

NEW SPECIMEN PAPERS PUBLISHED JUNE 2015

GCSE Mathematics Specification (8300/3H)



Paper 3 Higher tier

Date Morning 1 hour 30 minutes

Materials

For this paper you must have:

- a calculator
- mathematical instruments.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the bottom of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book.
- In all calculations, show clearly how you work out your answer.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper.
 These must be tagged securely to this answer book.

Centre number			Ca	ındic	date	e nu	ımb	er							
Surname															
Forename(s)															
Candidate signa	ature _														- /

Answer all questions in the spaces provided.

1 Work out the square root of 100 million.

Circle your answer.

[1 mark]

1000

10 000

100 000

1 000 000

$$\mathbf{a} = \begin{pmatrix} 5 \\ -2 \end{pmatrix} \quad \text{and} \quad \mathbf{b} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$$

Circle the vector $\mathbf{a} - \mathbf{b}$

[1 mark]

$$\begin{pmatrix} -3 \\ -5 \end{pmatrix}$$

$$\begin{pmatrix} 7 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} 3 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} 7 \\ -5 \end{pmatrix}$$

3 Circle the decimal that is closest in value to $\frac{2}{3}$

[1 mark]

0.6

0.66

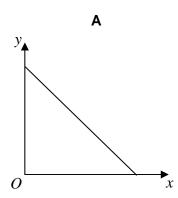
0.667

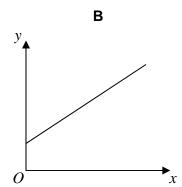
0.67

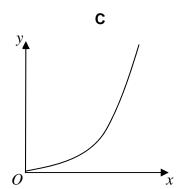
4 y is directly proportional to x.

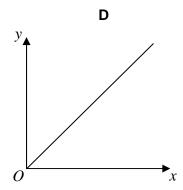
Which graph shows this? Circle the correct letter.

[1 mark]









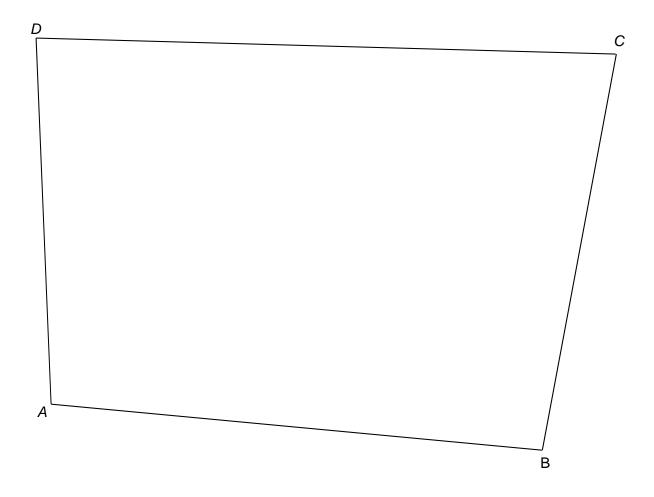
Turn over for the next question

In 2013 it was £6.31 per ho	3411			
Work out the percentage in	ncrease in the	minimum wa	ge.	
	Answer			%
A bag contains counters th	at are red, blu	ue, green or y	ellow.	
	red	blue	green	yellow
	ieu	Dide	green	yenow
Number of counters	9	3 x	<i>x</i> – 5	2 <i>x</i>
		3 <i>x</i>	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand	dom.	3 <i>x</i>	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3 <i>x</i>	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3x	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3x	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand The probability it is red is -	dom. <u>9</u> 100	3x	<i>x</i> – 5	2 <i>x</i>
A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3x	<i>x</i> – 5	2x
A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3x	<i>x</i> – 5	2x
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A counter is chosen at rand The probability it is red is	dom. <u>9</u> 100	3x	<i>x</i> – 5	2x

7 Use ruler and compasses to answer this question.

Point P is

- the same distance from AB and AD
- 6 cm from *C*.



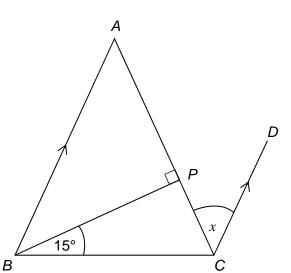
Show the position of *P* on the diagram.

[3 marks]

Turn over for the next question

8	(a)	Use your calculator to		² – ³ √1006 ÷ 4.95		[1 mark]
			Answer			
8	(b)	Use approximations to You must show your		nswer to part (a) is se	nsible.	[2 marks]
9		The exterior angle of a		s 45°		[1 mark]
		pentagon	hexagon	octagon	decagon	

10 ABC is a triangle with AB = ACBA is parallel to CD.



Not drawn accurately

Show that angle $x = 30^{\circ}$

_		[3 marks]

The pressure at sea level is 101 325 Pascals.	
Any rise of 1 km above sea level decreases the pressure by 14%	
For example,	
at 3 km above sea level the pressure is 14% less than at 2 km	
Work out the pressure at 4 km above sea level.	
Give your answer to 2 significant figures.	
erre year anemer to 2 eigrimoant ngareer	[4 mark
Answer Pascals	

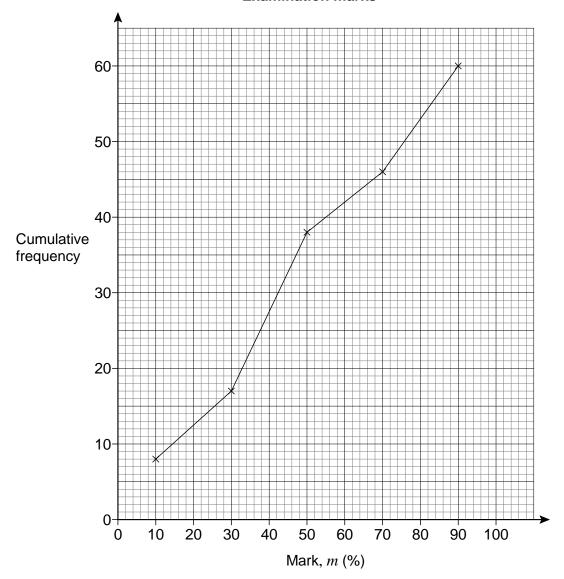
12	Tick whether each statement is true or false. Give a reason for your answer.
12 (a)	When $x^2 = 16$ the only value that x can be is 4 [1 mark]
	True False
	Reason
12 (b)	When n is a positive integer, the value of $2n$ is always a factor of the value of $20n$. [1 mark] True False
	Reason
12 (c)	When y is positive, the value of y^2 is always greater than the value of y . [1 mark] True False
	Reason

Here are the examination marks for 60 pupils.

Mark, <i>m</i> (%)	Frequency
0 ≤ <i>m</i> < 20	8
20 ≤ <i>m</i> < 40	9
40 ≤ <i>m</i> < 60	21
60 ≤ <i>m</i> < 80	10
80 ≤ <i>m</i> < 100	12

Molly drew this cumulative frequency graph to show the data.





Make two criticism	ns of Molly's graph.	[2
Criticism 1		
Criticism 2		
	Turn over for the next question	
	Turn over for the next question	

14 (a) The <i>n</i> th term of a sequence is $2^n +$	4 (a)	a) The n th term of a se	equence is 2	$2^{n} + 2^{n-1}$
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Work out the 10th term of the sequence.

[1 mark]

14 (b) The *n*th term of a different sequence is $4(2^n + 2^{n-1})$

Circle the expression that is equivalent to $4(2^n + 2^{n-1})$

[1 mark]

$$2^{n+2} + 2^{n+1}$$

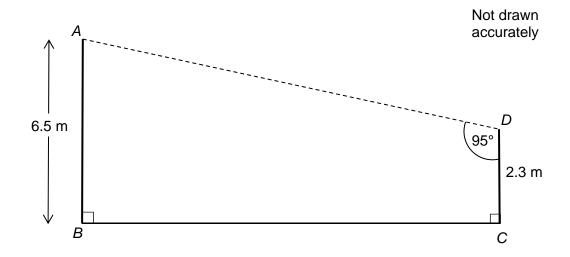
$$2^{2n} + 2^{2(n-1)}$$

$$8^{n} + 8^{n-1}$$

$$2^{n+2} + 2^{n-1}$$

15 The diagram shows a design for a zipwire.

The zipwire will run between the top of two vertical posts, AB and CD.



Work out the distance AD.	[4 marks]

Answer m

6	During a game, players can win and lose counters.	
	At the start of the game	
	Rob, Tim and Zak share the counters in the ratio 5:6:7	
	At the end of the game	
	Rob, Tim and Zak share the same number of counters in the ratio 7:9:	: 8
	Show that Rob ends the game with more counters than he started with.	[3 marks]
7	Factorise $3x^2 + 14x + 8$	[2 marks]
7	Factorise $3x^2 + 14x + 8$	[2 marks]
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7		[2 marks]
7	Factorise $3x^2 + 14x + 8$ Answer	[2 marks]
7		[2 marks]

Here is some information about the number of books read by a group of people in 2014

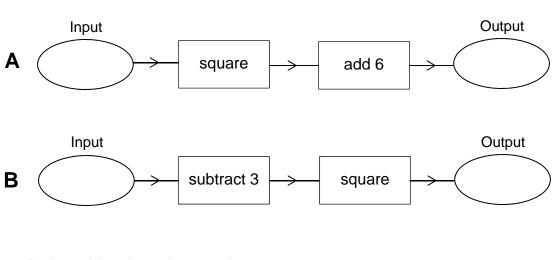
One of the frequencies is missing.

Number of books	Frequency	Midpoint	
0 – 4	16	2	
5 – 9		7	
10 – 14	20	12	
15 – 19	10	17	

Midpoints are used to work out an estimate for the mean number of books read. The answer is 8.5

	[5 marks]
	[J IIIdi KS]
Answer	

19 Here are two function machines, A and B.



Both machines have the same input.

Work out the range of input values for which

the output of ${\bf A}$ is ${\bf less}$ than the output of ${\bf B}.$

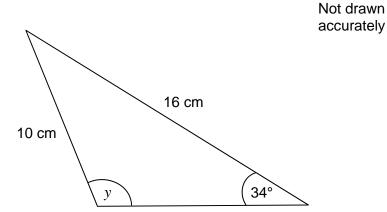
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Answer

Version 1.0 8300/3H

[4 marks]

20	In the triangle,	angle y is	obtuse.
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Work	out 1	tne	size	OT	andie	ν.

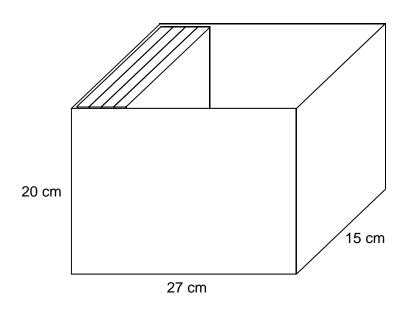
[3 marks]

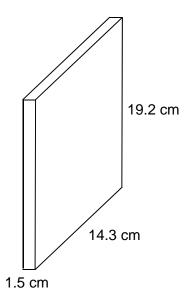
degrees Answer

Turn over for the next question

A box is a cuboid with dimensions 27 cm by 15 cm by 20 cm.
These dimensions are to the nearest **centimetre**.

DVD cases are cuboids with dimensions 1.5 cm by 14.3 cm by 19.2 cm. These dimensions are to the nearest **millimetre**.





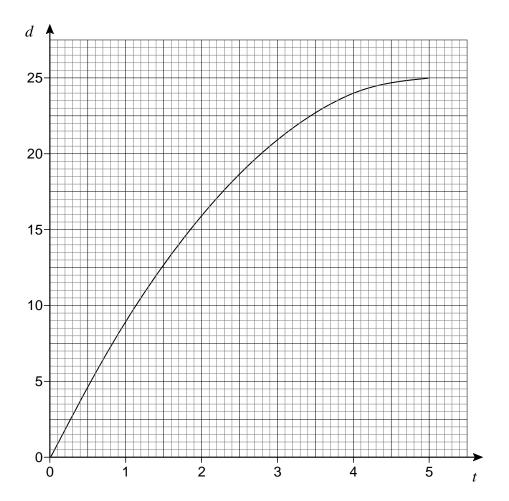
Show that 17 DVD cases, stacked as shown, will definitely fit in the box.

[4 marks]

Bag X contains 9 blue balls and 18 red balls. Bag Y contains 7 blue balls and 14 red balls.	
Liz picks a ball at random from bag X.	
She puts the ball into bag Y.	
Mike now picks a ball at random from bag Y.	
Show that	
P (Liz picks a blue ball) = P (Mike picks a blue ball)	
	[4 marks]

A container is filled with water in 5 seconds.

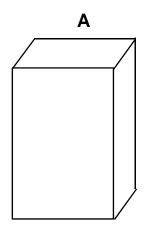
The graph shows the depth of water, d cm, at time t seconds.

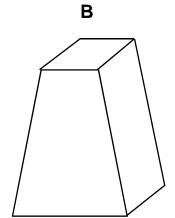


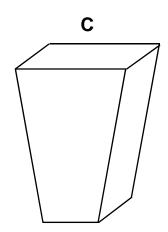
23	(a)	The water flows into the container at a constant rate.
	` '	

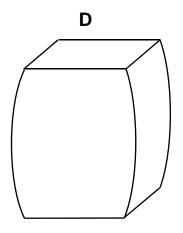
Which diagram represents the container? Circle the correct letter.

[1 mark]









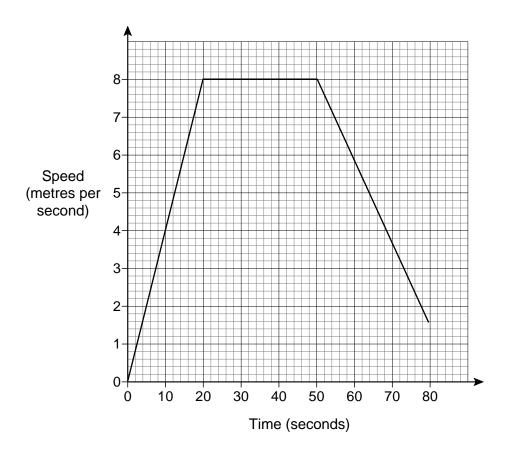
23 (b) Use the graph to estimate the rate at which the depth of water is increasing at 3 seconds. You **must** show your working.

Answer _____ cm/s

[2 marks]

24 Amina and Ben had a cycle race.

Here is Amina's speed-time graph from the start of the race.



24	The distance of the race was 400 metres. Ben cycled the 400 metres in 64 seconds.					
	Who won the race?					
	You must show your working.	[4 marks]				
	Answer	-				
	Turn over for the next question					

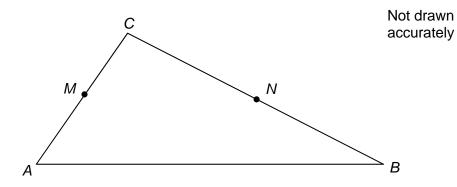
25	In triangle	ABC
	iii tiidiigio	,,,,,,,

M is the midpoint of *AC*

N is the point on BC where BN: NC = 2:3

$$\rightarrow$$
 $AC = 2a$

$$\overrightarrow{AB} = 3\mathbf{b}$$



			\rightarrow	
25	(a)	Work out	MN	in terms of a and b .

C:		00011101	:	:4~	-:	-14	f ~ ""	
Give	your	answer	m	แร	SIIII	piesi	101111	

[3 marks]

Answer			

[1	mark]
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An approximate solution to an equation is found using this iterative process.

$$x_{n+1} = \frac{(x_n)^3 - 3}{8}$$
 and $x_1 = -1$

26 (a) Work out the values of x_2 and x_3

[2 marks]

 $x_2 = \underline{\hspace{1cm}}$

 $x_3 =$

26 (b) Work out the solution to 6 decimal places.

[1 mark]

r –

The curve with equation $y = x^2 - 5x + 2$ is reflected in the *x*-axis.

Circle the equation of the reflected curve.

[1 mark]

$$y = x^2 - 5x - 2$$

$$y = -x^2 + 5x + 2$$

$$y = -x^2 + 5x - 2$$

$$y = x^2 + 5x + 2$$

27	
The diagram shows a line joining O to P .	
<i>y</i>	Not drawn accurately
• P	$\longrightarrow_{\mathcal{X}}$
The gradient of the line is $\sqrt{2645}$	
Work out the coordinates of <i>P</i> .	[4 mar
Answer (
END OF QUESTIONS	
	The diagram shows a line joining O to P . The gradient of the line is 2 The length of the line is $\sqrt{2645}$ Work out the coordinates of P .

