

THE PATCH FRAME AND ITS RELATIONS WITH SEPARATION IN POINT-FREE TOPOLOGY

ABSTRACT.

1. INTRODUCTION

Aquí va la introducción.

2. PRELIMINARIES

3. HAUSDORFF PROPERTIES IMPLIES PATCH TRIVIALITY

Gadgets:

A the base frame

Its point space $S = \text{pt}(A)$.

The compact saturated sets of S ,

$$Q(S).$$

The preframe of open filters of A ,

$$A^\wedge.$$

The preframe of open filters of $\Omega(S)$.

$$\Omega(S)^\wedge.$$

First we recall that every open filter $F \in A^\wedge$ has three faces, that is, determines (and its determine) by :

- The compact saturated $Q \in QS$.
- $\nabla \in \Omega(S)^\wedge$.
- The compact quotient $A \rightarrow A_F$.
- The fitted nucleus v_F .

Hoffman-Mislove can be rephrase:

There is a bijection between compact quotients of A and compact saturated sets of S

Definition 3.1. A frame has KC if every compact quotient of A is a closed one. In other words every compact sublocale is close.

Denote by \mathcal{Hrm} the subcategory of \mathcal{Frm} of Hausdorff frames in the sense of Johnstone and Shu.

The block structure on a frame is an important problem and its related with some separation properties of frames.

Proposition 3.2. *For every $A \in \mathcal{H}rm$ the interval corresponding to the block determined by a open filter $F \in A^\wedge$ is trivial, that is,*

$$[v_F, w_F] = \{*\}$$

Proposition 3.3. *Every Hausdorff frame A (in the sense of Johnstone and Shou) is tidy, that is, A is patch trivial.*

Proof.

□

REFERENCES