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# **Algorithms Lab**

### **Exercise** – *Stamp Exhibition*

The National Postal Museum organizes a major exhibition of postage stamps. Many collectors from all over Europe have already agreed to present their most valuable pieces at this special event. However, Mr. Pennybag—owner of a well preserved "Basel Dove"—is still hesitating. He fears that the bright light in the museum might cause damage to his stamps. In order to prevent this, you were hired to set up the lamps.

The museum consists of one large room. The stamps are placed on the floor and the lamps hang down from the ceiling, lighting the room from above. In principle, any lamp can light any stamp in the museum. However, to enhance the ambiance, a number of movable wall-elements—simply called *walls* in the following—are placed all over the museum. The walls reach up to the ceiling of the room and block the light emitted by the lamps.

For simplicity, we model the situation in  $\mathbb{R}^2$ , much like the situation would be seen from above. Both lamps and stamps appear as points and the walls appear as line segments. All lamps can be dimmed individually. That is, you can set the power  $p_i$  of the i-th lamp to an arbitrary real value  $1 \le p_i \le 2^{12}$ . An object at distance r from the i-th lamp is illuminated at intensity  $I(r) = p_i r^{-2}$ , if there is no wall between them; or zero, if the line segment between the lamp and the stamp intersects a wall (any intersection counts, even if it is at an endpoint of the wall segment). Note that only walls block light, whereas lamps and stamps do not interfere with illumination.

The total illumination intensity  $I_j$  for the j-th stamp is obtained by adding up the respective intensities for all lamps. On the one hand, each stamp must be illuminated with total intensity at least one  $(I_j \ge 1)$  in order to be visible. On the other hand, for each stamp the respective owner may prescribe a maximum total illumination intensity  $M_j$  that is not to be exceeded  $(I_j \le M_j)$ .

You may assume that all input objects (lamps, stamps and walls) are pairwise disjoint.

**Input** The first line of the input contains the number of test cases  $t \le 100$ . Each of the following t test cases is described as follows.

- It starts with a line that contains three integers  $\ell, s, w$  separated by single spaces denoting the number of lamps, stamps and walls, respectively  $(0 \le w \le 2'000, 0 \le \ell, s \le 200)$ .
- $\ell$  lines follow. The *i*-th such line contains two integers  $x_i, y_i$  separated by single spaces, describing the position  $(x_i, y_i)$  of the *i*-th lamp  $(|x_i|, |y_i| \le 2^{24})$ .
- s lines follow. The j-th such line contains three integers  $x_j, y_j, M_j$  separated by single spaces, describing the position  $(x_j, y_j)$  of the j-th stamp and the maximal allowed light intensity  $M_j$  ( $|x_j|, |y_j| \le 2^{24}, 1 \le M_j \le 2^{24}$ ).
- w lines follow. The k-th such line contains four integers  $a_k, b_k, c_k, d_k$ , where  $(a_k, b_k)$  and  $(c_k, d_k)$  are the endpoints of the k-th wall  $(|a_k|, |b_k|, |c_k|, |d_k| \le 2^{24}, (a_k, b_k) \ne (c_k, d_k))$ .

(See the next page for the rest of the description.)

**Output** For every test case the corresponding output appears on a separate line. It consists of a single word: yes, if it is possible to illuminate all stamps as required (i.e.  $1 \le I_j \le M_j$  for  $j = 1, \ldots, s$ ); and no, otherwise.

**Points** There are three groups of test sets. The hidden group is worth 20 points and the other two 40 each. Therefore the maximum total number of points is 100.

- 1. For the first group of test sets, you may assume that there are no walls (w = 0). Corresponding example test sets are contained in the files stamps-test1.in/out.
- 2. For the second group of test sets, there are no additional restrictions. Corresponding example test sets are contained in the files stamps-test2.in/out.
- 3. For the third (hidden) group of test sets there are no additional assumptions.

#### Sample Input

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#### Sample Output

no no yes