

Big O Notation

Time complexity of an algorithm

"How much time it takes to run a function as the size of the input grows."

Runtime

Const

array1 = [, , , , ]

array
number of elements

n=5

Let's see if there is a needle in the haystack!

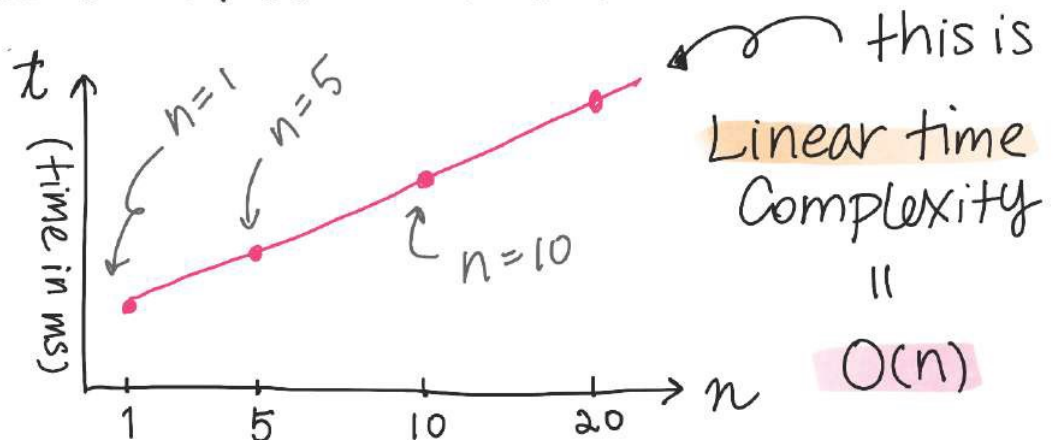
JS

```
Const numNeedles = (haystack, needle) => {  
  let count = 0  
  for (let i = 0; haystack.length; i++) {  
    if (haystack[i] === needle) count += 1;  
  }  
  return count;  
}
```



How long does it take to execute when the number of elements (n) is:

execution time grows linearly as array size increases!



Big O Notation

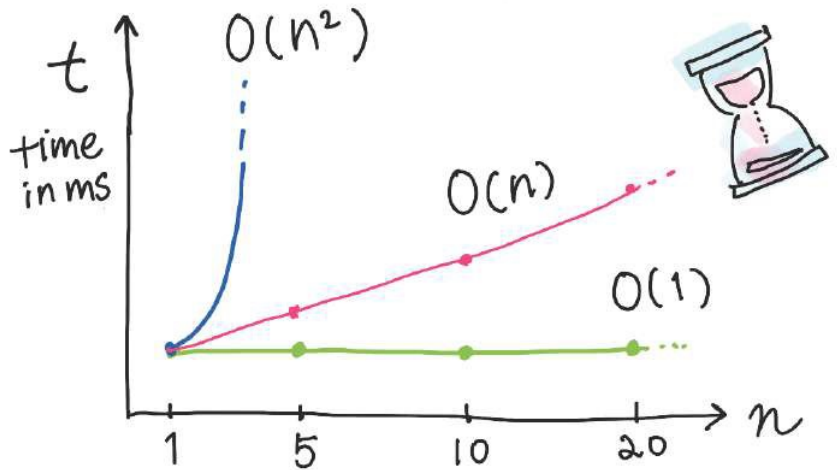
JS Let's see if we have some function that doesn't actually loop the array:

```
const alwaysTrueNoMatterWhat = (haystack) => {
  return true;
}
```

$n=5$
 $n=10$
 $n=20$
 \vdots

↪ Array size has no effect on the runtime

☆ Constant time
 ||
 $O(1)$



☆ Quadratic time = $O(n^2)$

Const

array2 = [cat, flower, cake, cake, spoon] ;

↪ $n=5$, however the runtime is proportional to n^2

JS Const hasDuplicates = (arr) => {

```

  for (let i = 0; i < arr.length; i++)
    let item = arr[i];
    if (arr.slice(i+1).indexOf(item) !== -1) {
      return true;
    }
  return false;
}
```

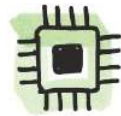
① Loop thru the array

② Another array lookup w/ indexOf method

Data Structures

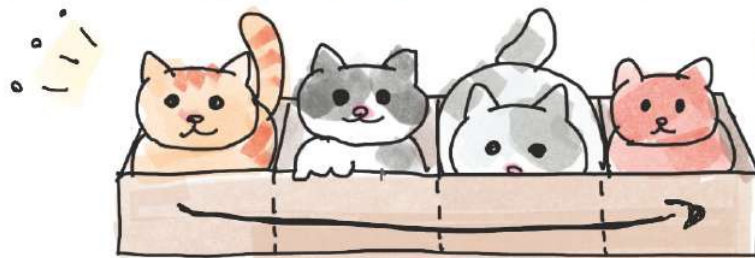
Array & Linked List

Array a linear data structure, stored in contiguous memory locations.



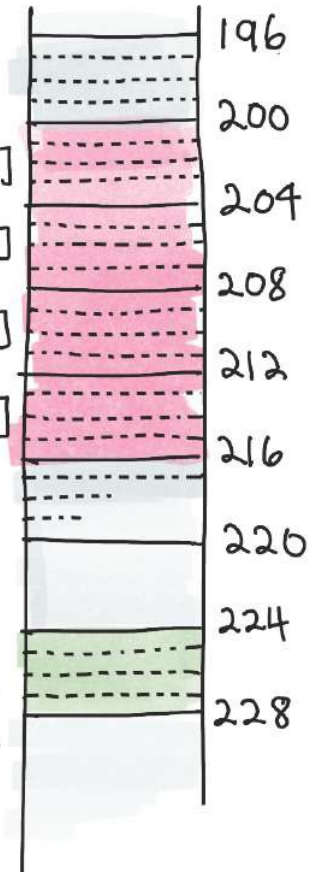
memory

Address 200 204 208 212



Array [0] [1] [2] [3]

$a[0]$
 $a[1]$
 $a[2]$
 $a[3]$



- ♥ Assume each 🐱 is an integer
= requires 4 bytes space
- ♥ The array of 🐱 must be allocated contiguously!
→ address 200 — 216



🎉 yay!

- ♥ can randomly access w/ index
 $a[2] \rightarrow$ 🐱
- ♥ contiguous = no extra memory allocated = no memory overflow

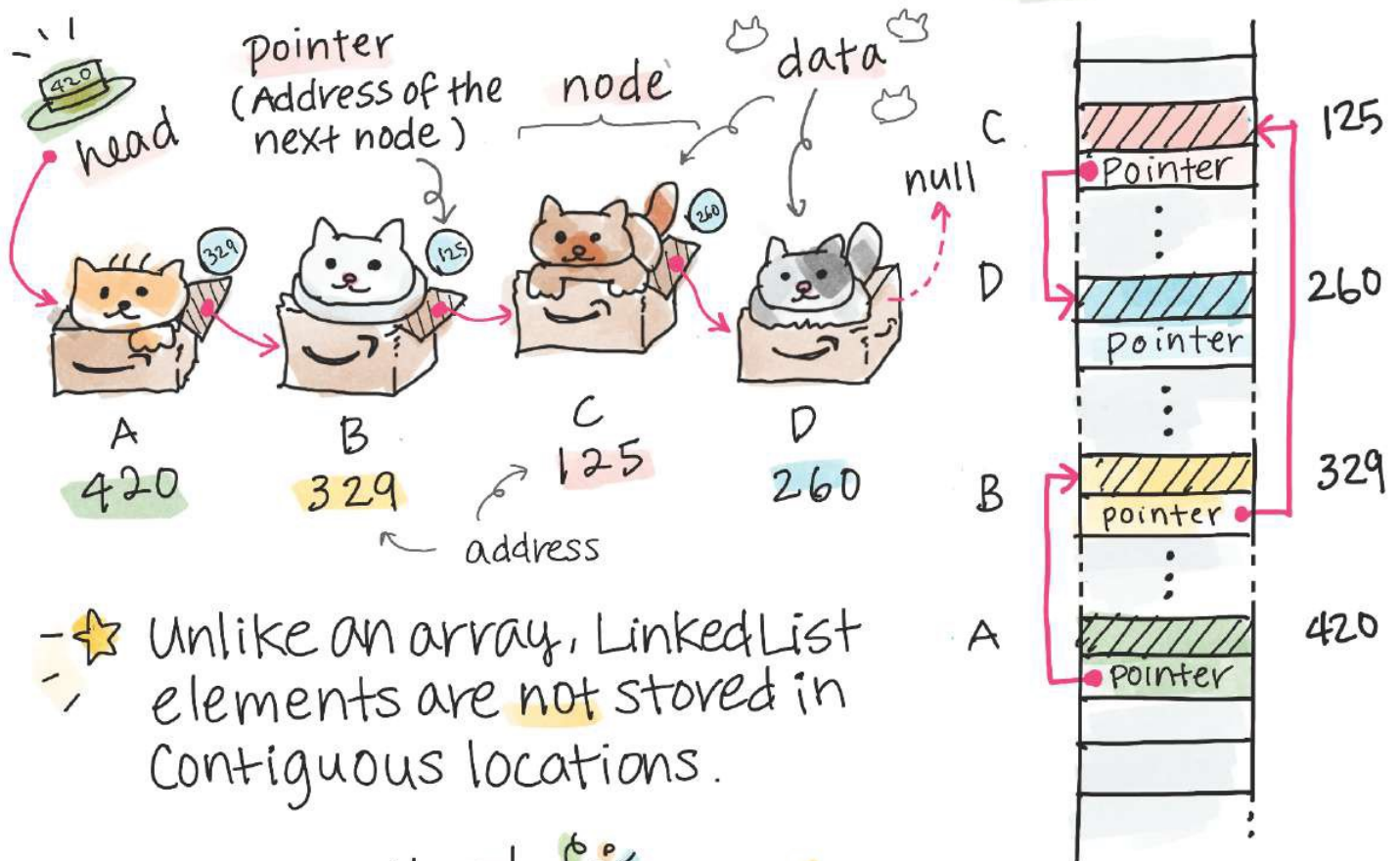
👎 meh!

- 💀 fixed size. Large space may not be avail for big array
∴ 🐱 took the space! ∴
- 💀 Insert & delete elements are costly.
→ may need to create a new copy of the array & allocate at a new address.

Linked list

Array & Linked List

- ★ a linear data structure
- ★ each element is a separated object & elements are linked w/ pointers



- ★ Unlike an array, Linked List elements are not stored in Contiguous locations.

Yay! 🎉

- ♥ Dynamic data
= size can grow or shrink
- ♥ Insert & delete element are flexible.
→ no need to shift nodes like array insertion
- ♥ memory is allocated at runtime

👎 meh!

- ☹ No random access memory.
→ Need to traverse n times
→ time complexity is $O(n)$. array is $O(1)$
- ☹ Reverse traverse is hard

Data Structures

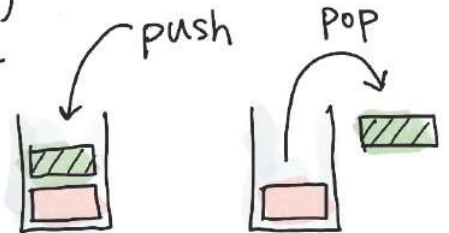
Stack & Queue

FIFO

LIFO

@girlie_mac

A stack is a LIFO (Last-in-First-out) data structure, where an element added last (=push) gets removed first (=pop)



♡ just like a stack of ice cream scoops!



☆ Stack as an array in JS

```
let stack = [ ];
```

arrays in JavaScript are dynamic!

stack is:

```
stack.push('mint choc'); // ['mint choc']
stack.push('vanilla');   // ['mint choc', 'vanilla']
stack.push('strawberry'); // ['mint choc', 'vanilla', 'strawberry']
```

```
let eaten = stack.pop(); // eaten is 'strawberry'
```

♡ Time complexity is $O(1)$ for both pop + push.

```
['mint choc', 'vanilla']
```

Data Structures

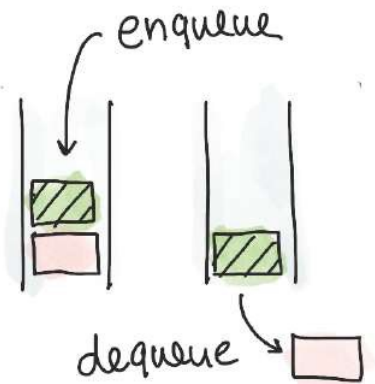
Stack & Queue

FIFO

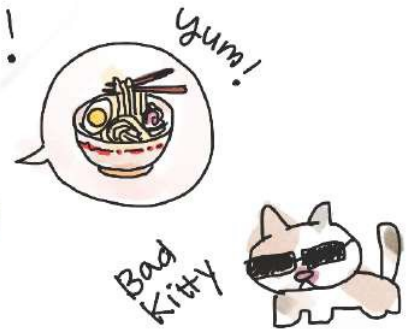
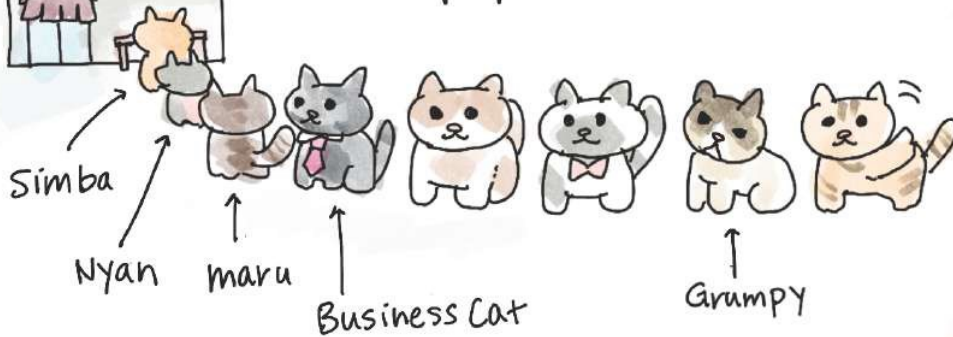
LIFO

@girlie_mae

A queue is a FIFO (First-in-First-out) data structure, where an element added first (= enqueue) gets removed first (= dequeue)



just like waiting in line at a popular restaurant!



★ Stack as an array in JS

```
let queue = [ ];  
queue.push('Simba'); // ['Simba']  
queue.push('Nyan'); // ['Simba', 'nyan']  
queue.push('maru'); // ['Simba', 'nyan', 'maru']  
let eater = queue.shift(); // eater is 'Simba'
```

if you queue.unshift('bad Kitty'), then the cat cuts in to the front of line!

Wrong!

Time complexity should be $O(1)$ for both enqueue + dequeue but JS shift() is slower!

queue is ['nyan', 'maru']

Data Structures Hash Table

- ⇒ A hash table is used to index large amount of data
- ⇒ Quick Key-value look up. $O(1)$ on average
 - ↳ Faster than brute-force linear search

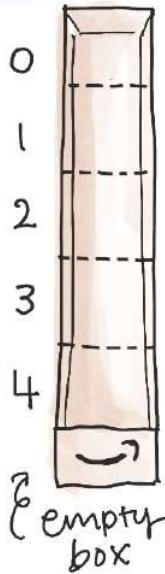
① Let's create an array of size 5.

We're going to add 🐱 data.

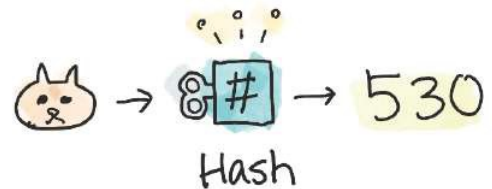
Key = "Tabby"

Value = "pizza"

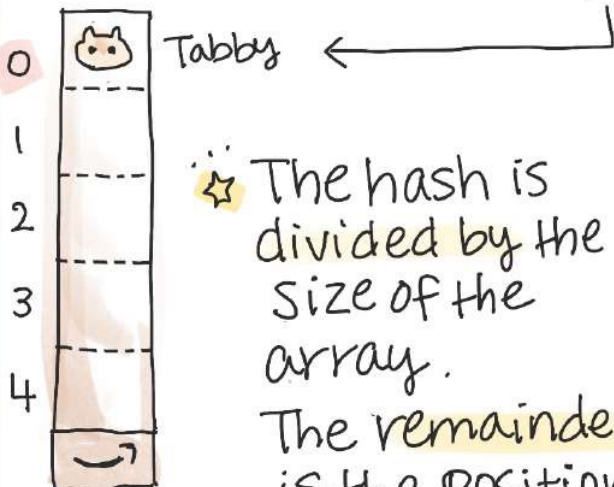
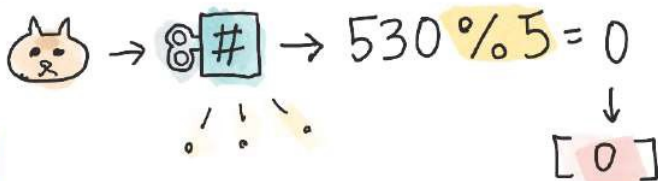
Some data
Let's say, favorite food!



② Calculate the hash value by using the Key, "Tabby".
e.g. ASCII code, MD5, SHA1

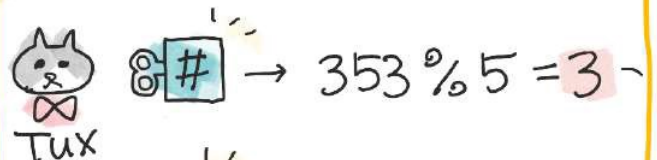


③ Use modulo to pick a position in the array!

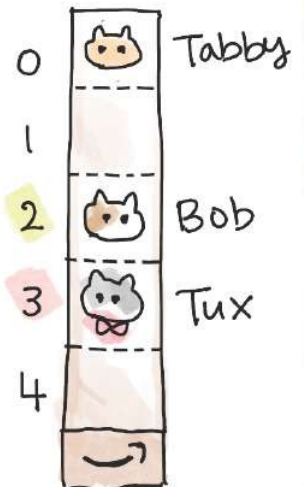


☆ The hash is divided by the size of the array.
The remainder is the position!

④ Let's add more data.



Use the same method to add more 🐱



★ Collision!



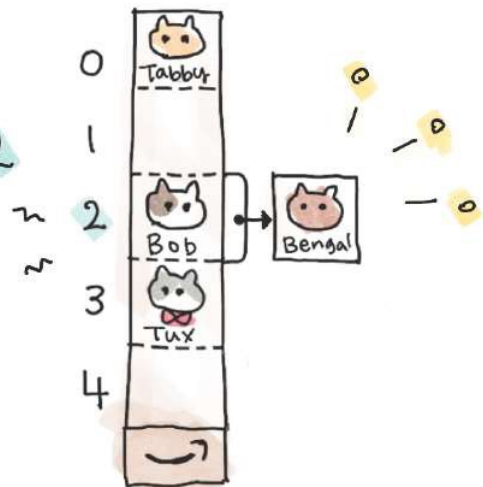
Hash Table

@girlie-mac

Now we want to add more data.
Let's add "Bengal".

🐱 "Bengal" → 8# → $617 \% 5 = 2$

But [2] slot has been taken
by "Bob" already! = collision!
so let's chain Bengal next
to Bob! = chaining

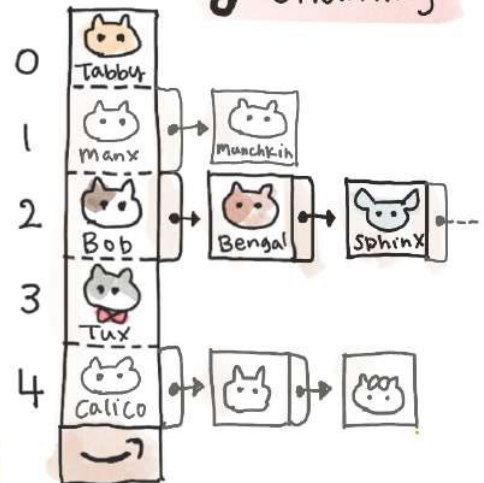


key: "Bengal"
Value: "Dosa"

"Sphinx"
"Fish +
Chips"

Keep
adding
data

🔗 chaining



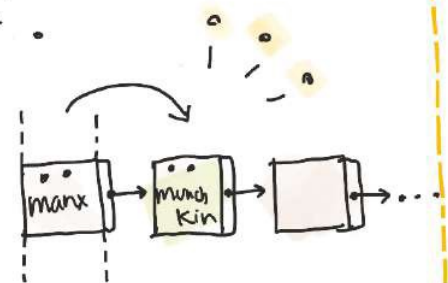
Searching for data

★ Let's look up the value for "Bob"

- ① Get the hash → 307
- ② Get the index → $307 \% 5 = 2$
- ③ Look up Array [2] → found!

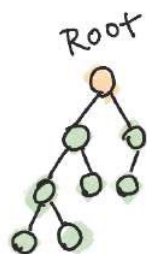
★ Let's look up "munchkin"

- ① Hash → 861
 - ② Index → $861 \% 5 = 1$
 - ③ Array [1] → "Manx"
 - ④ Operate a linear-search to find "munchkin"
- ↳ Average $O(n)$



Data Structures

Binary Heap



Binary tree

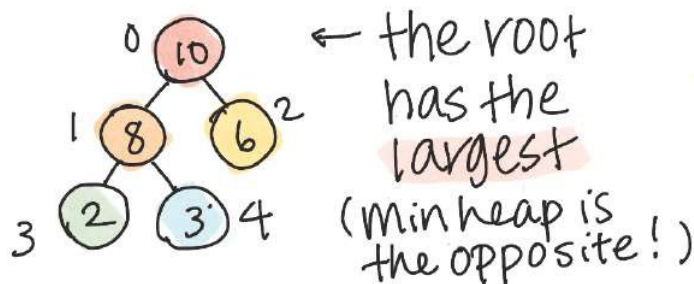
tree data structure
each node has at most 2 children

Binary search tree

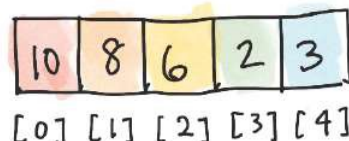
Binary heap

- Complete tree
- Min heap or max heap
- used for priority queue, heap sort etc.

★ Max heap

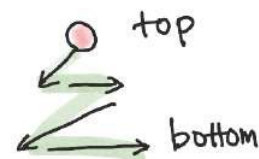


in array



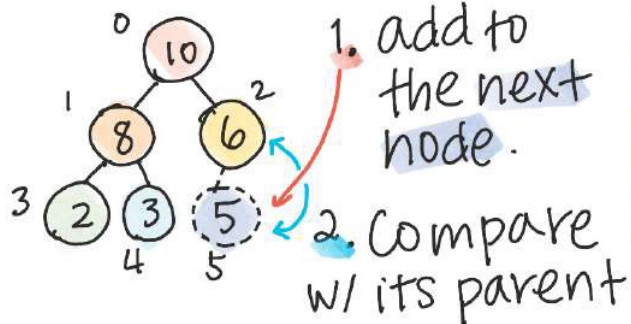
each node has 0 - 2 children

always fill top → bottom, left → right



★ Insertion

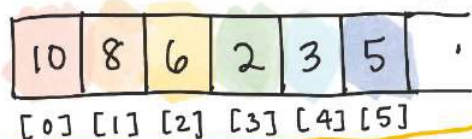
Let's add 5 to the heap!



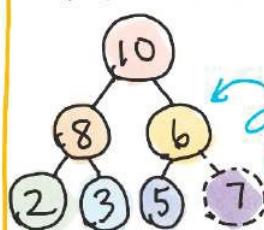
3. the parent is greater.

Cool, it's done!

Let's add more!



Add 7



1. Add to the next node

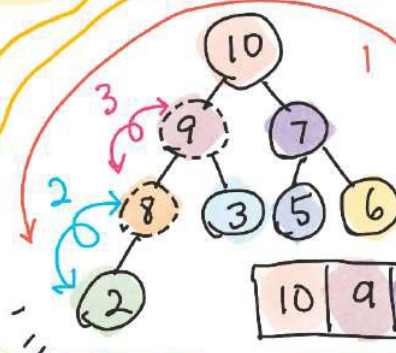
2. Compare w/ parent.

Oh, no!

the parent is smaller than its child! Swap them !!!

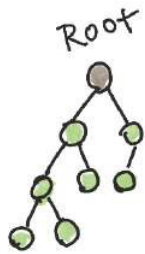


Add to the next node & repeat the process!



Data Structures

Binary Search Tree



Binary tree

- tree data structure
- each node has at most 2 children

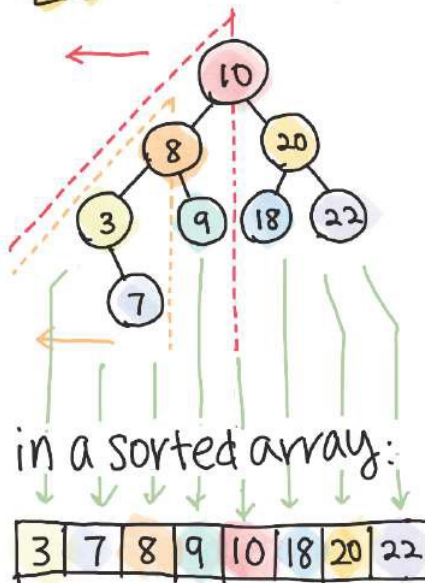
Binary heap

Binary Search Tree

- a.k.a. Ordered or sorted binary tree

- fast look up
e.g. phone number lookup table by name

👍 Rule of thumb



★ each value of all nodes in the left subtrees is lesser

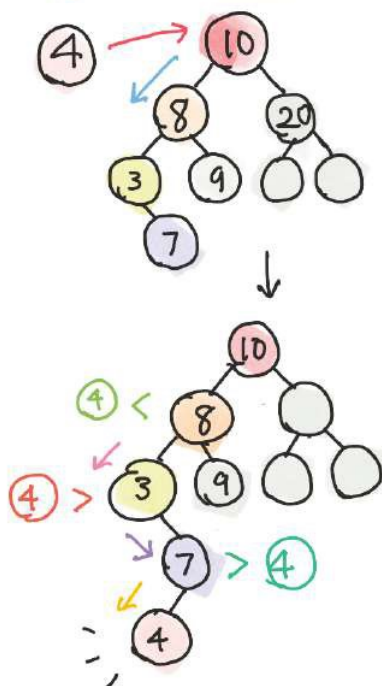
△ 10's left subtrees: 8, 3, 9, 7

△ 8: 3, 7 ← smaller than parent

★ each value of all nodes in the right subtrees is larger

★ no duplicate values

☆ Insertion → Always add to the lowest spot to be a leaf ~~leaf~~ No rearrange!



Let's add 4

1. Compare w/ the root first.

2. 4 < 10 so go left.

3. then compare w/ the next, 8

4. 4 < 8 so go left

5. Compare w/ the 3

6. 4 > 3 so go right.

7. Compare w/ the 7

8. 4 < 7, so add to the left! Done.

Complexity:

Ave. $O(\log n)$

Worst. $O(n)$