

① Derive modificación $P_t(n|\lambda)$ en la que $Q(N=0)=0$, $Q(N=1)=1/3$

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$$P(N_t=n) = \frac{e^{-\lambda} \lambda^n}{n!} \quad \forall n \geq 2 \quad \text{dado que fijos serán } \{2, 3, \dots\}$$

modificaremos $A=\{0, 1\}$

$$\left(1 - \sum_{j=0}^1 \frac{e^{-\lambda} \lambda^j}{j!}\right) \Rightarrow \frac{P(N_t=n)}{1 - \tilde{P}(N_t \in A)} = \frac{\frac{e^{-\lambda} \lambda^n}{n!}}{1 - \sum_{j=0}^1 \frac{e^{-\lambda} \lambda^j}{j!}}$$

$$Q(N_t) = 1 - Q(N_t=0) - Q(N_t=1) \Rightarrow q_n = (1 - 1/3) \cdot \frac{e^{-\lambda} \lambda^n}{1 - \sum_{j=0}^1 \frac{e^{-\lambda} \lambda^j}{j!}}$$

$$\therefore Q(N_t=n) = \begin{cases} 0 & \text{si } n=0 \\ 1/3 & \text{si } n=1 \\ 2/3 \cdot \frac{e^{-\lambda} \lambda^n / n!}{1 - \sum_{j=0}^1 \frac{e^{-\lambda} \lambda^j}{j!}} & \text{si } n \geq 2 \end{cases}$$

② modificación en la que

$$N_+ | N_+ \leq 15 \sim P_0(n|30)$$

$$N_+ | N_+ > 15 \sim \text{Bin}(n|100, 1/3)$$

modificar el intervalo $\{16, 17, \dots\} = A$

fijos $\{1, 2, \dots, 15\}$

$$q_n = p_n = \frac{e^{-\lambda} \lambda^n}{n!} \mathbb{I}_{\{0, \dots, 15\}}$$

$$\begin{aligned} \frac{\tilde{P}(N_t=n)}{1 - \tilde{P}(N_t \in A)} &= \frac{\text{Bin}(n|m, p)}{1 - \sum_{j=0}^5 \text{Bin}(j|m, p)} \\ &= \frac{\binom{100}{n} \theta^n (1-\theta)^{100-n}}{1 - \sum_{j=0}^5 \binom{100}{j} \theta^j (1-\theta)^{100-j}} \mathbb{I}_{\{n > 15\}} \end{aligned}$$