 0000 0000 0000 0000</p>																																																																																																				
	<p>Solution:</p>																																																																																																				
	$1\ 00100100\ 1001000000000000000000000$																																																																																																				
	$(-1)^1(1 + 2^{-1} + 2^{-4})(2^{36-127}) = -6.31089 * 10^{-28}$																																																																																																				
	$0\ 11110110\ 1001000000000000000000000$																																																																																																				
	$(-1)^0(1 + 2^{-1} + 2^{-4})(2^{246-127}) = 1.03846 * 10^{36}$																																																																																																				
5	<p>Convert the following floating point numbers to decimal. Show enough decimal places for the numbers to be distinguishable.</p>																																																																																																				
	<p>1. 1000 0000 0100 1000 0000 0000 0000 0000</p>																																																																																																				
	<p>2. 0000 0000 0100 1000 0000 0000 0000 0001</p>																																																																																																				
	<p>Solution:</p>																																																																																																				

	$1\ 00000000\ 10010000000000000000000000$ $(-1)^1(0 + 2^{-1} + 2^{-4})(2^{1-127}) = -6.61215572 * 10^{-39}$ $0\ 00000000\ 100100000000000000000000001$ $(-1)^0(0 + 2^{-1} + 2^{-4} + 2^{-23})(2^{1-127}) = 6.61215712 * 10^{-39}$
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