

Problem Statement

The Finite State Machine Project 1 is a four-bit password checker, checking four binary values, applied one at a time to the FSM. The FSM must only reset once all four bits have been input, even if the bits are wrong.

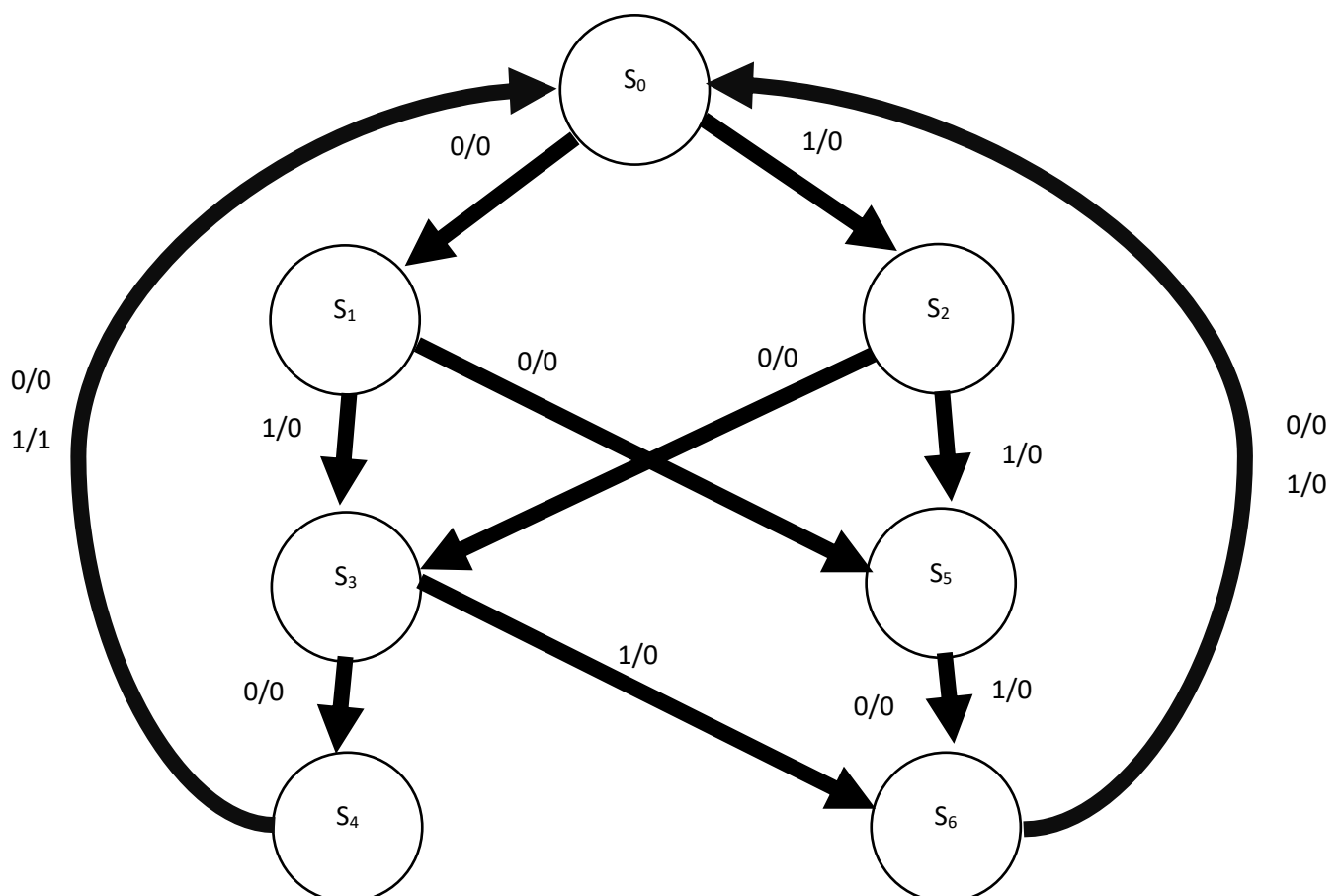
Two possible passwords exist: 0101 and 1001 (or 5 and 9). If either of these numbers are detected, then it outputs a “true”, a single bit 1. Otherwise, it outputs 0.

For this, I have assumed that every single input will be a 0 or 1 and have not accounted for undeclared or invalid bits. Also, the FSM will continue to check for a correct code, even after the correct code has been entered.

Finite State Machine Design

Because the output is dependent on the current input, this FSM is a Mealy machine.

State	Sequence Received
S ₀	Reset
S ₁	0
S ₂	1
S ₃	01 / 10
S ₄	010 / 100
S ₅	Two incorrect inputs
S ₆	Three incorrect inputs



Current State (ABC)	Input	Next State (ABC)	Output
S ₀ (000)	0	S ₁ (001)	0
	1	S ₂ (010)	0
S ₁ (001)	0	S ₅ (101)	0
	1	S ₃ (011)	0
S ₂ (010)	0	S ₃ (011)	0
	1	S ₅ (101)	0
S ₃ (011)	0	S ₄ (100)	0
	1	S ₆ (110)	0
S ₄ (100)	0	S ₀ (000)	0
	1	S ₀ (000)	1
S ₅ (101)	0	S ₆ (110)	0
	1	S ₆ (110)	0
S ₆ (110)	0	S ₀ (000)	0
	1	S ₀ (000)	0
S ₇ (111)	0	X (XXX)	X
	1	X (XXX)	X

$$A = C \text{ INPUT}' + BC + AC + AB \text{ INPUT}$$

AB	C INPUT	00	01	11	10
00					1
01			1	1	1
11				X	X
10				1	1

$$B = C \text{ INPUT} + AC + A'B' \text{ INPUT} + A'BC' \text{ INPUT}'$$

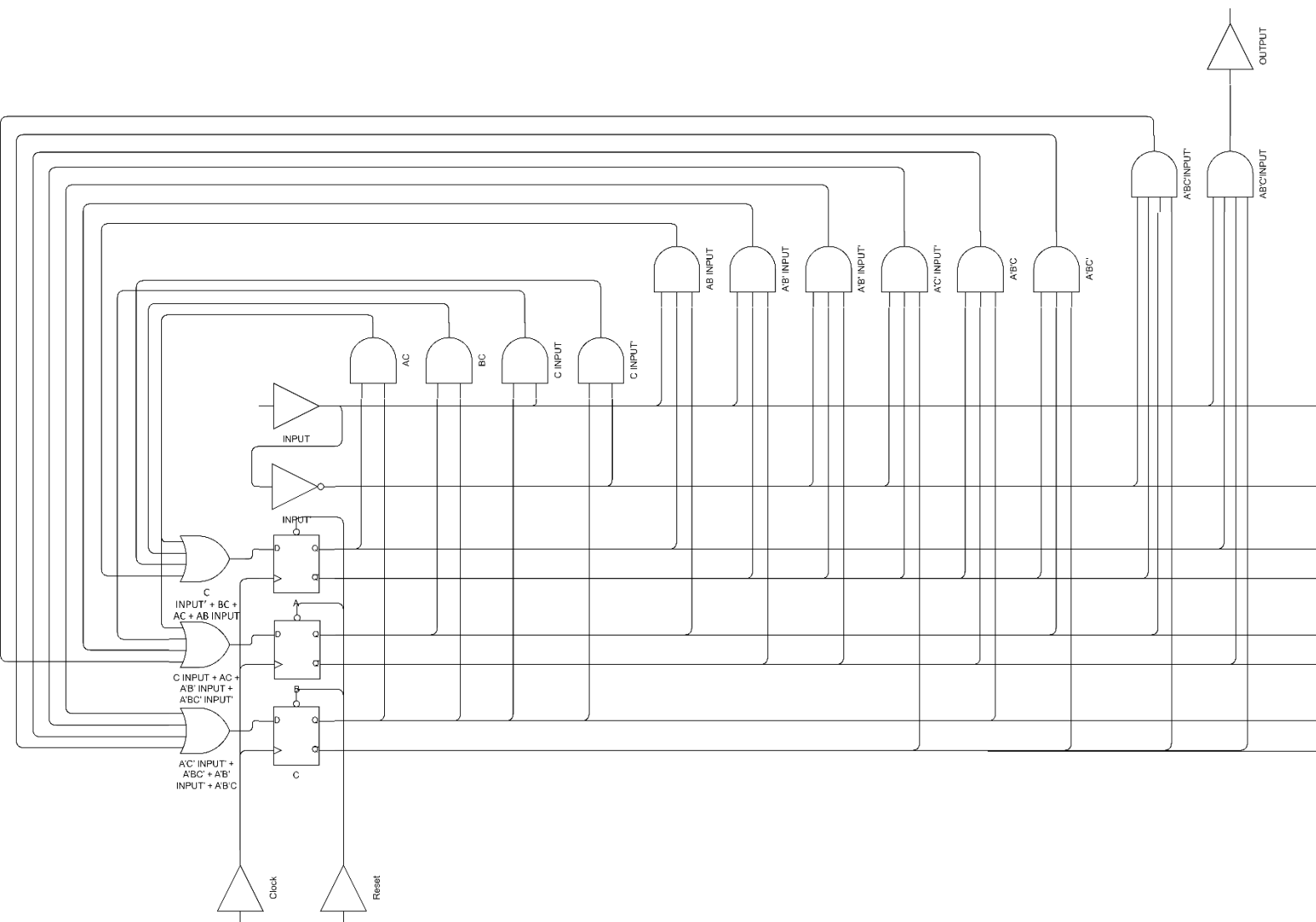
AB	C INPUT	00	01	11	10
00			1	1	
01	1			1	
11				X	X
10				1	1

$$C = A'C' \text{ INPUT}' + A'BC' + A'B' \text{ INPUT}' + A'B'C$$

AB	C INPUT	00	01	11	10
00		1		1	1
01		1	1		
11				X	X
10					

$$\text{OUTPUT} = AB'C' \text{ INPUT}$$

AB	C INPUT	00	01	11	10
00					
01					
11				X	X
10			1		



The Verification Plan

To test this FSM, it's fairly easy to just test every possible 4-bit integer, and see which integer causes the machine to output a 1. To achieve this, I have 2 for loops; one to pick the number, and the other to split the number into the single bit chunks the FSM receives. As we can see here, the machine outputs a 1 after 5 (0101) and 9(1001), as expected.

