



Center for Computer Graphics
and Virtual Reality, Ewha



e-Entertainment을 위한 실시간 물리 시뮬레이션 기술

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Slides

- <http://graphics.ewha.ac.kr/HCI2010.pdf>



실시간 물리 시뮬레이션

개념: 객체들 간의 상호작용이 현실 세계의 물리 법칙을 따르도록 실시간에 시각적으로 시뮬레이션 하는 기술



강체



관절체 (ragdoll)



Particle



차량



물리 엔진 응용 게임



마비노기 영웅전, Nexon



Forza Motorsport 3, Microsoft



허슬 당구, Dream Arrow



Fight Night Round 4, EA

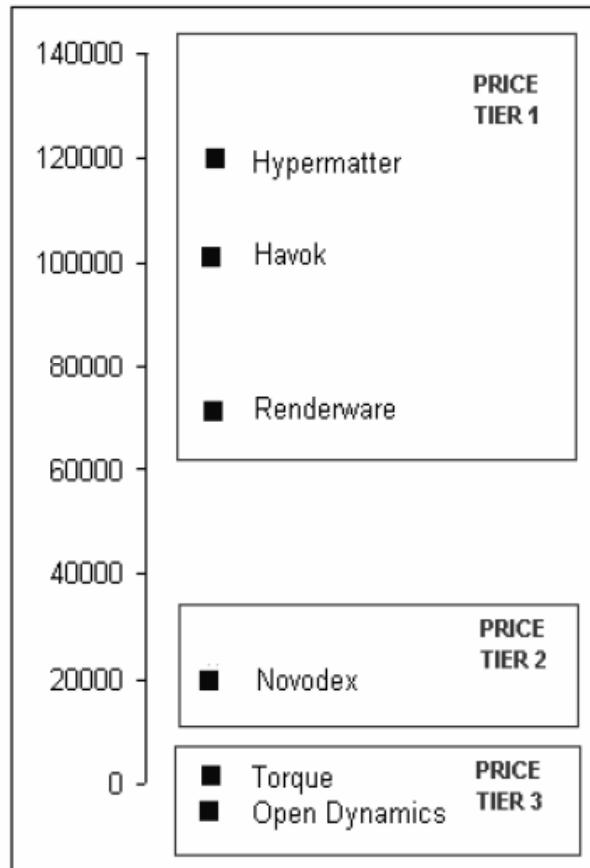


기술 동향 – 대표적 물리 SW

개발회사명	상품명	형태	국가명	역사
HAVOK	HAVOK	SW (\$100K)	아일랜드	1998년에 Trinity대학의 연구 그룹에 의해서 시작된 대표적인 실시간 물리 시뮬레이션 개발 회사로, 영국과 미국에 분소가 있으며, 2007년에 Intel에 인수됨
AGEIA	PhysX	SW/HW (\$20K)	스위스	1995년에 스위스의 ETH공대의 연구 그룹에 의해서 시작된 회사로, 초기에는 NovodeX라는 프로덕트로 알려져 있었음. 2005년에 Meqon 물리엔진 인수. 2008년 nVIDIA에 인수됨
Open Dynamics Engine	Open Dynamics Engine	SW (무료)	미국	2000년에 Russel Smith에 의해 시작된 개인 프로젝트. 강체/관절체 시뮬레이션등 제한적 기능.
BULLET	BULLET	SW (무료)	미국	Sony Playstation Research의 Erwin Coumans에 의해서 유지되는 물리 시뮬레이션 소프트웨어. 강체/관절체 시뮬레이션등 제한적 기능.



기술 동향 – SW 가격



- 가격대
 1. 9천만 원~1억5천만 원
 2. 2천만 원~3천만 원
 3. 10만 원 이하

[Saral and Schmieder 2004]

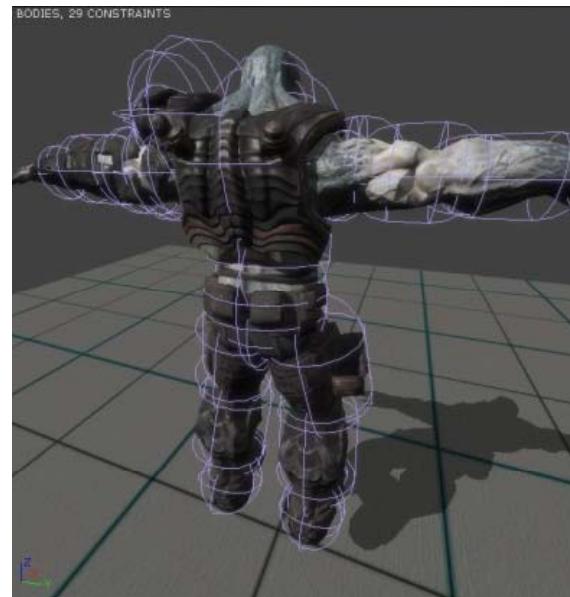


차세대 물리엔진개발의 필요성

- 흥행 게임 타이틀 필수 요소
- 렌더링 퀄러티와 인터랙션 퀄러티의 격차



고품질 렌더링 결과
(Unreal3 엔진)



단순화된 물리 시뮬레이션



차세대 물리엔진개발의 필요성

- 비 실시간 위주의 국내 기존 연구



유체, ETRI



Qualoth, FxGear

- 멀티 코어 CPU, GPU, PPU등의 차세대 하드웨어 플랫폼의 등장

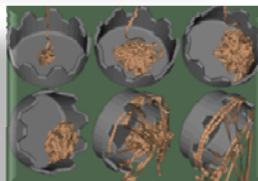


실시간 (30 FPS) VS 비실시간 물리 엔진



관절체: 3초 / frame

↔ 100X 속도 향상 필요



Cloth (리본): 3~30 초 / frame

↔ 1000X 속도 향상 필요



깨진 토끼: 1 분/ frame

↔ 2000X 속도 향상 필요



유체: 10일

↔ ☺



차세대 물리엔진개발의 필요성

- 한국적 상황에 맞는 물리 엔진 제작 필요성
 - 모바일, light-weight, customization
- 모든 영역에 최적화된 물리 엔진은 존재안함
 - Havok, PhysX가 cover하지 못하는 영역이 존재
 - 예: Rockstar games의 GTA4



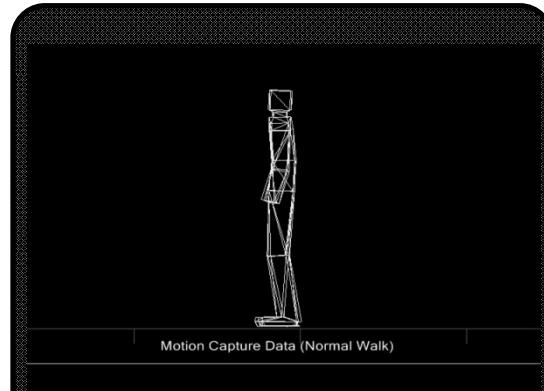
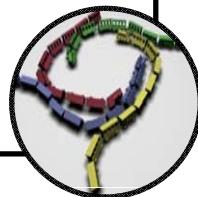


워샵 발표 내용

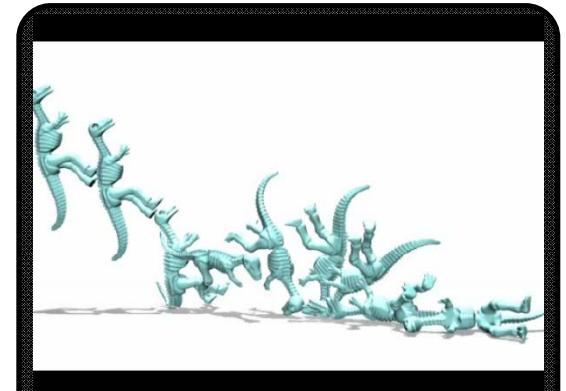
차세대 물리 시뮬레이션 기술 개발



동역학 시뮬레이션



데이터 기반
물리 시뮬레이션



변형 시뮬레이션





발표 순서

1:30 pm – 2:40 pm	워샵 소개
1:40 pm – 2:15 pm	실시간 강체 및 관절체 충돌검사 (김영준, 이화여대)
2:15 pm – 2:50 pm	실시간 강체 동역학 시뮬레이션 (김진욱, KIST)
2:50 pm – 3:00 pm	휴식
3:00 pm – 3:35 pm	물리기반 캐릭터 시뮬레이션 (이윤상/이제희, 서울대)
3:35 pm – 4:10 pm	대용량 변형 모델 실시간 충돌검사 (윤성의, KAIST)
4:10 pm – 4:20 pm	휴식
4:20 pm – 4:55 pm	실시간 유연체 시뮬레이션 (최민규, 광운대)
4:55 pm – 5:15 pm	Space Foosball: 콘텐츠 제작 사례 (방현우, 서울대)
5:15 pm – 5:25 pm	Q&A



Real-time Collision Detection for Rigid and Articulated-Body Dynamics

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<http://graphics.ewha.ac.kr>



Why Proximity Calculation?

- Contact dynamics
 - 1. Collision detection
 - 2. Collision response





Collision Processing Loop in Contact Dynamics

- Broad phase: n-body collision detection

GPU-based n-body collision detection

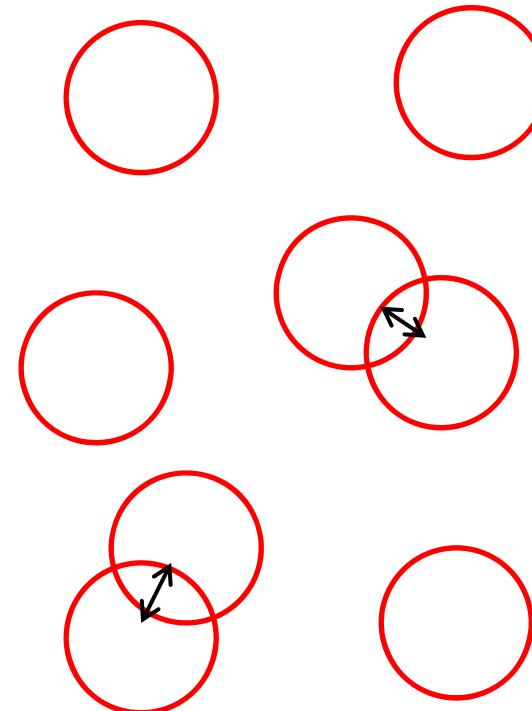
- Narrow phase:

1. Collision detection
 - Collision point, normal
 - *Penetration depth*
 - *Continuous CD*

Real-time penetration depth

Real-time continuous collision detection

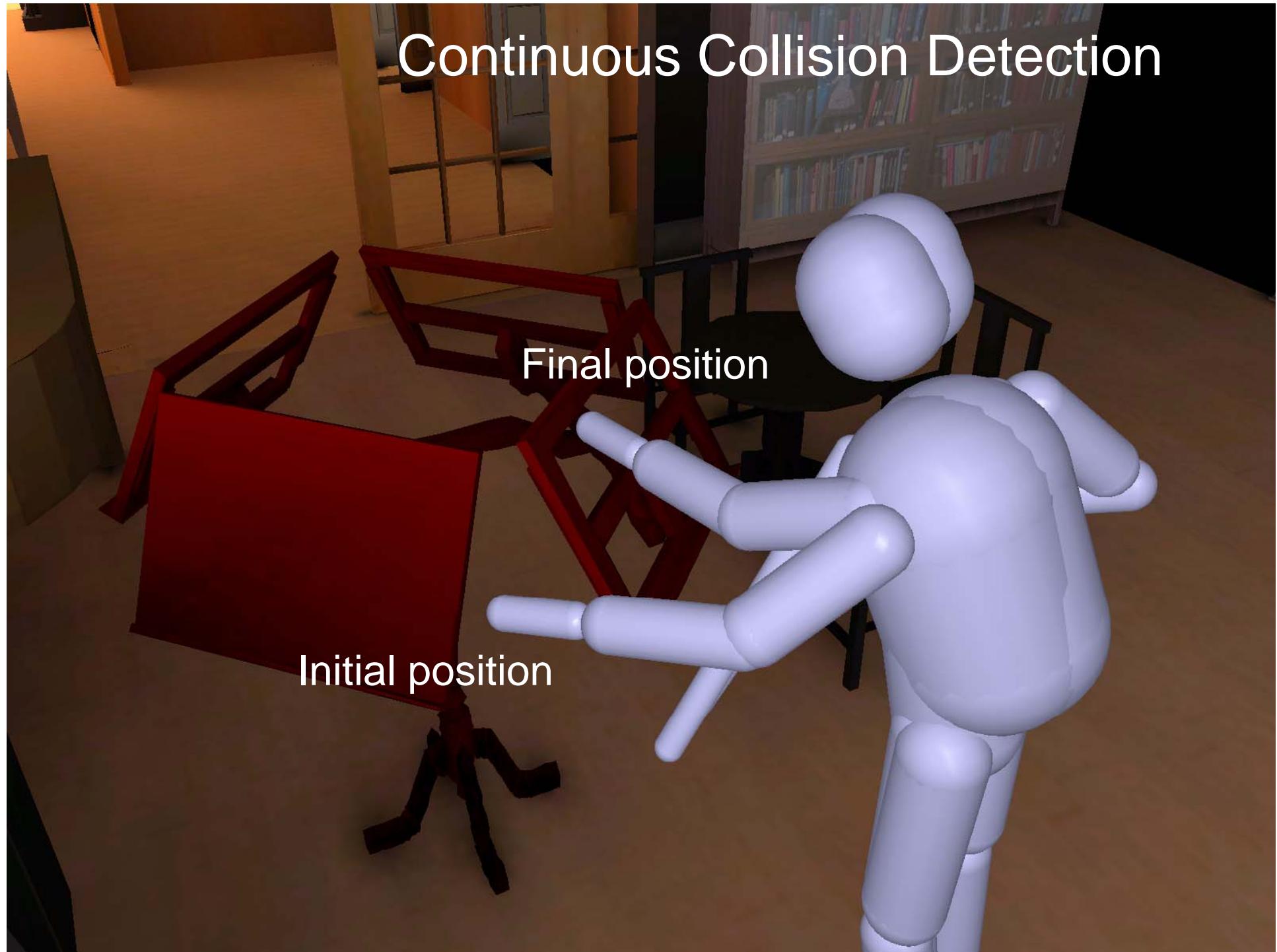
Parallel collision detection





REAL-TIME CONTINUOUS COLLISION DETECTION

Continuous Collision Detection

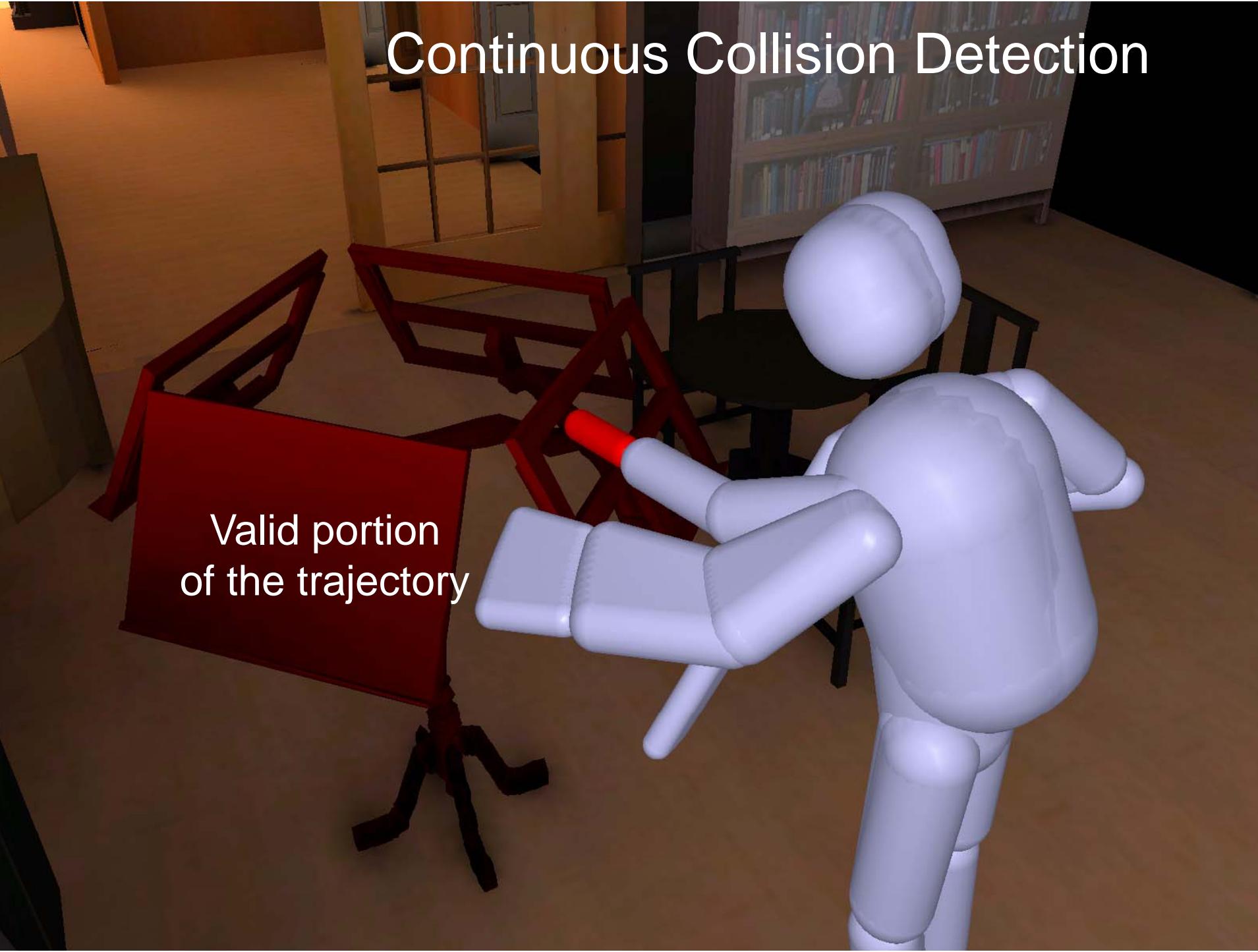


Continuous Collision Detection

Interpolation and
Collision Checking



Continuous Collision Detection

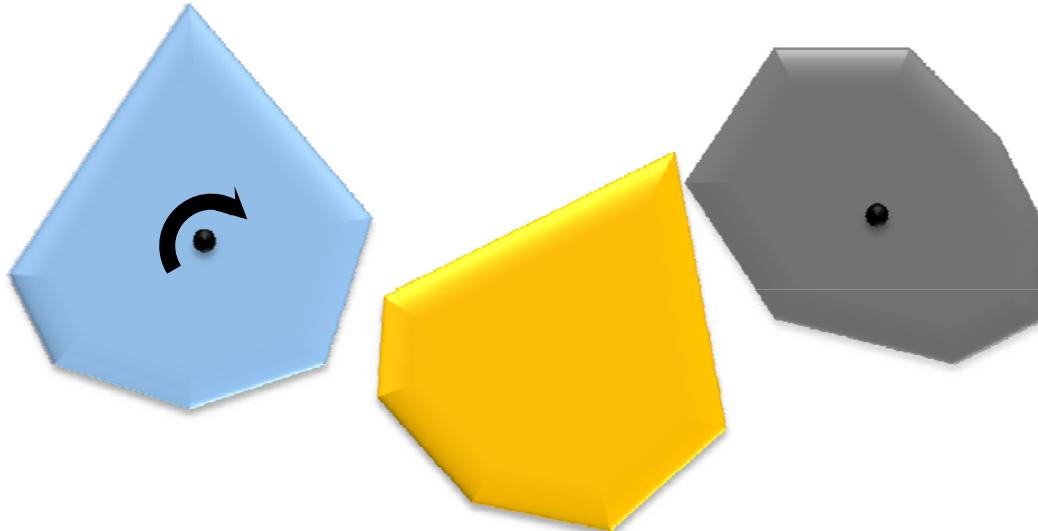


Valid portion
of the trajectory



Conservative Advancement (CA)

- Assume objects are *convex*
- Find the 1st time of contact (ToC) of a moving object

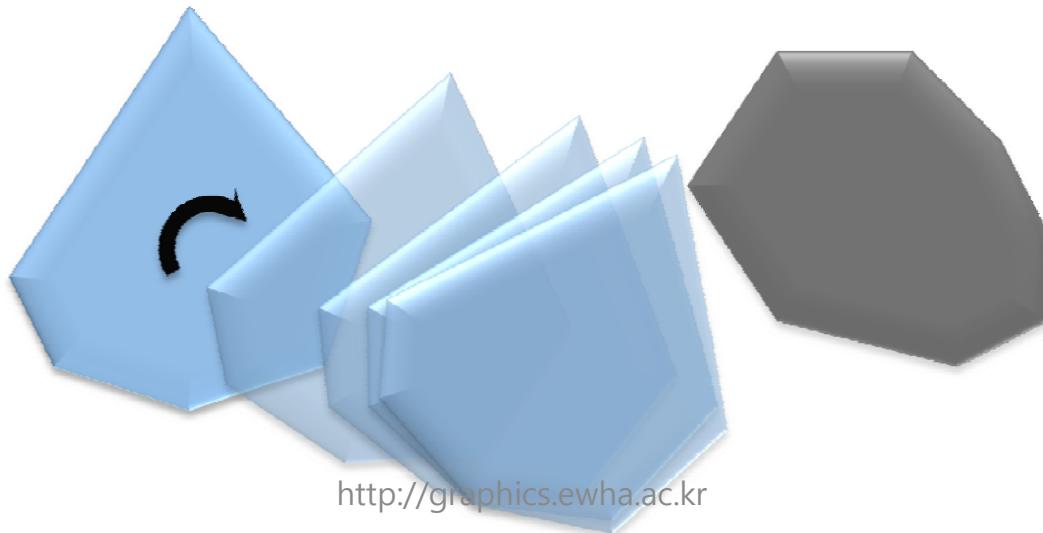




Conservative Advancement (CA)

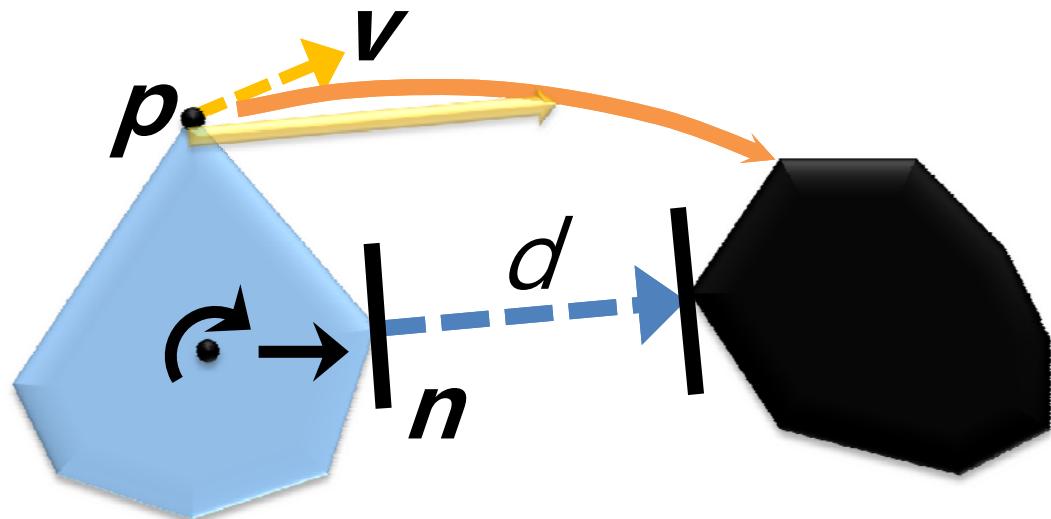
1. Find a step size Δt_i to conservatively advance the object without collision
2. Repeat until inter-distance $< \varepsilon$

$$ToC = \Delta t_1 + \Delta t_2 + \Delta t_3 + \Delta t_4$$





Calculating Δt in CA



d , n : closest distance,
direction vector
 v : velocity

$$= \mu$$
$$\int_0^{\Delta t} \left| \Psi \left(\int_0^{\Delta t} \max(|\psi(dt) \cdot n(dt)|) dt \right) \right| dt$$



Calculating Δt in CA

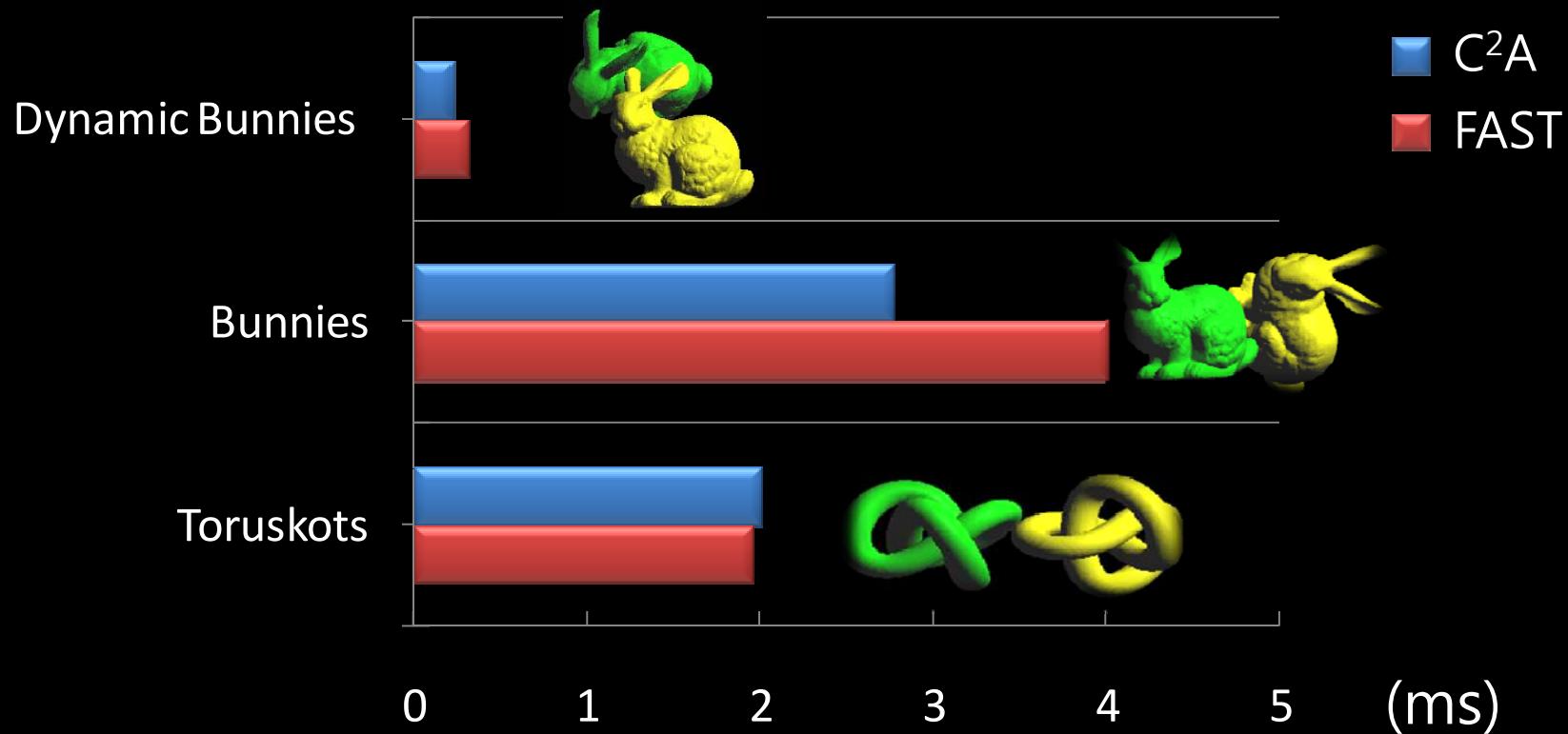
$$\mu \Delta t \leq d \quad \therefore \Delta t \leq \frac{d}{\mu}$$
$$\int_0^{\Delta t} |v(t) \bullet n(t)| dt \leq \int_0^{\Delta t} \boxed{\max(|v(t) \bullet n(t)|)} dt \leq d$$



FAST: 2-Manifold Models



C²A: Polygon Soup Models



- FAST can handle only manifold surfaces



Articulated Models (Demo)

- CCD performance
 - 1.22 msec
- Mannequin
 - 15 links, 20K tri
- Obstacles
 - 101K tri
- Locomotion SW
 - Footstep™





Articulated Models

- Mannequin
 - 15 links, 20K triangles
- **Self-CCD performance**
 - 0.38 msec





Articulated Body Dynamics Benchmark

- Four trains
 - 10 links, 23K tri (each)
- **CCD performance**
 - 535 msec





Software Implementations

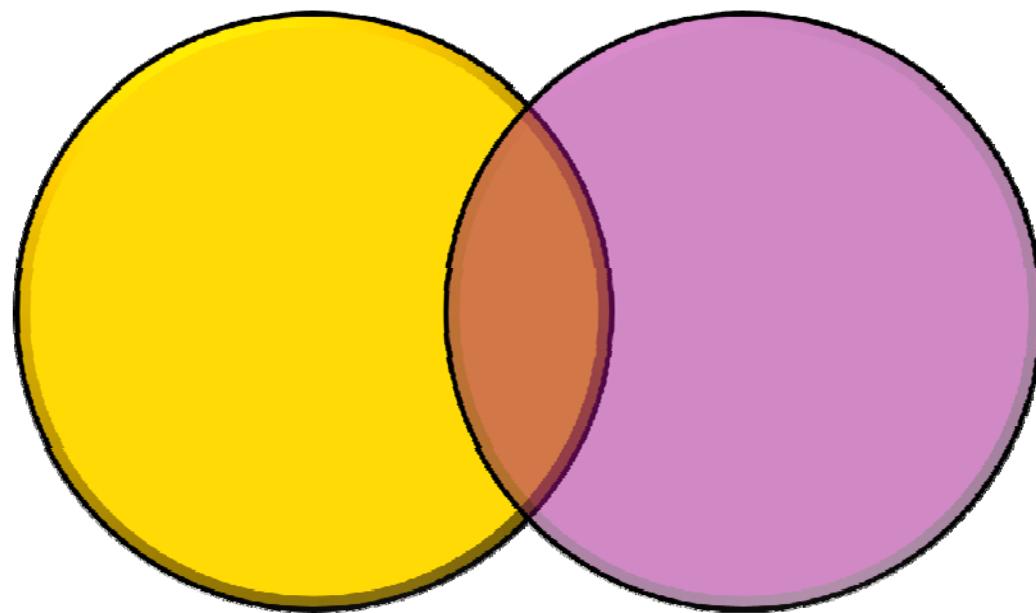
- Source codes:
 - <http://graphics.ewha.ac.kr/FAST> (2-manifold)
 - <http://graphics.ewha.ac.kr/C2A> (polygon soups)
 - <http://graphics.ewha.ac.kr/CATCH> (articulated models)



REAL-TIME PENETRATION DEPTH COMPUTATION



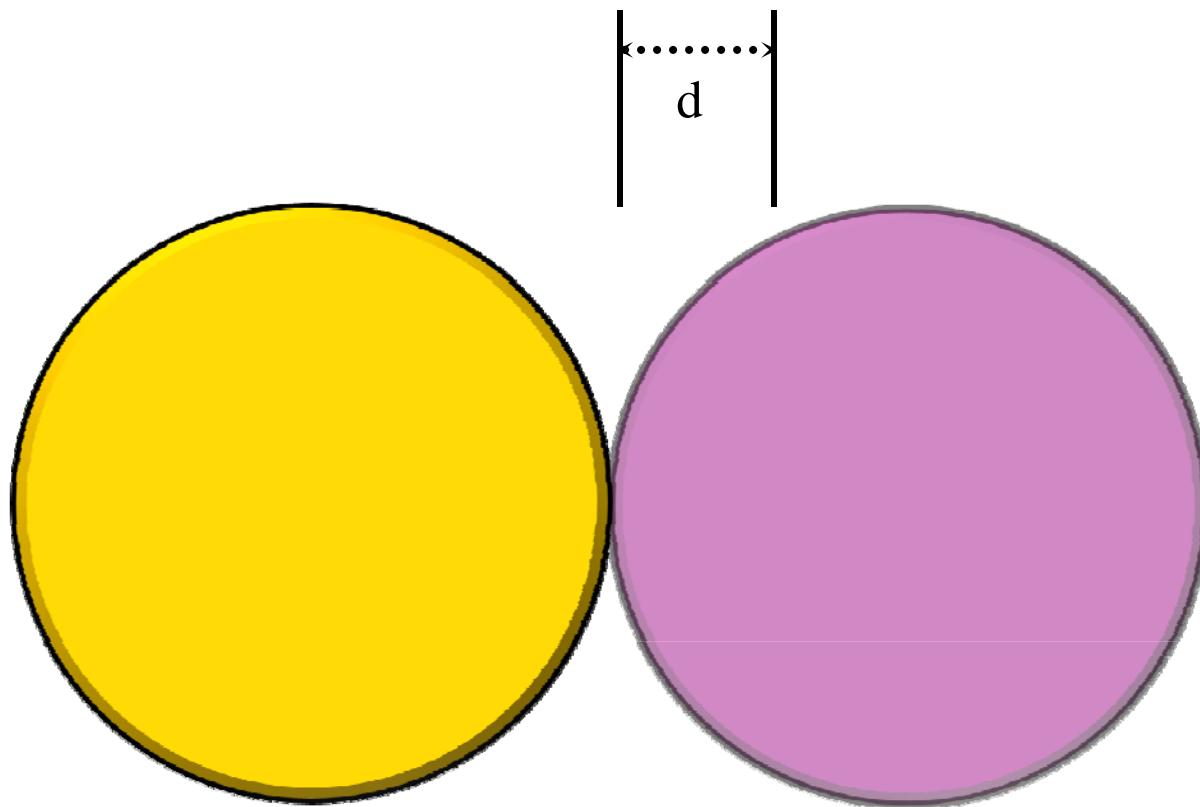
Penetration Depth



Minimum translational distance needed to separate objects



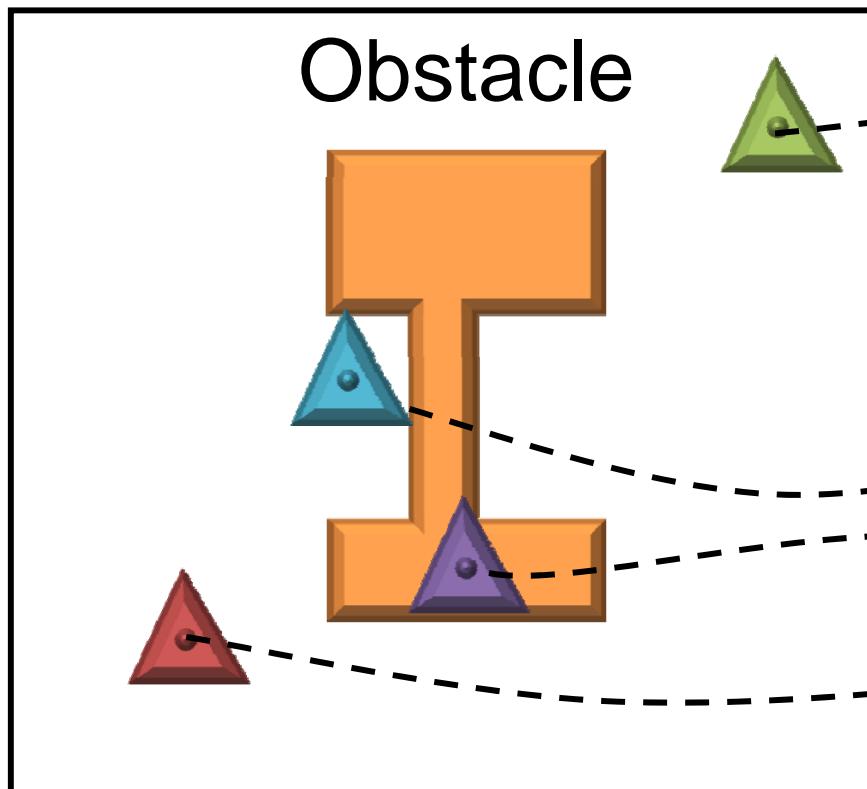
Penetration Depth



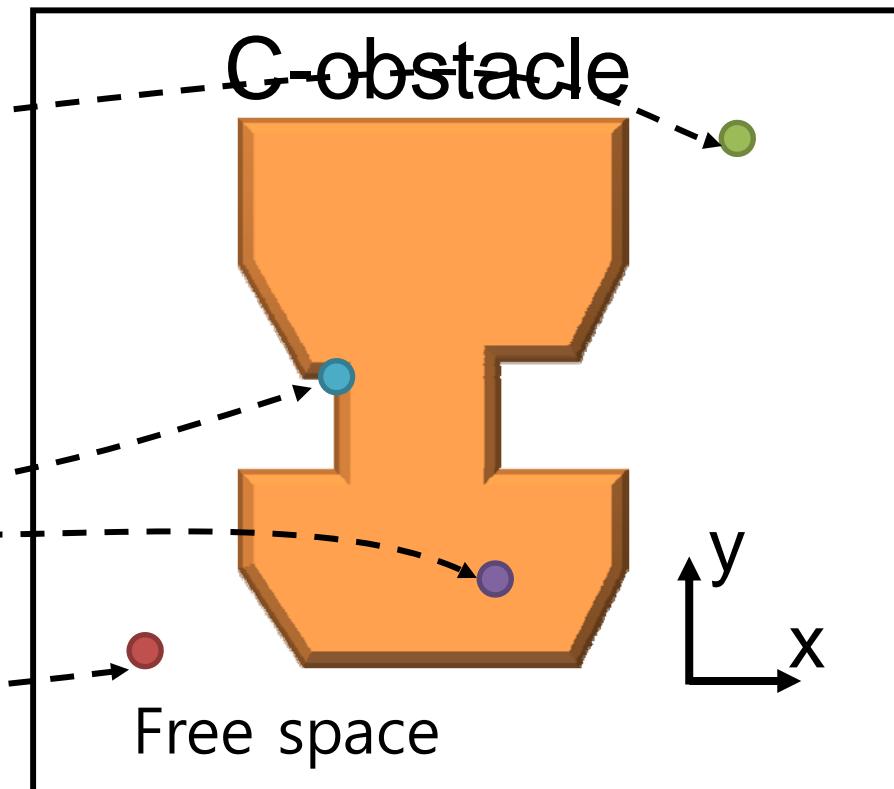
Minimum translational distance needed to separate objects



Configuration Space



Work Space

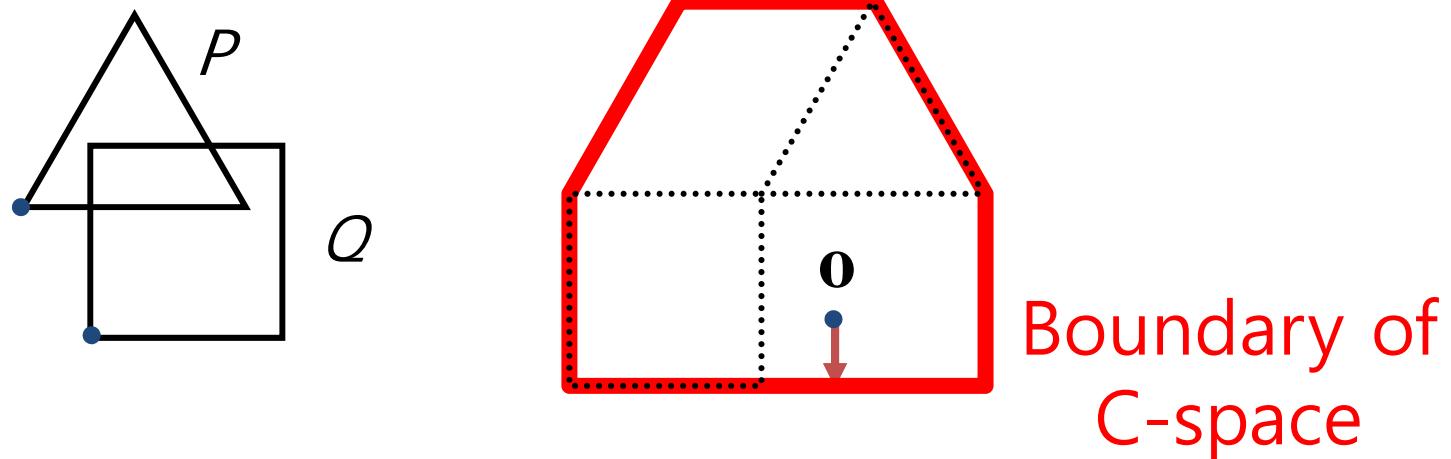


Configuration Space



C-Space and PD

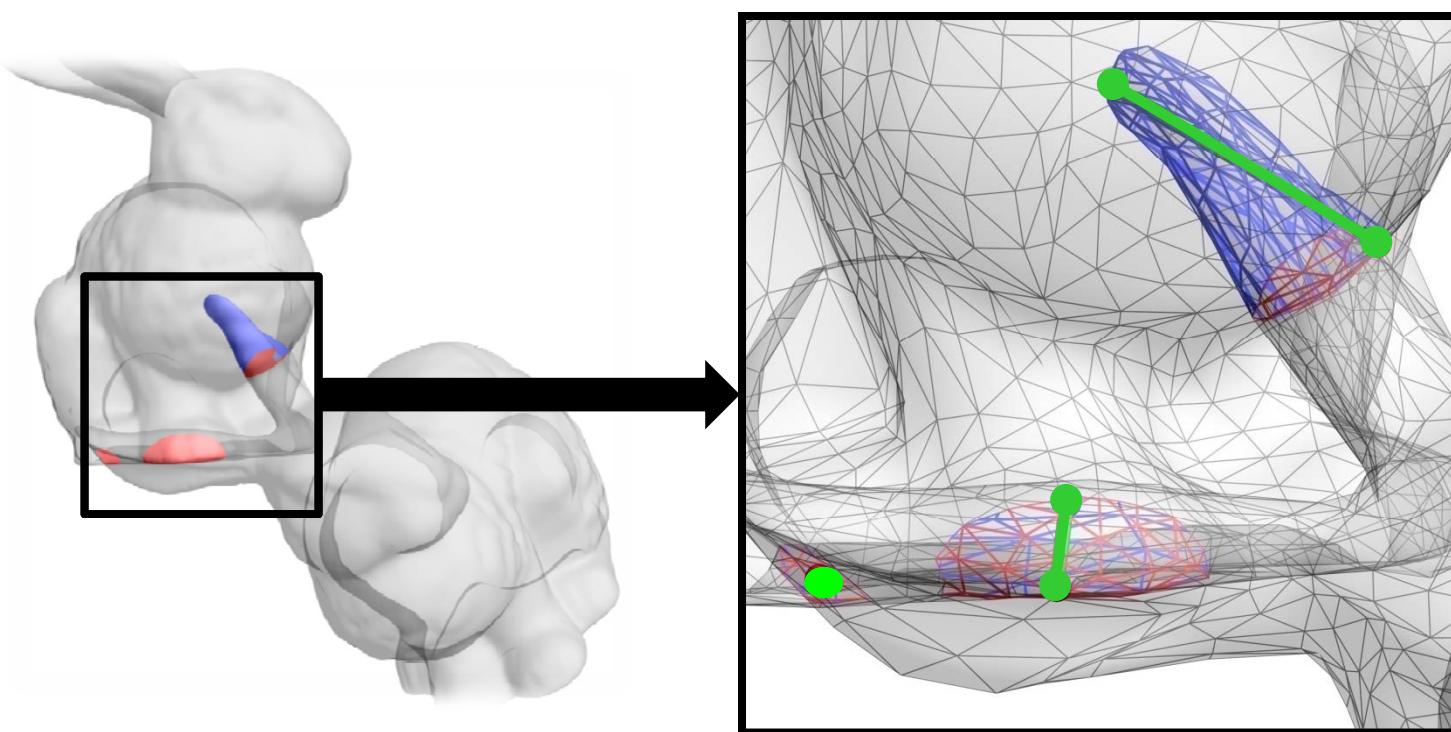
- $PD^t = \min$ distance btwn the origin and the boundary of C-space





Pointwise Penetration Depth

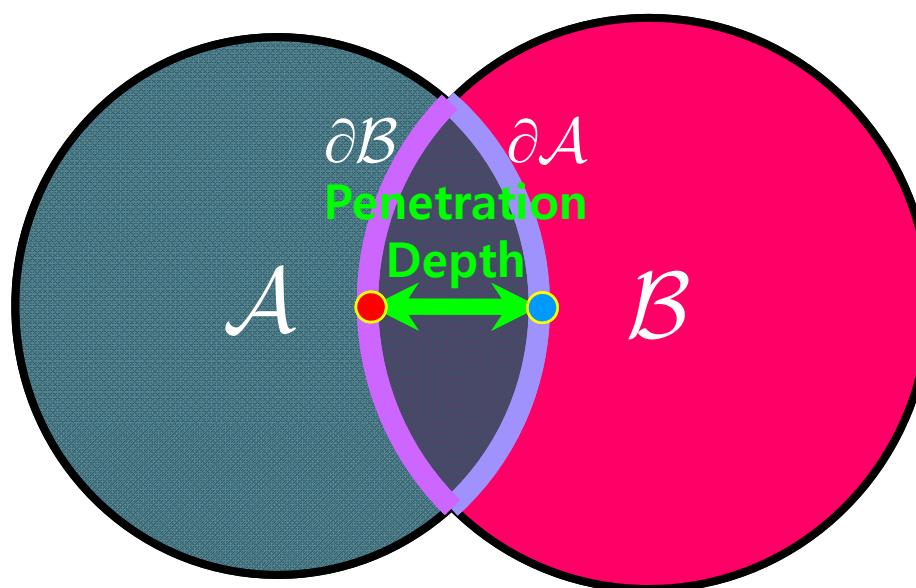
- Defined as deepest interpenetrating points





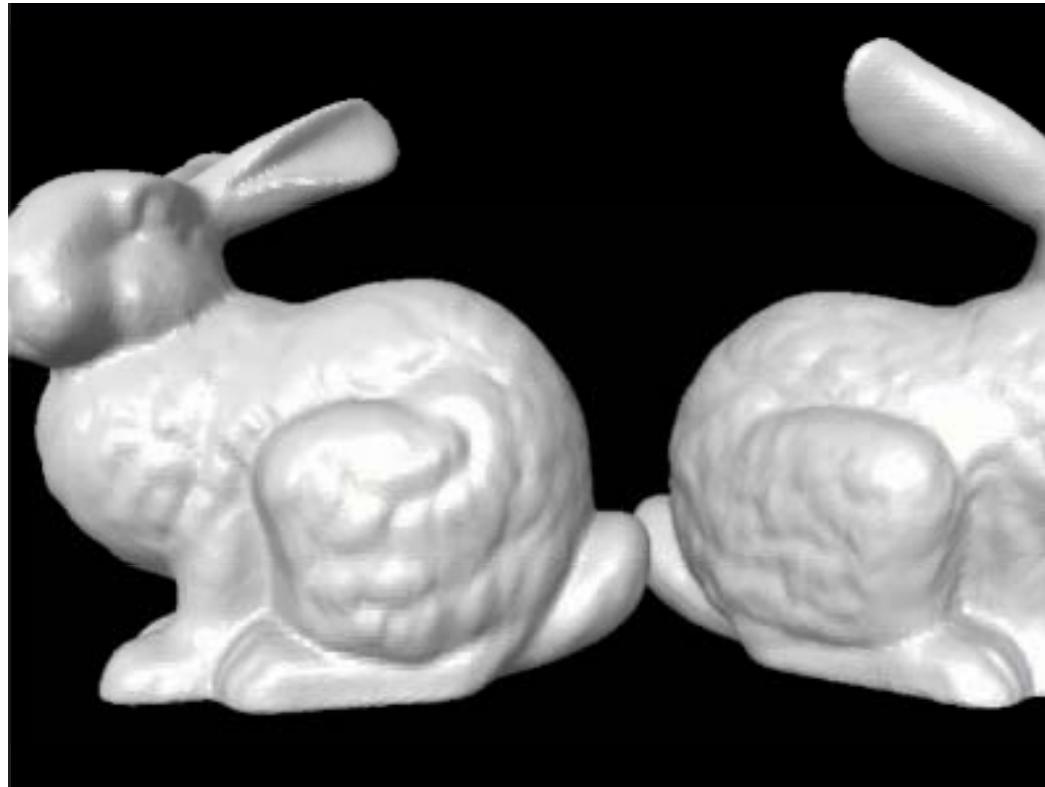
Penetration Depth

1. Find intersection surfaces $\partial\mathcal{A}$ and $\partial\mathcal{B}$
2. Penetration depth = $H(\partial\mathcal{A}, \partial\mathcal{B})$





Penetration Depth

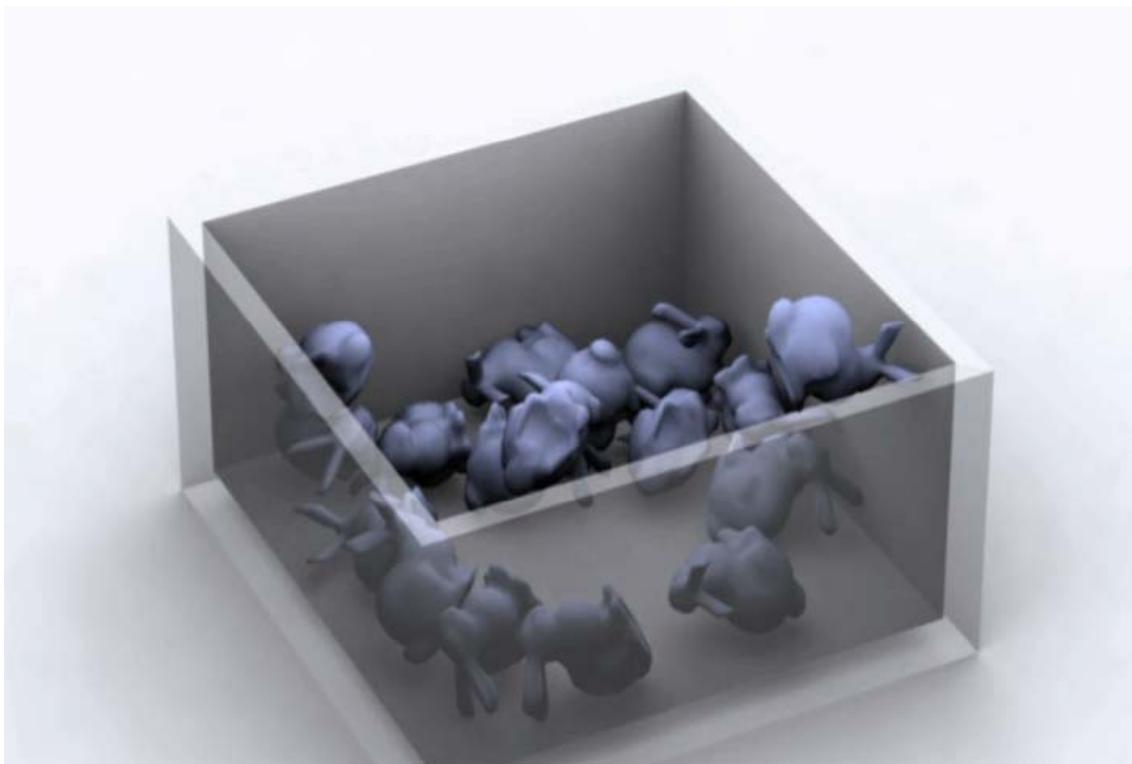


Demo (40K Bunny vs 40K Bunny)



Benchmark 1

- Run rigid body dynamics and measure the average timing of penetration depth computation



Model complexity

— 50K tri

Avg. Performance

— 3.88ms/pair



Benchmark 2

- Run rigid body dynamics and measure the average timing of penetration depth computation



Model complexity

— 3.5K tri

Avg. performance

— 0.95ms/pair

**MORE ON 1/28, 13:00
휘닉스볼룸 2 GRAPH 세션**

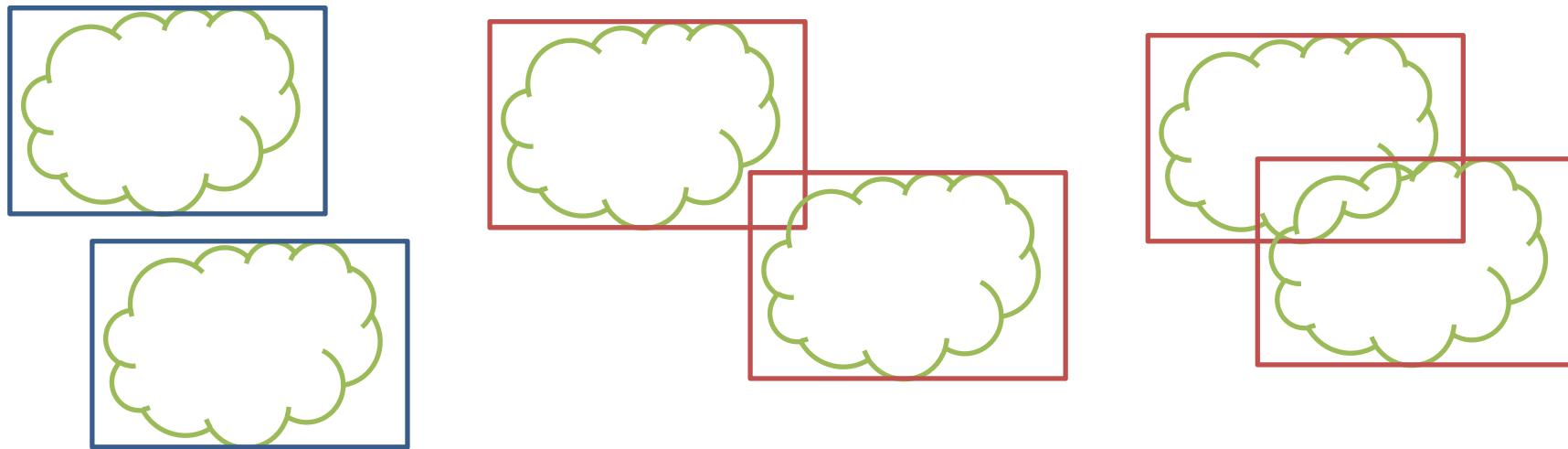


PARALLEL COLLISION DETECTION



Bounding Volume

- Simplify surface representation for fast proximity queries

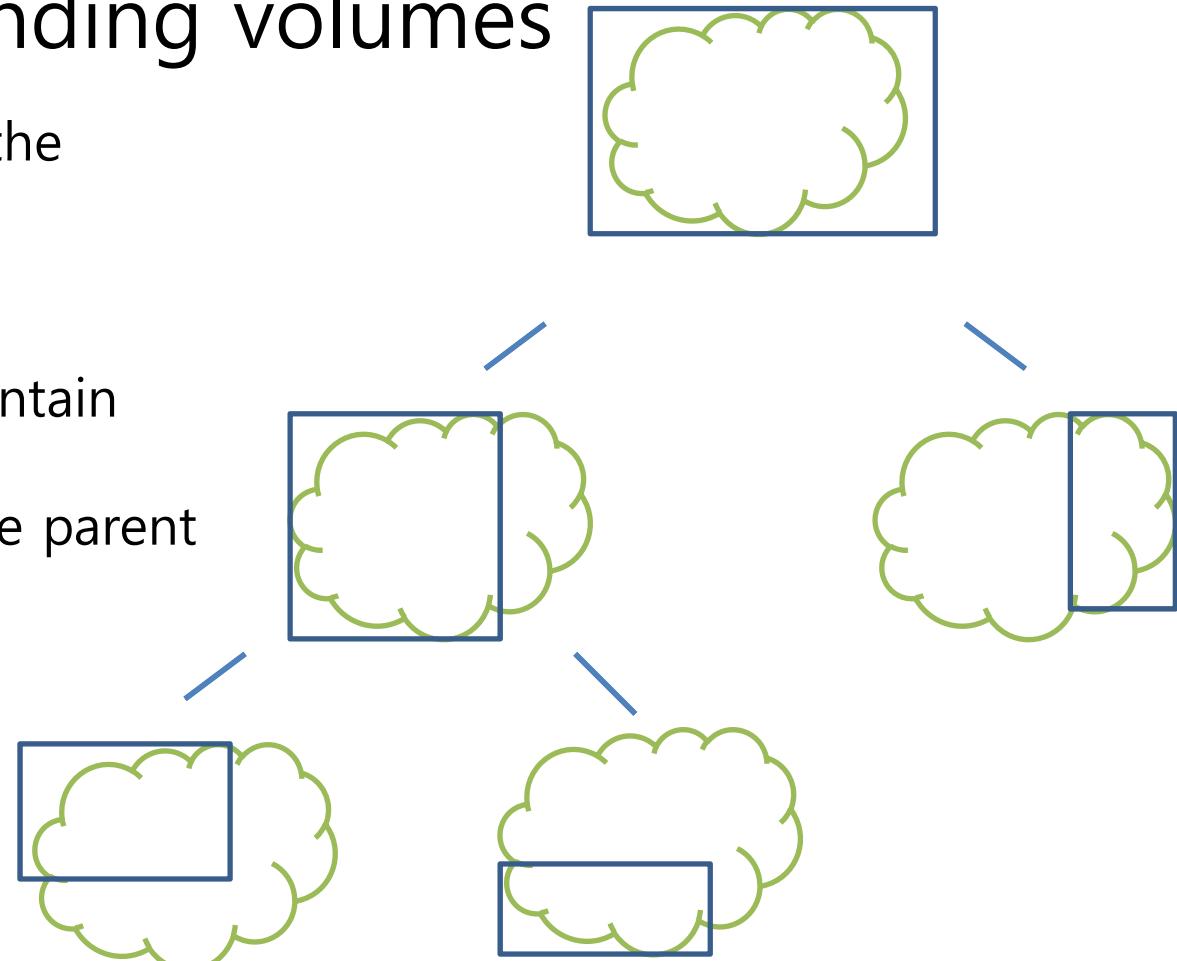




Bounding Volume Hierarchy

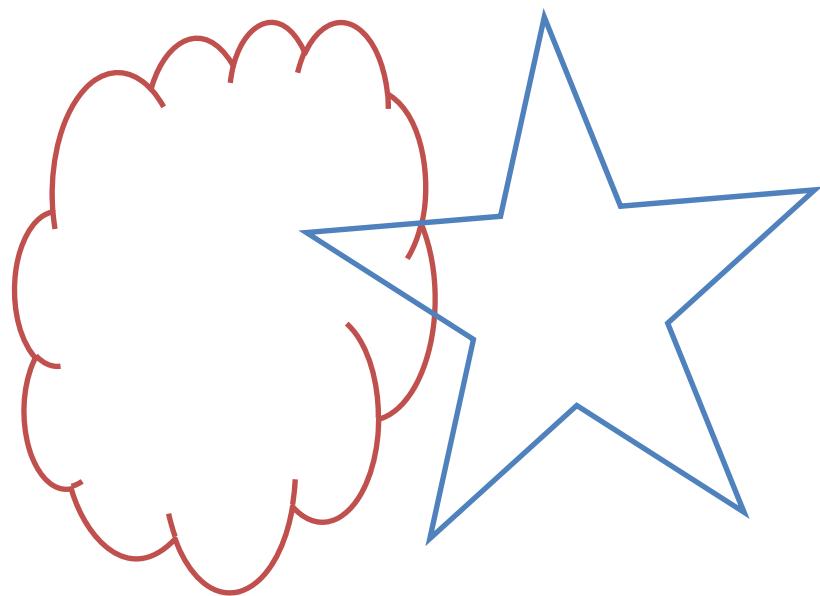
- A tree of bounding volumes

- **Root node** contains all the primitives of a model
- **Leaf nodes** contain one primitive
- **Children nodes** each contain separate partitions of the primitives enclosed by the parent



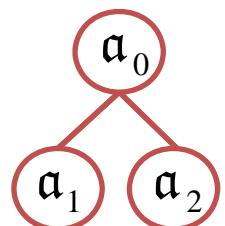
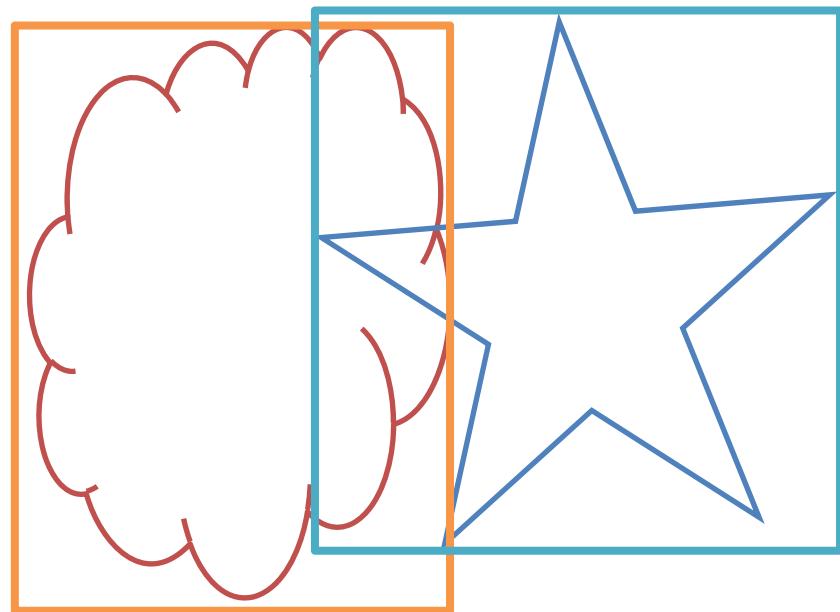


BVH Collision Test

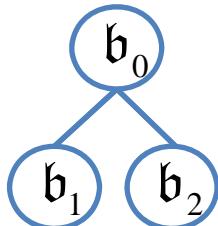




BVH Collision Test



$\text{BVH}_{\mathfrak{A}}$

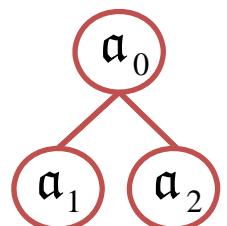
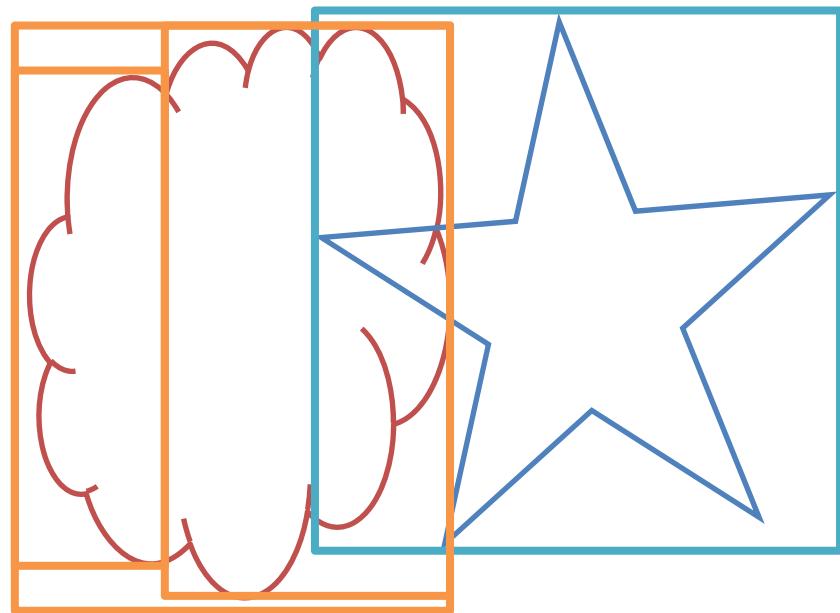


$\text{BVH}_{\mathfrak{B}}$

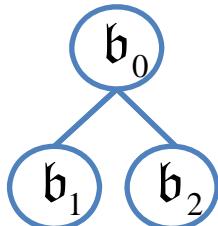




BVH Collision Test



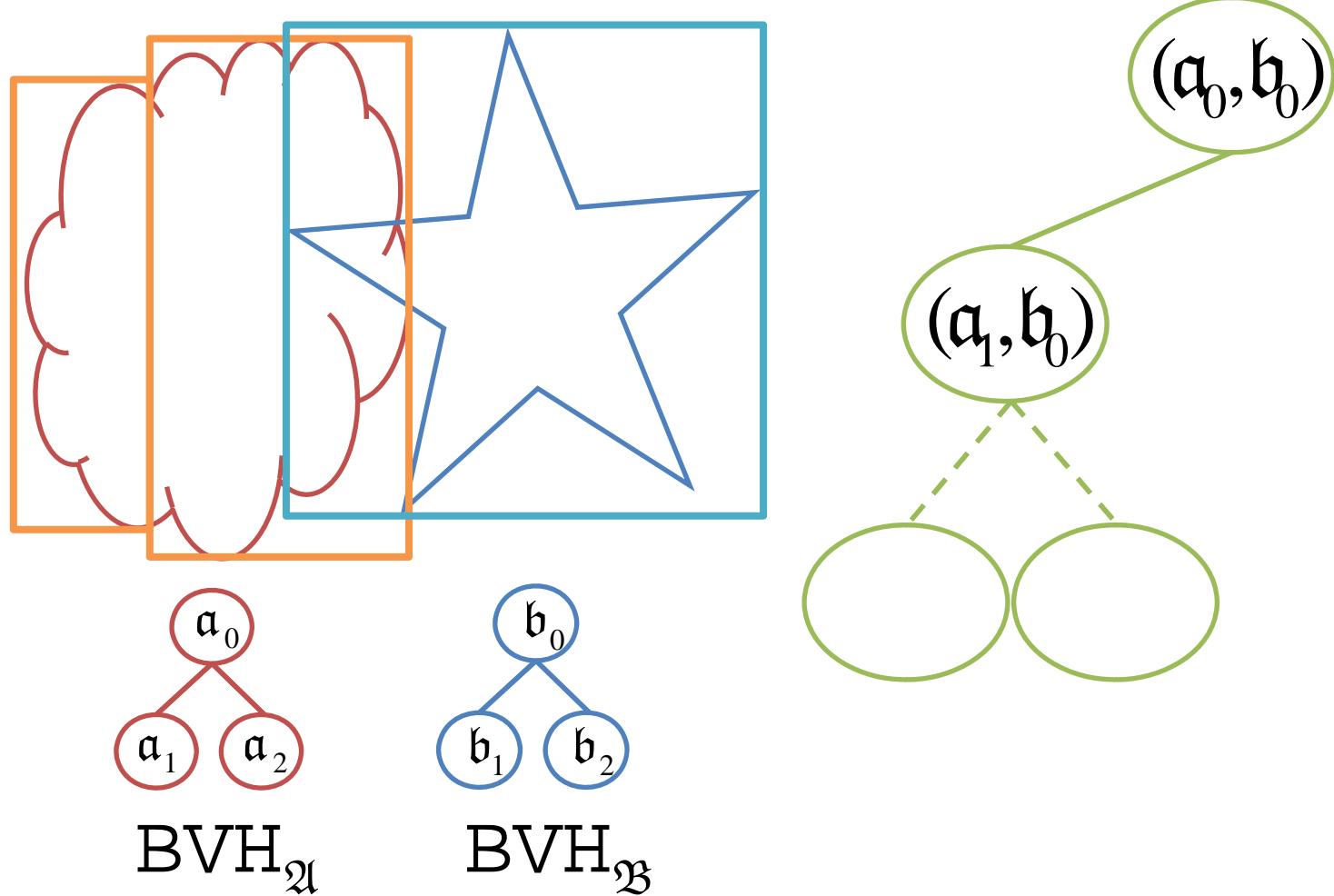
$\text{BVH}_{\mathfrak{A}}$



$\text{BVH}_{\mathfrak{B}}$

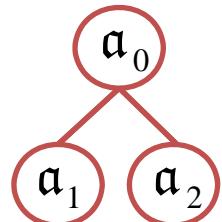
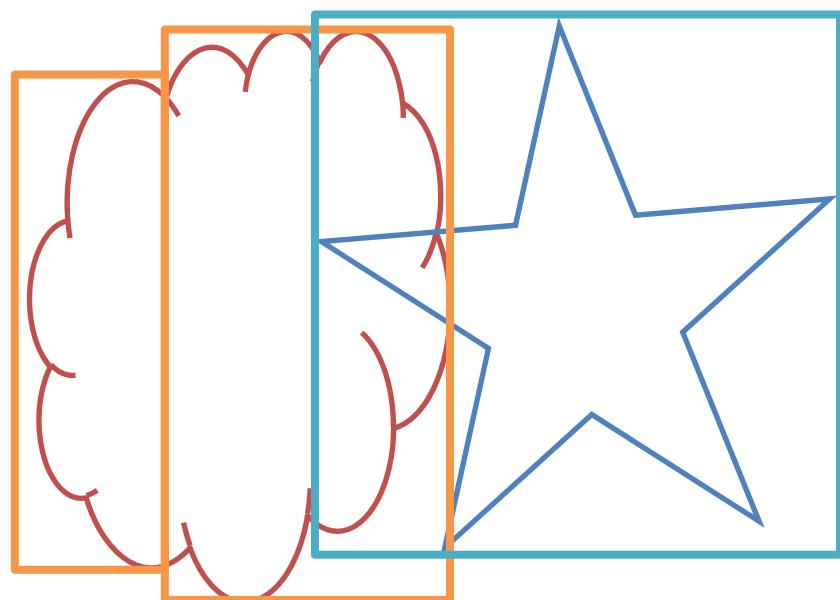


BVH Collision Test

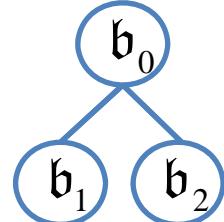




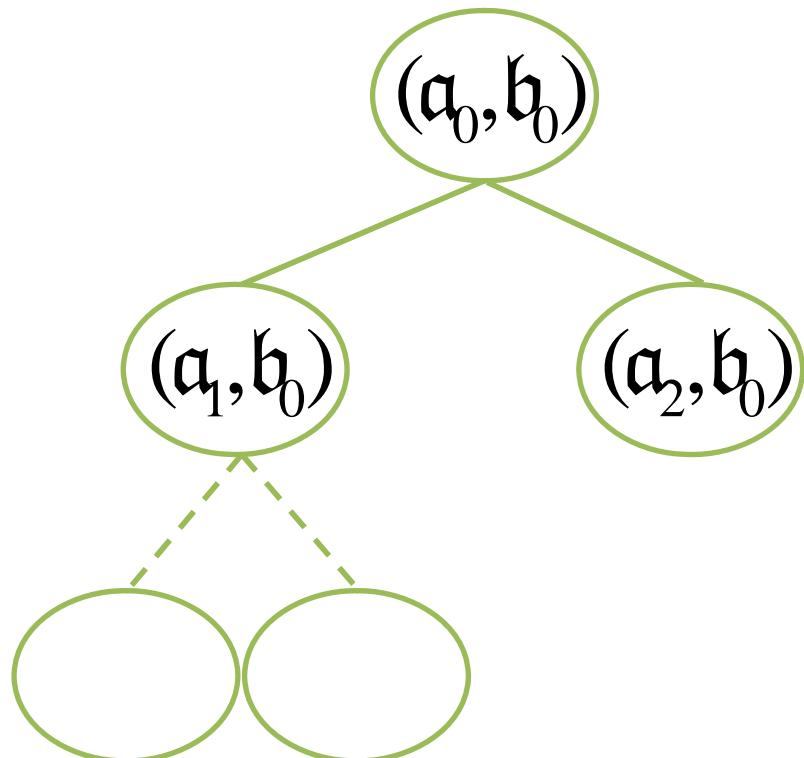
BVH Collision Test



$\text{BVH}_{\mathfrak{A}}$

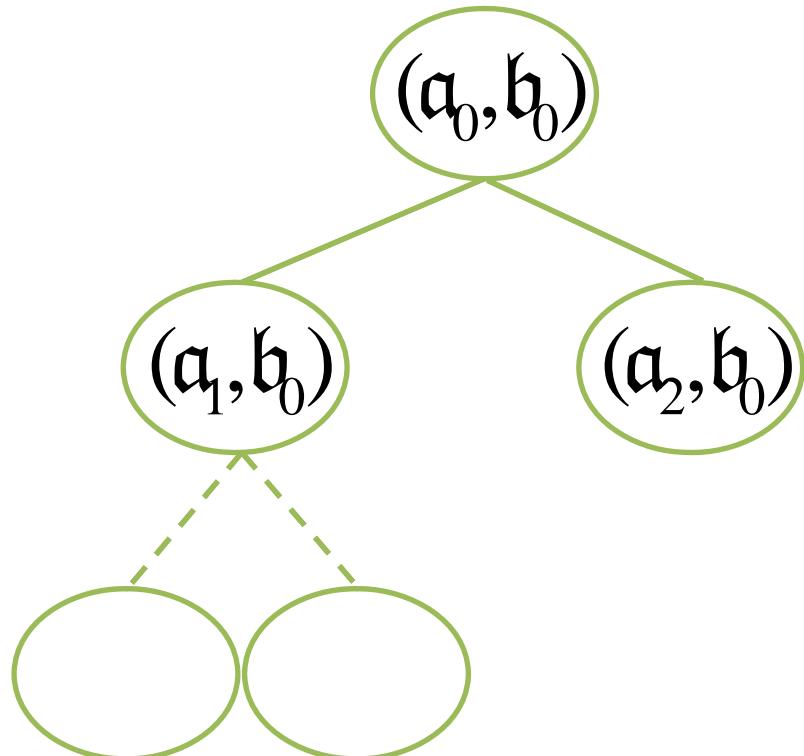
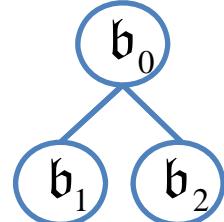
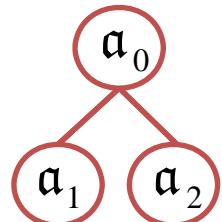
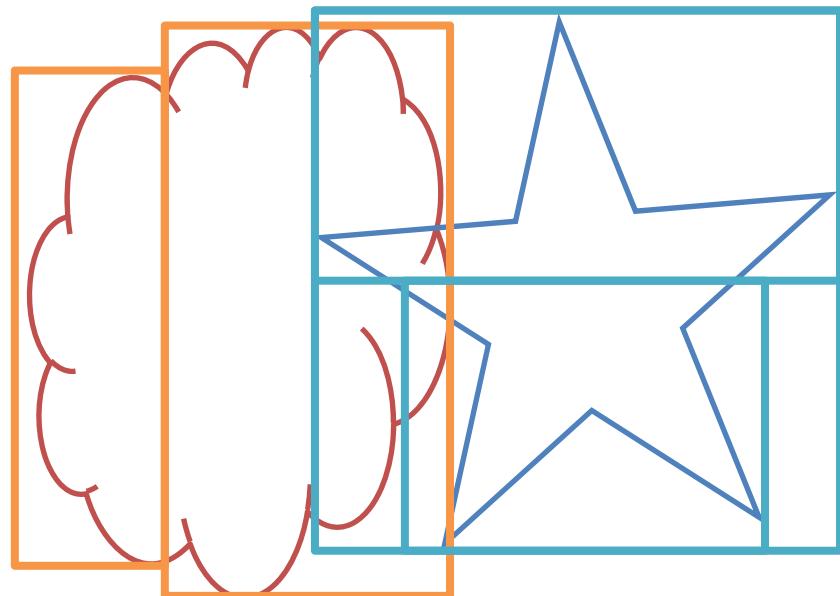


$\text{BVH}_{\mathfrak{B}}$



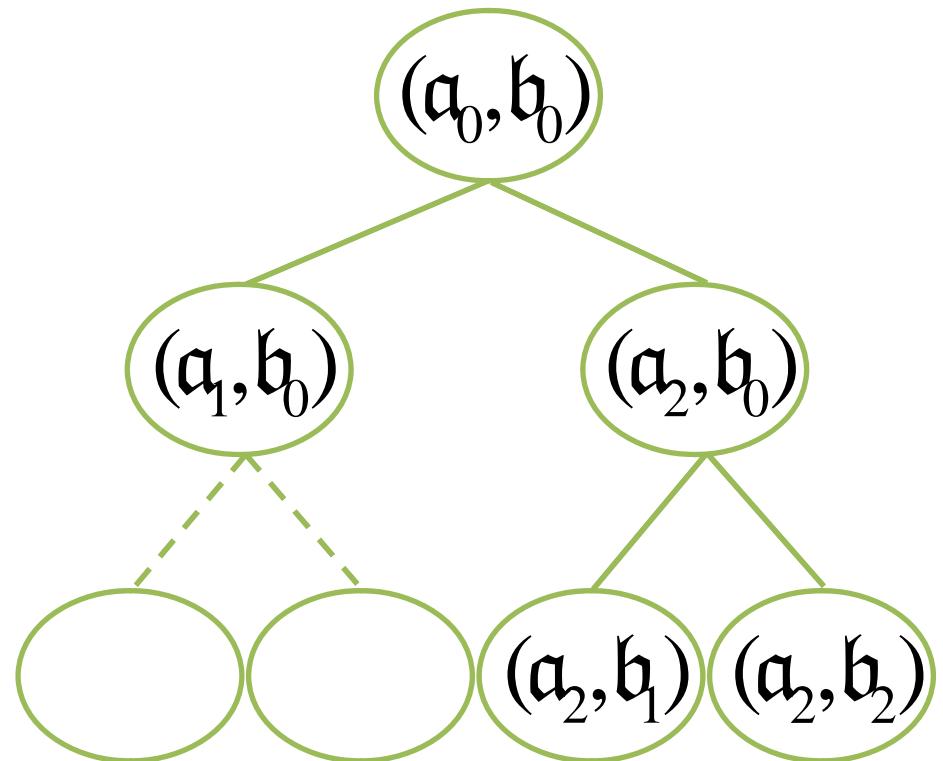
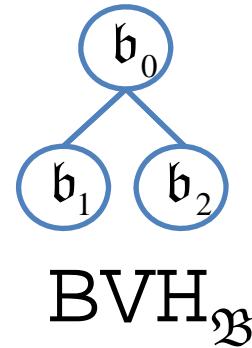
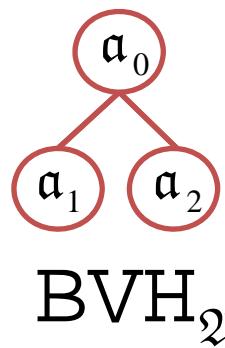
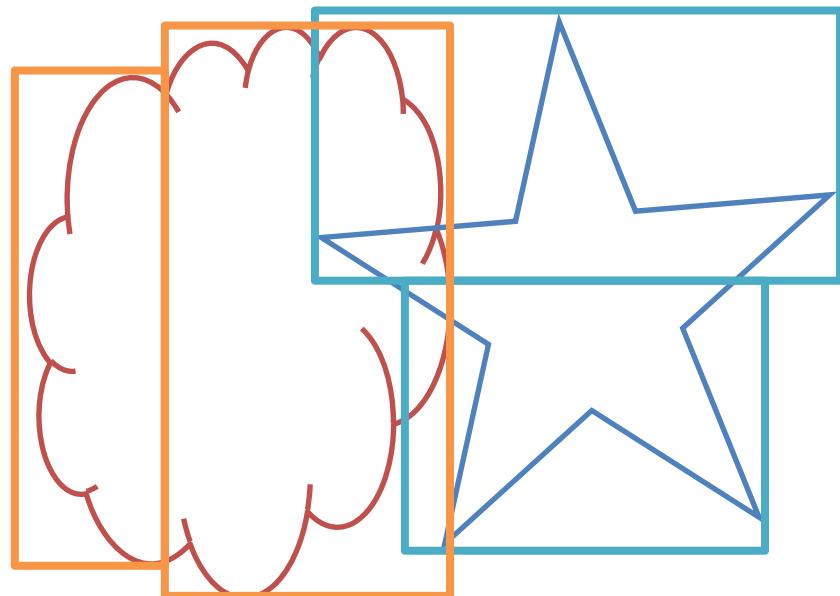


BVH Collision Test



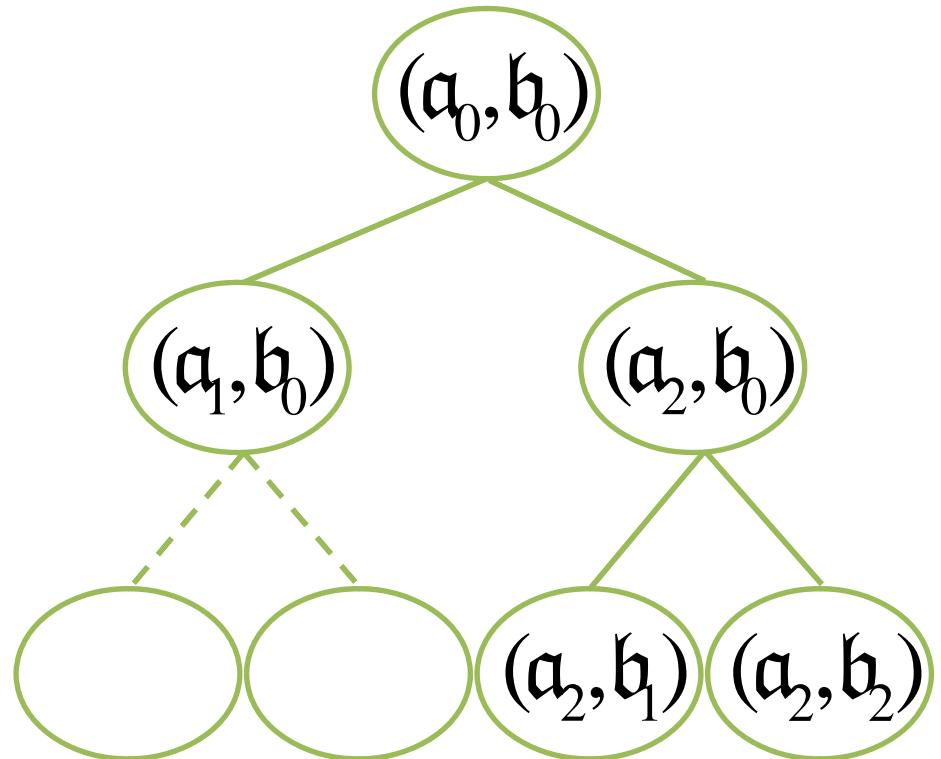
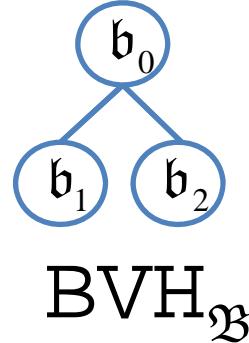
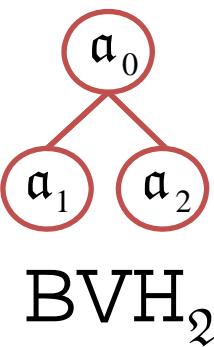
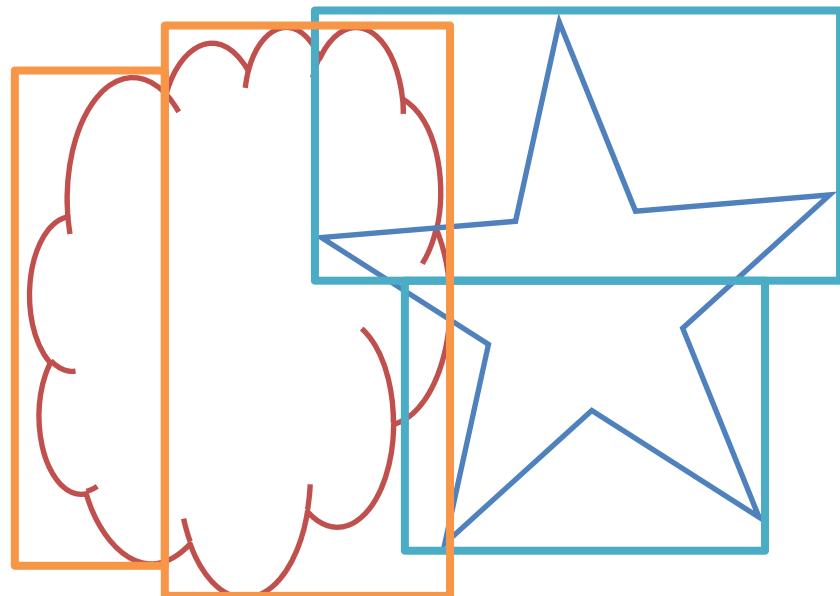


Bounding Volume Traversal Tree





Bounding Volume Traversal Tree

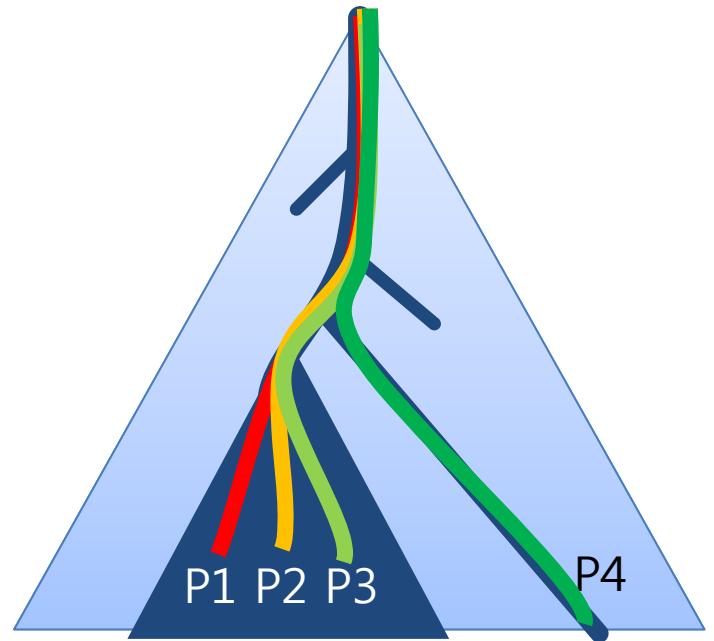


BVTT



Idea

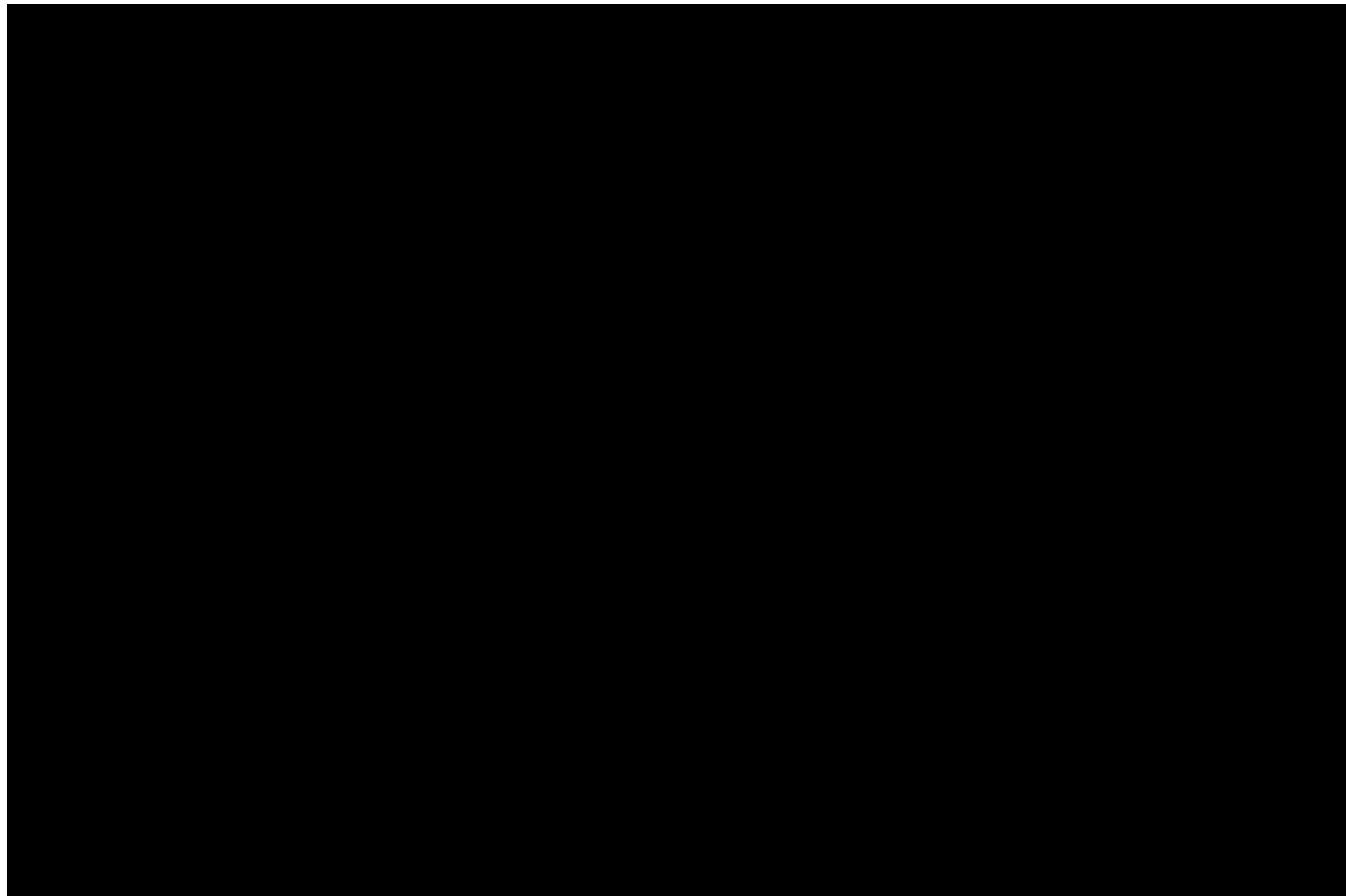
- Traverse the BVTT in parallel
 - Concurrency
 - Dependency
 - Efficient load balancing



BVTT

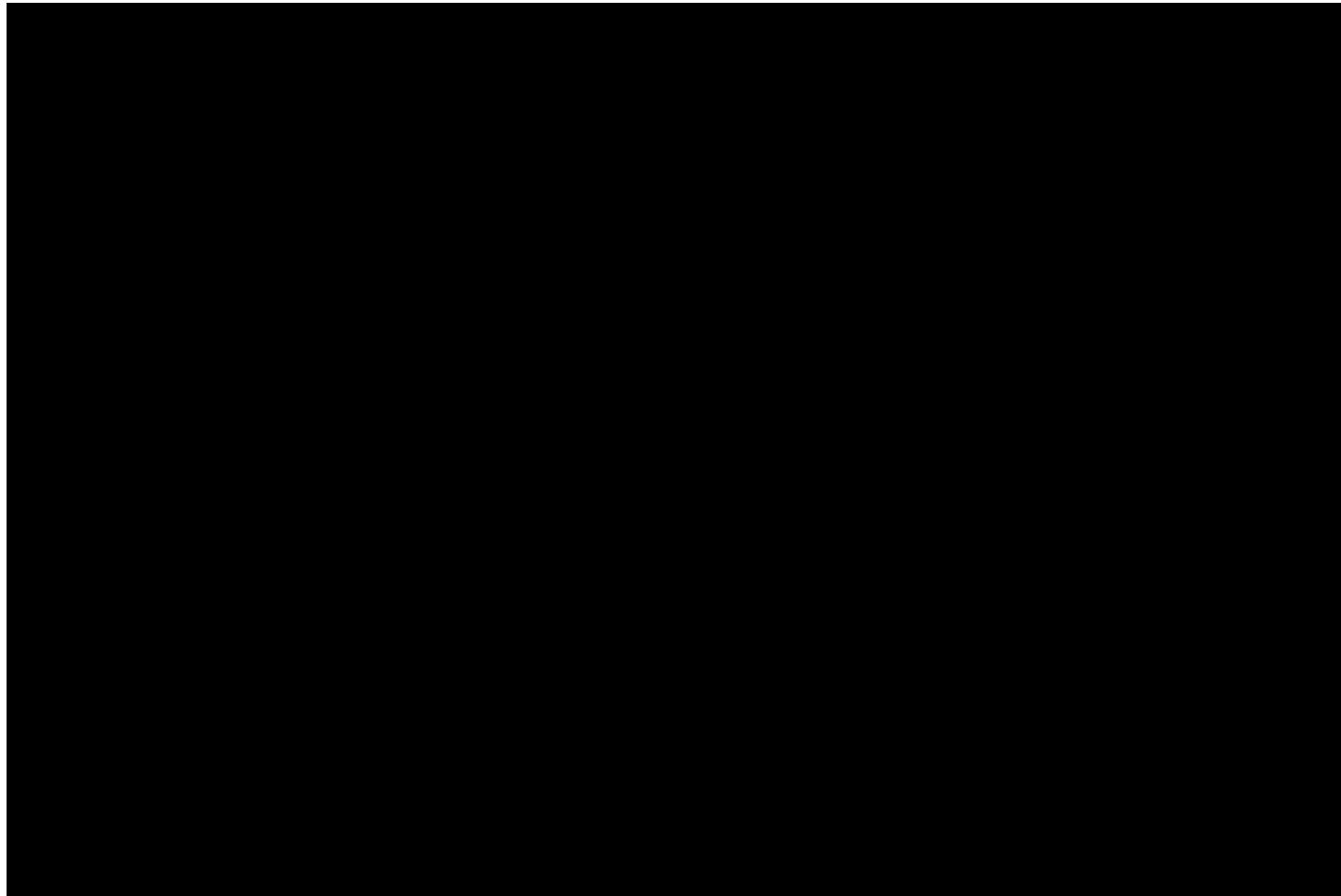


Parallel Collision Detection Demo



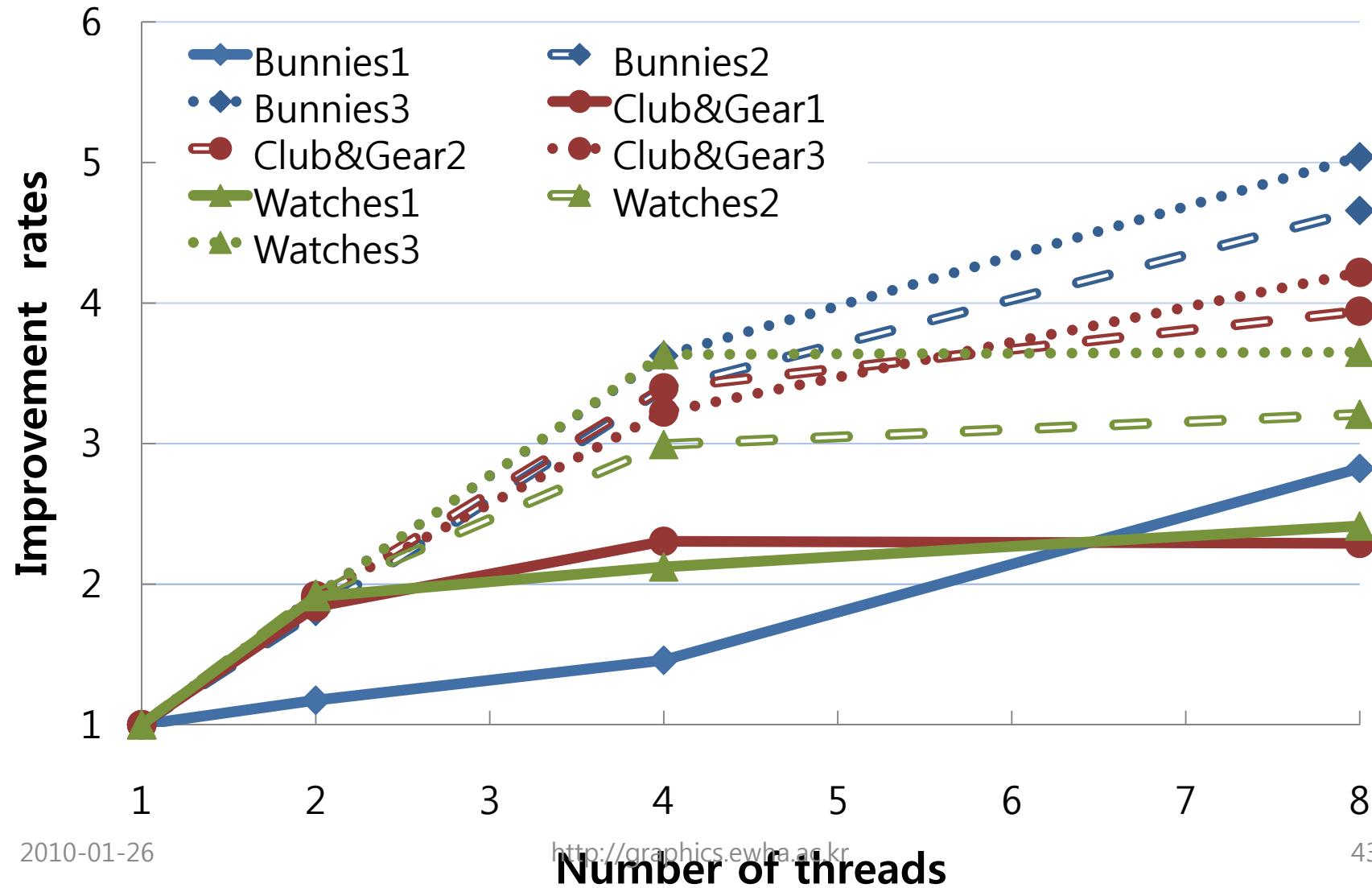


Parallel Distance Calculation Demo



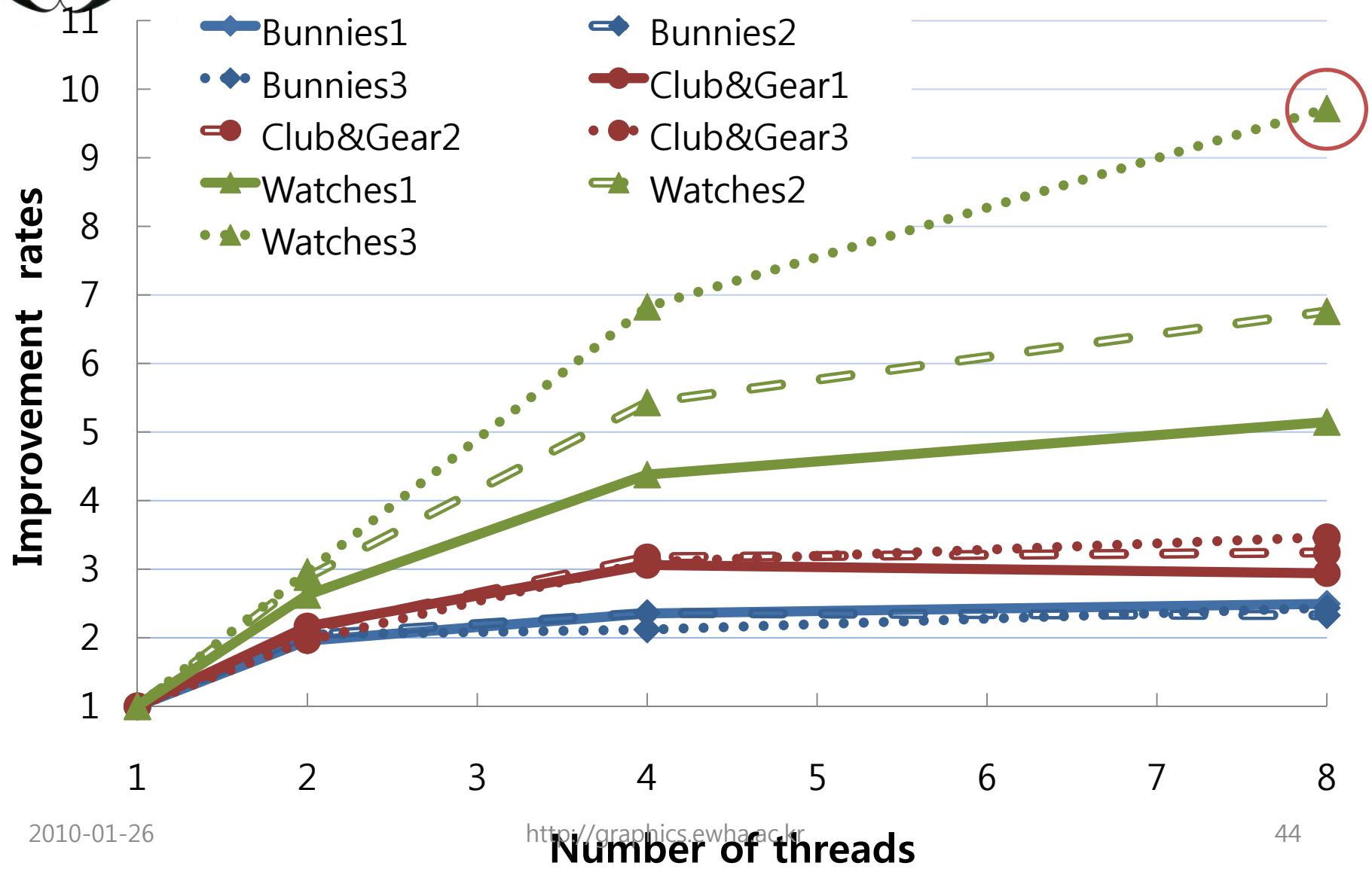


Collision Detection Results

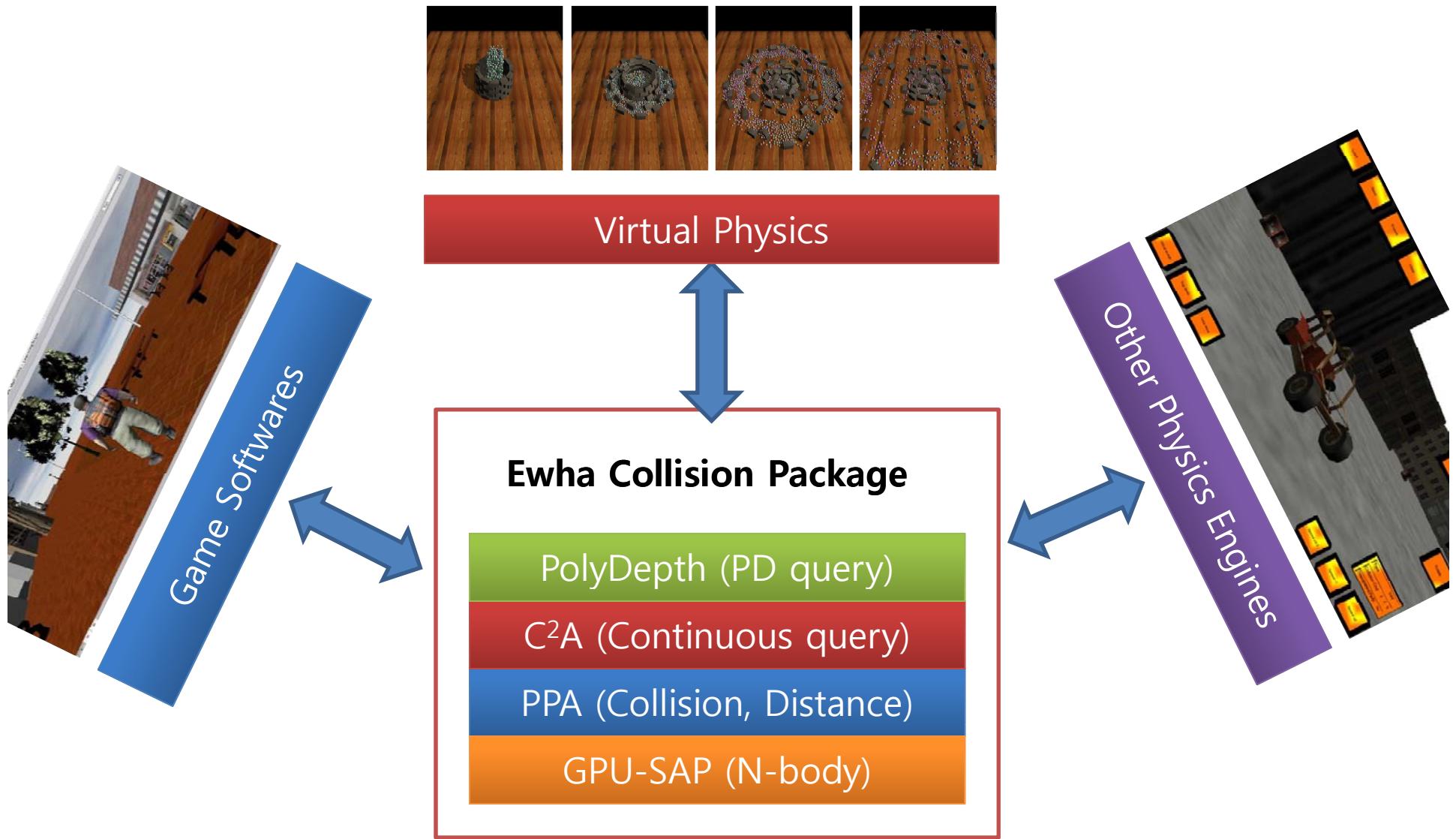




Distance Calculation Results



Summary





Future Work

- Collision detection for fracturing
- N-body penetration depth
- Real-time generalized penetration depth



Thank you!

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김 진 욱

Physically Based Simulation

- Newton's physics law

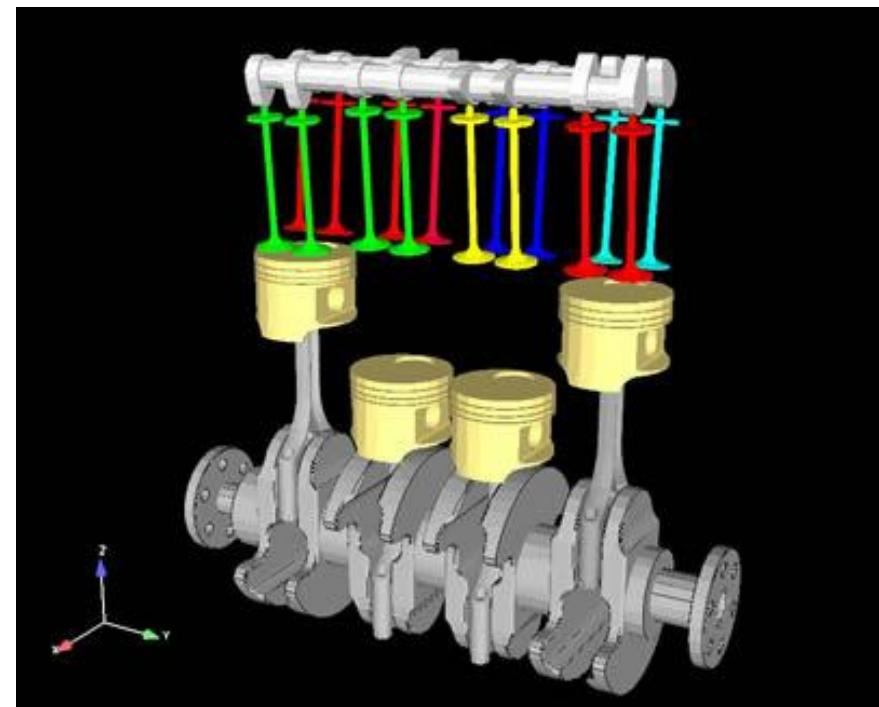
$$f = m\ddot{x}$$

- If you push something, it will move
- Different governing equations
 - Particle
 - Rigid body
 - Articulated body
 - Deformable body
 - Fluid system

Application Domains

Engineering

- Everywhere modeling and simulation are required
 - Adaptive control
 - Structure simulation
 - Mechanism design



Engine block simulation
(ADAMS, MSC)

Application Domains

Entertainment

- To enhance visual realism
 - Virtual reality
 - Digital contents
 - Video games

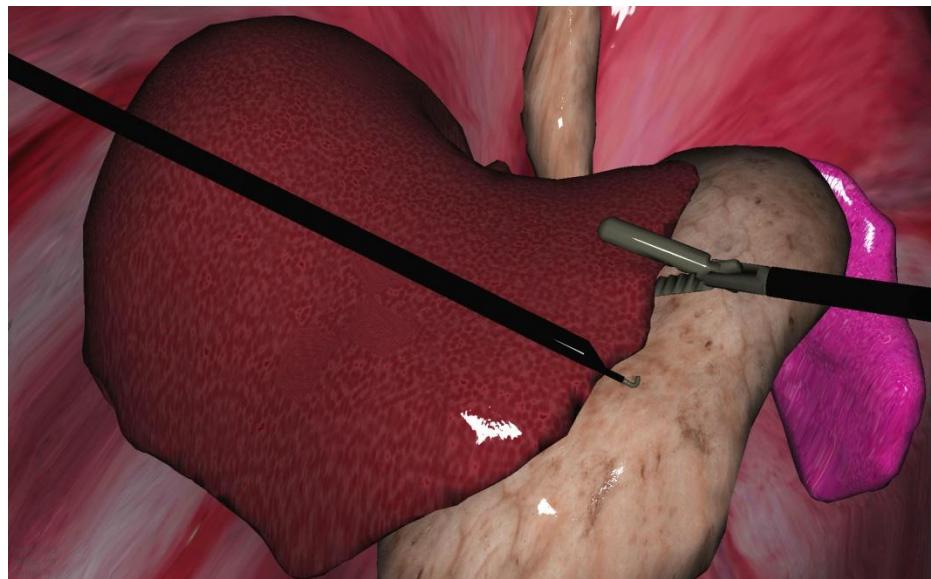


Monster Inc.(PIXAR)

Application Domains

Medical Simulation

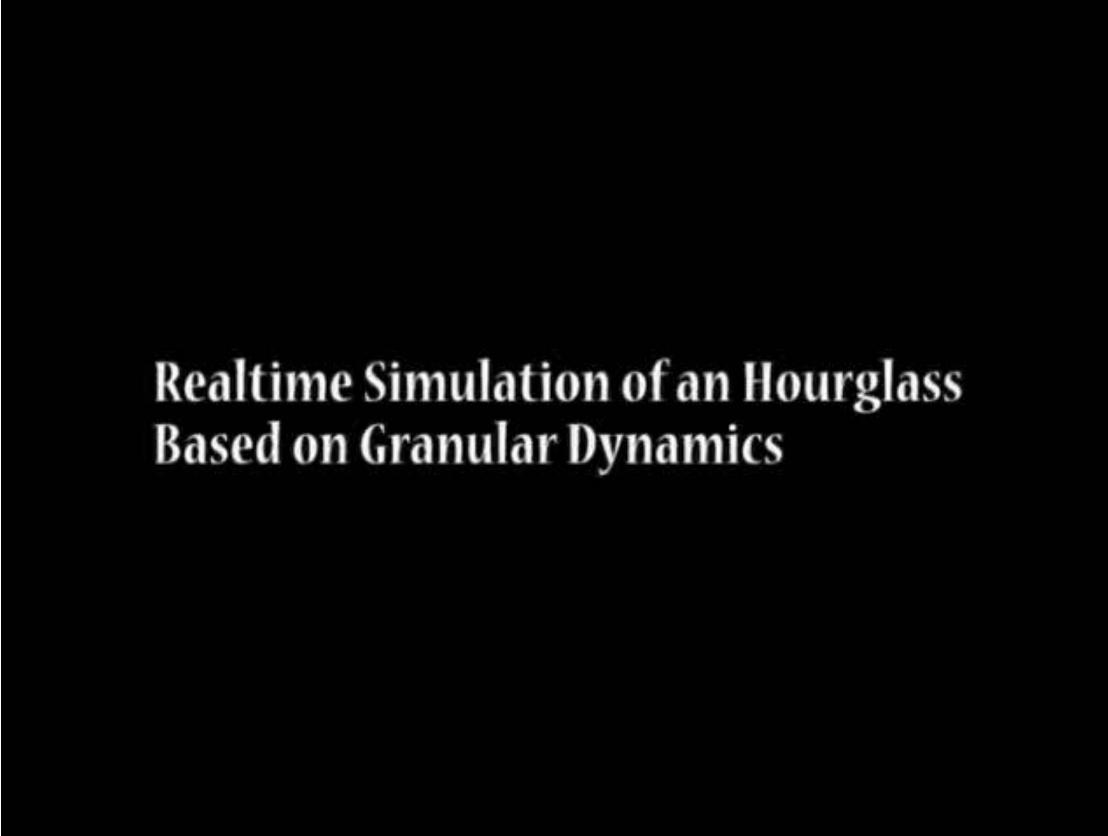
- To predict experimental medical treatment
 - Virtual surgery
 - Tissue simulation
 - Developing medical instruments



VR based endoscopic surgery(M. Srinivasan, MIT)

Particle System

- Simplified body without volume

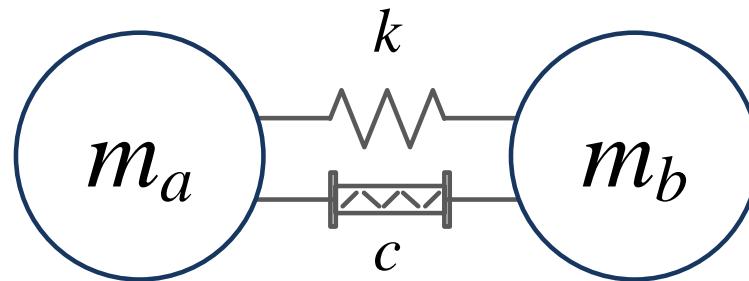


Realtime Simulation of an Hourglass
Based on Granular Dynamics

Granular Dynamics(R. Yasuda, U.Tokyo)

Particle System

Mass-Spring-Damper System



$$m\ddot{x} = f$$

$$f = -kx - cx$$

- Easy to implement
- Hard to define proper k and c
- Tends to be unstable

Particle System

Forward Dynamics

- Evaluate force applied to the particle
 - gravity, spring, damper, collision, ...
- Calculate acceleration

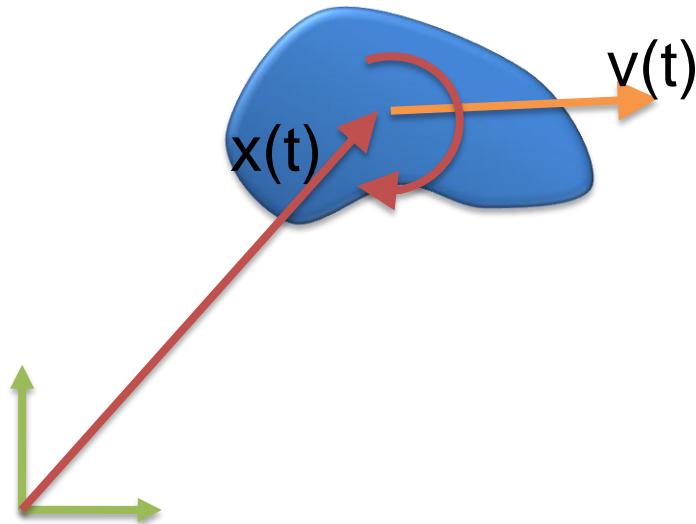
$$a = f / m$$

- Step forward in time
 - Integrate dynamics

$$\ddot{x} = a$$

Rigid Body System

- Body with a volume
- Dynamics state
 - Position/orientation
 - Linear/angular velocity



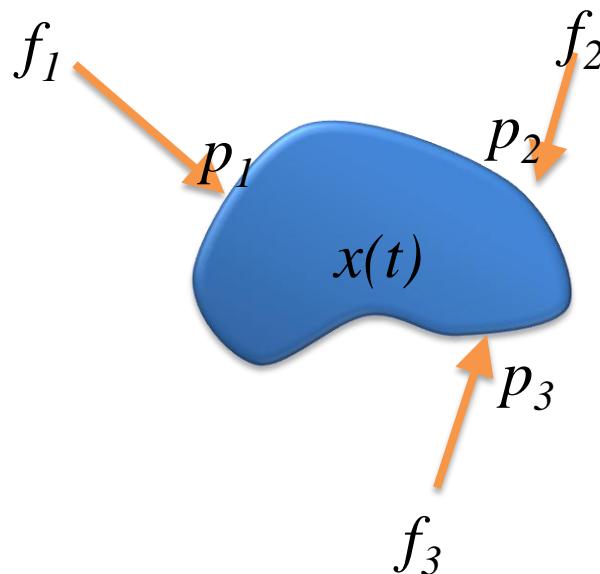
Rigid Body System

Rigid Body Dynamics

- Newton-Euler equation

$$f = m\dot{v}$$

$$\tau = I\dot{w} + w \times (Iw)$$



$$f = \sum f_i$$

$$\tau = \sum (p_i - x(t)) \times f_i$$

Rigid Body System

Collision & Contact

■ Collision

- A body hits another body.
- Relative normal velocity is negative.
- *Impulse* governs the dynamics.

■ Contact

- A body rests against another body.
- Relative normal velocity is negligible.
- *Resting force* prevents inter-penetration.

Rigid Body System

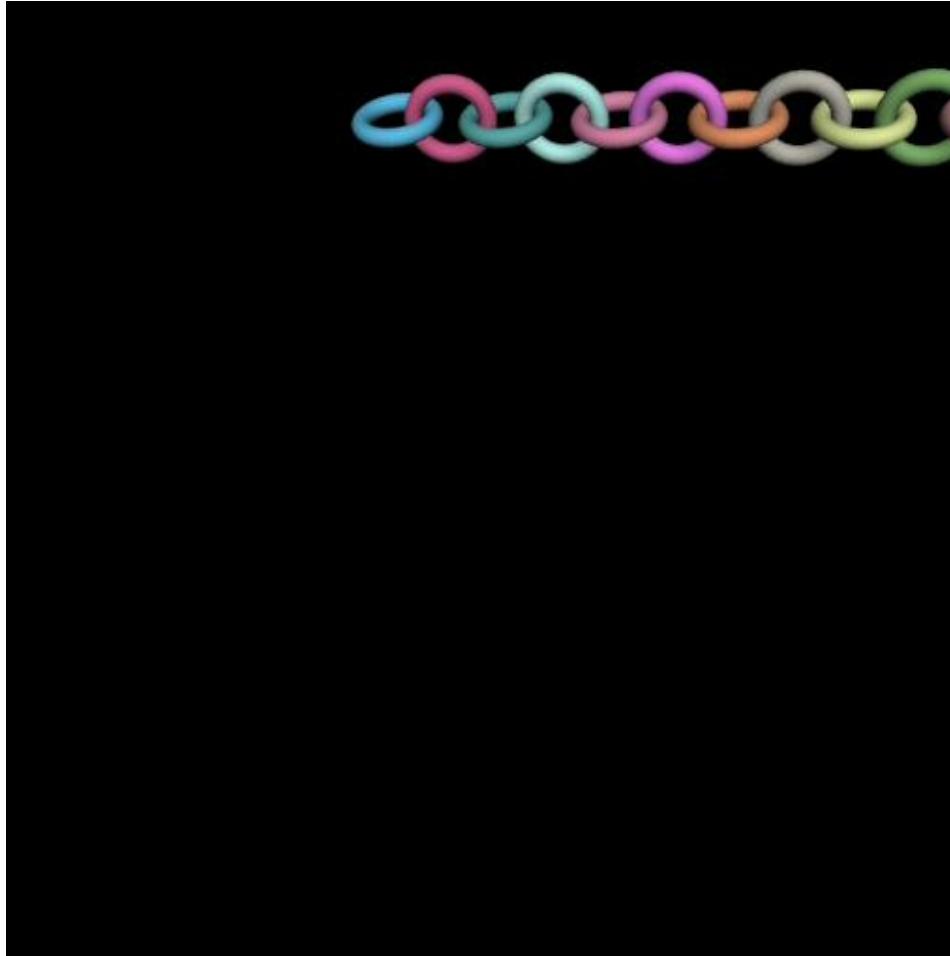
Examples



accurate frictional, rolling behavior

Rigid Body System

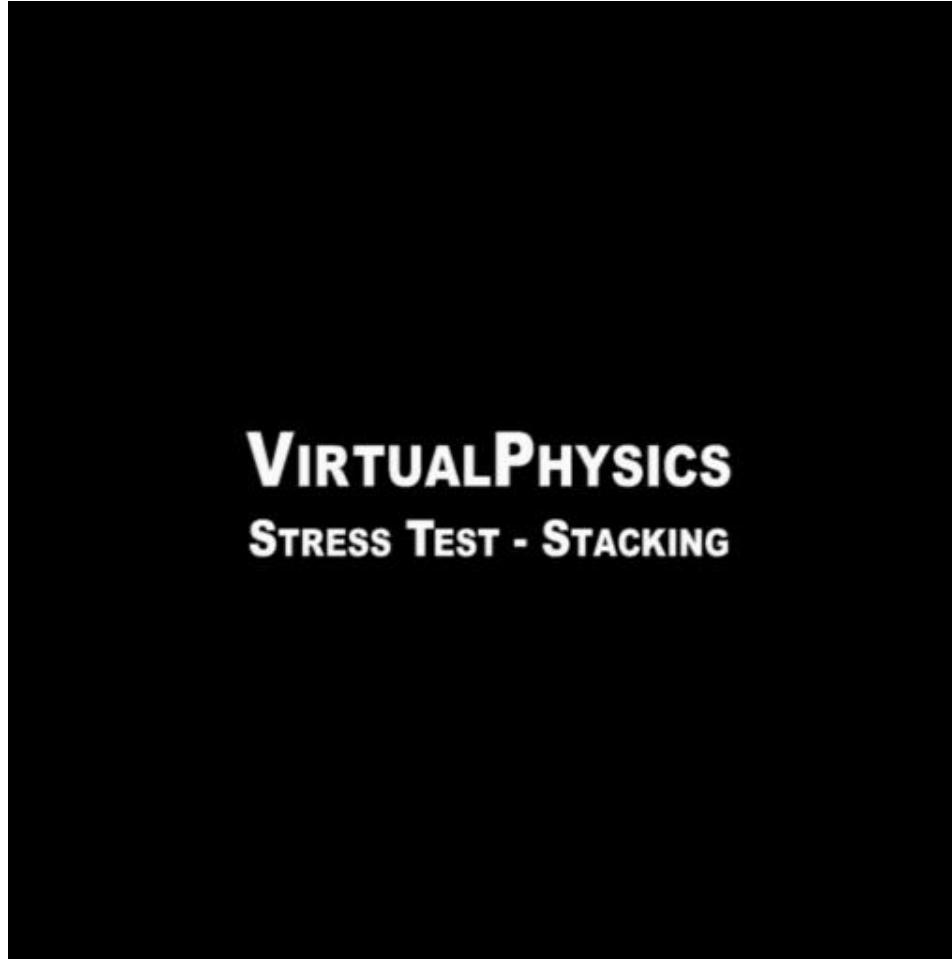
Examples



non-convex geometries

Rigid Body System

Examples



stress test(300 stacked objects)

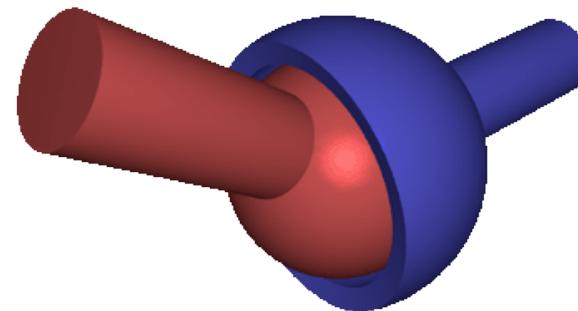
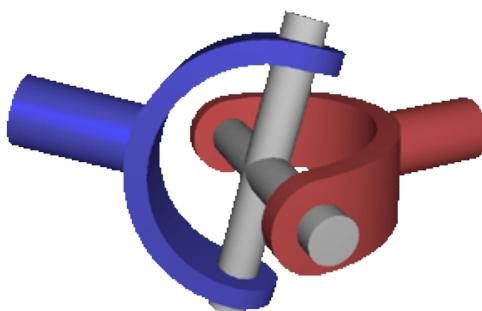
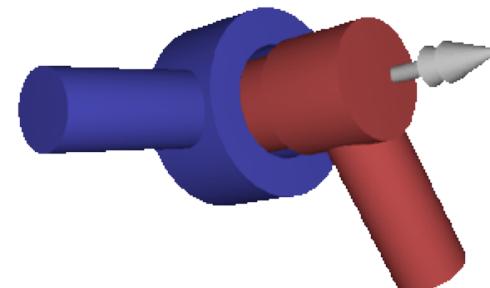
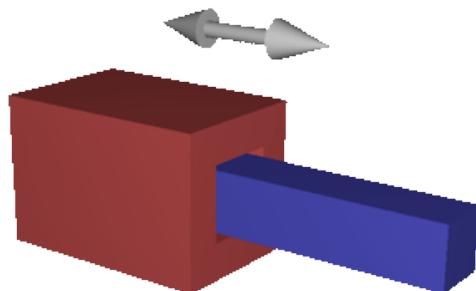
Articulated Body System

- A set of constrained rigid bodies
- Lagrangian approach
 - Solve dynamics with implicit constraint equations
 - In most of the available physics engine
 - $O(n^3)$
- Independent coordinates approach
 - Express dynamics only with the independent variables
 - Popular in Robotics
 - $O(n^3)$: Composite body algorithm
 - $O(n)$: Featherstone algorithm

Articulated Body System

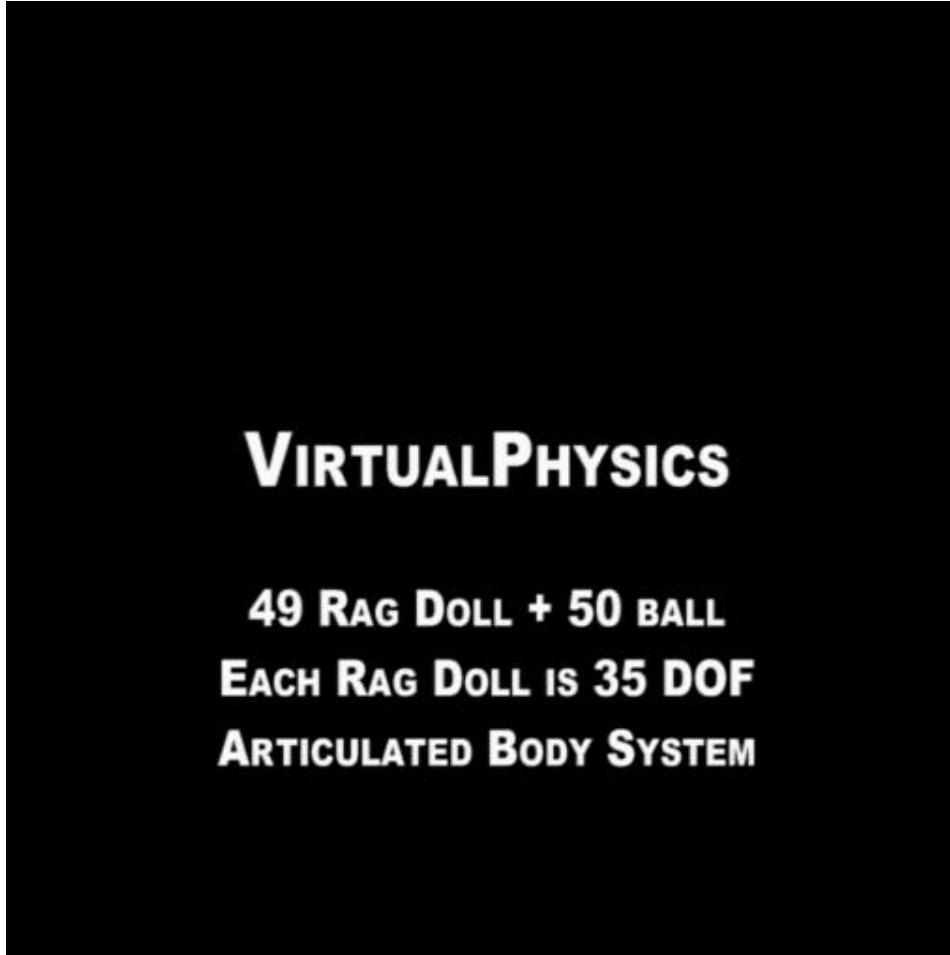
Joint Constraints

- Joint variable as an independent coordinate



Articulated Body System

Examples



49 rag dolls(35DOF each)

Rigid Body Dynamics

- Newton's Law

$$\mathbf{f} = \mathbf{m}\mathbf{a}$$

- In 3D case,

$$\mathbf{f} = \mathbf{m}\mathbf{a}$$

$$\mathbf{m} = I\boldsymbol{\alpha} + \mathbf{w} \times (I\mathbf{w})$$

- Using Lie group notation,

$$\mathbf{F} = J\dot{V} - ad_V^* JV$$

Lie Group

- Lie group
 - a group and a differentiable manifold
 - a set with a binary operator
 - locally similar to Euclidean space
- Lie algebra
 - a vector space with a binary operator(Lie bracket)
 - Linearization of Lie group at the identity
 - Exponential maps Lie algebra to Lie group

Why Lie Group?

■ Examples of Lie group

- General linear group

$$GL(n, \mathbf{R}) = \{M \in \mathbf{R}^{n \times n} \mid \det M \neq 0\}$$

- Rotation group

$$SO(n) = \{R \in \mathbf{R}^{n \times n} \mid RR^T = I, \det R = 1\}$$

- Special Euclidean group

$$SE(3) = \{(R, p) \mid R \in SO(3), p \in \mathbf{R}^3\}$$

SO(3): Rotation Group

- Matrix multiplication rules SO(3)

$$R = R_1 R_2$$

$$\begin{aligned}RR^T &= R_1 R_2 (R_1 R_2)^T \\&= R_1 R_2 {R_2}^T {R_1}^T = I\end{aligned}$$

- Differentiating a rotation matrix

$$RR^T = I$$

$$\dot{R}R^T + R\dot{R}^T = \dot{R}R^T + (\dot{R}R^T)^T = 0$$

so(3): Lie Algebra of SO(3)

- $\dot{R}R^T$ is a skew symmetric matrix.

$$\dot{R}R^T = \begin{bmatrix} 0 & -w_z & w_y \\ w_z & 0 & -w_x \\ -w_y & w_x & 0 \end{bmatrix} = [w]$$

$$w = (w_x, w_y, w_z) \in \mathbf{R}^3$$

- Similarly $R^T\dot{R}$ is skew symmetric as well.
- so(3) is a set of 3X3 skew symmetric matrix

under the Lie bracket defined as

$$[w, v] = [w \times v]$$

or in matrix representation

$$[[w], [v]] = [w][v] - [v][w]$$

Exponential Map

- The exponential of a general square matrix

$$e^A = I + A + \frac{1}{2} A^2 + \frac{1}{3} A^3 + \dots$$

- If A is in $\text{so}(3)$,

$$e^{\theta[w]} = I + \sin \theta[w] + (1 - \cos \theta)[w]^2 \text{ is in } \text{SO}(3).$$

- Corresponds to a rotation about w by an angle θ

SE(3): Special Euclidean Group

- aka homogeneous transformation matrix

$$\begin{bmatrix} R & p \\ 0 & 1 \end{bmatrix}, R \in SO(3), p \in \mathbf{R}^3$$

- Ordered pair (R, p) with group multiplication

$$(R_1, p_1) \cdot (R_2, p_2) = (R_1 R_2, R_1 p_2 + p_1)$$

or in matrix representation

$$\begin{bmatrix} R_1 & p_1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} R_2 & p_2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} R_1 R_2 & R_1 p_2 + p_1 \\ 0 & 1 \end{bmatrix}$$

se(3): Lie Algebra of SE(3)

- a pair of two 3dim vector $V = (w, v)$

or

$$\begin{bmatrix} [w] & v \\ 0 & 0 \end{bmatrix}, w, v \in \mathbf{R}^3 \text{ in matrix representation}$$

- Lie bracket of se(3)

$$[(w_1, v_1), (w_2, v_2)] = (w_1 \times w_2, w_1 \times v_2 - w_2 \times v_1) = ad_{V_1} V_2$$

- Exponential map

$$\exp(w, v) = e^{\begin{bmatrix} [w] & v \\ 0 & 0 \end{bmatrix}}$$

Adjoint map

$\text{Ad}_T : \text{se}(3) \rightarrow \text{se}(3)$

$$\begin{aligned} \text{Ad}_T V = T V T^{-1} &= \begin{bmatrix} R & p \\ 0 & 1 \end{bmatrix} \begin{bmatrix} [w] & v \\ 0 & 0 \end{bmatrix} \begin{bmatrix} R^T & -R^T p \\ 0 & 1 \end{bmatrix} \\ &= \begin{bmatrix} [Rw] & p \times Rw + Rv \\ 0 & 0 \end{bmatrix} \end{aligned}$$

$$\text{Ad}_T V = (Rw, p \times Rw + Rv)$$

or in matrix representation

$$\text{Ad}_T V = \begin{bmatrix} R & 0 \\ [p]R & R \end{bmatrix} \begin{bmatrix} w \\ v \end{bmatrix}$$

Generalized Force

- $\text{se}(3)^*$, dual of $\text{se}(3)$

$$F = (m, f)$$

f : force vector

m : moment vector

- Transformation of $\text{se}(3)^*$

dual Adjoint operator

$$F_B = \text{Ad}_{T_B^A}^* F_A$$

Generalized Inertia Tensor

- triple (I, m, r)
 - I : 3X3 inertia matrix of the rigid body
 - m : mass of the rigid body
 - r : 3dim. offset vector
 - in matrix representation

$$J = \begin{bmatrix} I & [r] \\ -[r] & ml \end{bmatrix}$$

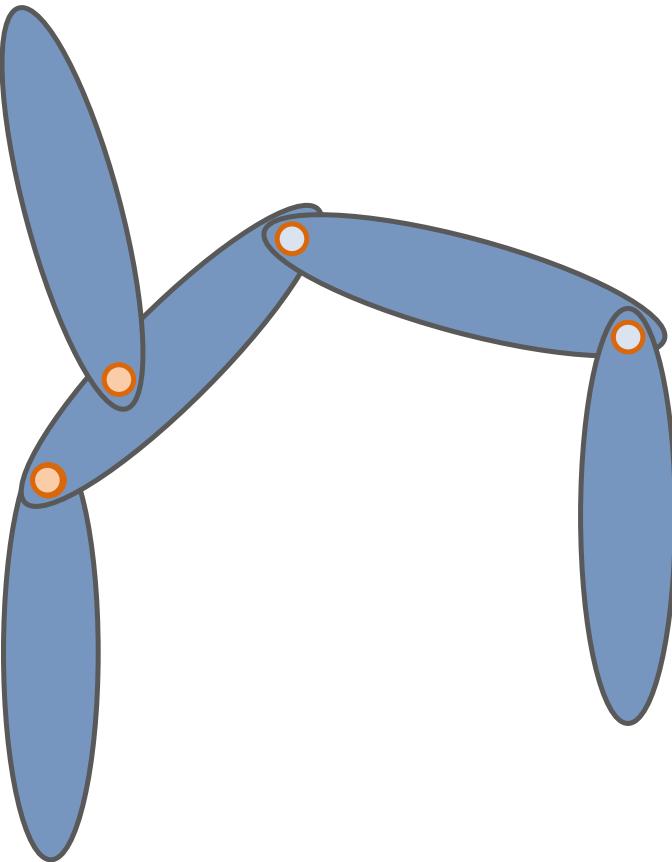
- maps $\text{se}(3)$ to $\text{se}(3)^*$

$$JV = (Iw + r \times v, mv - r \times w)$$

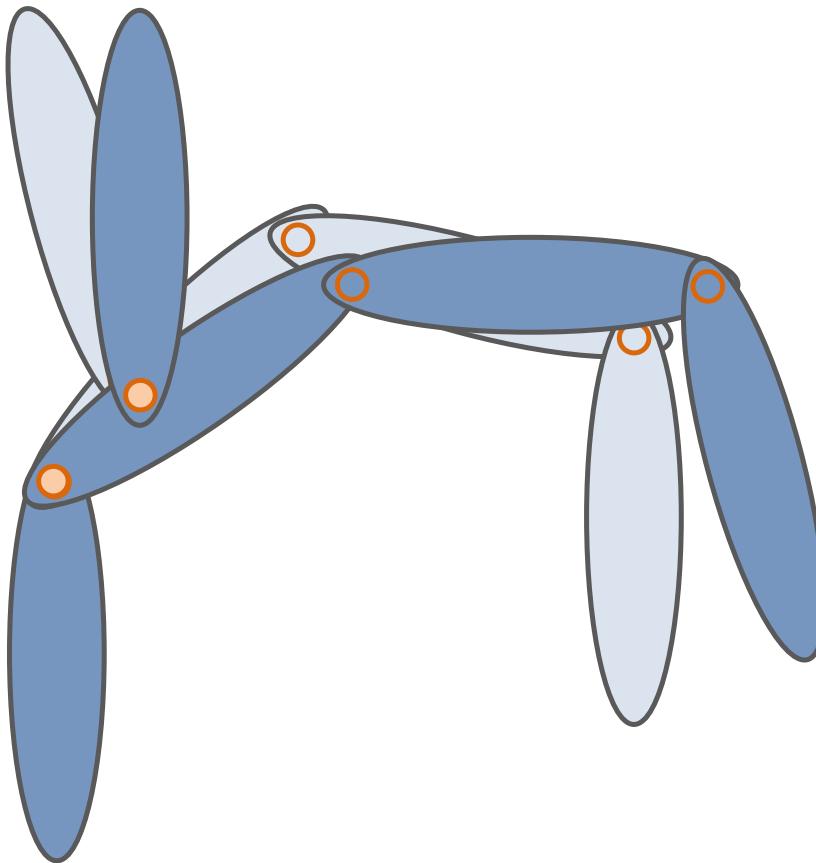
- Transformation of generalized inertia tensor

$$J_B = Ad_T^* J_A Ad_T$$

Articulated Rigid Body System



Articulated Rigid Body System



Joint

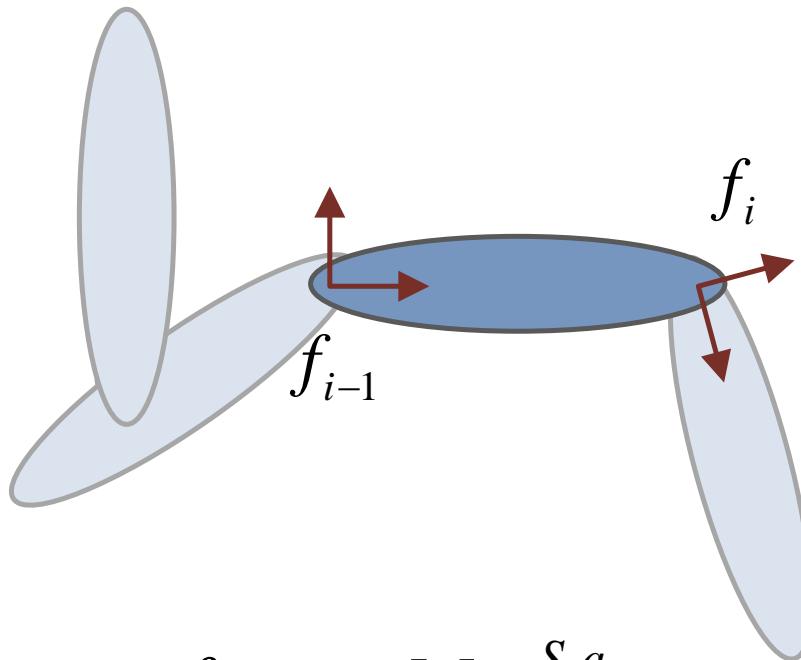
- Allows relative motion between adjacent bodies
- Can be parameterized through exponential map if the joint is 1DOF

$$T = e^{Sq}$$

$$T^{-1}\dot{T} = S\dot{q}$$

- Example
 - Rotational joint $S = (w, 0)$
 - Prismatic joint $S = (0, v)$

Kinematics



$$f_{i-1,i} = M_i e^{S_i q_i}$$

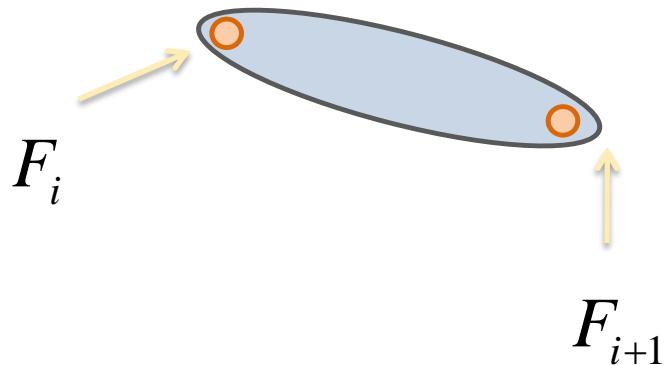
$$f_i = f_{0,1} \cdots f_{i-1,i}$$

$$= f_{i-1} f_{i-1,i}$$

Velocity and Acceleration

$$\begin{aligned}
 V_i &= f_i^{-1} \dot{f}_i \\
 &= (f_{i-1} f_{i-1,i})^{-1} (\dot{f}_{i-1} f_{i-1,i} + f_{i-1} \dot{f}_{i-1,i}) \\
 &= f_{i-1,i}^{-1} f_{i-1}^{-1} \dot{f}_{i-1} f_{i-1,i} + f_{i-1,i}^{-1} f_i^{-1} f_{i-1} \dot{f}_{i-1,i} \\
 &= f_{i-1,i}^{-1} V_{i-1} f_{i-1,i} + f_{i-1,i}^{-1} \dot{f}_{i-1,i} \\
 &= Ad_{f_{i-1,i}^{-1}} V_{i-1} + S_i \dot{q}_i \\
 \dot{V}_i &= Ad_{f_{i-1,i}^{-1}} \dot{V}_{i-1} + S_i \ddot{q}_i + ad_{V_i} S_i \dot{q}_i
 \end{aligned}$$

Dynamics



$$F_i = Ad_{f_{i,i+1}^{-1}}^* F_{i+1} + J_i \dot{V}_i - ad_{V_i}^* J_i V_i$$

$$\tau_i = \langle S_i, F_i \rangle$$

Recursive Inverse Dynamics

initialize

$$V_0, V_0, F_{n+1}, \dot{q}, \ddot{q}$$

$$f_{i-1,i} = M_i e^{S_i q_i}$$

Forward recursion

i=1:n

$$V_i = Ad_{f_{i-1,i}^{-1}} V_{i-1} + S_i \dot{q}_i$$

$$\dot{V}_i = Ad_{f_{i-1,i}^{-1}} \dot{V}_{i-1} + S_i \ddot{q}_i + ad_{V_i} S_i \dot{q}_i$$

Backward recursion

i=n:1

$$F_i = Ad_{f_{i,i+1}^{-1}}^* F_{i+1} + J_i \dot{V}_i - ad_{V_i}^* J_i V_i$$

$$\tau_i = \langle S_i, F_i \rangle$$

Recursive Forward Dynamics

Forward recursion

i=1:n

$$f_{i-1,i} = M_i e^{S_i q_i}$$

$$V_i = Ad_{f_{i-1,i}^{-1}} V_{i-1} + S_i \dot{q}_i$$

$$\hat{J}_{i-1} = J_{i-1} + Ad_{f_{i-1,i}^{-1}}^\dagger \left(J_i - \frac{1}{\Omega_i} (\zeta_i \otimes \zeta_i) \right)$$

$$b_{i-1} = -ad_{V_{i-1}}^* J_{i-1} V_{i-1} + Ad_{f_{i-1,i}^{-1}}^* \left(c_i + \frac{T_i - \langle S_i, c_i \rangle}{\Omega_i} \zeta_i \right)$$

$$c_{i-1} = \hat{J}_{i-1} ad_{v_{i-1}} S_{i-1} \dot{q}_{i-1} + b_{i-1}$$

$$\zeta_{i-1} = \hat{J}_{i-1} S_{i-1}$$

$$\Omega_{i-1} = \langle S_{i-1}, \zeta_{i-1} \rangle$$

Backward recursion

i=n:1

Forward recursion

i=1:n

$$\dot{q}_i = \frac{1}{\Omega_i} \left(\tau_i - \left\langle Ad_{f_{i-1,i}^{-1}} \dot{V}_{i-1}, \zeta_i \right\rangle - \langle S_i, c_i \rangle \right)$$

$$\dot{V}_i = Ad_{f_{i-1,i}^{-1}} \dot{V}_{i-1} + S_i \ddot{q}_i + ad_{V_i} S_i \dot{q}_i$$

Comparison to Spatial Notation

- Lie group notation

$$\hat{J}_{i-1} = J_{i-1} + Ad_{f_{i-1,i}^{-1}}^{\dagger} \left(\hat{J}_i - \frac{(\hat{J}_i S_i) \otimes (\hat{J}_i S_i)}{\langle S_i, \hat{J}_i S_i \rangle} \right)$$

- Spatial notation by Featherstone

$$I_{i-1}^A = I_{i-1} + {}_{i-1}X_i \left(I_i^A - \frac{I_i^A S_i S_i^T I_i^A}{S_i^T I_i^A S_i} \right)_i X_{i-1}$$

Implementing Lie Group

- Lie group elements can be represented as a matrix form.
- However it is not a clever idea to use matrices when computing operations on Lie group.

Implementing Lie Group

$$Ad_T V = (Rw, p \times Rw + Rv)$$

$$= \begin{bmatrix} R & 0 \\ [p]R & R \end{bmatrix} \begin{bmatrix} w \\ v \end{bmatrix}$$

$$Ad_T^\dagger J = \left(R^T (I + [r][p] + [p][r] - m[p]^2) R, m, R^T(r - mp) \right)$$

$$= \begin{bmatrix} R & 0 \\ [p]R & R \end{bmatrix} \begin{bmatrix} I & [r] \\ -[r] & m1 \end{bmatrix} \begin{bmatrix} R & 0 \\ [p]R & R \end{bmatrix}^T$$

Operation Count

	Geometric computation		Matrix based computation		ratio	
	x	+	x	+	x	+
$Ad_T V$	24	18	63	48	38%	37.5%
$ad_V W$	18	12	36	30	50%	40%
JV	24	18	36	30	67%	60%
$Ad_T^\dagger J$	101	66	459	378	22%	17%

SE(3) Class

- Substitution

$$\mathbf{SE3} \leftarrow \mathbf{SE3}$$

- Multiplication

$$\mathbf{SE3} \leftarrow \mathbf{SE3} * \mathbf{SE3}$$

- Inverse

$$\mathbf{SE3} \leftarrow \mathbf{Inv}(\mathbf{SE3})$$

- Exponential map

$$\mathbf{SE3} \leftarrow \mathbf{Exp}(\mathbf{se3})$$

- Adjoint map

$$\mathbf{se3} \leftarrow \mathbf{Ad}(\mathbf{SE3}, \mathbf{se3})$$
$$\mathbf{dse3} \leftarrow \mathbf{dAd}(\mathbf{SE3}, \mathbf{dse3})$$

se(3) Class

- Substitution **se3** \leftarrow **se3**
- Addition **se3** \leftarrow **se3** + **se3**
- Multiplication **se3** \leftarrow **scalar** * **se3**
- Reciprocal product **scalar** \leftarrow **se3** * d**se3**
- Lie bracket **se3** \leftarrow **se3** ^ **se3**

Generalized Inertia Class

- Substitution **Inertia** \leftarrow **Inertia**
- Multiplication **dse3** \leftarrow **Inertia** * **se3**
- Transformation **Inertia** \leftarrow **Ad(SE3, Inertia)**

Articulated Inertia Class

- Substitution

```
AInertia ← Ainertia
```

```
AInertia ← Inertia
```

- Addition

```
AInertia ← Ainertia + AInertia
```

- Multiplication

```
AInertia ← scalar * AInertia
```

```
dse3 ← AInertia * se3
```

- Kronecker product

```
AInertia ← dse3 * dse3
```

- Transformation

```
Inertia ← Ad(SE3, Inertia)
```

Implementing Algorithm

$$\hat{J}_{i-1} = J_{i-1} + Ad_{f_{i-1,i}^{-1}}^\dagger \left(J_i - \frac{(\hat{J}_i S_i) \otimes (\hat{J}_i S_i)}{\langle S_i, \hat{J}_i S_i \rangle} \right)$$

1. **dse3** \leftarrow **AInertia** * **se3** $\zeta = \hat{J}_i S_i$
2. **AInertia** \leftarrow **dse3** * **dse3** $\Gamma = \zeta \otimes \zeta$
3. **scalar** \leftarrow **se3** * **dse3** $\Omega = \langle S_i, \zeta \rangle$
4. **AInertia** \leftarrow **scalar** * **AInertia** $\Theta = \frac{1}{\Omega} \Gamma$
5. **AInertia** \leftarrow **Ainertia** - **AInertia** $\Phi = \hat{J}_i - \Theta$
6. **AInertia** \leftarrow **Ad(SE3, AInertia)** $\Psi = Ad_{f_{i-1,i}^{-1}}^\dagger \Phi$
7. **Ainertia** \leftarrow **Inertia** + **AInertia** $\hat{J}_{i-1} = J_{i-1} + \Psi$

Code snippet

$$\hat{J}_{i-1} = J_{i-1} + Ad_{f_{i-1,i}^{-1}}^{\dagger} \left(\hat{J}_i - \frac{(\hat{J}_i S_i) \otimes (\hat{J}_i S_i)}{\langle S_i, \hat{J}_i S_i \rangle} \right)$$

```
SE3 f[n];
```

```
Inertia J[n]; AInertia AJ[n];
```

```
se3 S[n]; dse3 ksi;
```

```
...
```

```
ksi = AJ[i] * S[i];
```

```
AJ[i-1] = J[i-1] + Ad(Inv(f[i]), AJ[i] -  

  (1/(S[i] * ksi)) * (ksi * ksi));
```

Lie Group Formulation

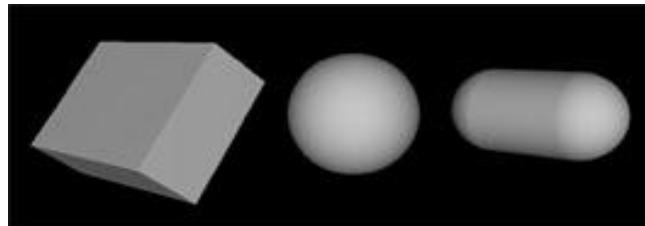
- looks beautiful
- offers further insight into the high-level structure of kinematics and dynamics
- is computationally efficient when implemented carefully

VirtualPhysics

- C++ library for realtime multi-body dynamics simulation
- based on Lie group formulation
- arbitrary joint modeling
- collision detection between geometric primitives
- analytic or penalty based collision response
- contact response by solving LCP
- mixed dynamics: working with kinematically controlled objects
- collision like joint limit
- dynamic configuration: excessive force can break joints

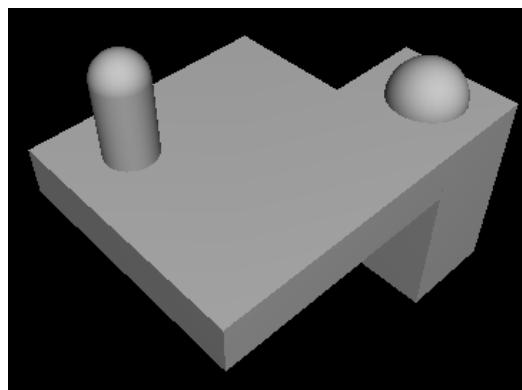
vpGeom

- Abstract class to represent primitive geometries



vpBox vpSphere vpCapsule

- Consider a rigid body as a set of primitive geometries



- Target of collision detection

vpBody

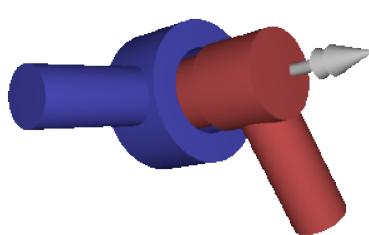
- A class to model rigid bodies
- consists of several vpGeom instances
- can be connected to another body with vpJoint.
- has a reference to vpMaterial
- can be set ground

vpMaterial

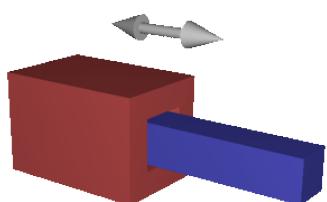
- A class about material properties
 - density
 - coefficient of restitution
 - coefficient of static/dynamic/spinning friction

vpJoint

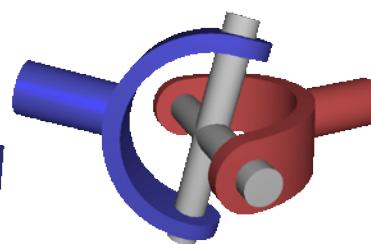
- Abstract class to connect two adjacent bodies
- Can be broken
 - , when a normal force/torque applied to the joint exceeds its threshhold.



vpRJointv



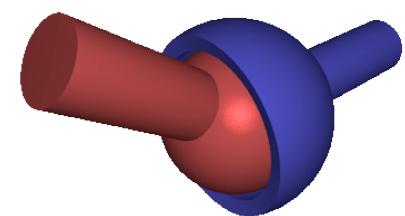
pPJoint



vpUJoint



vpSJoint



vpBJoint

vpWJoint

vpNDOFJoint

vpWorld

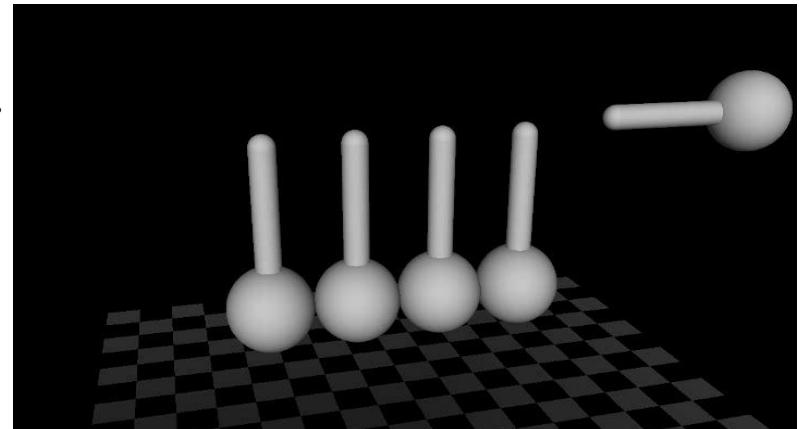
- A class to model a virtual world
- Add bodies to vpWorld
- Set global attributes such as gravity
- Set simulation attributes such as integration time step
- Initialize and run

Example: a pedulum

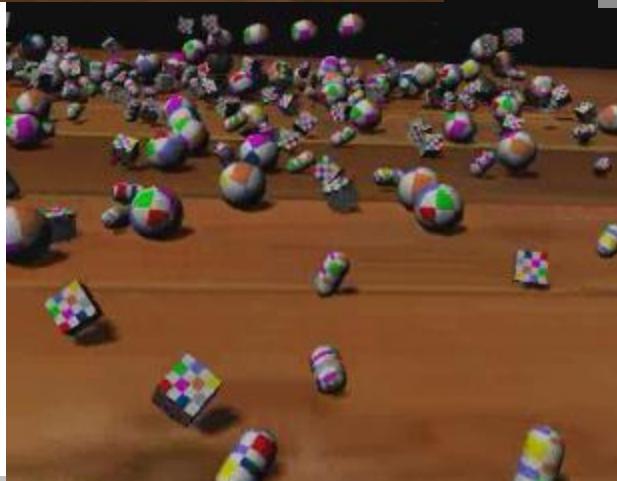
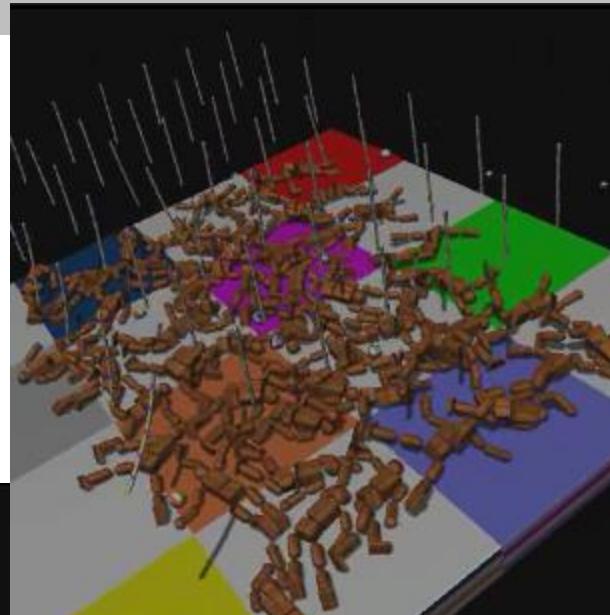
- Define geometry, add and initialize joint

```

vpBody G, B;
vpSphere sph(0.5);
vpCapsule rod(0.2,2);
B.AddGeometry(&rod, Vec3(0));
B.AddGeometry(&sph, Vec3(0,0,-1));
vpRJoint J;
G.SetJoint(&J, Vec3(0));
B.SetJoint(&J, Vec3(0,0,1));
J.SetAxis(Vec3(0,1,0));
G.SetGround();
vpWorld world;
world.AddBody(&G);
world.Initialize();
while ( true )
    world.StepAhead();
  
```



<http://virtualphysics.imrc.kist.re.kr>



Thank you

Any Question?



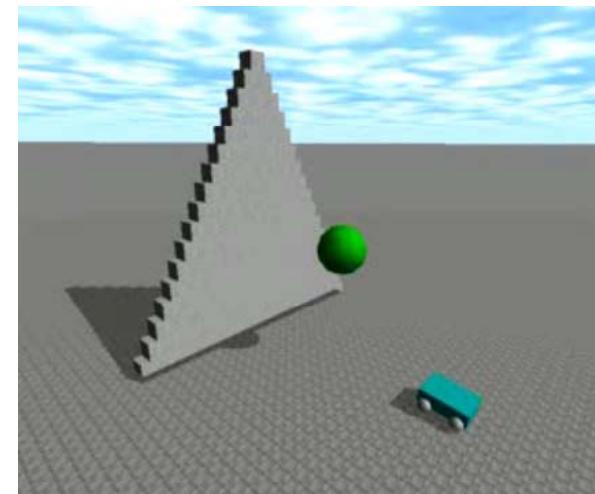
Physically Based Character Simulation



Yoonsang Lee,
Movement Research Lab., Seoul National University

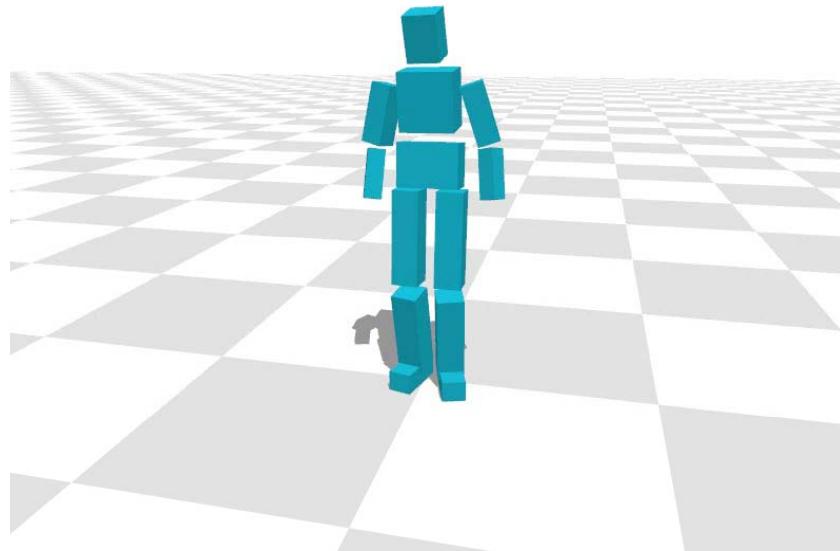
Why Simulation?

- ▶ Animating characters in dynamic environments is difficult
 - ▶ Physically correct interaction with environment is required
- ▶ Simulation automatically produces physically valid results



Character Control

- ▶ But, simulation of character requires **controller** that computes internal muscle forces (joint torques)

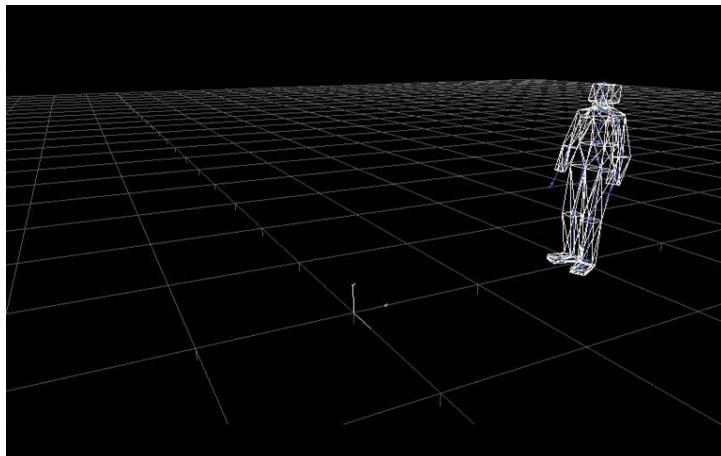


Simulation without internal forces



Character Control

- ▶ Character control is difficult problem
 - ▶ Maintaining balance
 - ▶ Reproducing various style of behavior
- ▶ Humanoid Robots :A lot hand tuning..



ASIMO
Honda Motor Company



QURIO
SONY CORPORATION

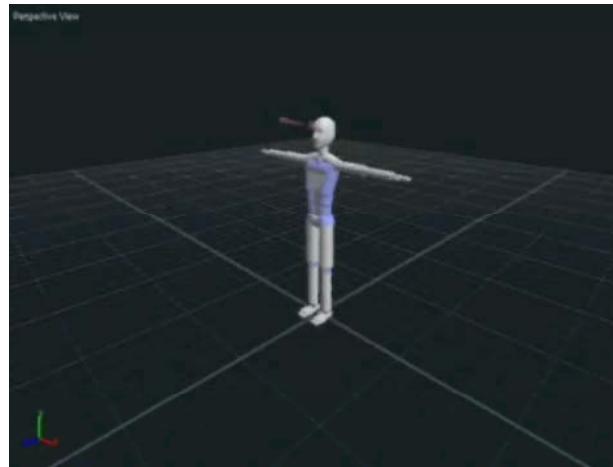


HUBO
KAIST



Character Control

- ▶ Current commercial physics engines supports character simulation of passive motion



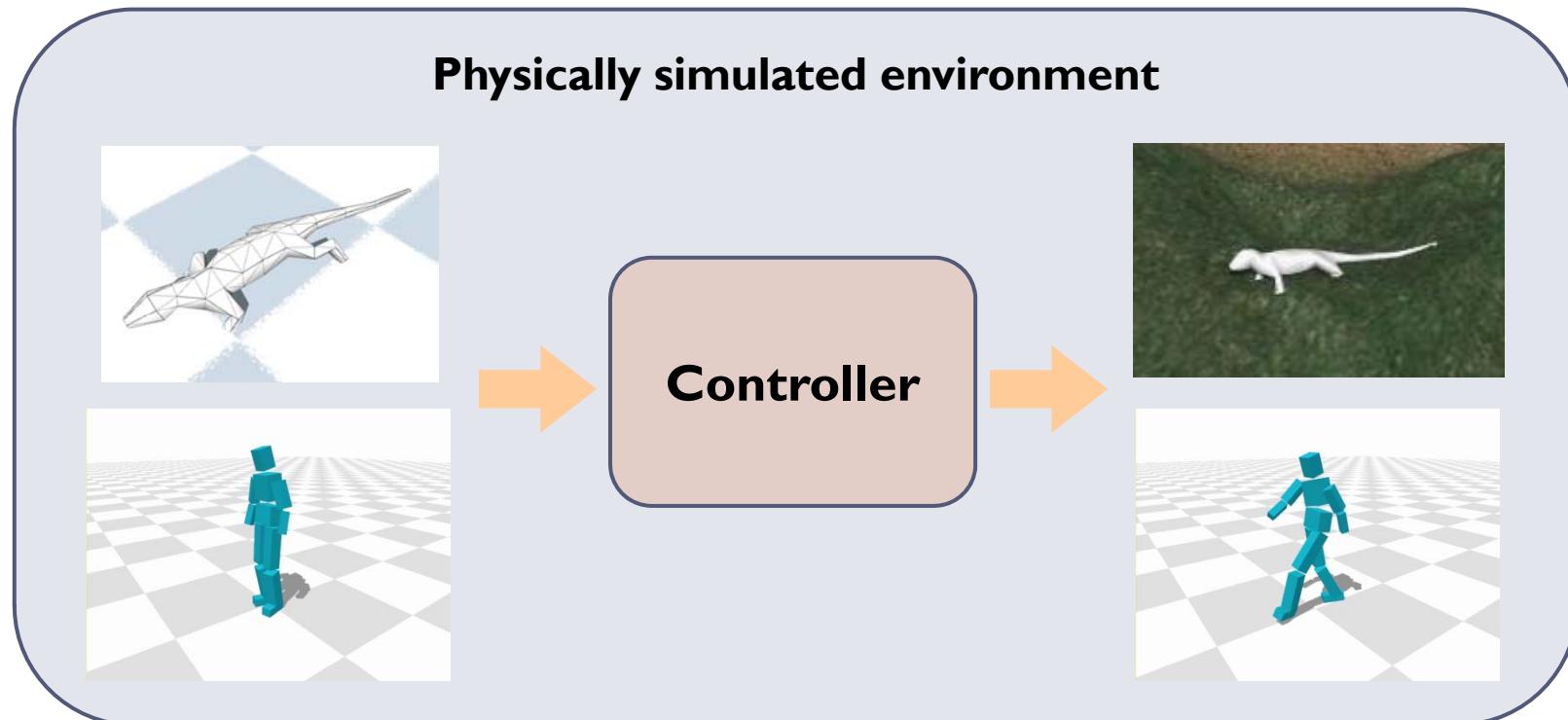
Endorphin

- ▶ Controller for active motion also can be applied to other area like robotics



Goal

- ▶ Control **various characters** interactively to perform desired motions in **physically simulated environment**



Goal

- ▶ Data-driven approach : use motion capture data
 - ▶ As a “guidance” of controller
 - ▶ Iguana, bird, human actor, ...



Table of Contents

- ▶ Iguana Character Simulation
- ▶ Bird Character Simulation (Motion Capture)
- ▶ Biped Character Simulation





Iguana Character Simulation

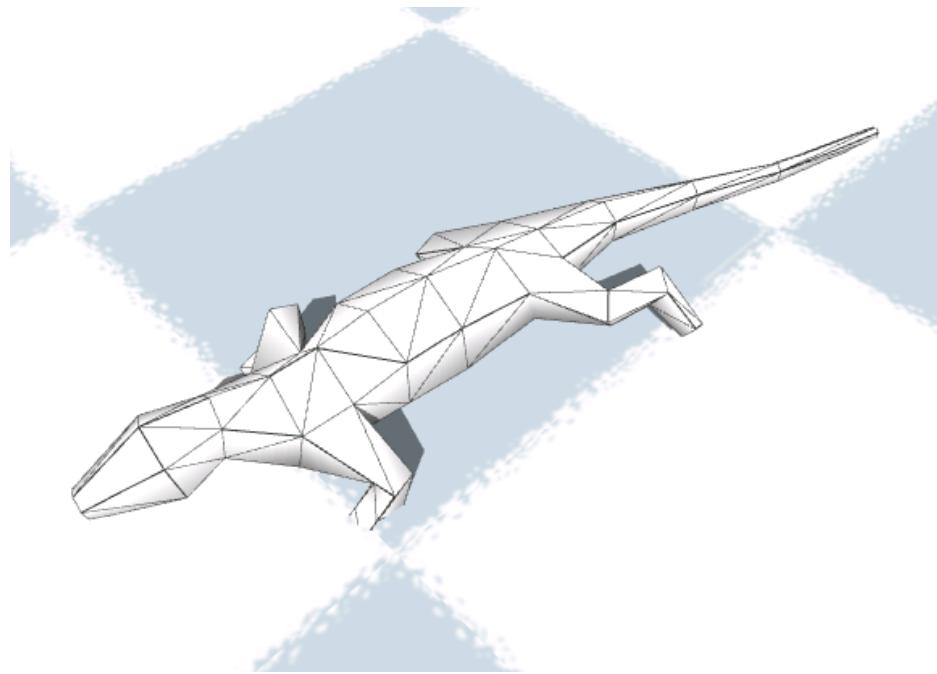


Iguana Motion Capture



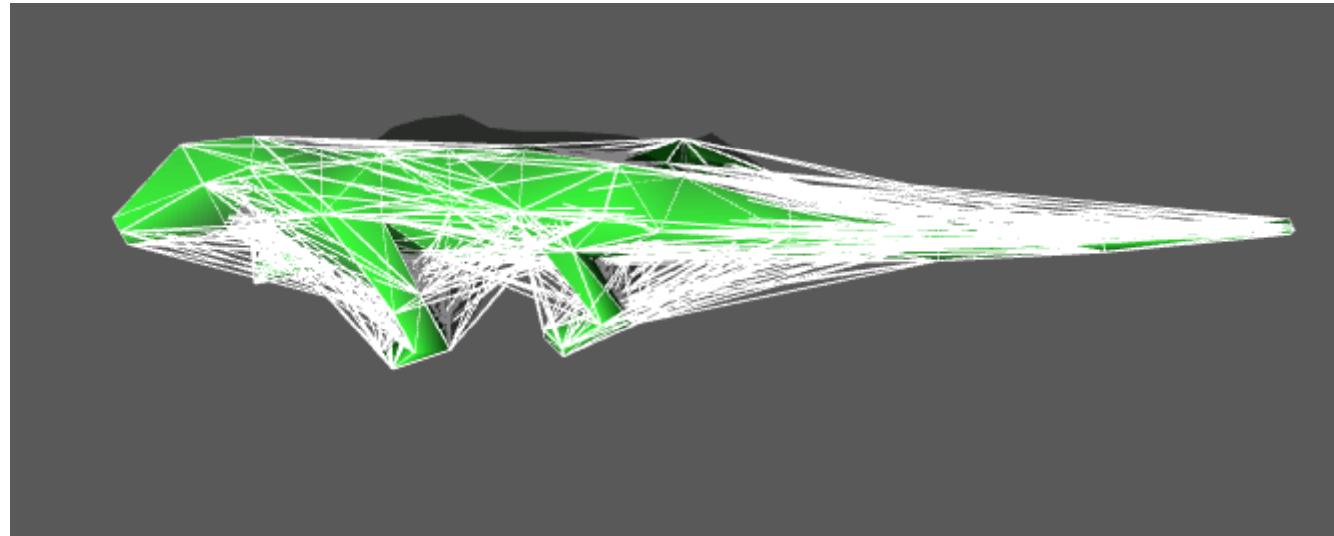
Iguana Simulation

- ▶ Target mesh
 - ▶ Skinning with dual quaternions [Kavan et al. 2008]

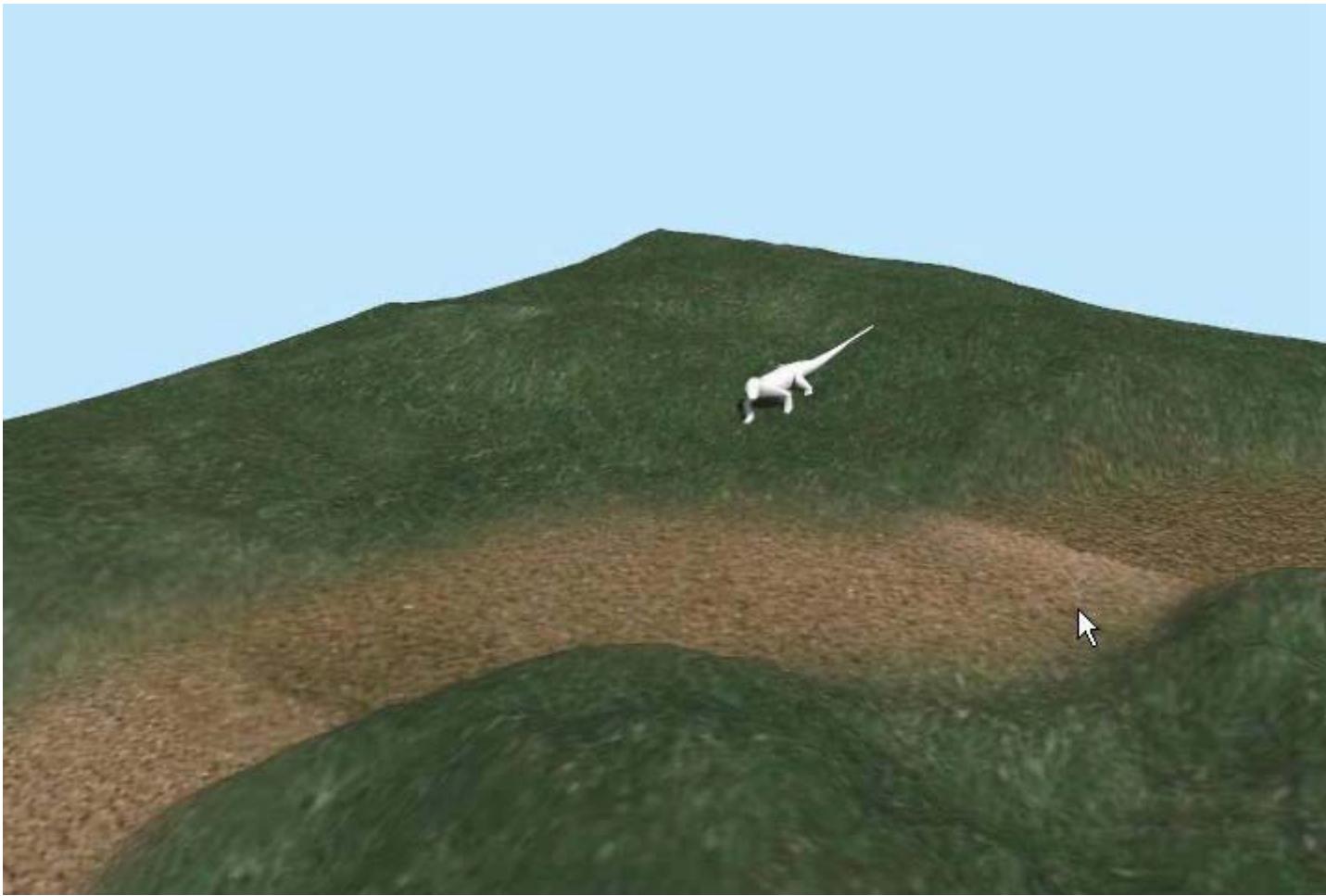


Iguana Simulation

- ▶ Flexible body model
 - ▶ Mass : proportional to the total area of neighboring triangles
 - ▶ Spring : between all pairs of vertices whose distance < 4



Iguana Simulation





Bird Character Simulation (Motion Capture)

Bird Motion Capture

Marker Size(11mm) & Setting





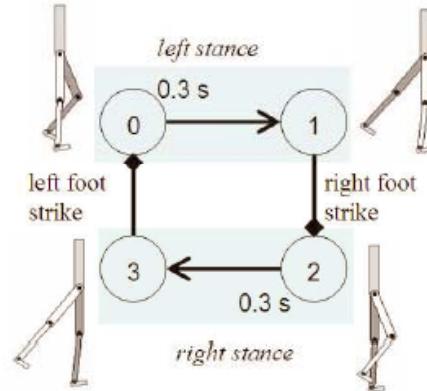
Biped Character Simulation



Related Work

- ▶ State machine approach
 - ▶ SIMBICON [Yin et al. 2007] :
Relatively simple & robust
 - ▶ Hard to reproduce natural results & various human skills

- ▶ Data-driven approach
 - ▶ Use mocap data as high quality & various human skills sources
 - ▶ Various methods proposed
 - ▶ Rectified motion set & simple regression model [Sok et al. 2007], QP [da Silva et al. 2008a], LQR [da Silva et al. 2008b], NQR [Muico et al. 2009]...

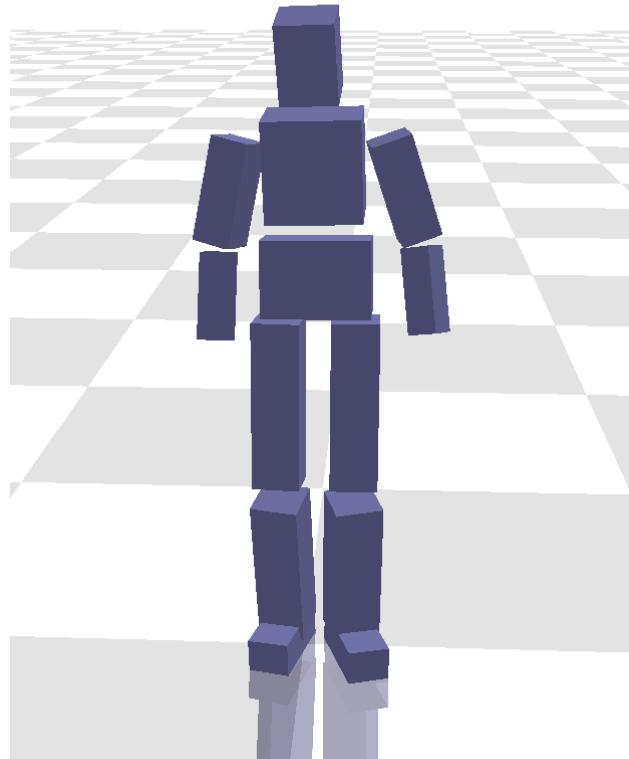


Our Approach

- **Data-driven**
 - Take advantage of high quality result & various human skill sources
- **Focuses on reference motion**
 - Modulate reference motion for synchronization & balancing
- **Advantage**
 - Existing data-driven animation techniques : editing, blending, motion graphs..
 - Simple dynamic controller : just tracking controller



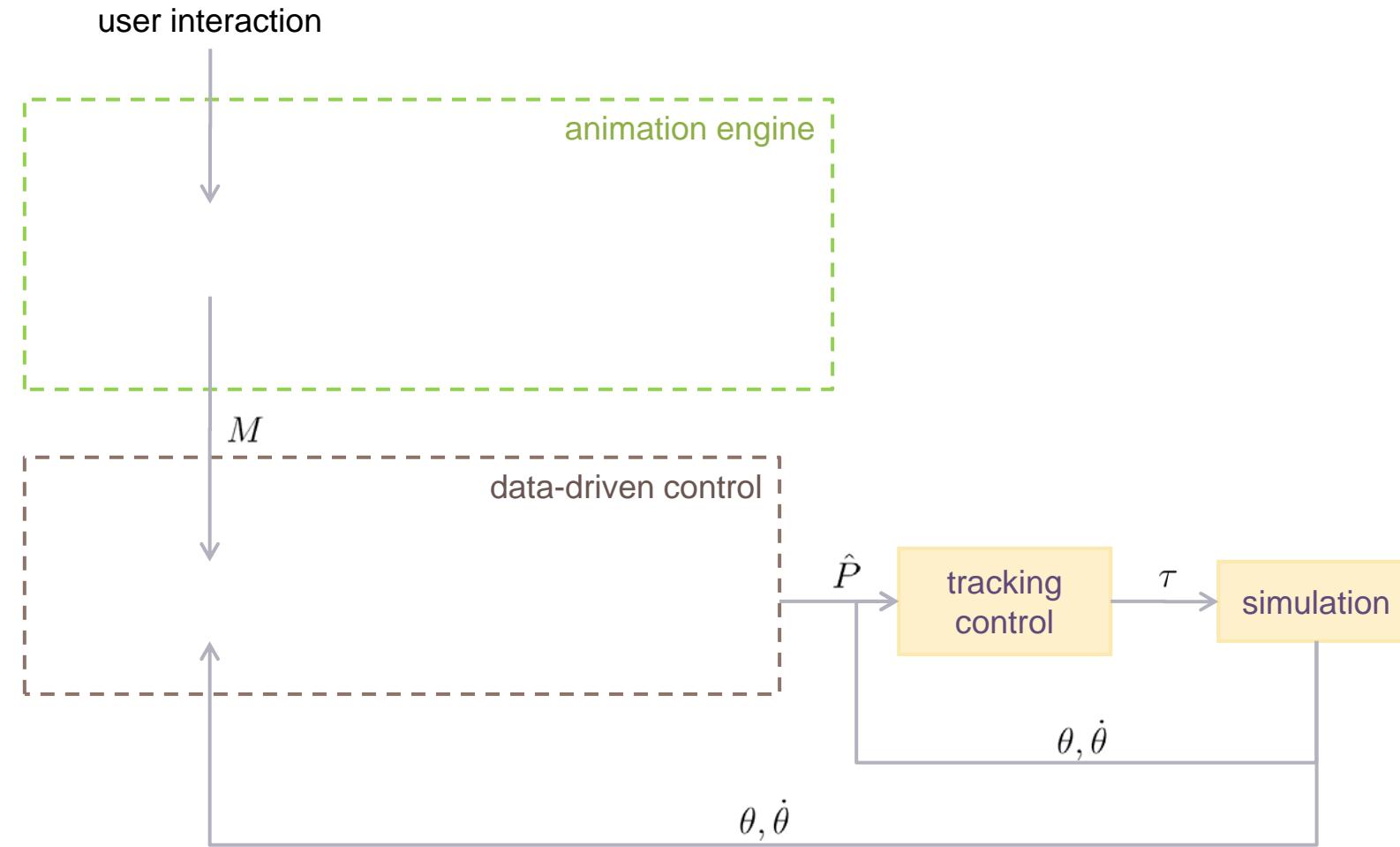
Biped Character



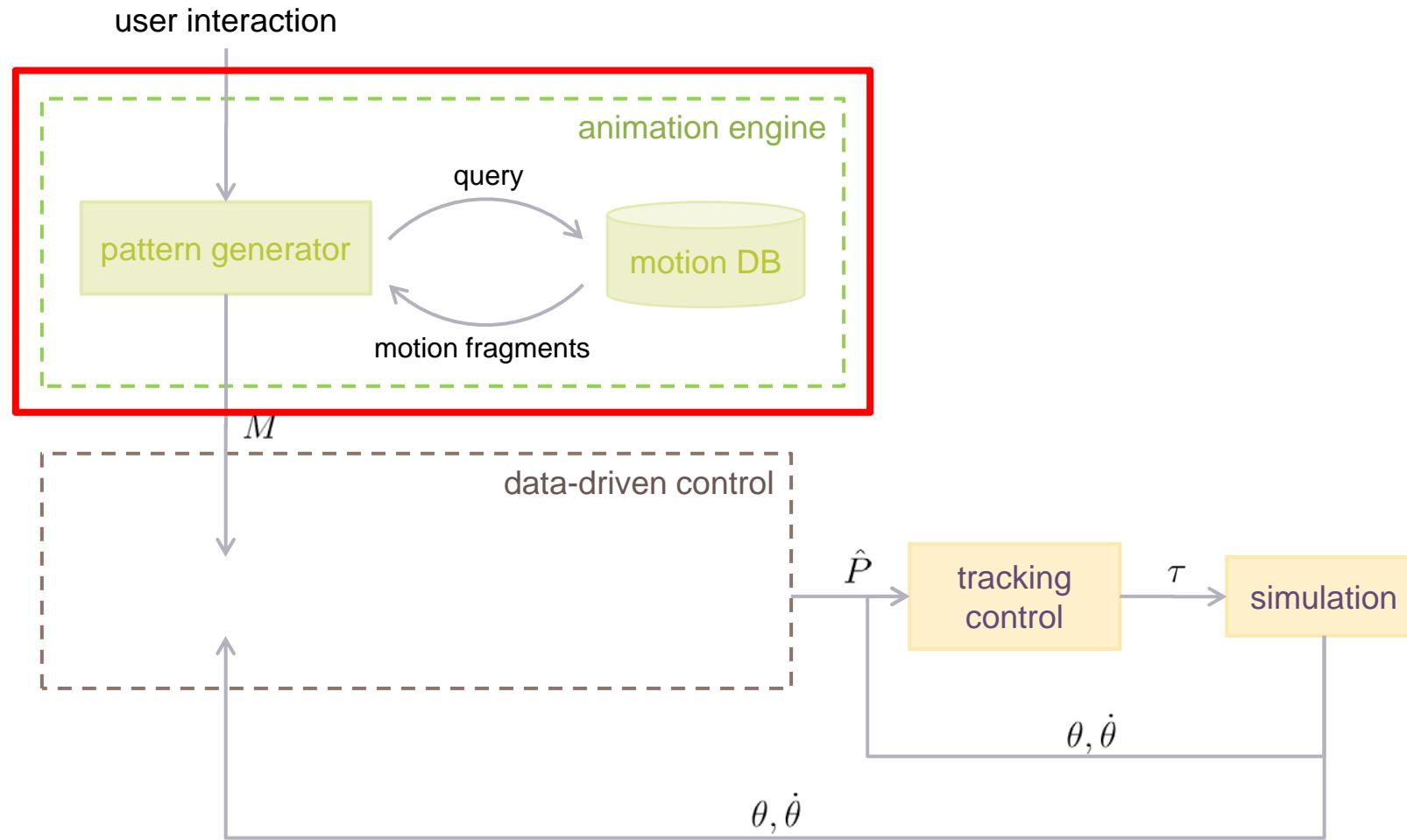
- ▶ 13 rigid body parts
- ▶ 12 ball-socket joints
- ▶ Total DOF is 42 (including 6 DOF of floating root joint)



Overview

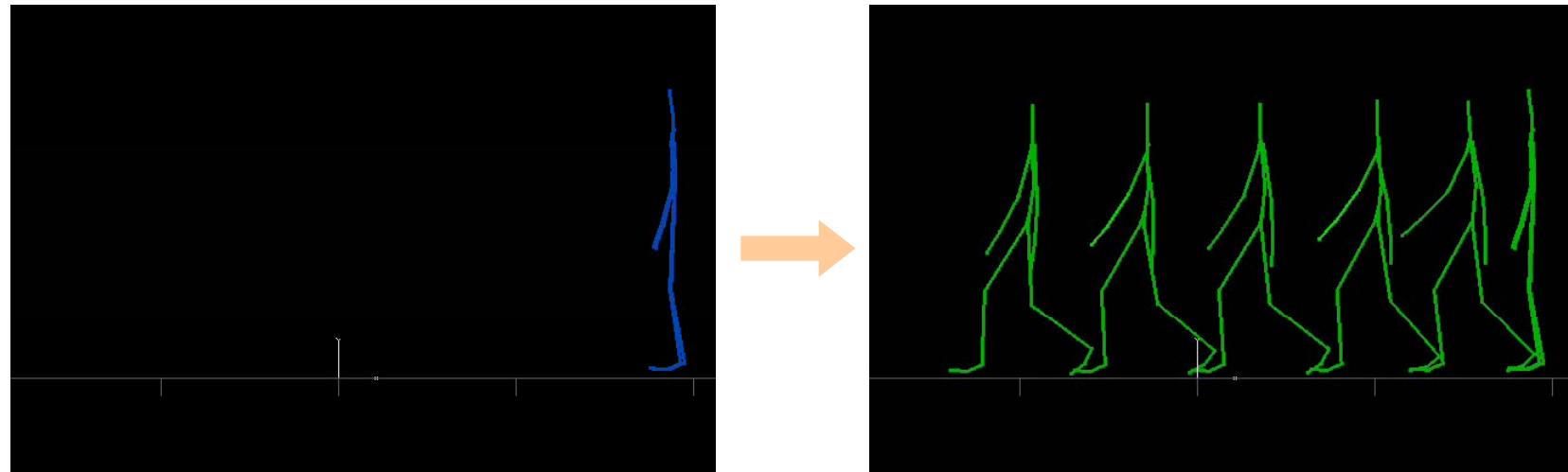


Animation Engine



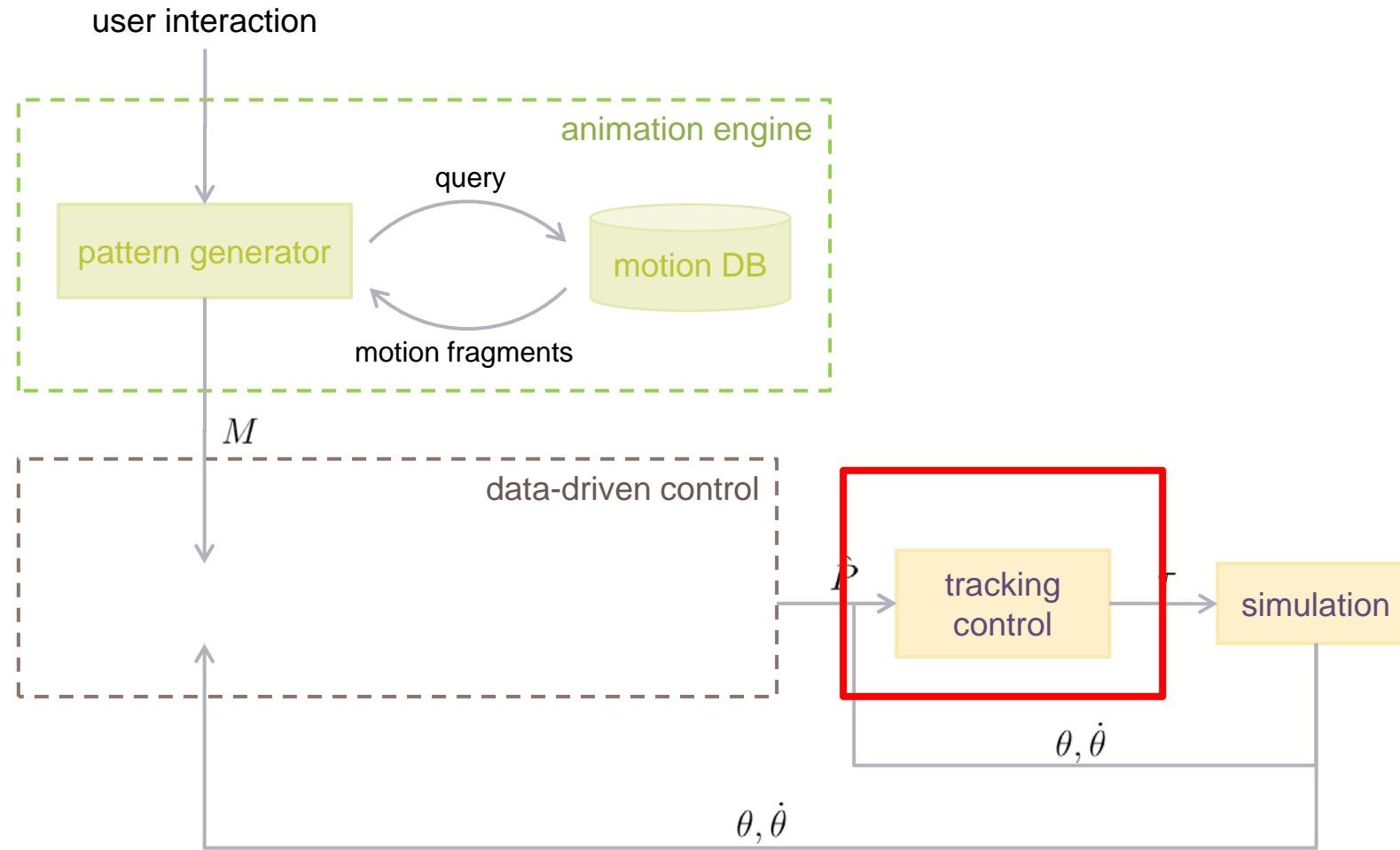
Motion Database

- ▶ Segment motion data into fragments where ground contact changes



- ▶ Motion fragments maintained in a directed graph to allow transitioning between them

Tracking Control



Tracking Control

- ▶ Attempts to follow reference motion by

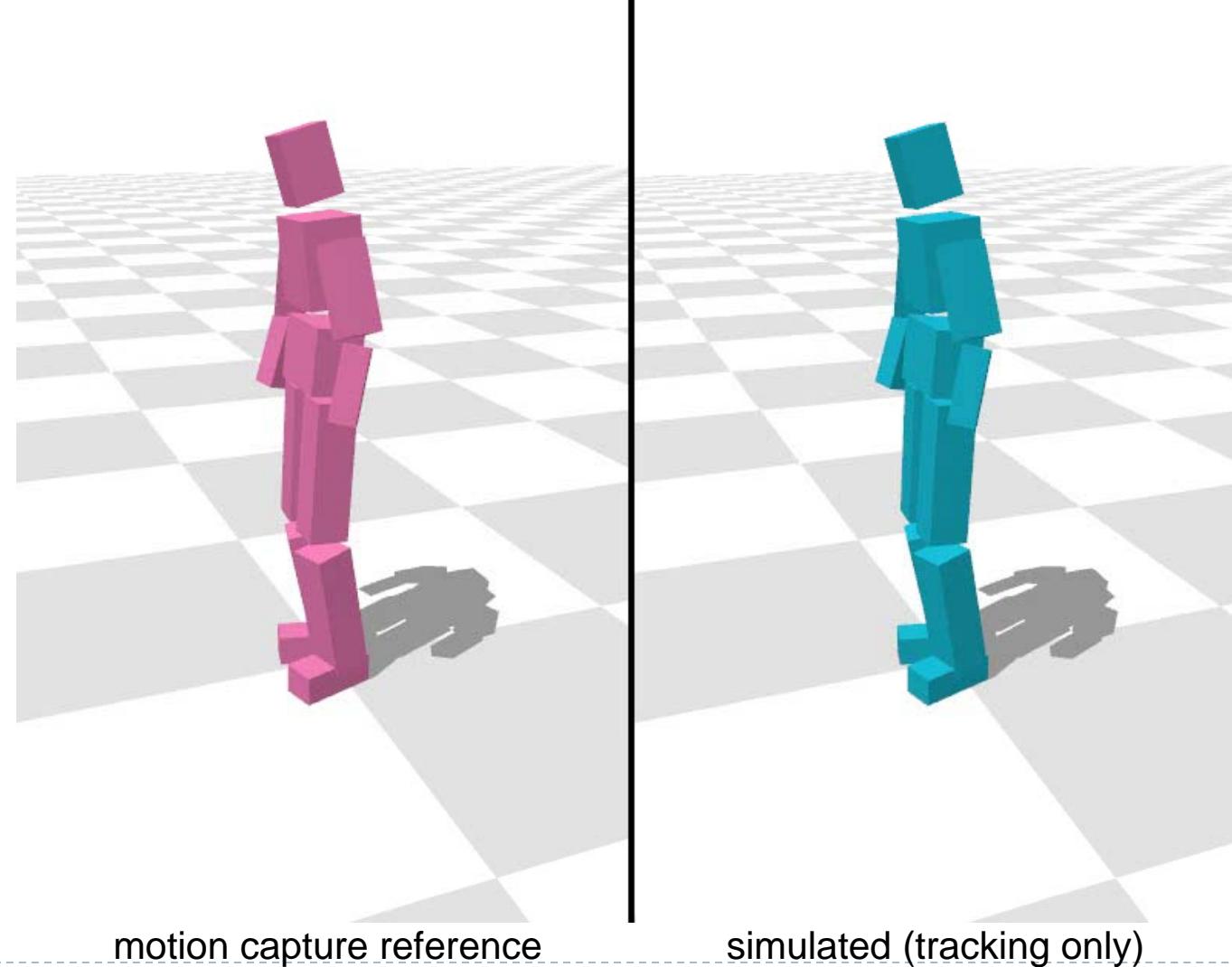
$$\ddot{\theta}_{desired} = k_t(\theta_r - \theta) + k_v(\dot{\theta}_r - \dot{\theta}) + \ddot{\theta}_r$$

$\theta_r, \dot{\theta}_r, \ddot{\theta}_r$: joint angles, joint velocities, joint accelerations from reference motion data

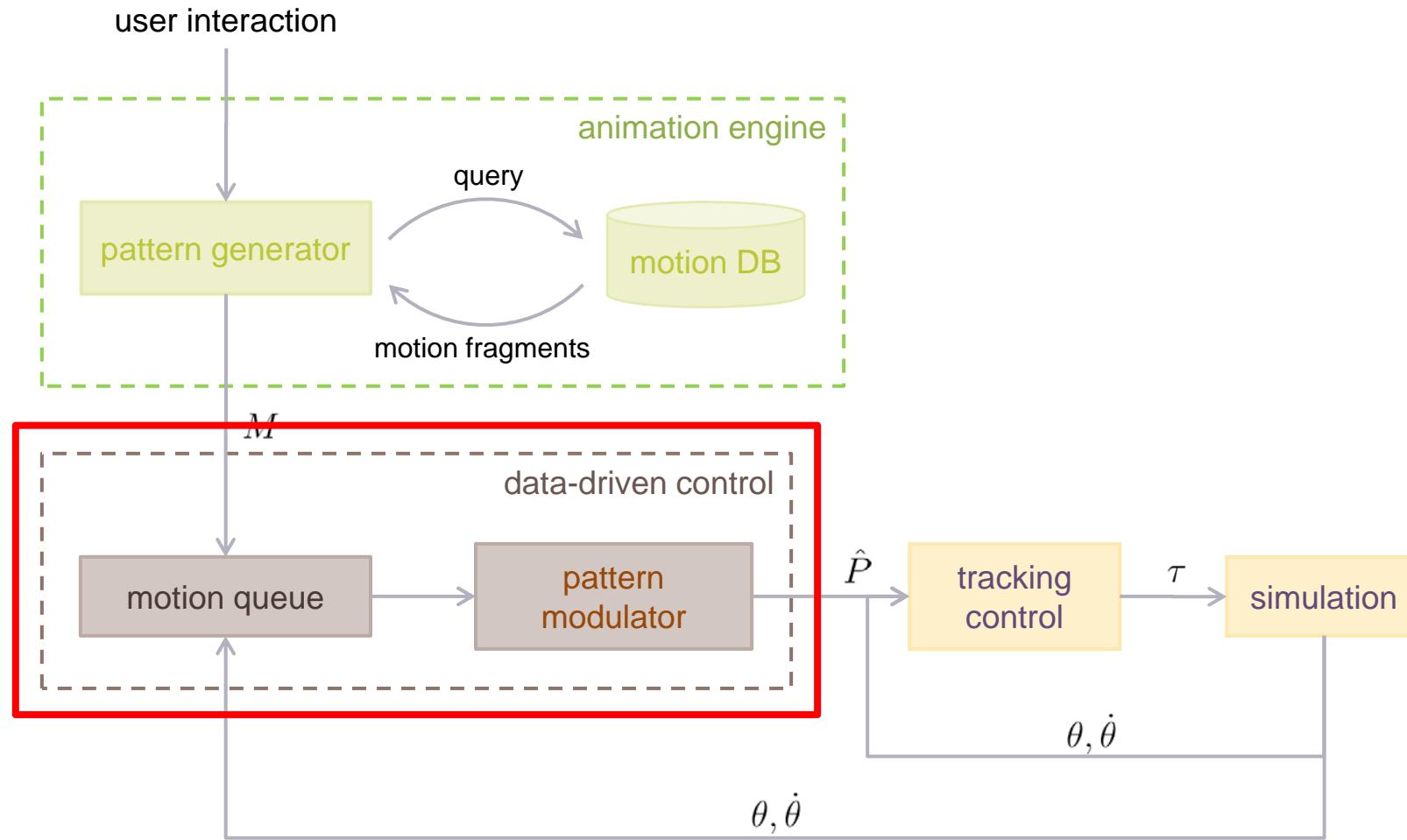
- ▶ Compute joint torques using inverse dynamics
- ▶ Penalty method for ground reaction force
- ▶ We used Virtual Physics to solve inverse dynamics and forward dynamics simulation



Tracking Result

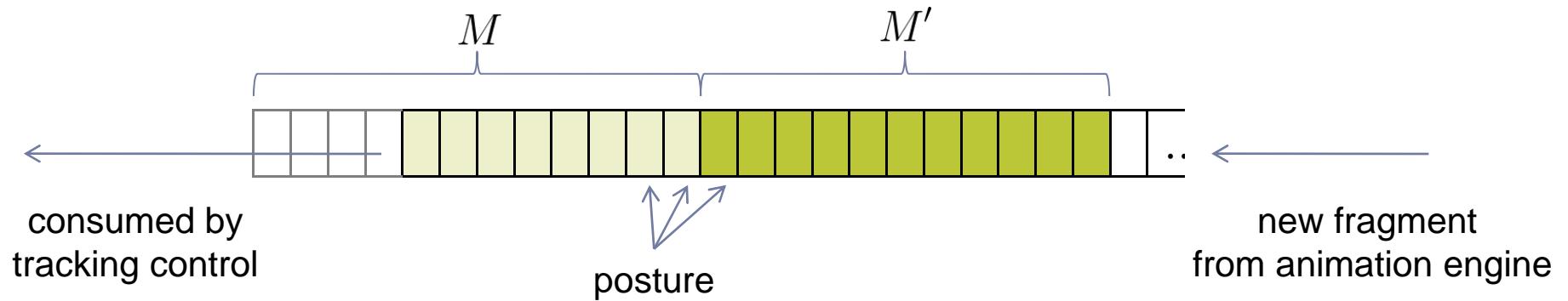


Data-Driven Control



Synchronization

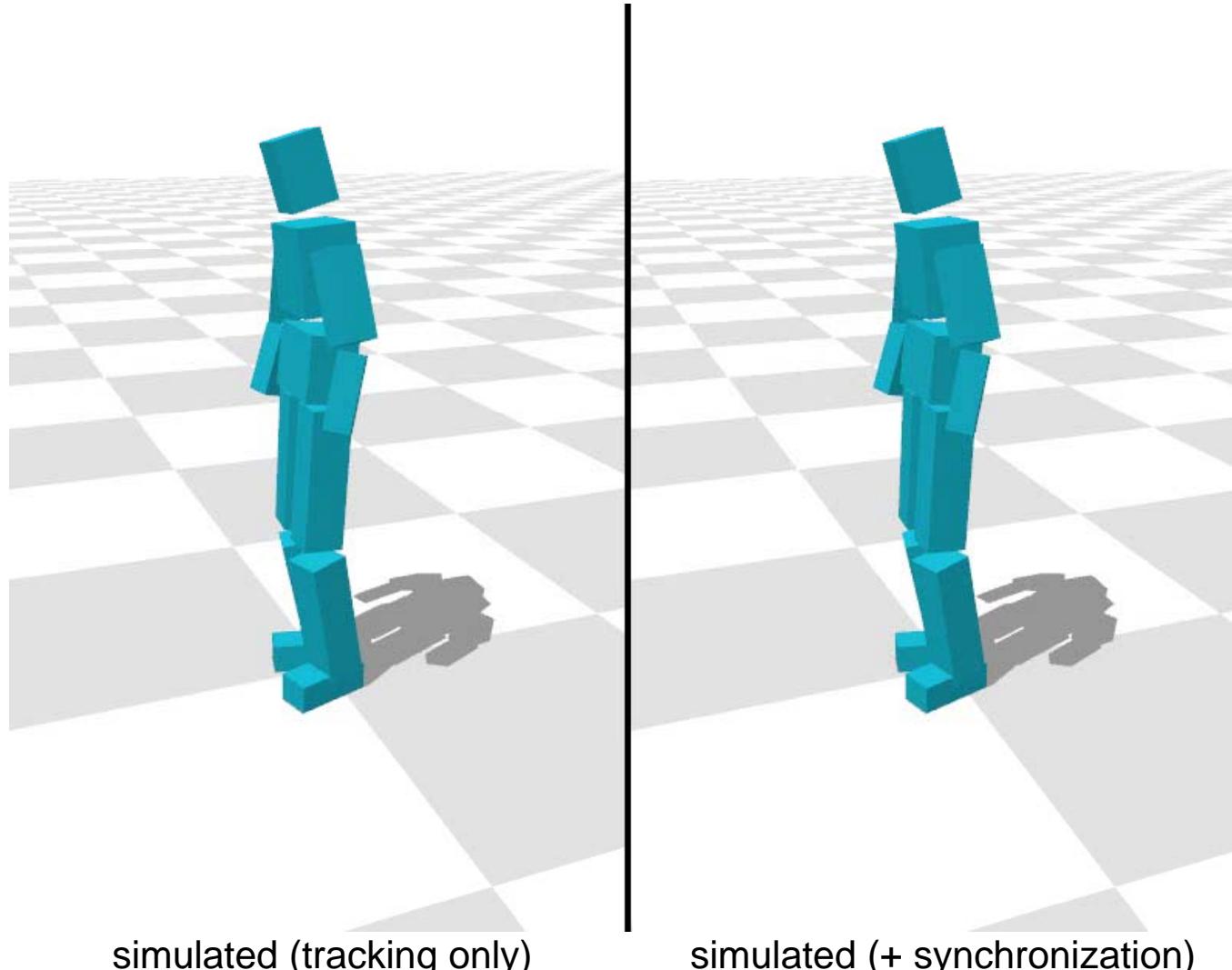
- ▶ Motion queue



- ▶ Synchronize reference motion & simulated biped at contact changes by inserting or deleting postures



Synchronization Result



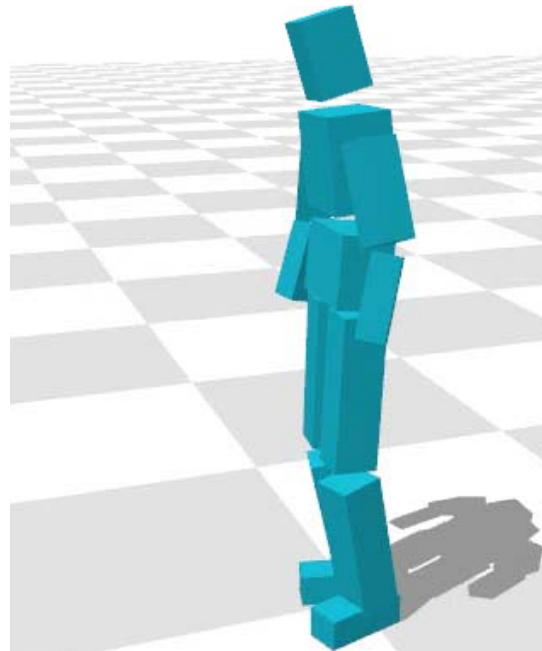
Balancing

- ▶ Compute continuous stream of target poses
 - ▶ based on current reference frame & simulated biped

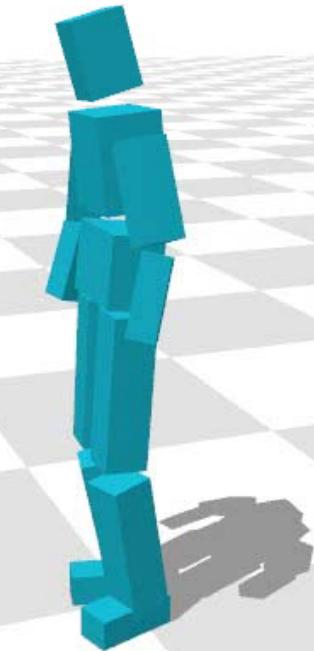
- ▶ Feedback on Stance Hip
- ▶ Feedback on Swing Hip and Stance Ankle



Balancing Result



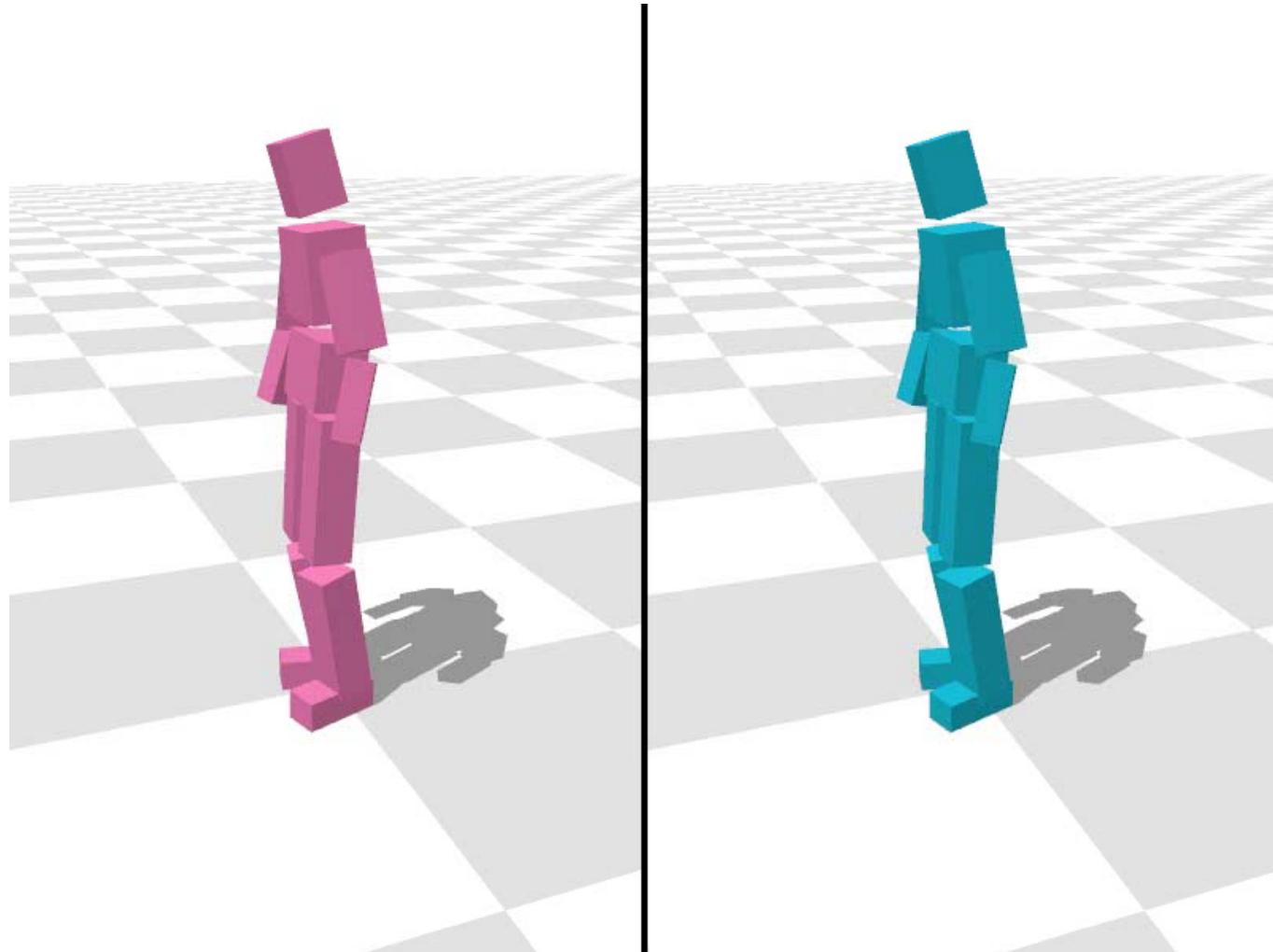
simulated (+ synchronization)



simulated (+ synchronization
+ balancing)



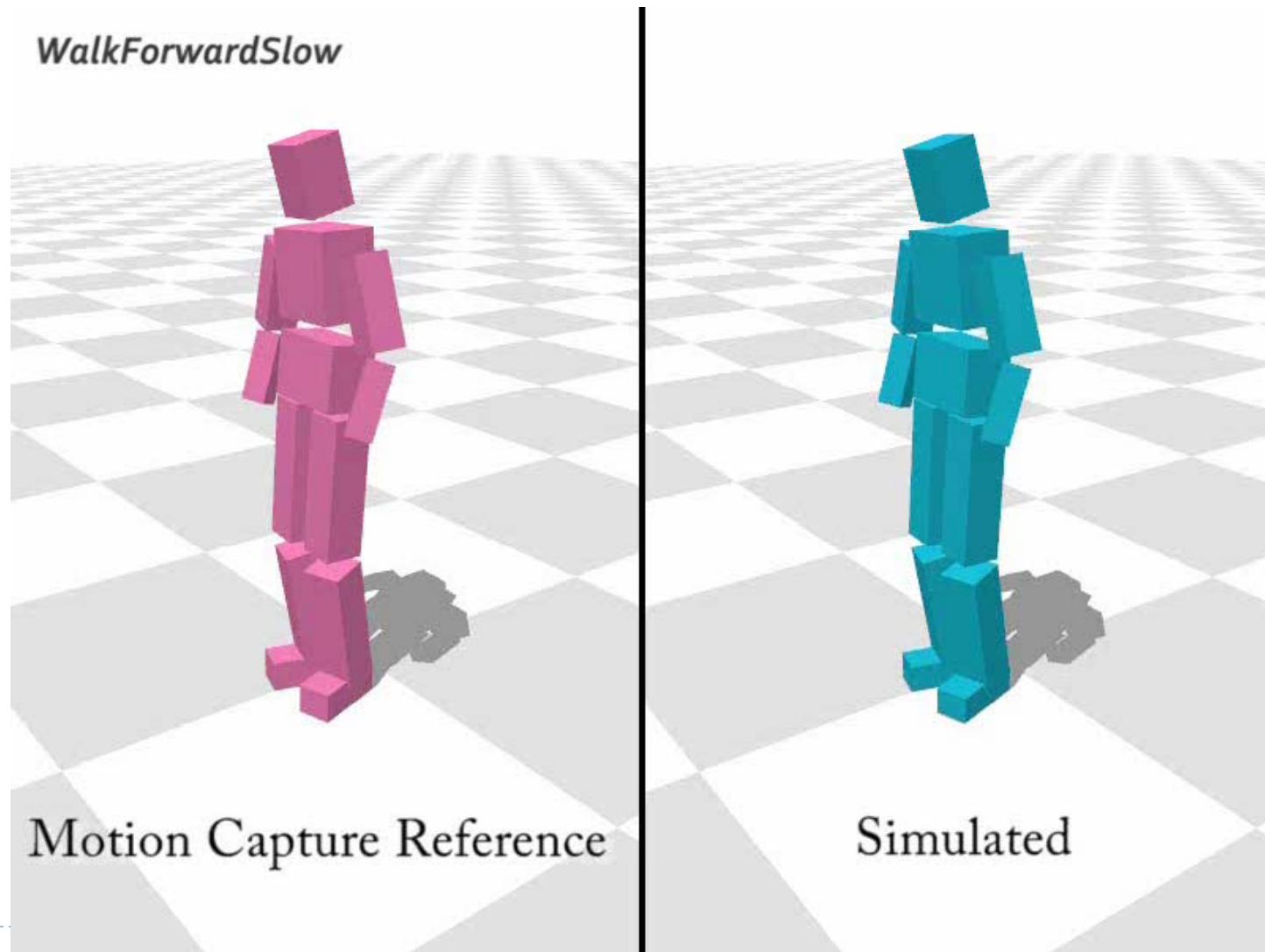
Balancing Result



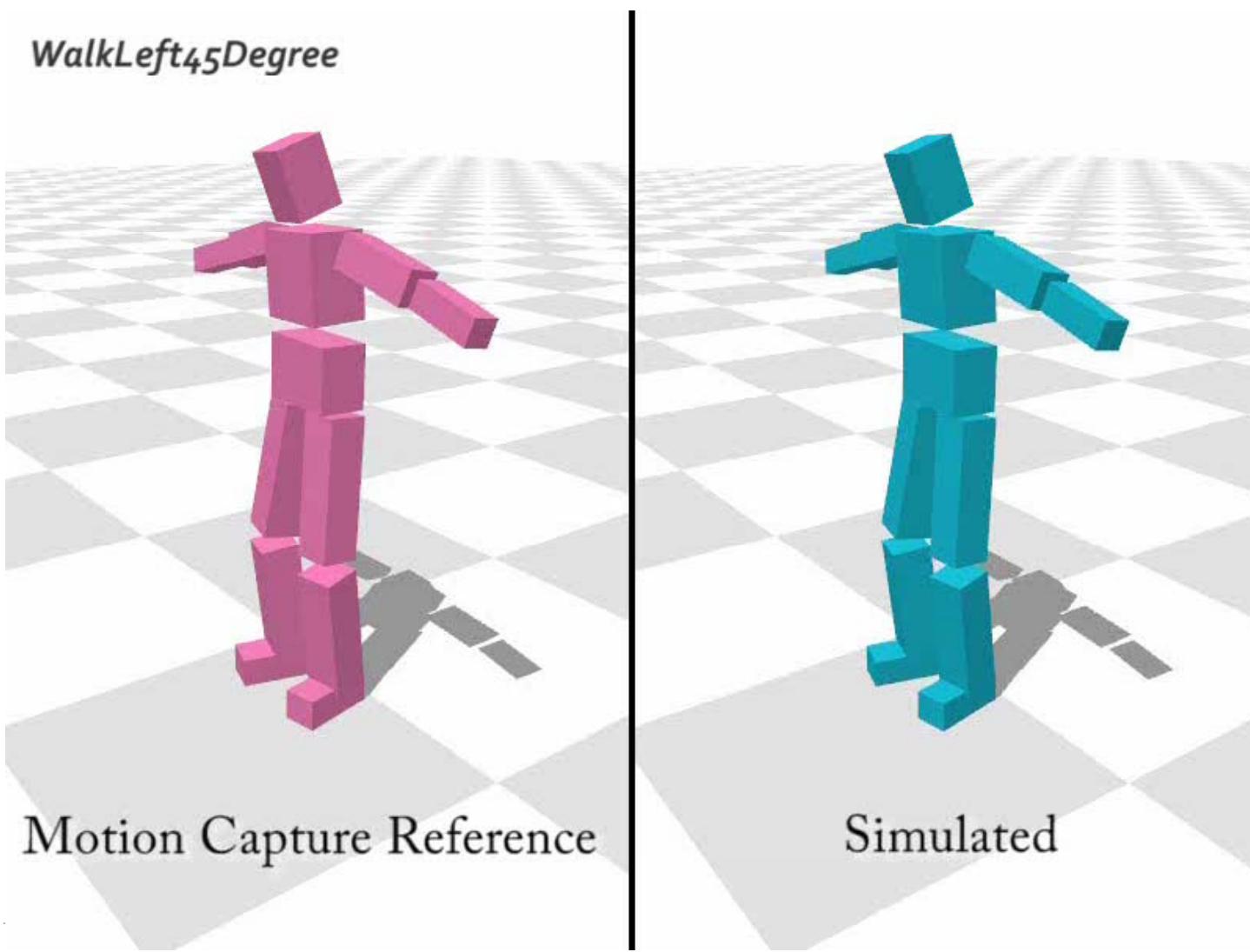
► motion capture reference

simulated (+ synchronization
+ balancing)

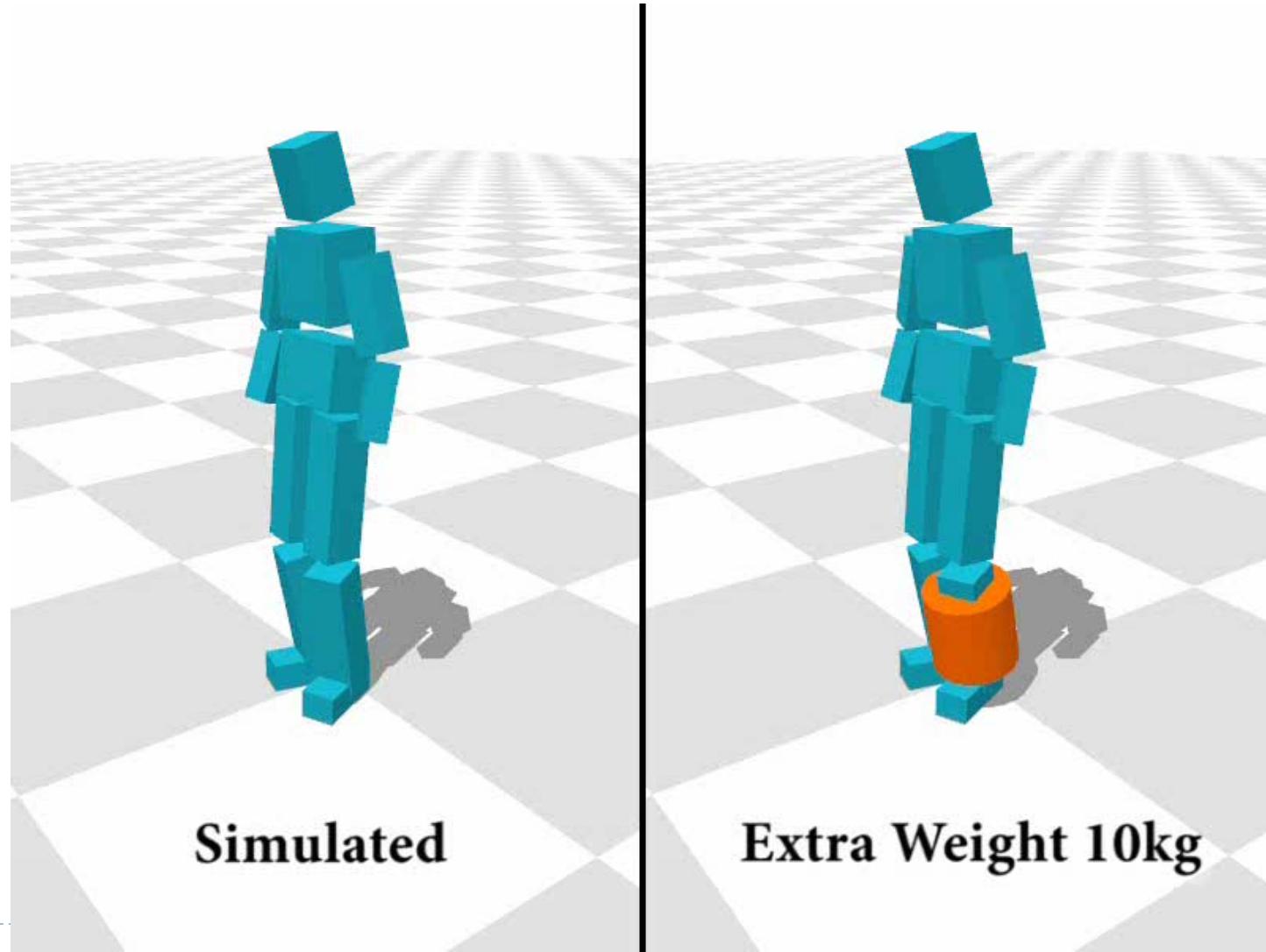
Result - Walking



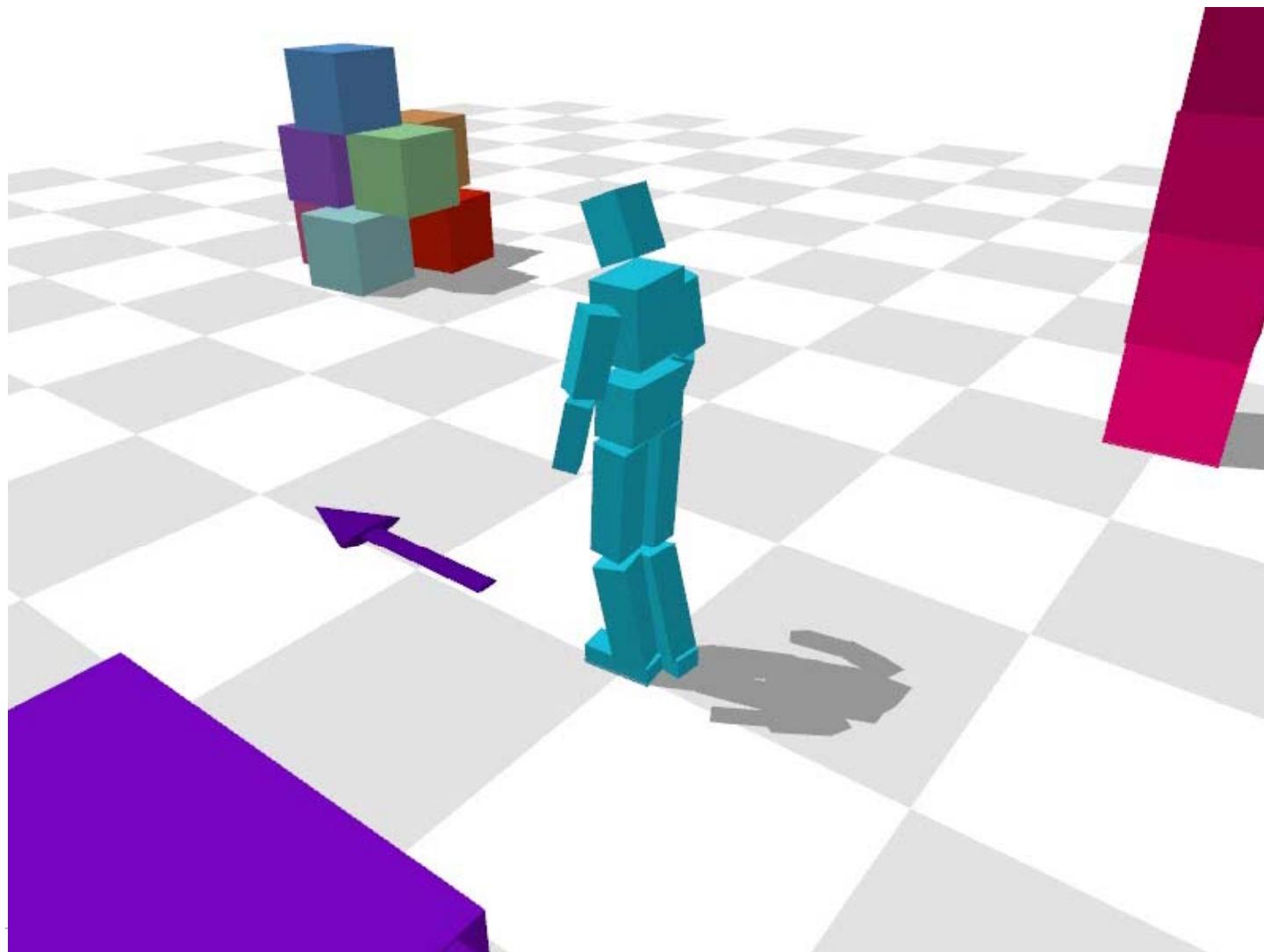
Result – Turning & Spinning



Result – Robustness Test



Result – Interactive Control



Interactive Collision Detection for Large-Scale Deformable Objects

Sung-Eui Yoon
Scalable Graphics Lab.
KAIST

<http://sglab.kaist.ac.kr/~sungeui/>

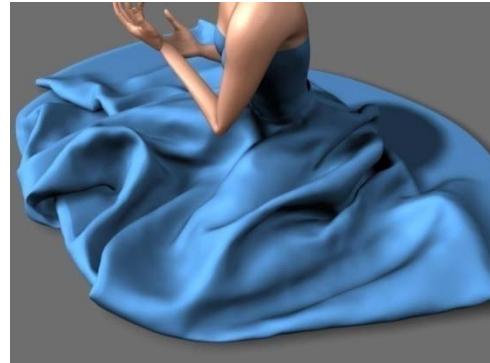


Collision Detection

- Collision detection is used in various fields
 - Game, movie, scientific simulation and robotics



<Figure from PIXAR>



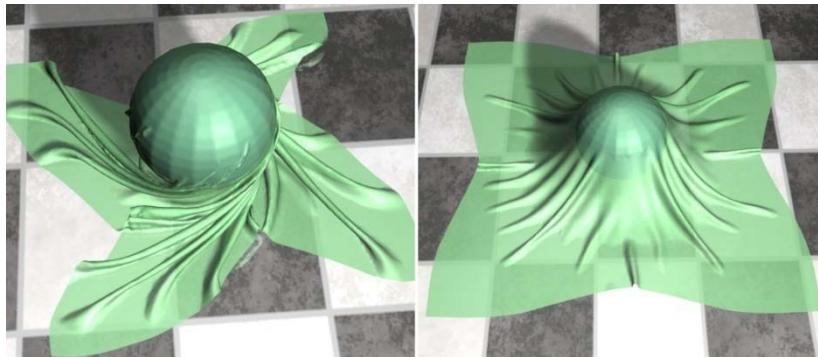
<Figure from C. Lauterbach >



<Figure from AION >

Goals

- Achieve interactive performance for exact collision detection between large-scale deformable models
 - E.g., deforming models consisting of tens or hundreds of thousand triangles



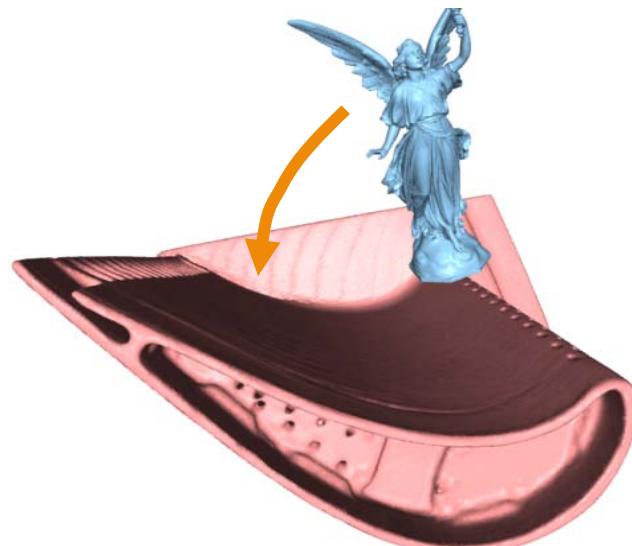
<Cloth-ball, 94K triangles>



<Breaking dragon, 252K triangles>

Large-Scale Applications

- Entertainment (games/movies)
- E-heritage applications
- Virtual reality, etc



Overview

- HPCCD: Hybrid parallel continuous collision detection
- FASTCD: Fracturing-Aware Stable Collision Detection
- HCCMeshes: Hierarchical-Culling oriented Compact Meshes

Overview

- HPCCD: Hybrid parallel continuous collision detection
- FASTCD: Fracturing-Aware Stable Collision Detection
- HCCMeshes: Hierarchical-Culling oriented Compact Meshes

Discrete vs. Continuous

- Discrete collision detection (DCD)
 - Detect collisions at each frame
 - Fast, but can miss collisions

Miss collisions



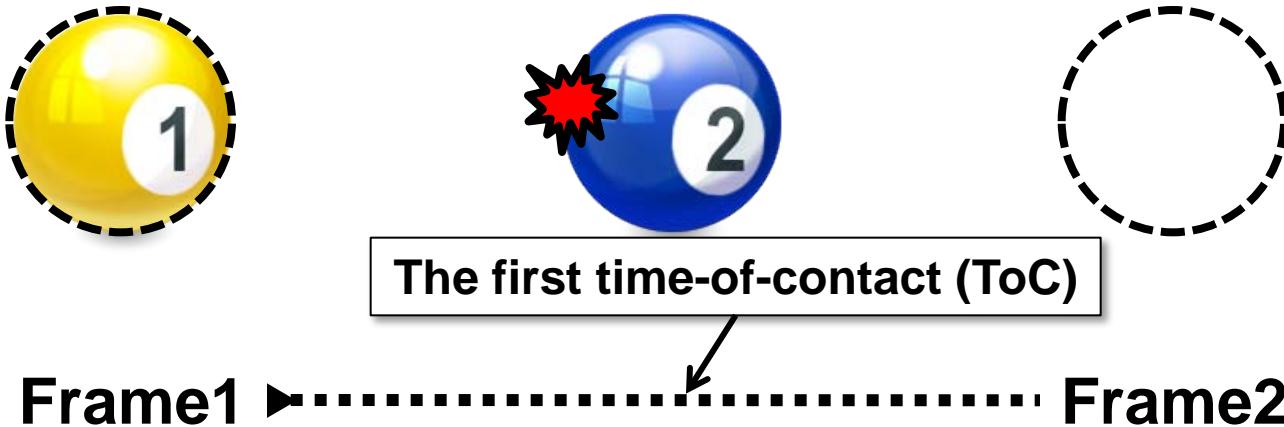
Frame1



Frame2

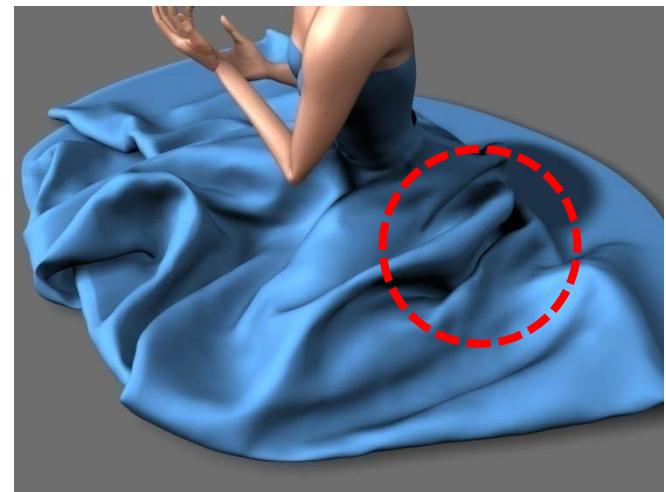
Discrete vs. Continuous

- Discrete collision detection (DCD)
- Continuous collision detection (CCD)
 - Identify the first time-of-contact (ToC)
 - Accurate, but requires a **long computation time**
 - Not widely used in interactive applications



Inter- and Self-Collisions

- Inter-collisions
 - Collisions between two objects
- Self-collisions
 - Collisions between two regions of a deformable object
 - Takes a **long computation time** to detect



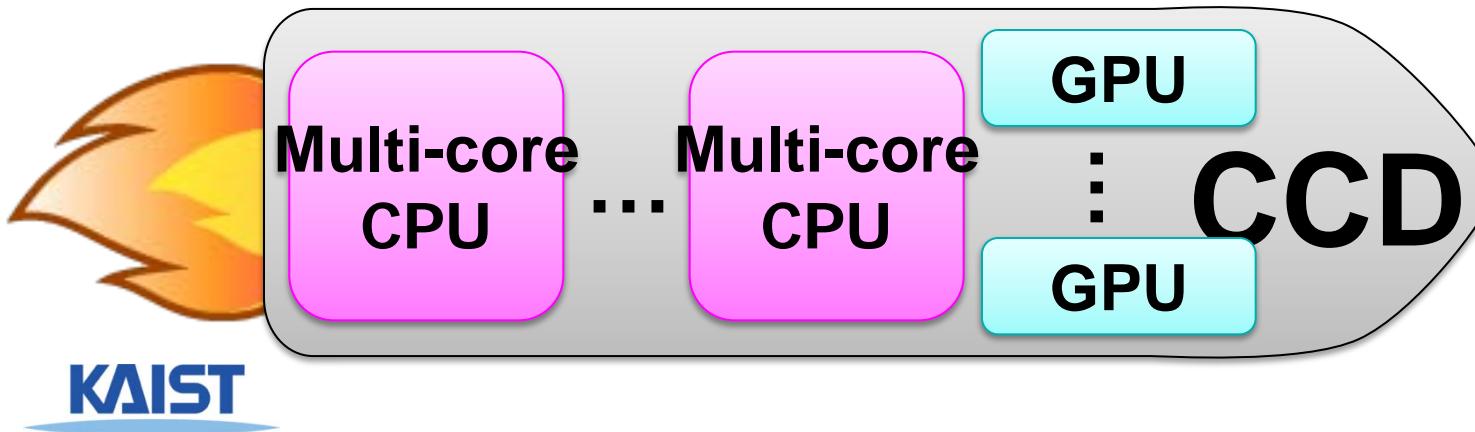
From Govindaraju's paper

Parallel Computing Trends

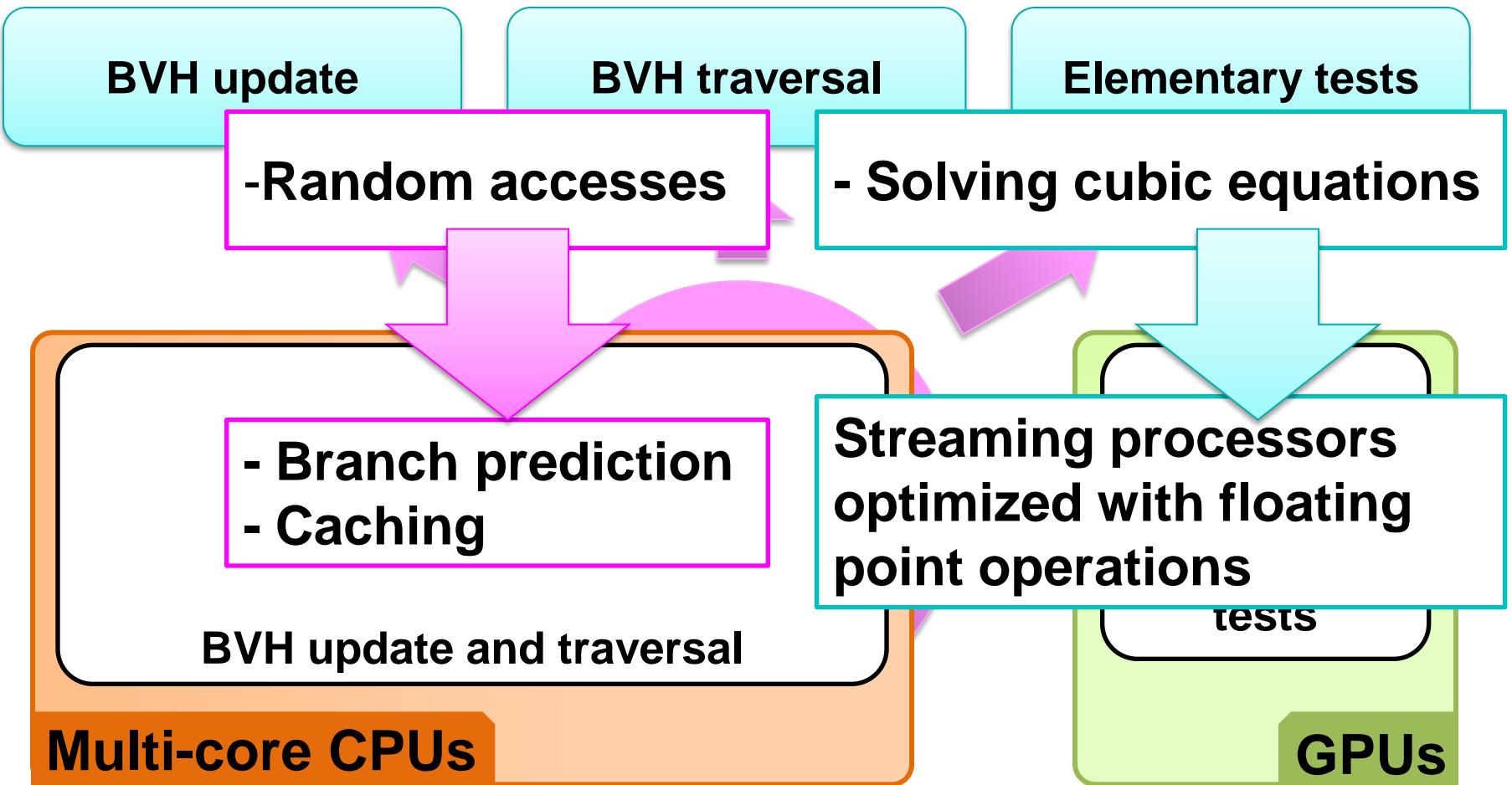
- Many core architectures
 - Multi-core CPU architectures
 - GPU architectures
- Heterogeneous architectures
 - Intel's Larabee and AMD's Fusion
- Designing parallel algorithms is important to utilize these parallel architectures

Main Contributions

- A novel, hybrid parallel CCD method
 - Utilize both multi-core CPUs and GPUs
 - No locking in the main loop of CD
 - GPU-based exact CD between two triangles
- High scalability & interactive performance
 - Kim et al. PG 09
 - Received a distinguished paper award



Task Distribution



Testing Environment

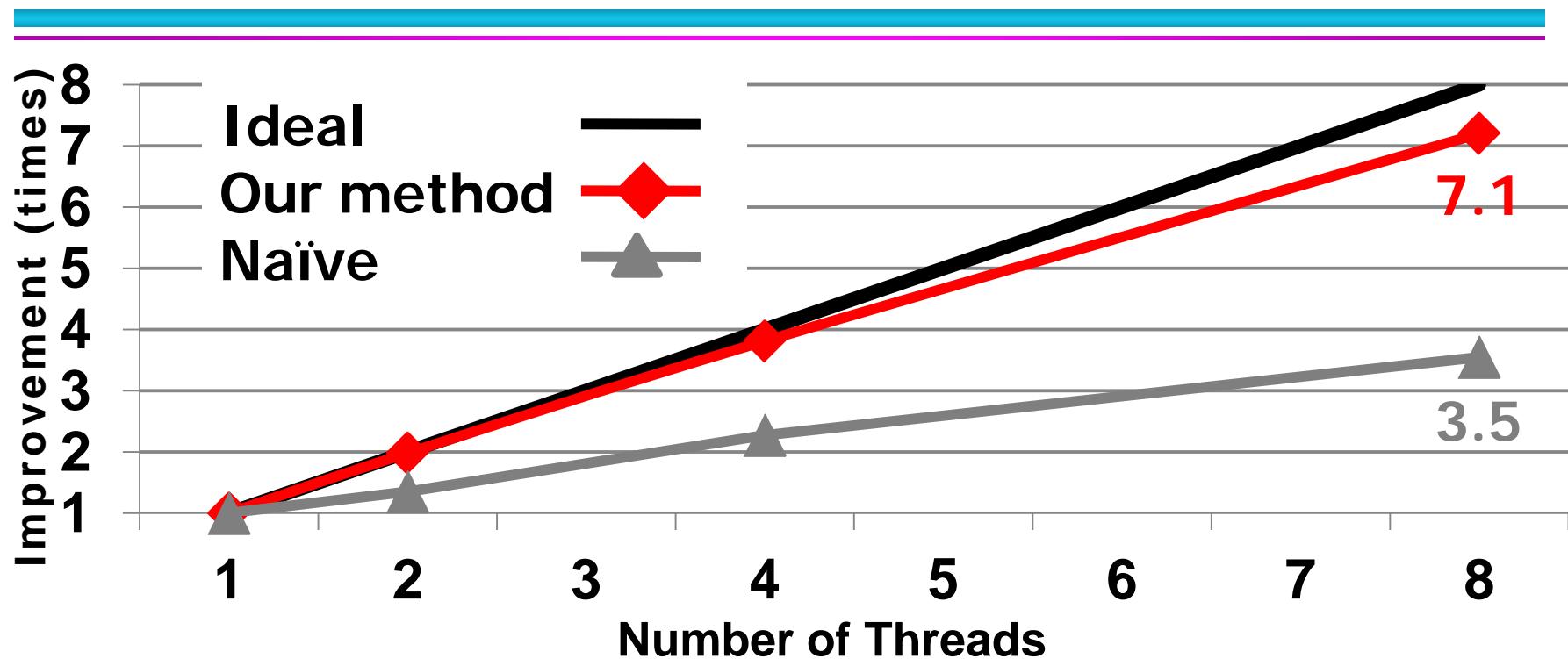
- Machine
 - One quad-core CPU (Intel i7 CPU, 3.2 GHz)
 - Two GPUs (Nvidia Geforce GTX285)
- Run eight CPU threads by using Intel's hyper threading technology



Results

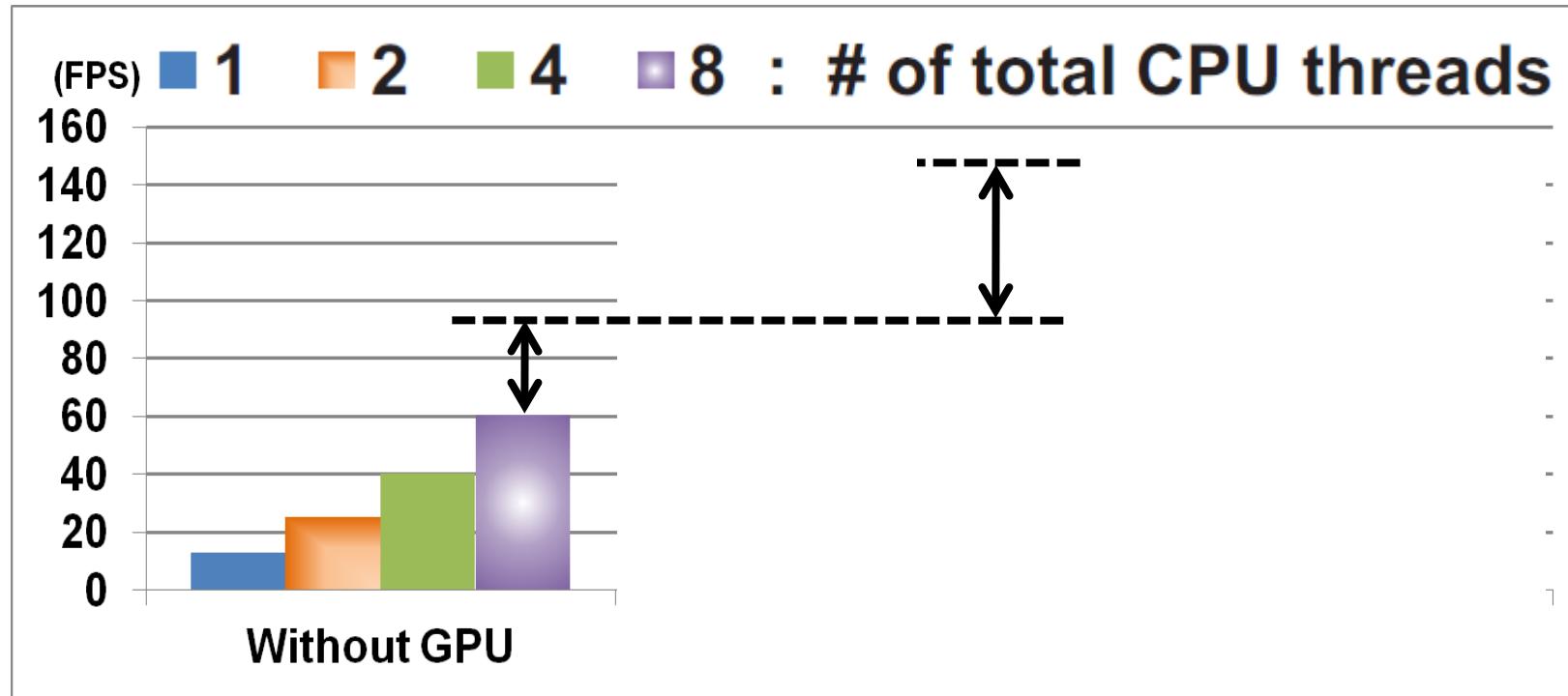


Results of Our CPU-based Parallel CCD



- Remove locking in the main loop of CD
- Employ efficient dynamic load-balancing based on inter-CD task units

Results of HPCCD



- As the number of GPUs is increased, we get higher performances

Limitation

- Low scalability for small rigid models

Summary

- A novel, hybrid parallel algorithm
 - Utilize both multi-core CPUs and GPUs
- High scalability

The implementation code will be available as
OpenCCD library
(<http://sglab.kaist.ac.kr/OpenCCD>)

- Show 19-140 FPS for various deformable models consisting of tens or hundreds of thousand triangles

Overview

- HPCCD: Hybrid parallel continuous collision detection
- FASTCD: Fracturing-Aware Stable Collision Detection
- HCCMeshes: Hierarchical-Culling oriented Compact Meshes

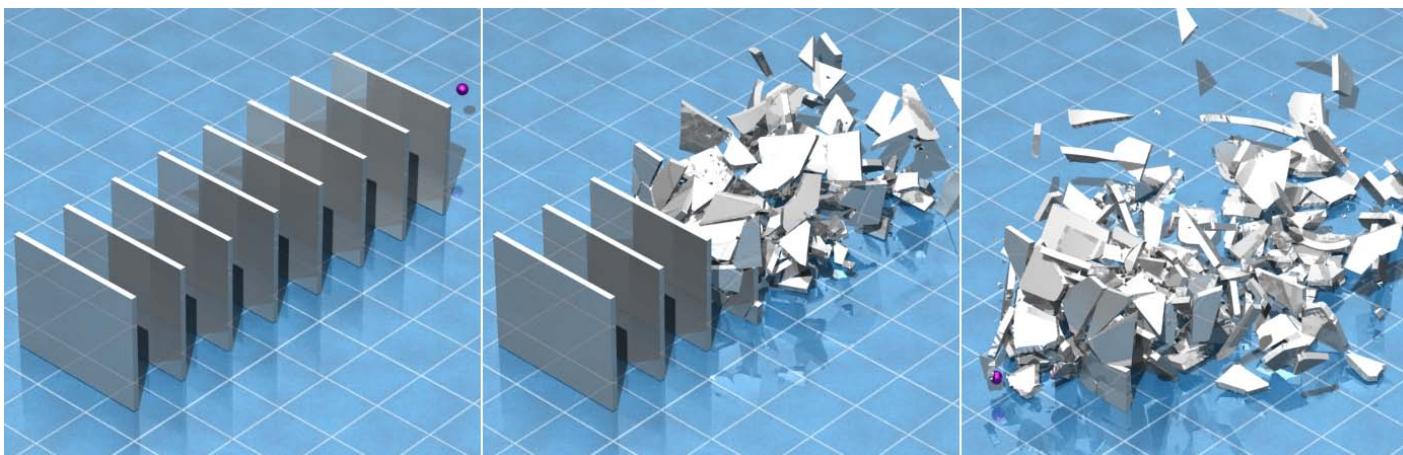
Fracturing in Simulations

- More widely used in various applications to create more realistic interactions
- Presents significant challenges to CD
- Self-CD can take more expensive time with fracturing models
 - Fractured segments can be located in a near proximity

Examples (Video)



252K



142K

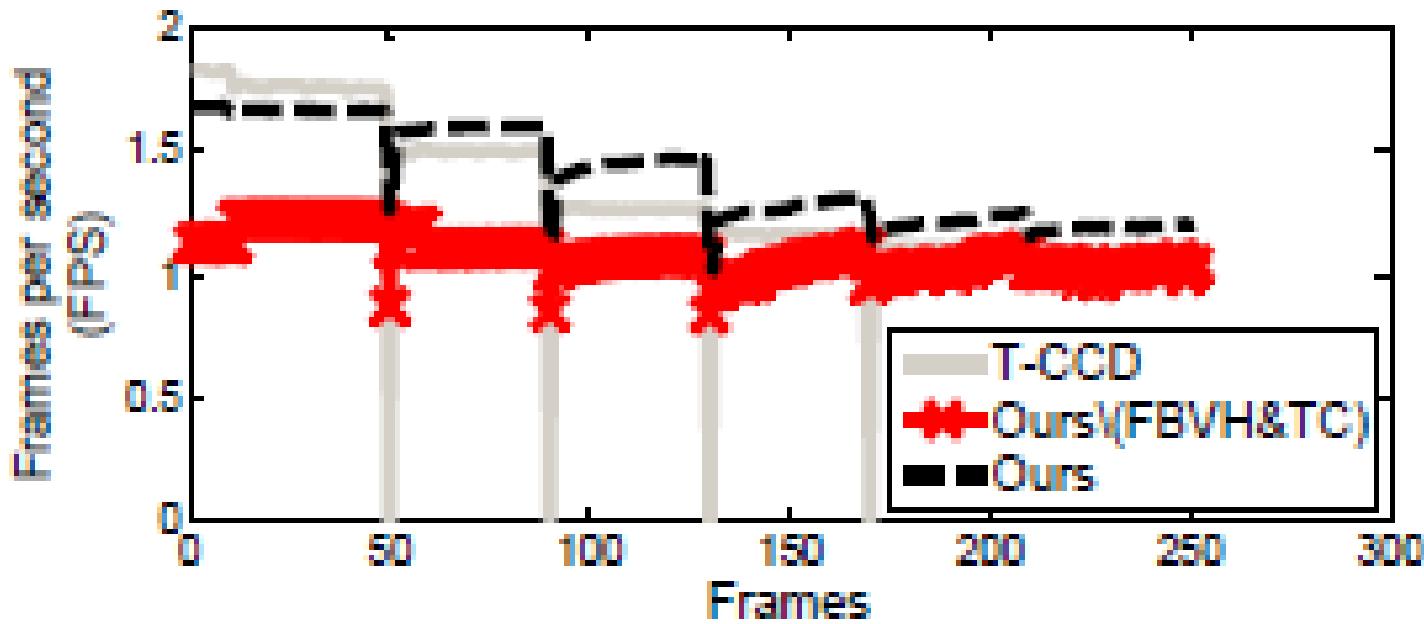
Research Challenges with Fracturing Models

- Most prior works assume fixed topologies
 - Can take prohibitive times when models change their topologies
- Self-CD can take more expensive time with fracturing models
 - Fractured segments can be located in a near proximity

Our Approach

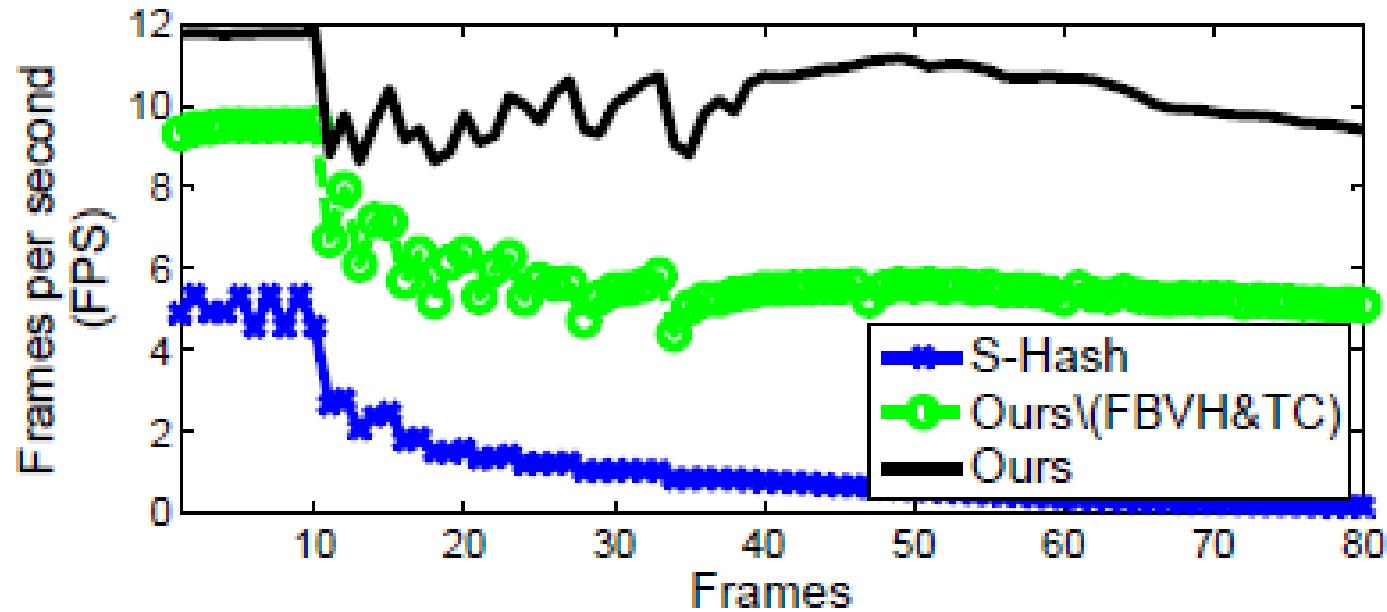
- Fracturing-aware stable CD
 - Incrementally update meshes and BVHs by utilizing topological changes of models
 - Design a simple self-CD culling method without much pre-computations

Results with the Exploding Dragon Model



T-CCD: Tang et al. [2008]

Results with the Breaking-Wall Model



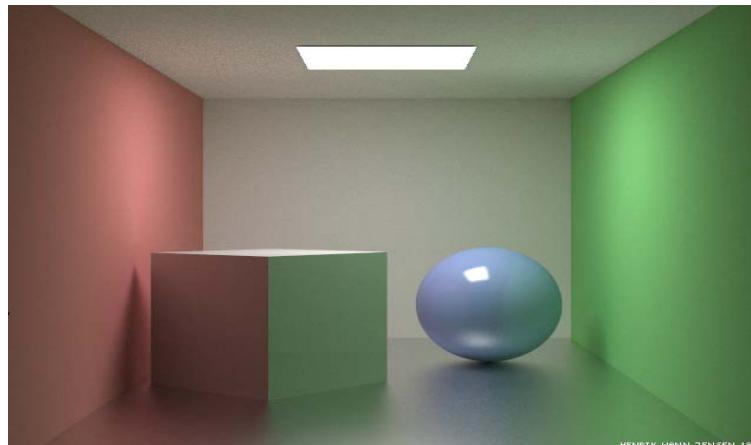
S-Hash: Optimized spatial hashing (Teschner et al. 03]

Overview

- HPCCD: Hybrid parallel continuous collision detection
- FASTCD: Fracturing-Aware Stable Collision Detection
- HCCMeshes: Hierarchical-Culling oriented Compact Meshes

Hierarchical Culling and Traversal

- Widely used in many search based algorithms
 - Various proximity queries
 - Ray tracing



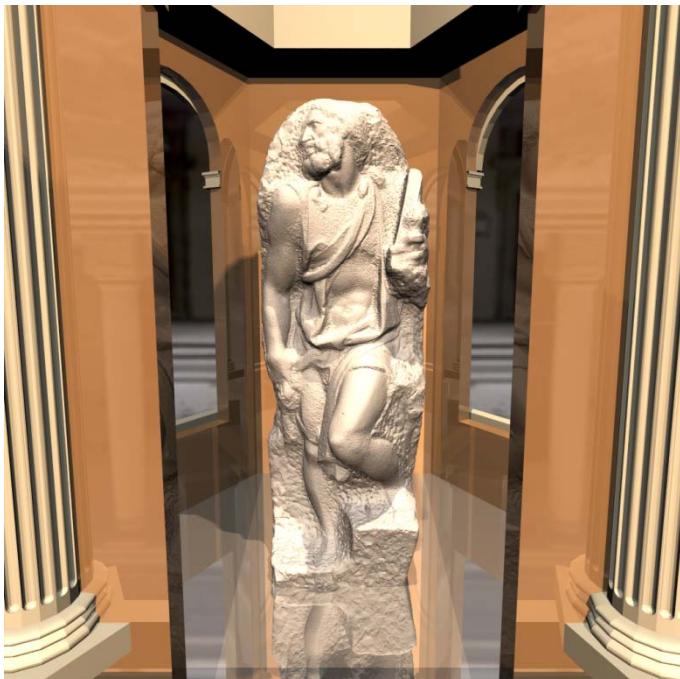
Path tracing



Photon mapping

[Images are from Jensen's homepage]

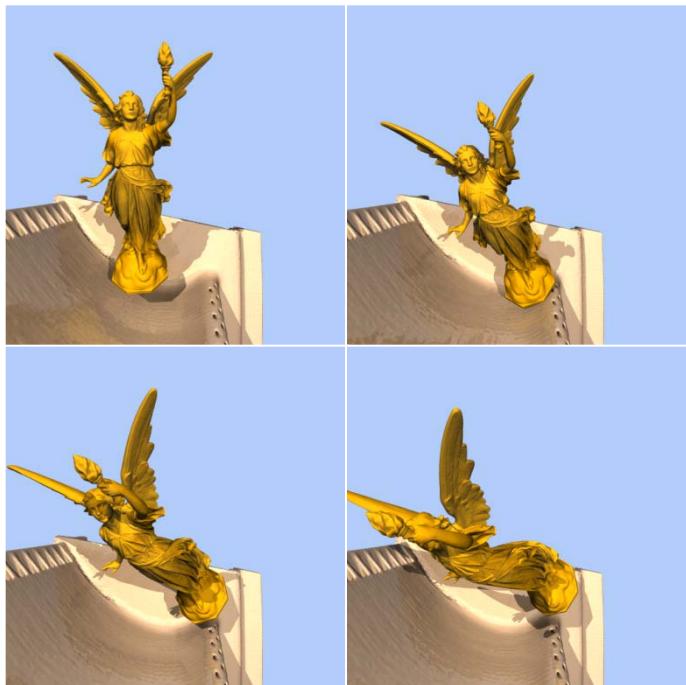
Ray Tracing – Massive Model



St. Matthew

- 128M triangles
- 256M BVH nodes
- 14GB data
- Size of memory < 4GB
- Rendering time : 40 min ↑

Collision Detection– Massive Model



- 30M triangles
- 60M BVH nodes
- 3.2GB data

Lucy & CAD turbine

Random-Accessible Compressed Data

- Compression methods of meshes and hierarchies
 - Reduce the memory requirements
 - Supports random accesses on meshes and hierarchies
 - Can be useful to many different applications

[Kim et al. Eurographics 2010 (to appear);

→ Kim et al., TVCG 09;

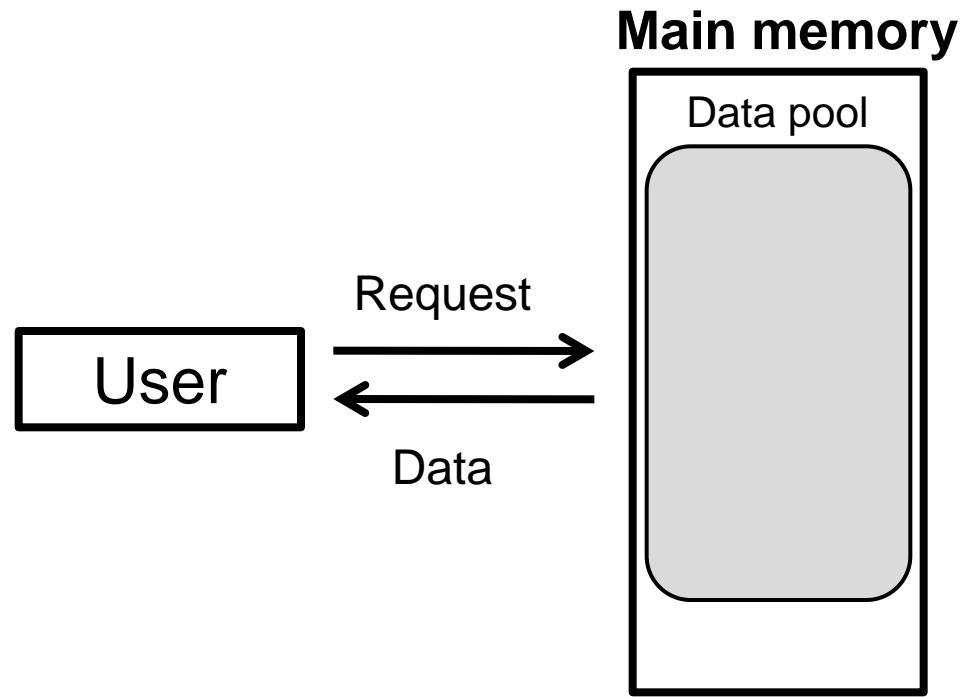
Yoon and Lindstrom, VIS 07]

→ 1st rank at ACM SIGGRAPH Student Competition

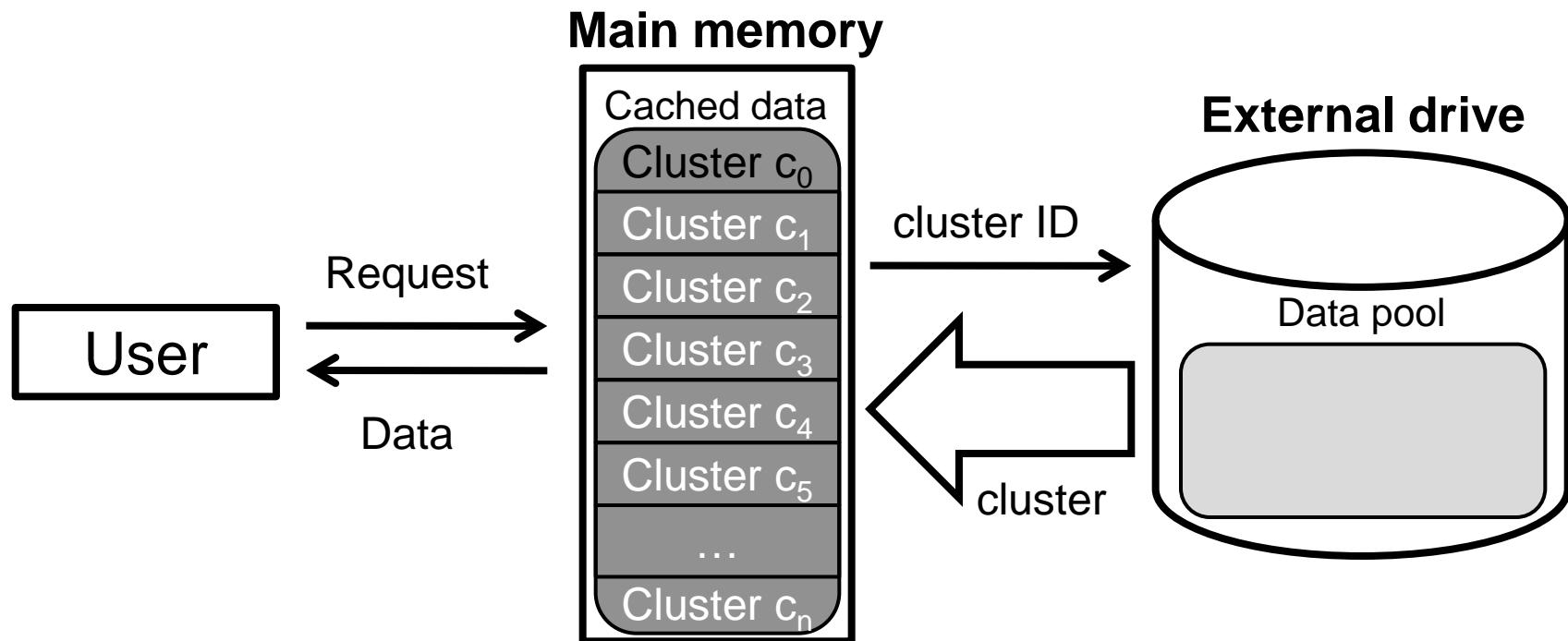
Hierarchical-Culling oriented Compact Meshes (HCCMeshes)

- Consists of two parts:
 - i-HCCMeshes (in-core representation)
 - o-HCCMeshes (out-of-core representation)

Data Access Framework

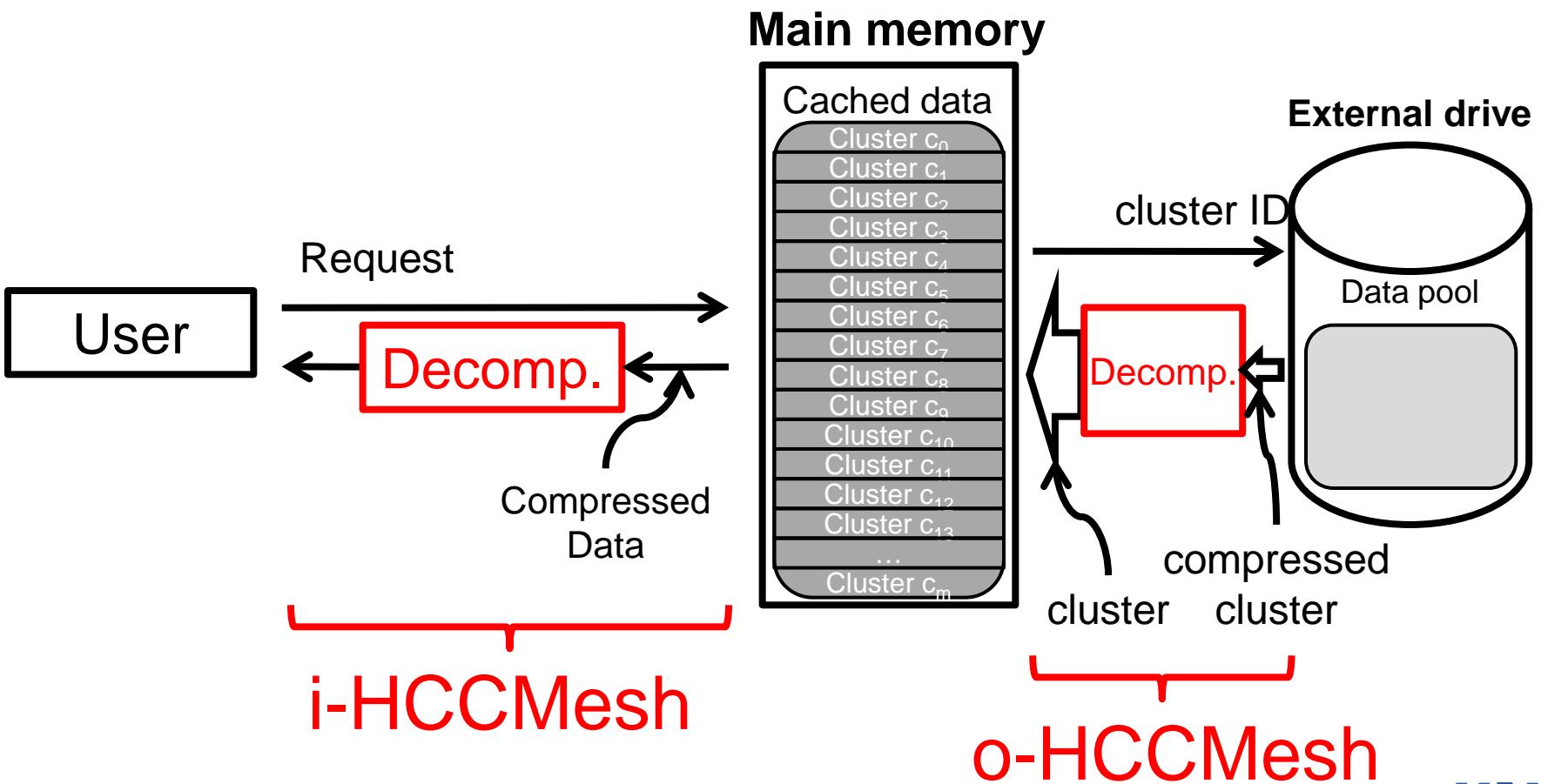


Data Access Framework - Out-of-Core Technique



HCCMeshes

Support hierarchical random access!



Main Benefits

- Use a lower memory space and working set size
 - o-HCCMeshes have 20:1 compression ratios
 - i-HCCMeshes have 6:1 compression ratios
- Improve runtime performance

Applications

- Whitted-style ray tracing
- LOD-based ray tracing
- Collision detection
- Photon mapping
- Non-photorealistic rendering

Results



St. Matthew

128 Million triangles
8 GB for the BVH

Single thread

7 lights, reflection,
and 3x3 stratified
sampling

Conclusions

- Discussed three different techniques for interactive CD among large-scale deforming models
 - HPCCD: Hybrid parallel continuous collision detection
 - FASTCD: Fracturing-Aware Stable Collision Detection
 - HCCMeshes: Hierarchical-Culling oriented Compact Meshes

Acknowledgements

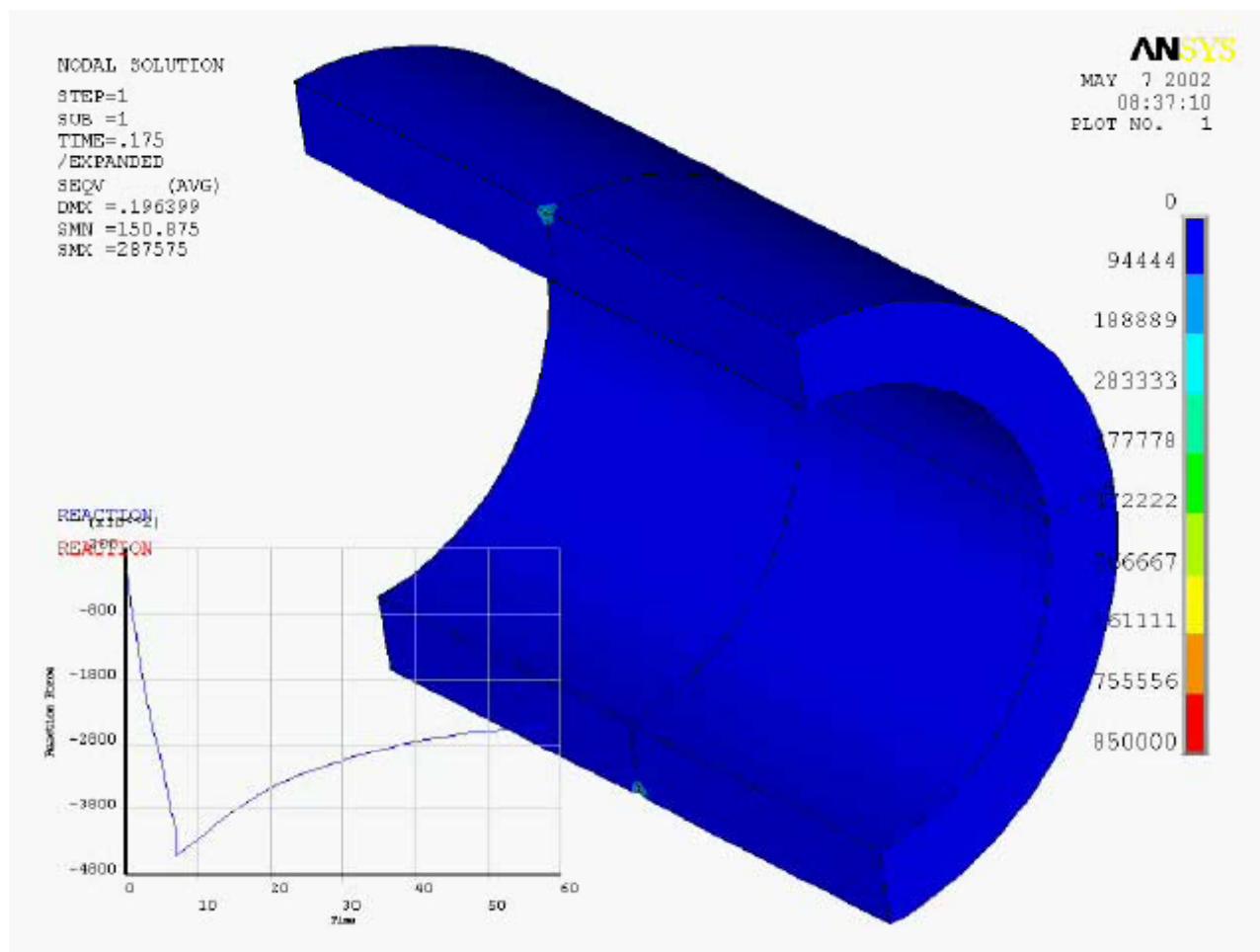
- Research collaborators
 - DukSu Kim, JaePil Heo, TaeJoon Kim, Pio Claudio, BooChang Moon, YongYoung Byun, SeungYong Lee, YongJin Kim, JaeHyuk Heo, John Kim
- Funding sources
 - Ministry of Knowledge Economy
 - Microsoft Research Asia
 - KAIST seed grant
 - Samsung
 - Korea Research Foundation

Real-Time Simulation of Flexible Bodies



**CG Lab.
Kwangwoon University**

Deformation in Mechanical Engineering



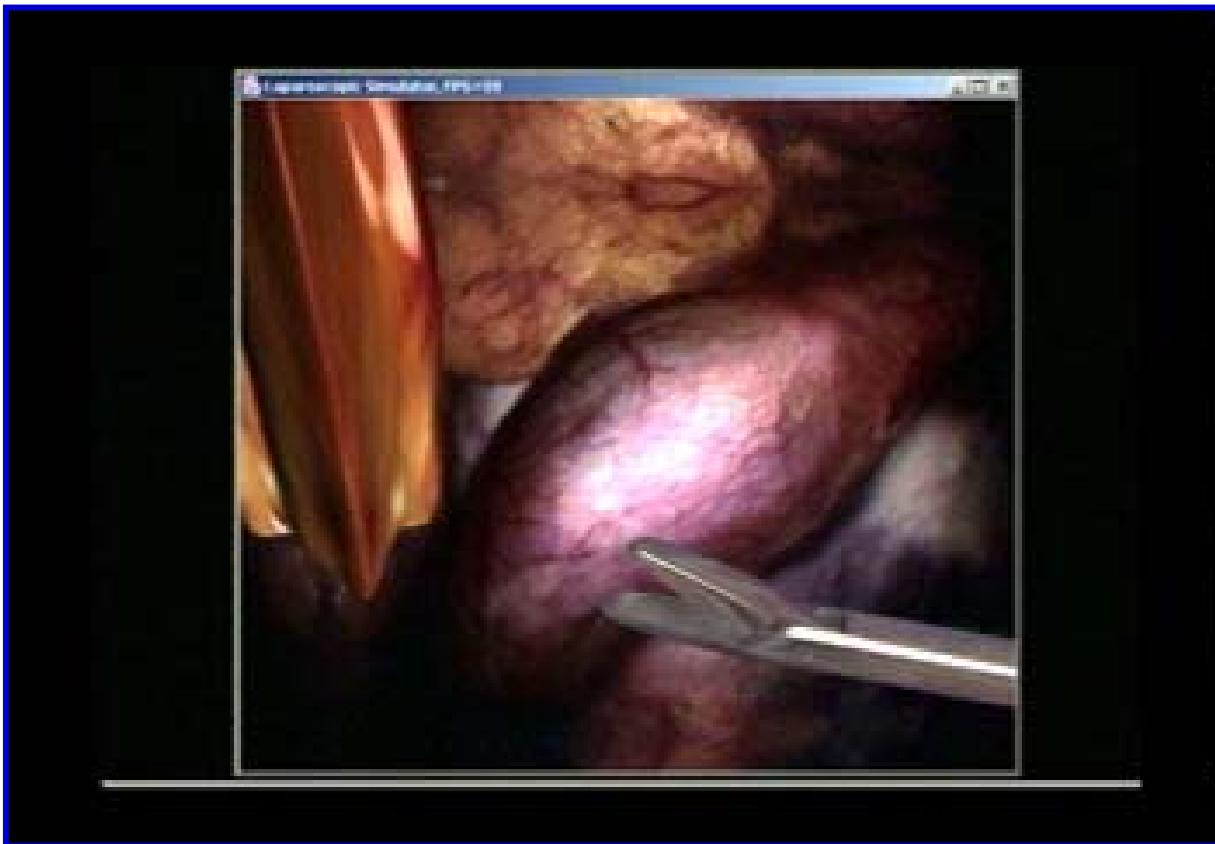
Character Skinning in CG



Hair Simulation in CG

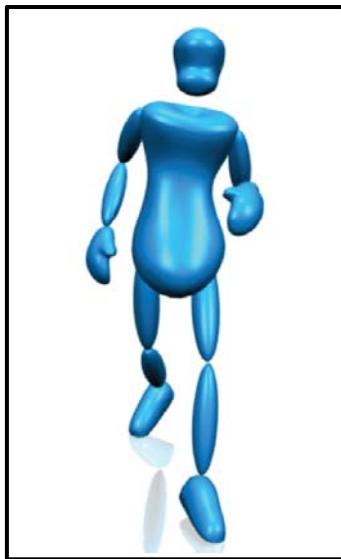


Surgery Simulation

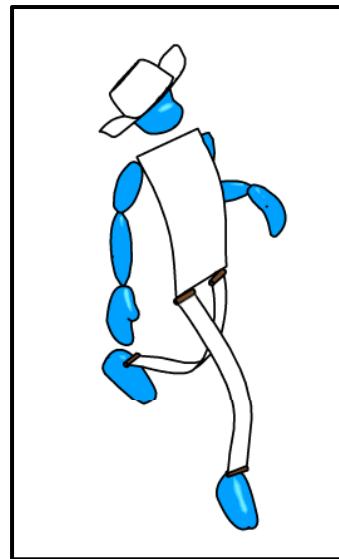


Overview

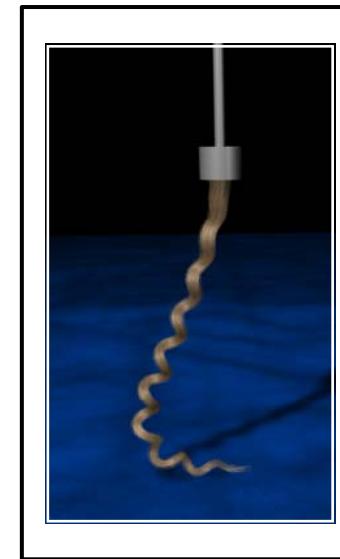
- ☐ Elastodynamic deformation of solids, shells, and rods



3D Solids



3D Thin Shells



3D Thin Rods

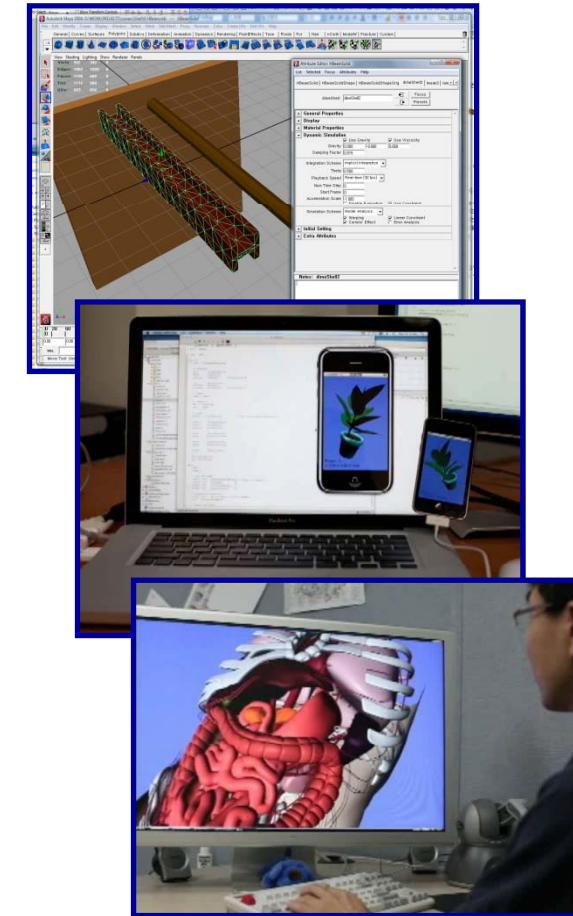
Overview

□ Authoring in the Maya platform

- Geometry
- Material constants
- Precomputation

----- Exporting -----

- Runtime simulation



Future Research Directions

- Extension of elastodynamic deformation



Meshing



Crack/Fracture



Viscosity/Plasticity

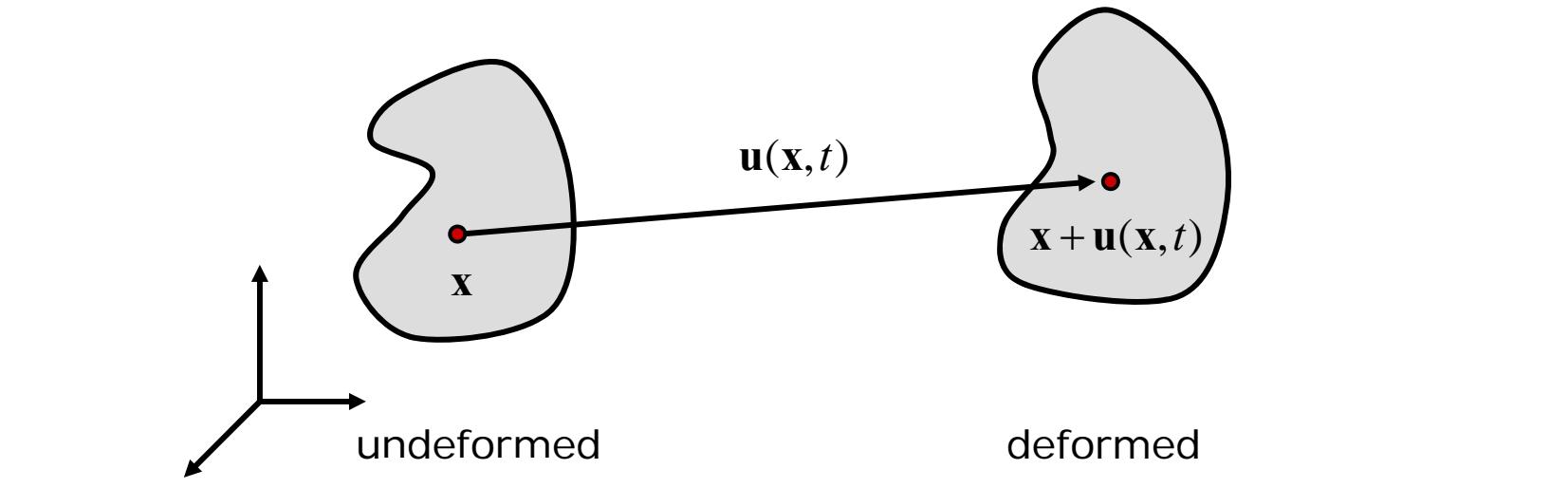
Ongoing, Scheduled Work

Dynamic Deformation

□ Governing equations: Euler-Lagrange equations

$$\frac{d}{dt} \left(\frac{\partial T(\mathbf{u})}{\partial \dot{\mathbf{u}}} \right) + \frac{\partial U(\mathbf{u})}{\partial \mathbf{u}} = \mathbf{f}_{ext}$$

kinetic energy ↓ elastic potential energy
 ← external force



Finite Element Discretization

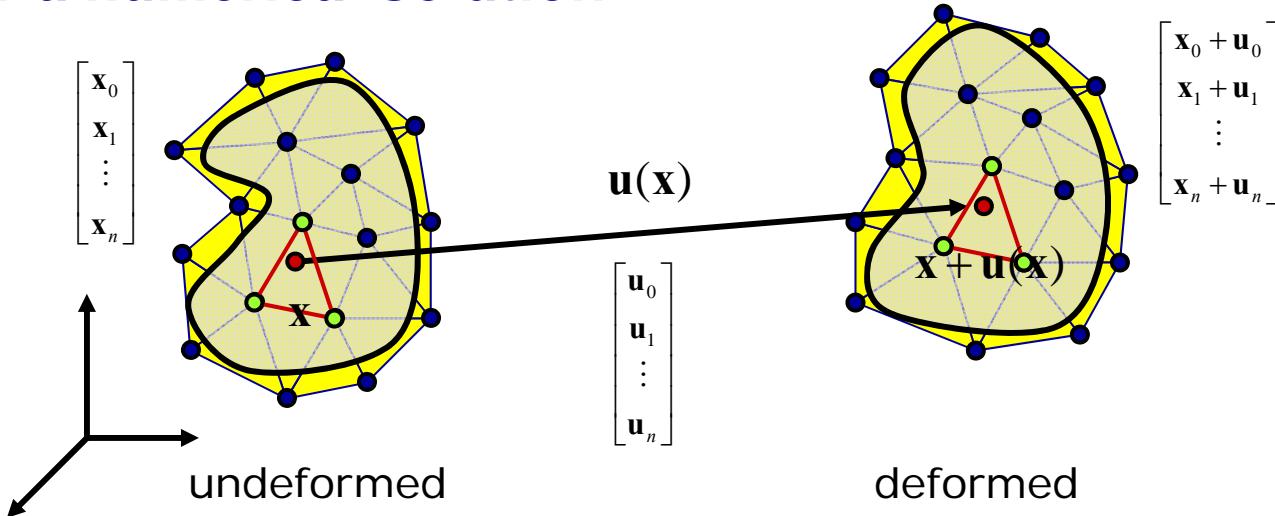
□ Governing equations: Euler-Lagrange equations

$$\frac{d}{dt} \left(\frac{\partial T(\mathbf{u})}{\partial \dot{\mathbf{u}}} \right) + \frac{\partial U(\mathbf{u})}{\partial \mathbf{u}} = \mathbf{f}_{ext}$$

kinetic energy elastic potential energy

external force

For a numerical solution



Real-Time Deformation of 3D Solids

□ Elastodynamic equation for FEM

$3n \times 3n$ matrix, $3n \times 1$ vector

$$\underline{\mathbf{M} \ddot{\mathbf{u}} + \mathbf{C} \dot{\mathbf{u}} + \mathbf{K}(\mathbf{u}) = \mathbf{F}}$$

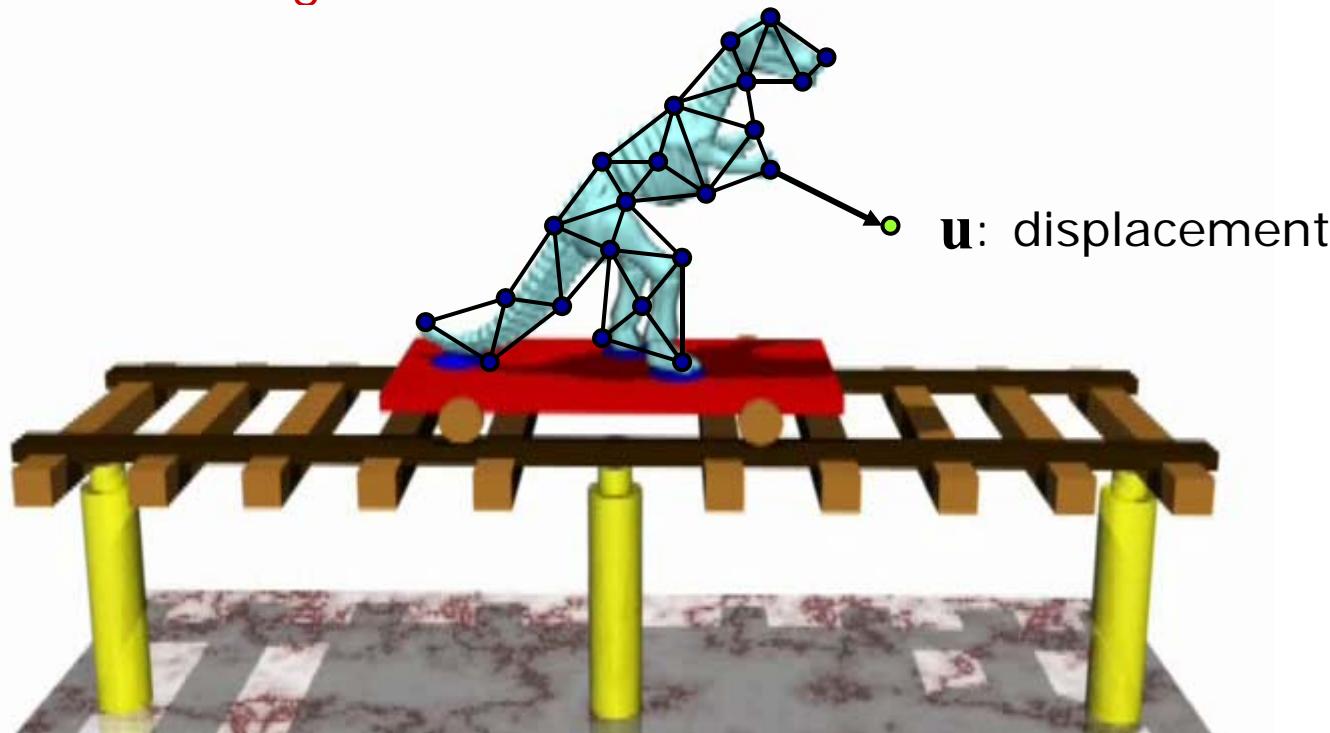
Time consuming!!!



$$\underline{\mathbf{M} \ddot{\mathbf{u}} + \mathbf{C} \dot{\mathbf{u}} + \mathbf{Ku} = \mathbf{F}}$$

Linearization

Not real time!!!



Real-Time Deformation of 3D Solids

□ Modal analysis in *local coordinate frames*

$$\mathbf{M} \ddot{\mathbf{u}} + \mathbf{C} \dot{\mathbf{u}} + \mathbf{K}(\mathbf{u}) = \mathbf{F} \quad \longrightarrow \quad \mathbf{M} \ddot{\mathbf{u}}^L + \mathbf{C} \dot{\mathbf{u}}^L + \mathbf{K} \mathbf{u}^L = \mathbf{R}^T \mathbf{F}$$

Linearization

G. Eigenvalue problem

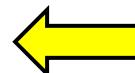
$$\mathbf{M} \Phi_i = \lambda_i \mathbf{K} \Phi_i$$

Modal basis

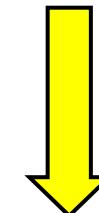
$$\mathbf{u}^L(t) = \Phi \mathbf{q}(t)$$

$$\mathbf{u}^k = \int_0^{t^k} \mathbf{R}(t) \Phi \dot{\mathbf{q}}(t) dt$$

Modal warping



$$\mathbf{M}_q \ddot{\mathbf{q}} + \mathbf{C}_q \dot{\mathbf{q}} + \mathbf{K}_q \mathbf{q} = \mathbf{Q}$$



Real-time performance without linearization artifacts!!!

Modal Rotation for Solids

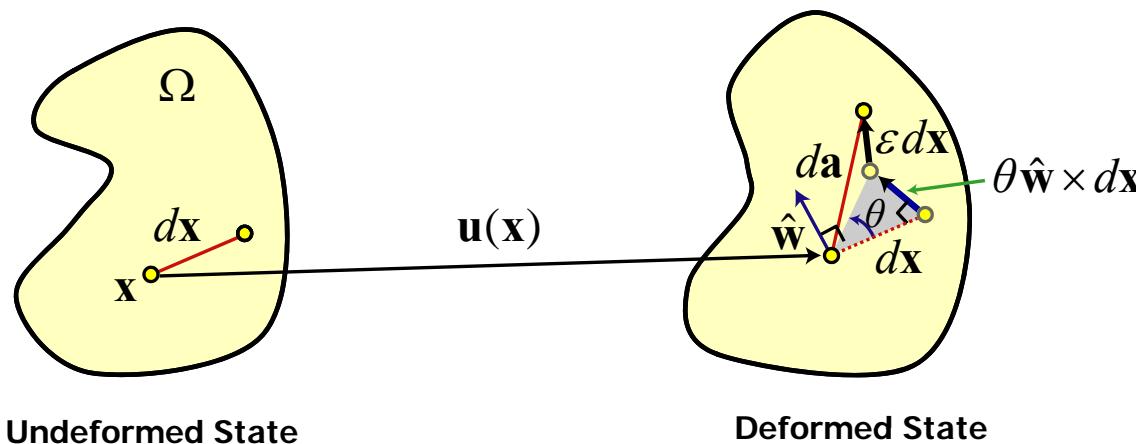
- Infinitesimal deformation = **rotation + strain**

- Element-wise rotation vector

$$\mathbf{w}_e(\mathbf{x}) = \frac{1}{2} \nabla \times \mathbf{u}(\mathbf{x}) = \mathbf{W}_e \mathbf{u}_e$$

- Globally-assembled rotation vector

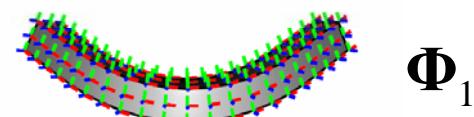
$$\mathbf{w}(t) = \mathbf{W}\mathbf{u}(t) = \{\mathbf{W}\Phi\}\mathbf{q}(t) = \Psi\mathbf{q}(t)$$



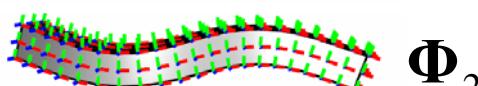
Modal Truncation

- Exploit dominant low frequency mode shapes only!
 - Higher modes heavily damped and die out fast.

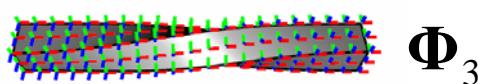
$$\mathbf{u}(t) = \tilde{\mathbf{R}}\Phi \mathbf{q}(t) = \tilde{\mathbf{R}}\Phi_i q_i(t)$$



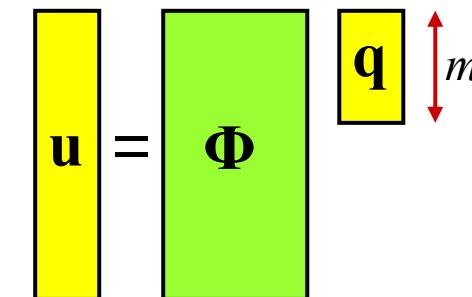
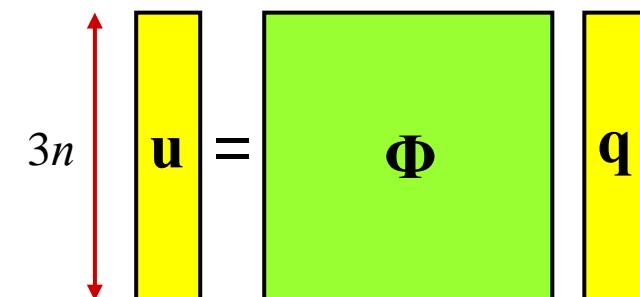
$$\Phi_1$$



$$\Phi_2$$

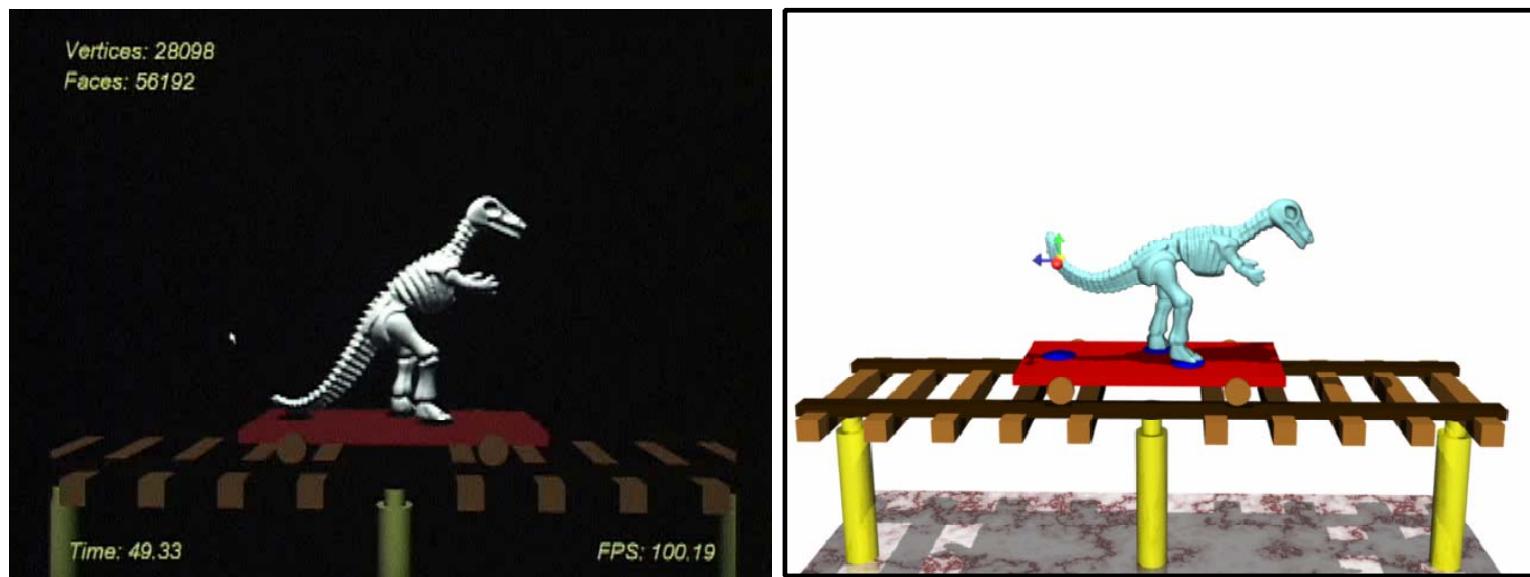


$$\Phi_3$$

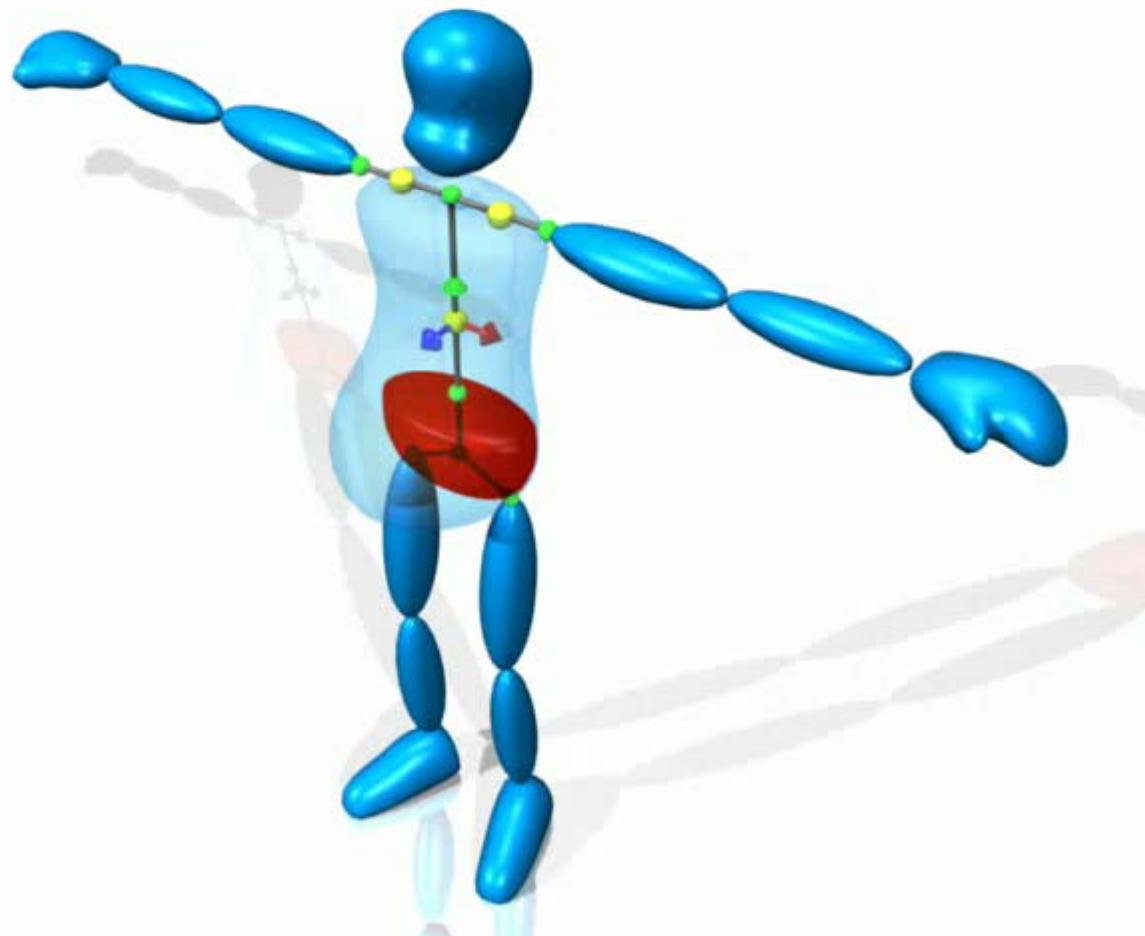


Deformation using GPU

- Programmable graphics H/W for large models
 - Written in NVIDIA Cg + DirectX
 - Small extra computation in vertex program: 11 lines, 47 inst.

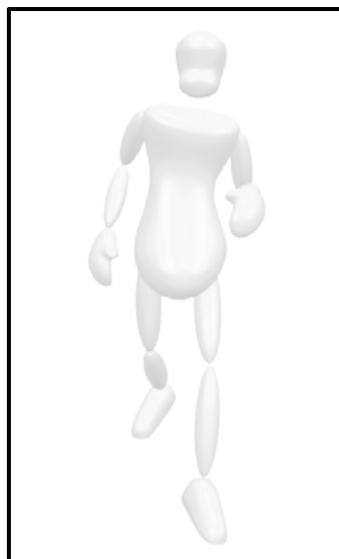


Passive Deformation as 2ndary Motion

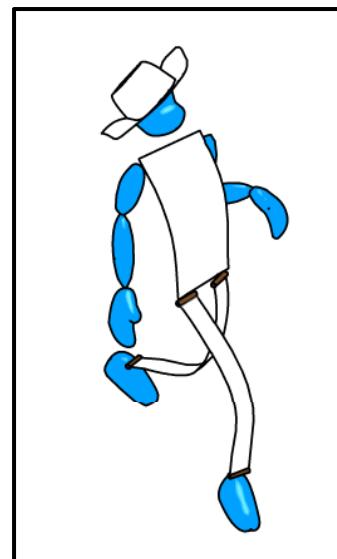


Real-Time Deformation of 3D Thin Shells

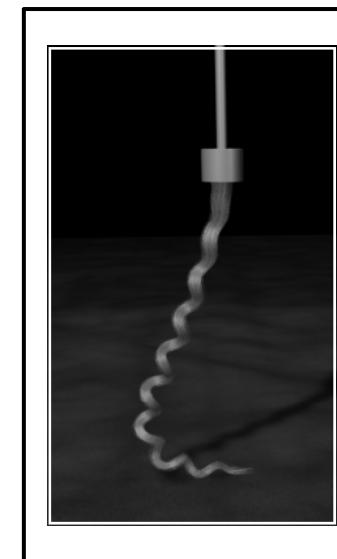
☐ Elastodynamic deformation in 3D



3D Solids



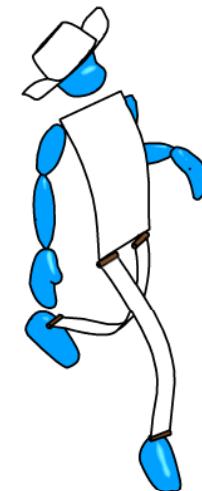
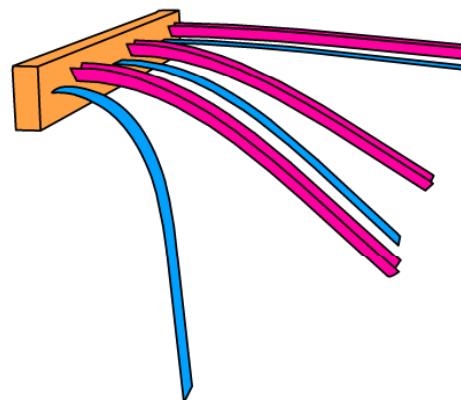
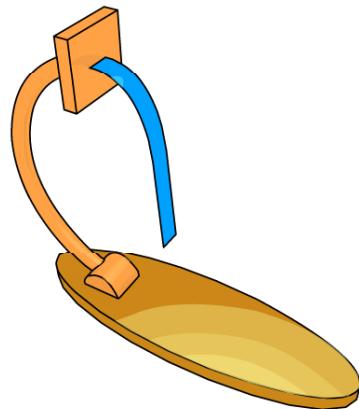
3D Thin Shells



3D Thin Rods

Thin Shell Structures

- Thin shells are **almost two-dimensional** structures.



Dynamics of Thin Shell Structures

□ Elastic potential energy of a thin shell

$$E = \underbrace{(k_A E_A + k_L E_L)}_{\text{Membrane energy}} + \underbrace{k_B E_B}_{\text{Flexural energy}}$$

□ Elastic force due to the elastic potential energy

$$\mathbf{K}(\mathbf{u}) = \frac{\partial E(\mathbf{u})}{\partial \mathbf{u}}$$

Modal Warping for 3D Thin Shells

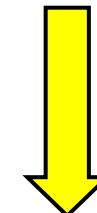
□ Modal analysis in *local coordinate frames*

$$\mathbf{M} \ddot{\mathbf{u}} + \mathbf{C} \dot{\mathbf{u}} + \mathbf{K}(\mathbf{u}) = \mathbf{F} \quad \longrightarrow \quad \mathbf{M} \ddot{\mathbf{u}}^L + \mathbf{C} \dot{\mathbf{u}}^L + \mathbf{K} \mathbf{u}^L = \mathbf{R}^T \mathbf{F}$$

Linearization in *LOCAL* coordinate frames

G. Eigenvalue problem
 $\mathbf{M} \Phi_i = \lambda_i \mathbf{K} \Phi_i$

Modal basis
 $\mathbf{u}^L(t) = \Phi \mathbf{q}(t)$



$$\mathbf{u}^k = \int_0^{t^k} \mathbf{R}(t) \Phi \dot{\mathbf{q}}(t) dt \quad \longleftarrow \quad \mathbf{M}_q \ddot{\mathbf{q}} + \mathbf{C}_q \dot{\mathbf{q}} + \mathbf{K}_q \mathbf{q} = \mathbf{Q}$$

Modal warping

Real-time performance without linearization artifacts!!!

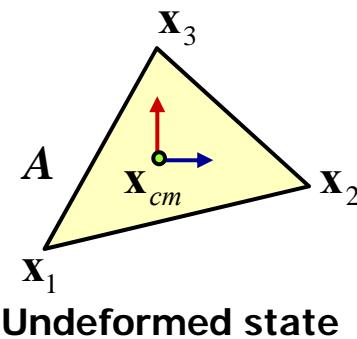
Modal Rotation for Shells

□ Rotation of a triangle near the rest state

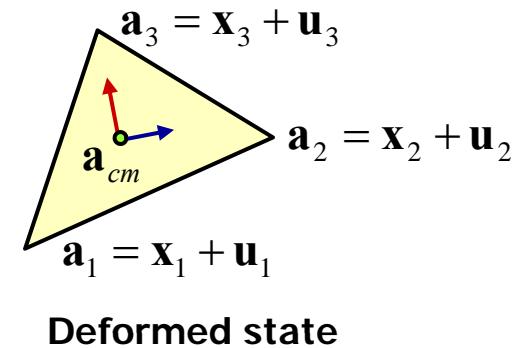
$$\arg \min_{\omega_A} \sum_{i=1}^3 \| \mathbf{p}_i + \omega_A \times \mathbf{p}_i - \mathbf{q}_i \|^2$$
$$\mathbf{p}_i = \mathbf{x}_i - \mathbf{x}_{cm}, \quad \mathbf{q}_i = \mathbf{a}_i - \mathbf{a}_{cm}$$

■ Element-wise rotation vector

$$\omega_A(\mathbf{u}_A) = - \left(\left[\sum_{i=1}^3 \mathbf{p}_i \times \mathbf{p}_i \times \right]^{-1} [\mathbf{p}_1 \times | \mathbf{p}_2 \times | \mathbf{p}_3 \times] \right) \mathbf{u}_A$$



$\omega_A(\mathbf{u}_A)$
Rotation vector
of a triangle A



Deformation using GPU

Vertices: 13235

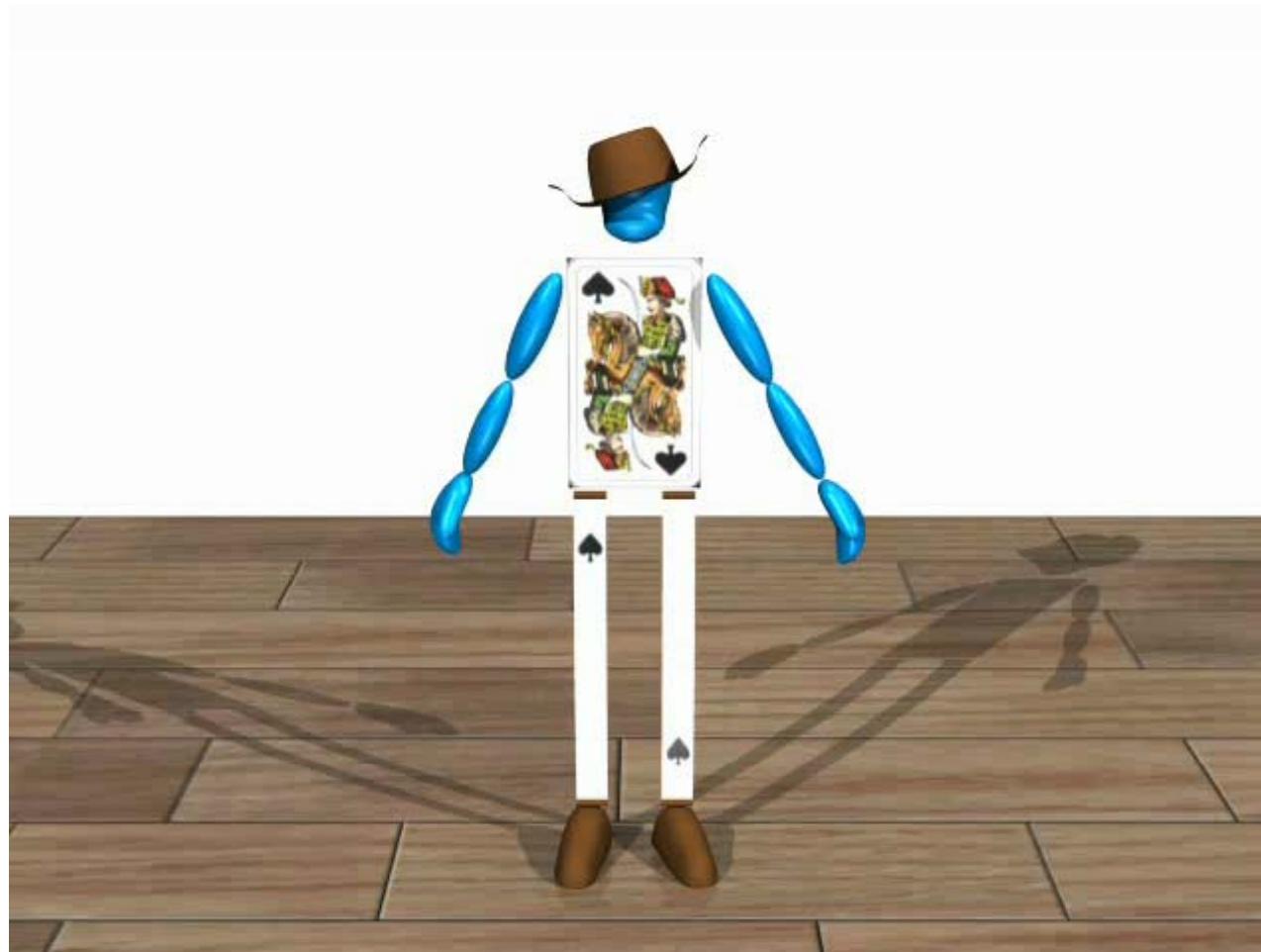
Faces: 26047

Edges: 38948



Programmable graphics hardware for large mesh

Passive Deformation as 2ndary Motion



Framework 4 Flexible Body Simulation

□ Authoring in the Maya platform

- Geometry
- Material constants
- Precomputation

----- Exporting -----

- Runtime simulation



Haptic Platform

□ Features

- Phantom Omni + GPU



iPod Touch Platform

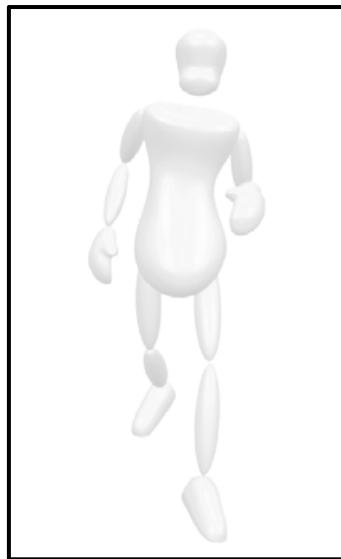
□ Features

- 3-axis linear accelerometers for excitation forces
- Multi-touch capabilities for drawing/simulation modes

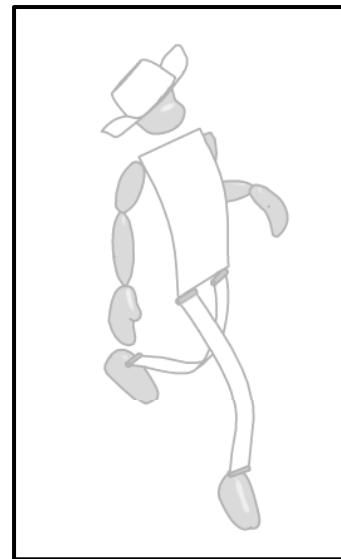


Real-Time Simulation of 3D Thin Rods

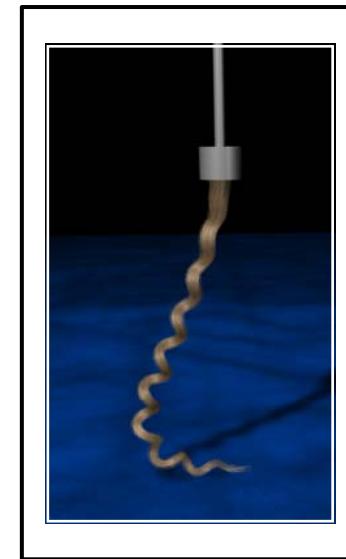
☐ Elastodynamic deformation in 3D



3D Solids



3D Thin Shells



3D Thin Rods

Next Step

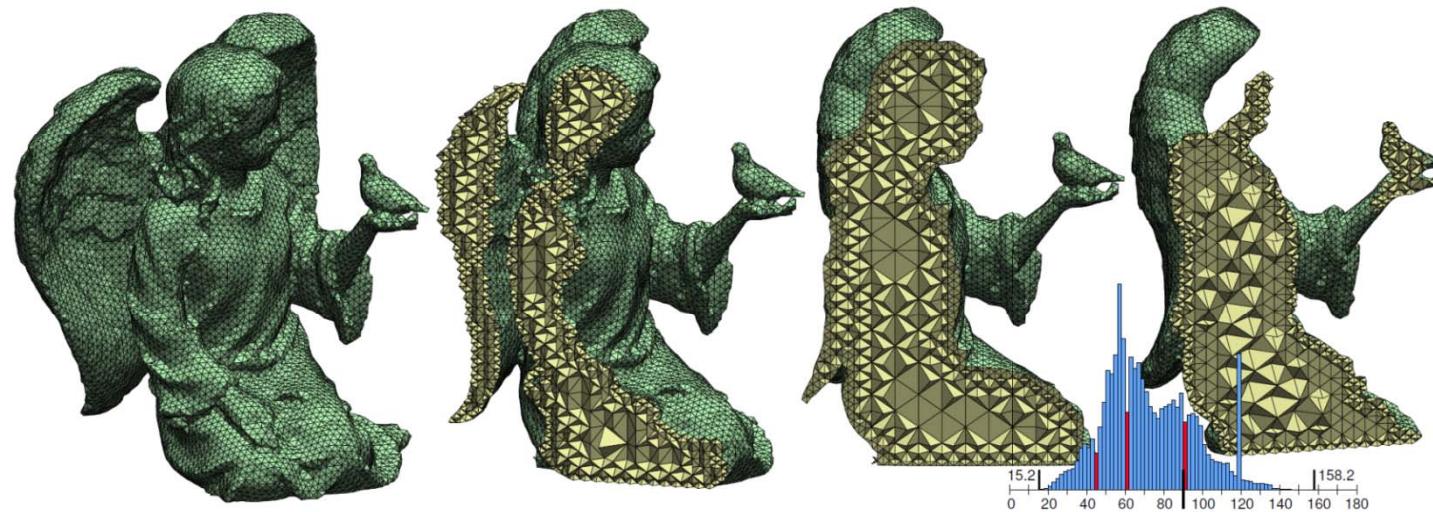
□ Hair simulation



Virtua Fighter 5 by SEGA

Next Step

- Meshing for flexible body simulation



Isosurface stuffing by Labelle and Shewchuk

Next Step

- Corotational FEM for crack/fracture simulation



Star Wars: The Force Unleashed by Parker and O'Brien

Next Step

- Elasticity, viscosity, and plasticity



Fast viscoelastic behavior by Wojtan and Turk

Questions?



Virtual Foosball:

A Tangible Implementation
of the Virtual Physics Library



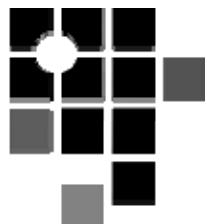
CREATIVE COMPUTING GROUP



Yunsil Heo
NML, Inc.



Hyunwoo Bang
New Media Lab., Seoul Nat'l Univ.



Jinwook Kim
Imaging Media Research Center,
KIST



Young J. Kim
Computer Graphics Lab., Ewha Womans
Univ.

Virtual Foosball

Concepts

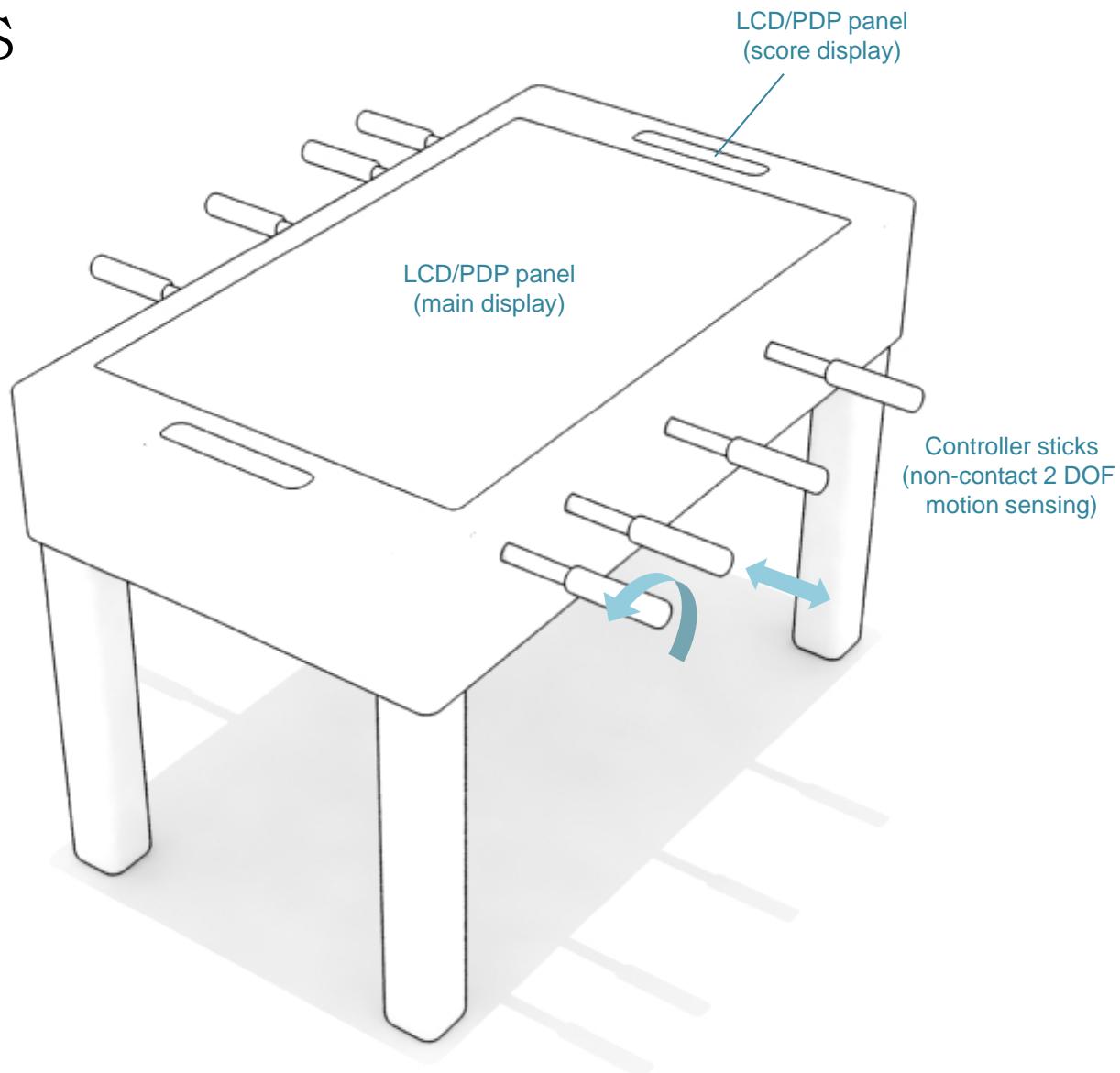
Concepts



Concepts



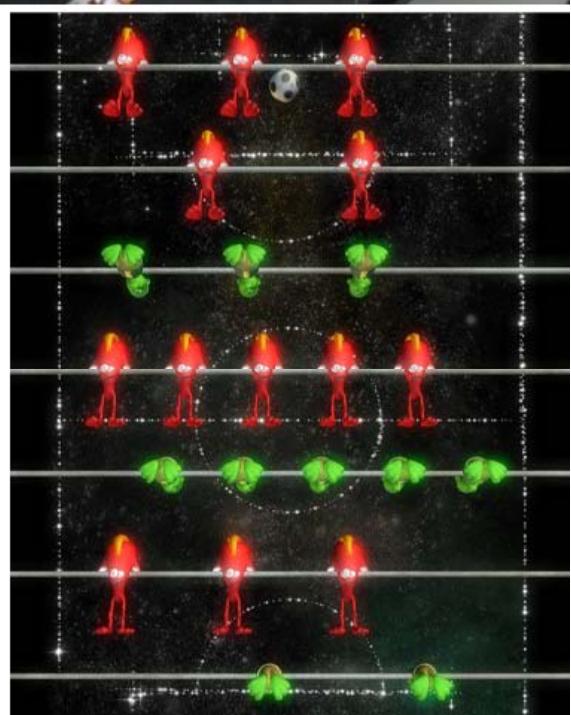
Concepts



Concepts

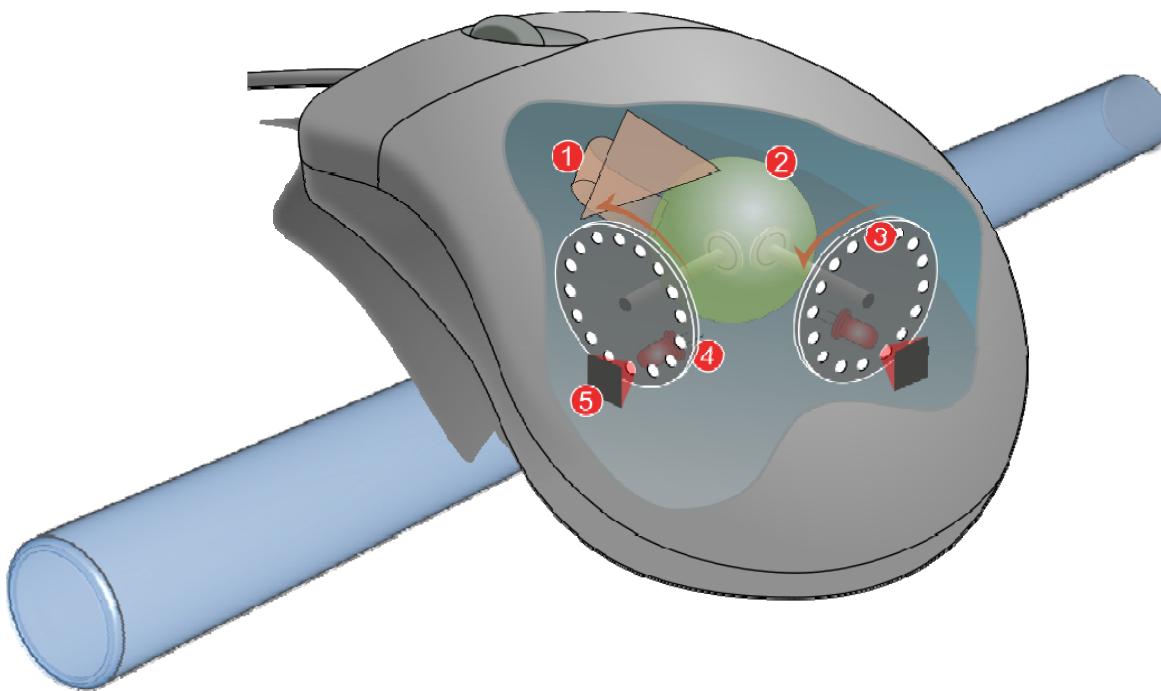




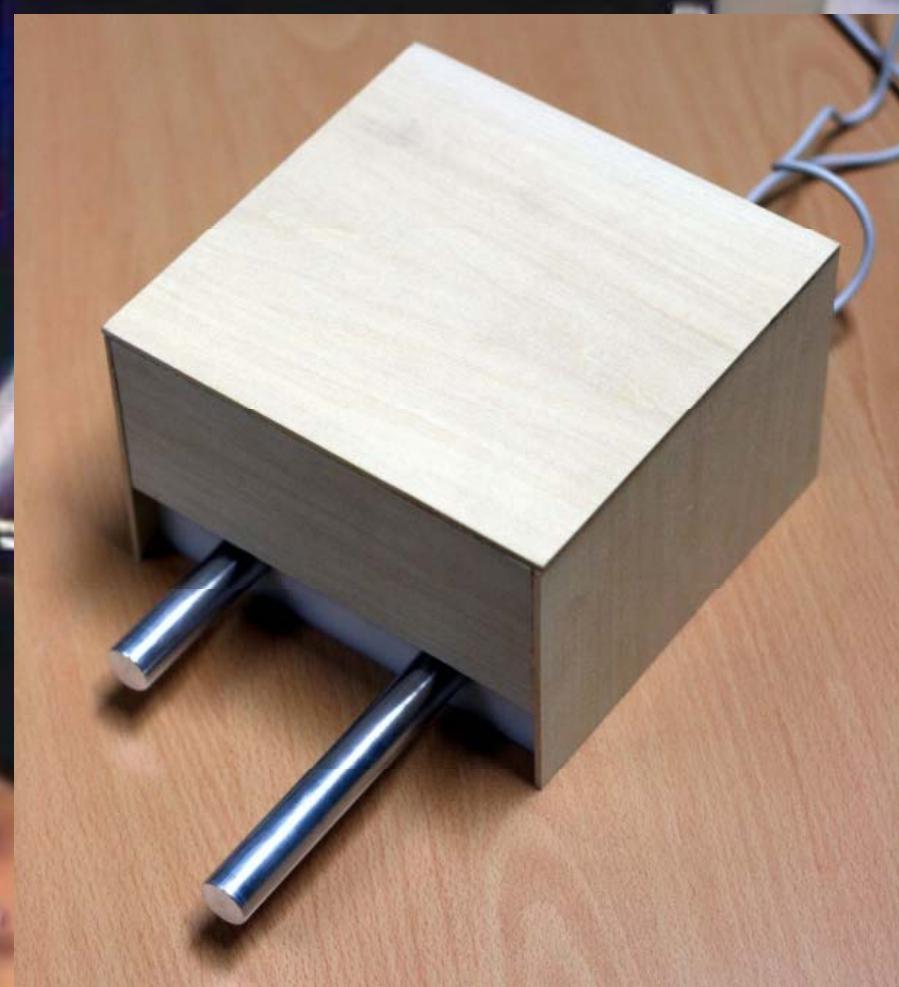


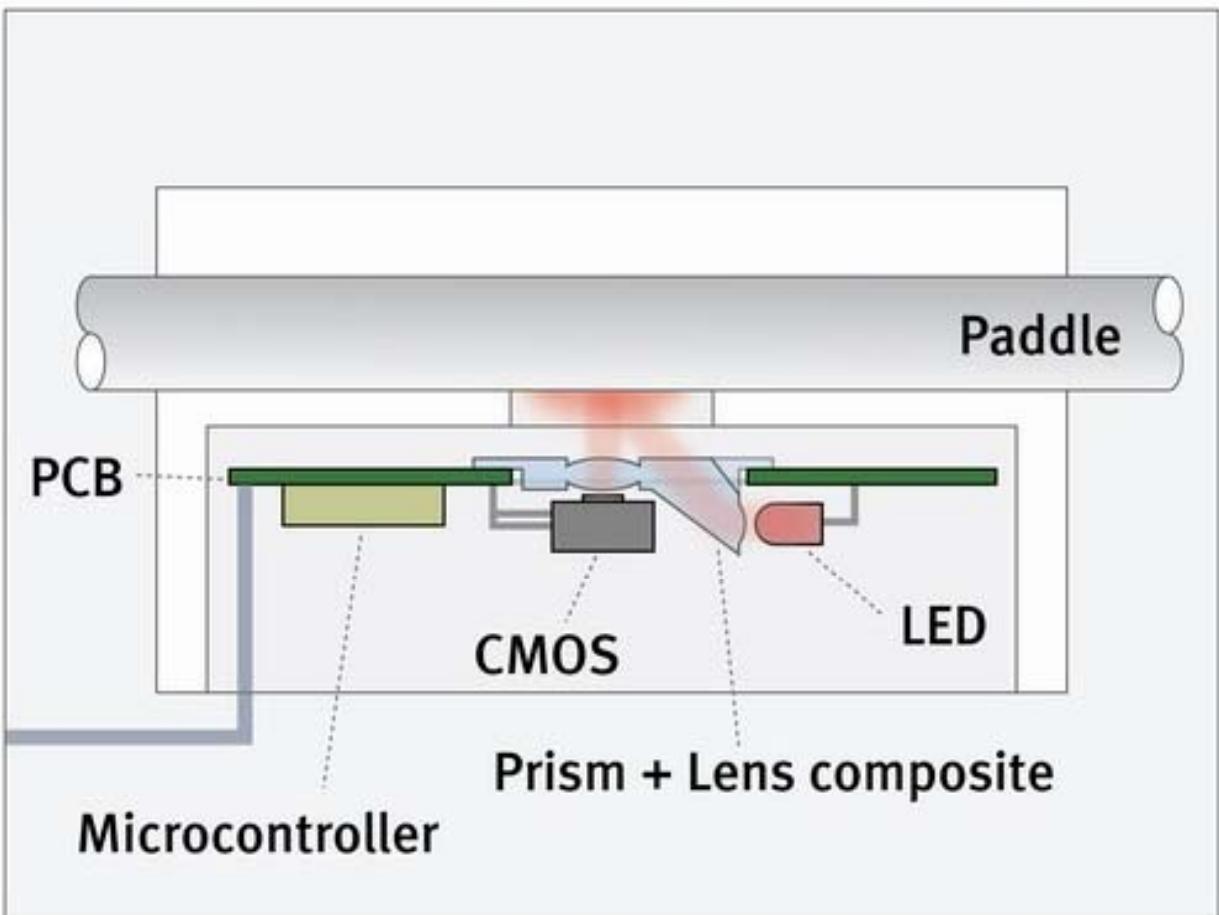
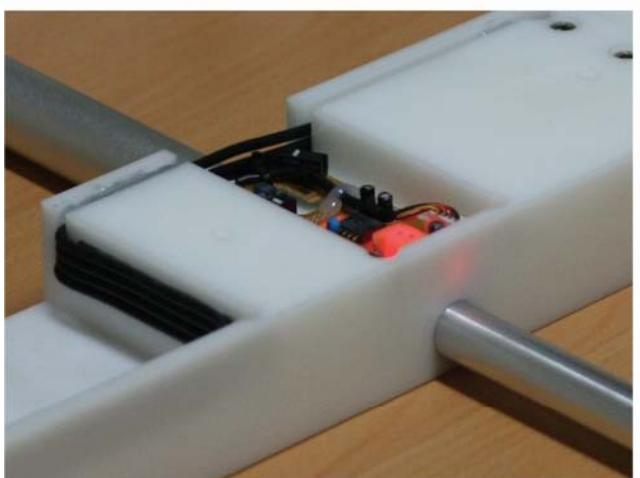
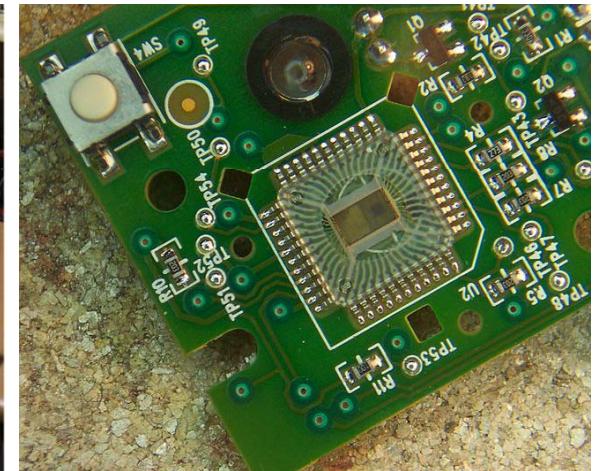
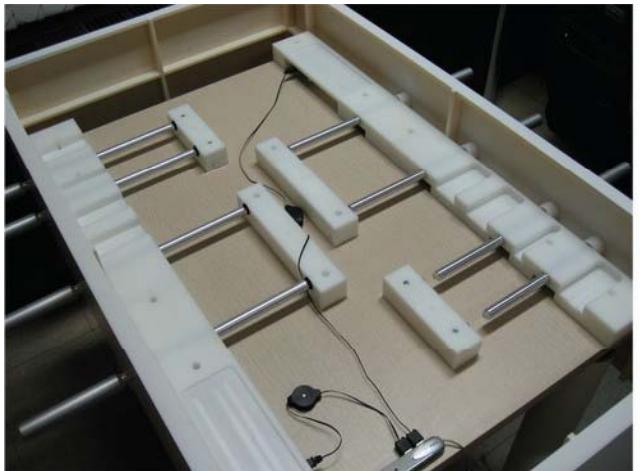
Virtual Foosball

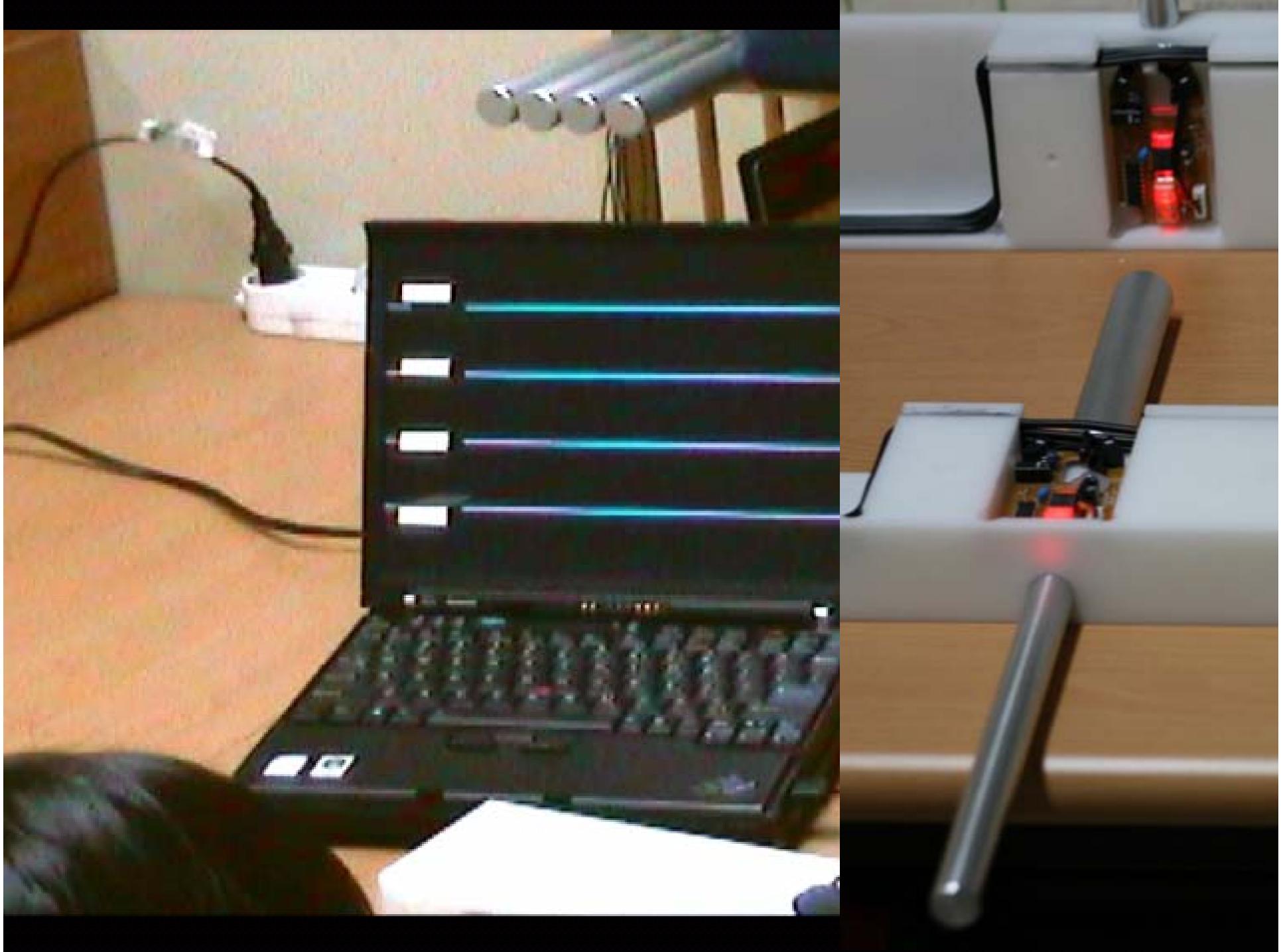
Hardware

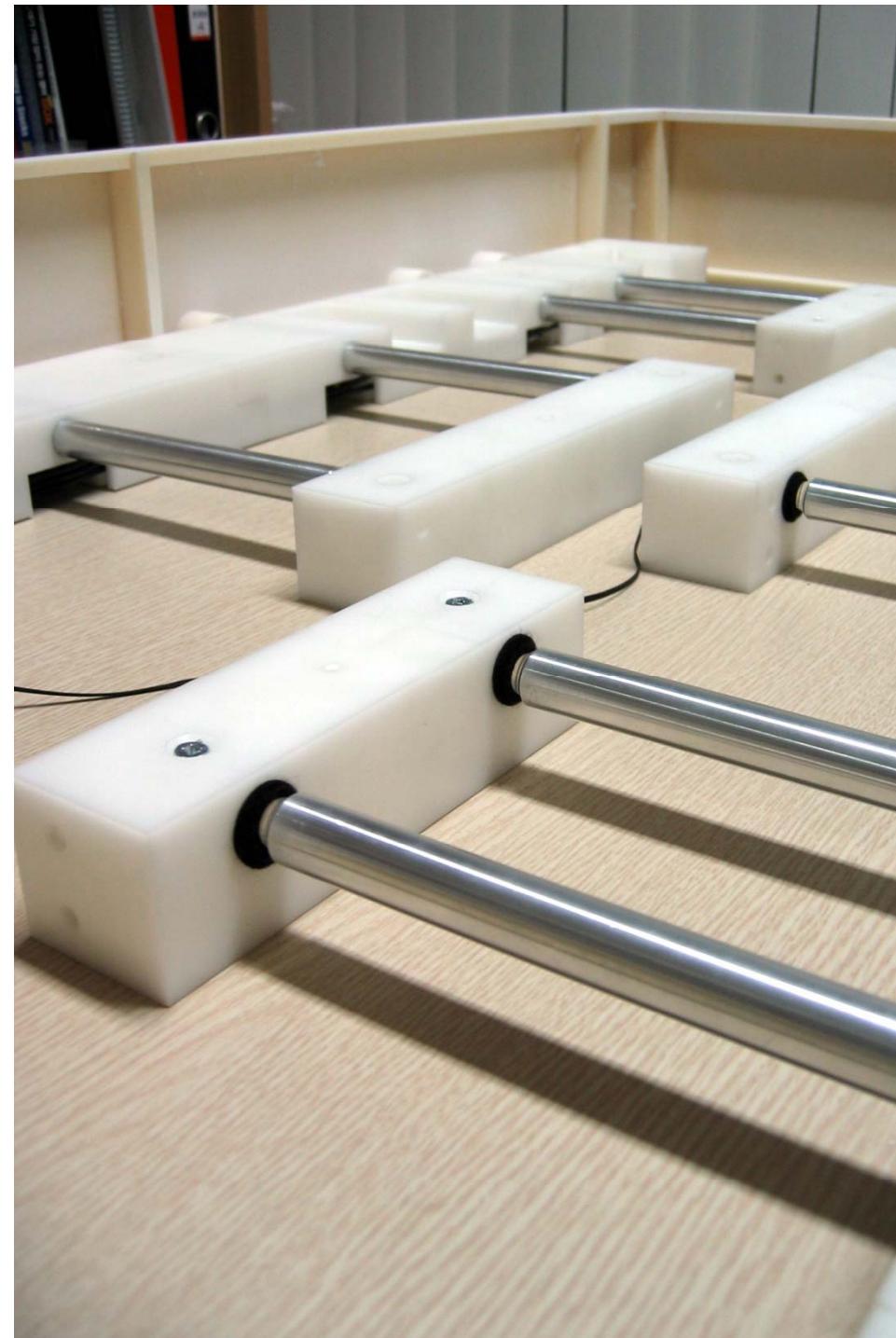


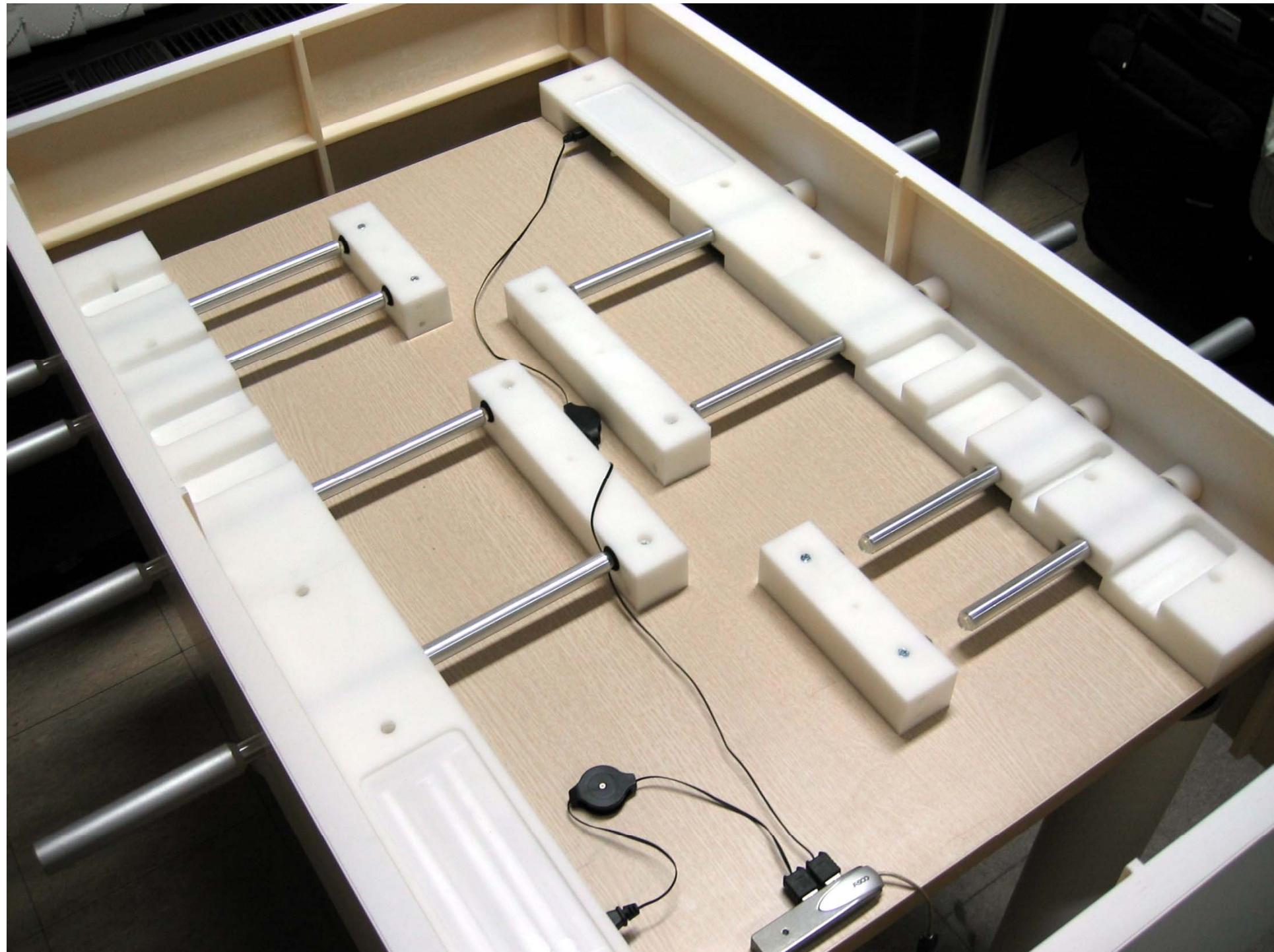
- 1: Moving the rod turns the ball.
- 2: X and Y rollers grip the ball and transfer movement.
- 3: Optical encoding disks include light holes.
- 4: Infrared LEDs shine through the disks.
- 5: Sensors gather light pulses to convert to X and Y vectors.











Virtual Foosball

Physics Engine

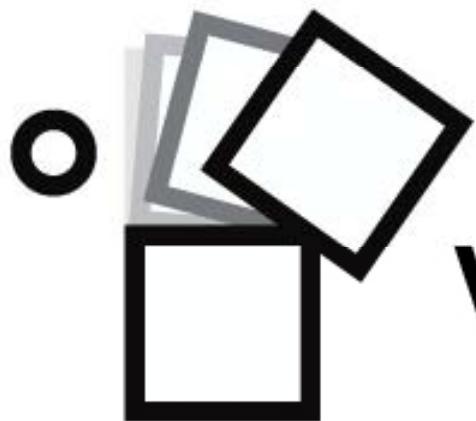
everyware

PhysX™

by

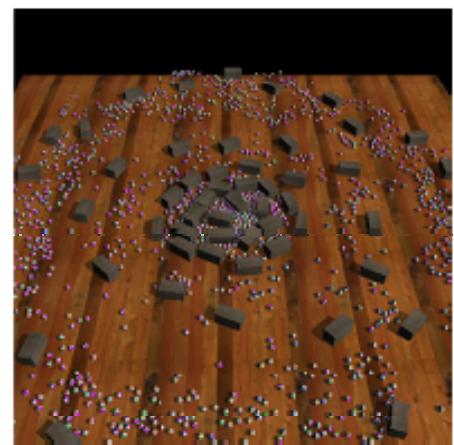
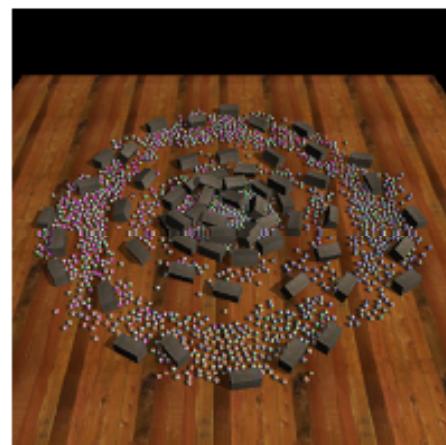
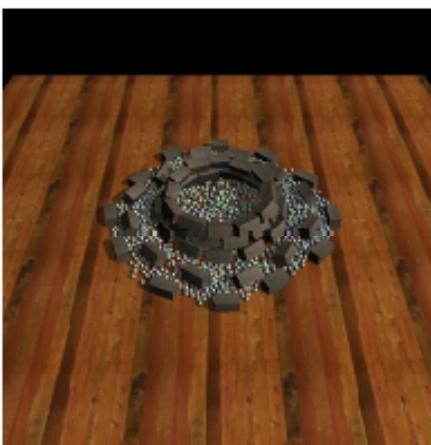
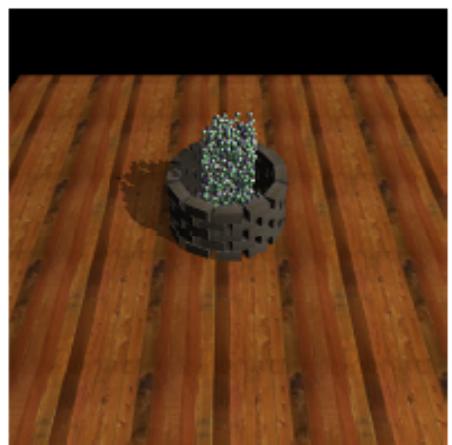
nVIDIA.





VIRTUAL PHYSICS

REALTIME DYNAMICS SIMULATION LIBRARY



Virtual Physics

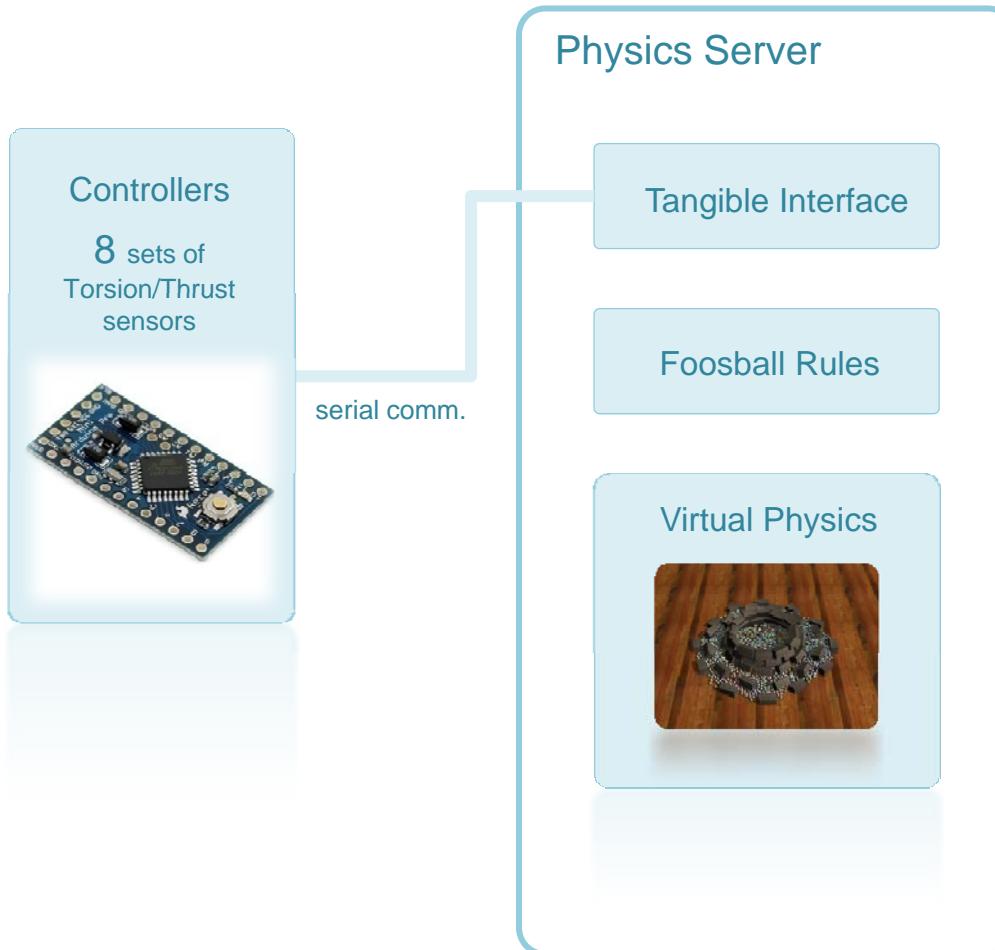


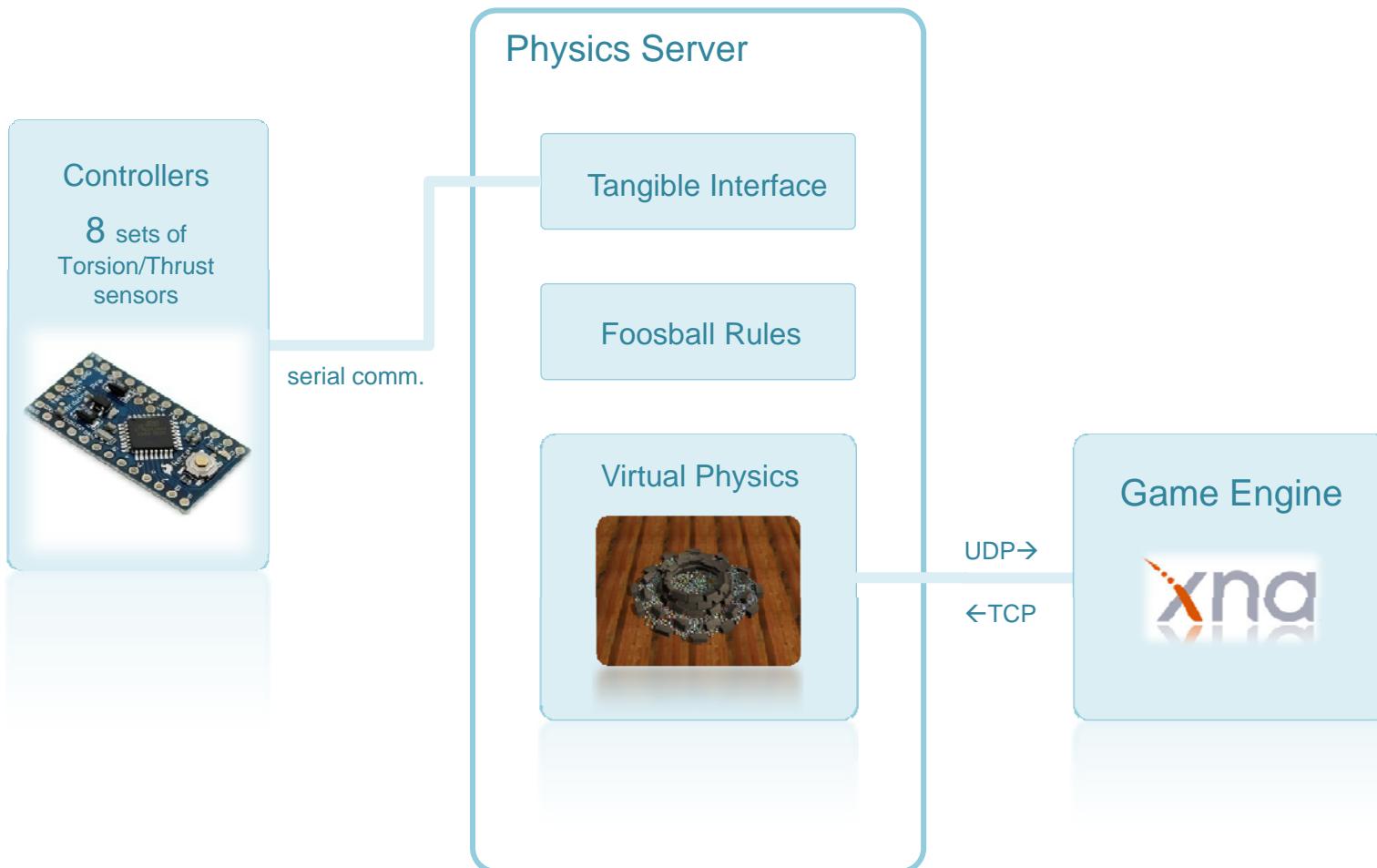
Physics Server

Foosball Rules

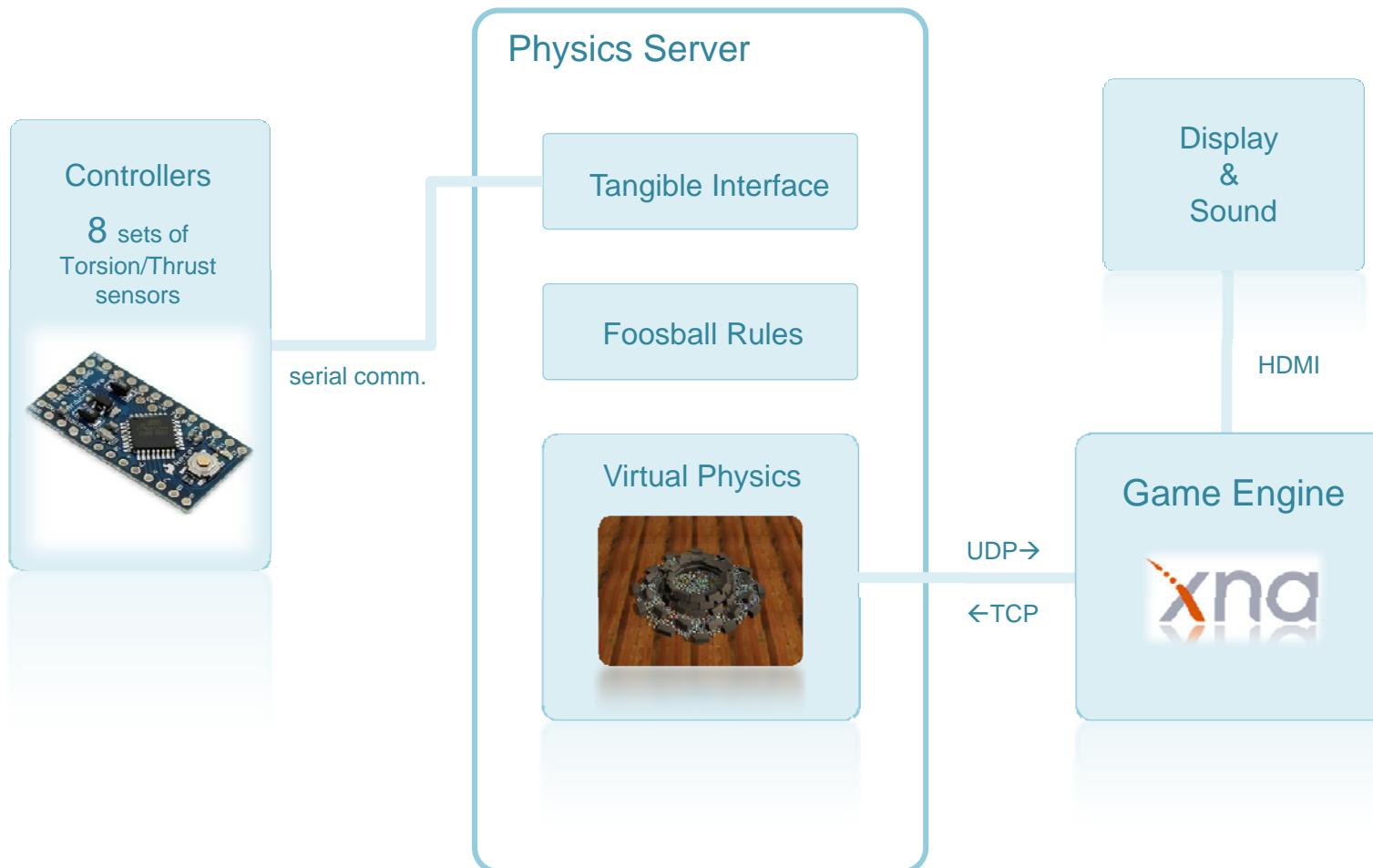
Virtual Physics







UDP : simulation objects posture refresh @ ~10000 times/s
TCP : simulation mode switching orders @ ~60 times/s



UDP : simulation objects posture refresh @ ~10000 times/s
TCP : simulation mode switching orders @ ~60 times/s

Virtual Foosball

Render Engine

everyware



The Dead Engine

Dead Space, Dante's Inferno

The Dead Engine

As Seen in: Dead Space, Dante's Inferno

Unreal Engine

As Seen In: Gears of War, Mass Effect, BioShock, Unreal Tournament, GRAW, Borderlands, Brothers in Arms, Mirror's Edge, Singularity ...

Naughty Dog Game Engine

As Seen in: Uncharted: Drake's Fortune, Uncharted 2: Among Thieves





Geo-Mod Engine

Red Faction: Guerrilla

Anvil Engine

Assassin's Creed series, Prince of Persia, Shaun White Snowboarding

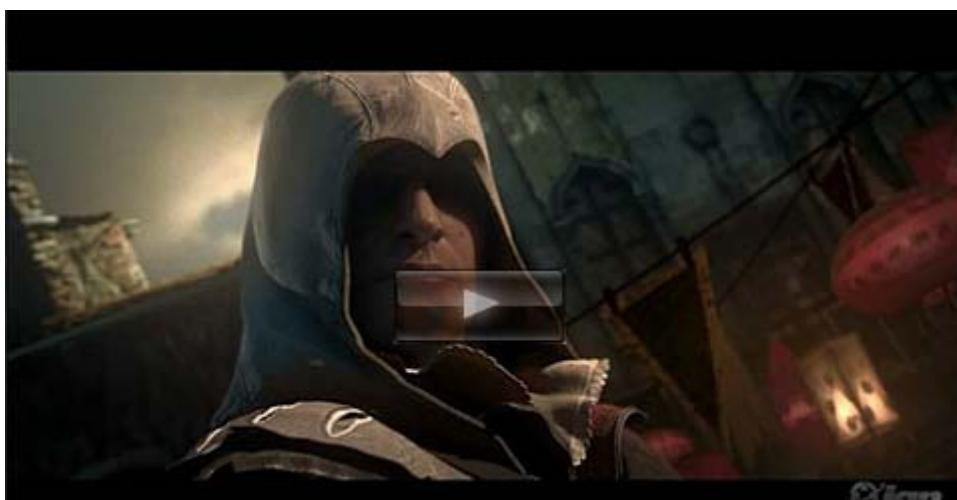


EGO Engine

Colin McRae: DiRT, Race Driver: GRiD, Operation Flashpoint, F1

IW Engine

Call of Duty Series



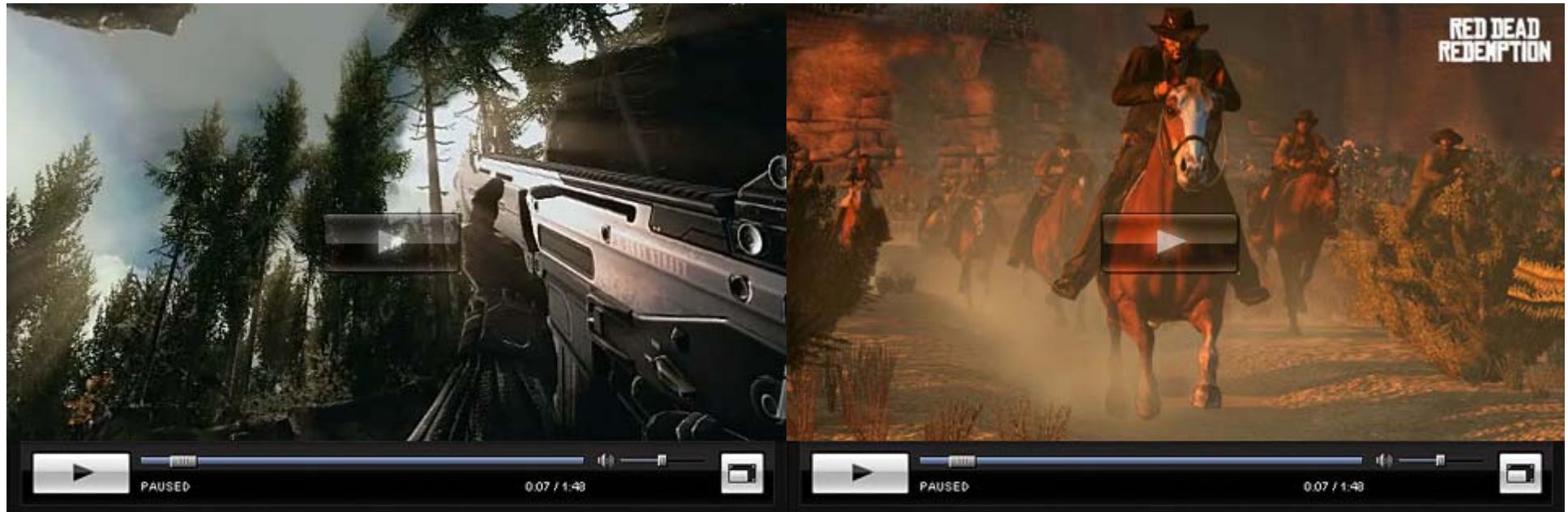
PAUSED

0:34 / 3:45



PAUSED

0:55 / 3:59



CryENGINE

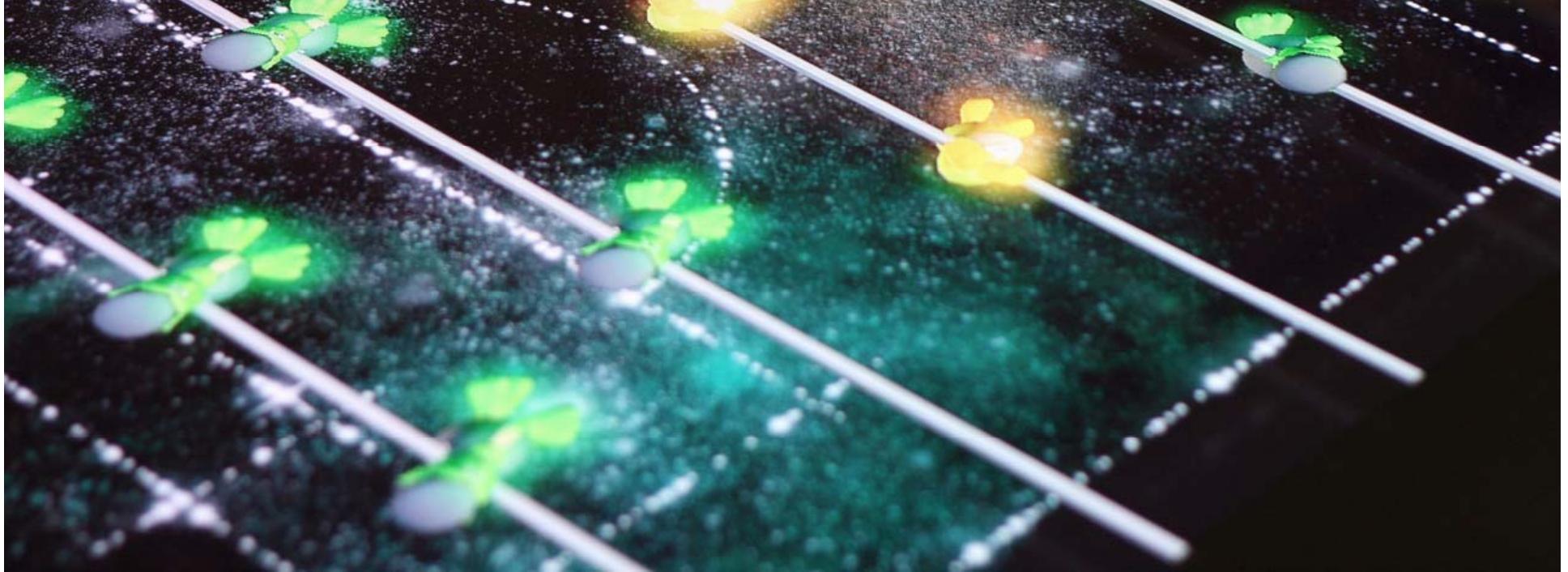
As Seen In: Far Cry, Crysis, Crysis Warhead, Crysis 2, Aion: Tower of Eternity

RAGE Engine

As Seen In: Rockstar Presents Table Tennis, GTA IV + Episodes, Midnight Club: Los Angeles, Red Dead Redemption, L.A. Noire (rumoured)

Realtime shadow
Global Illumination
Vertex Shader
Pixel Shader
Normal/Parallax Map

Halo
3D Audio
Motion Blur
Depth of Focus
Render to texture



Realtime shadow
Global Illumination
Vertex Shader
Pixel Shader
Normal/Parallax Map

Halo
3D Audio
Motion Blur
Depth of Focus
Render to texture

Virtual Foosball

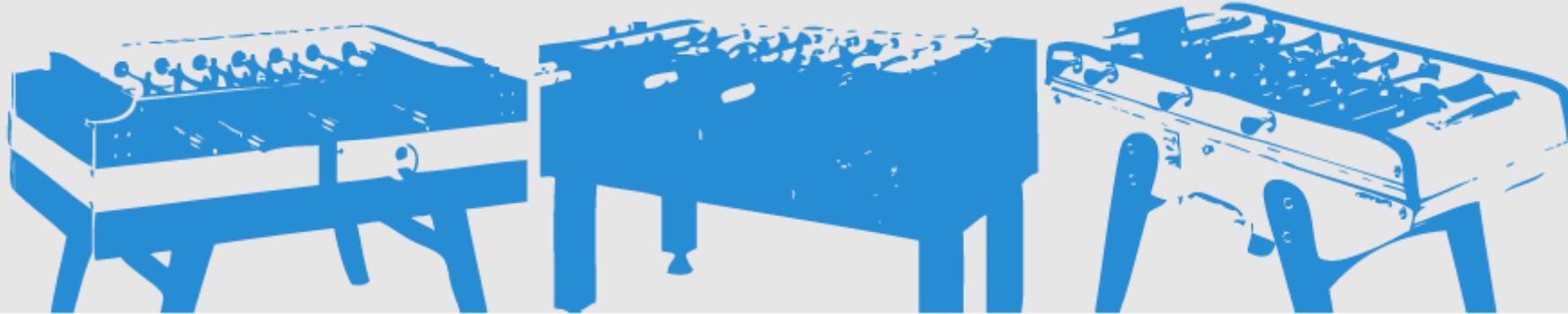
Sales

everyware





The British Foosball Association



Yunsil,

I'm interested in your space table football - I contacted you through Vimeo.

Firstly, I think you should think about entering the XMOS FoosTech Ideas Competition 2009 (<http://tinyurl.com/foostech> and <http://xmos.com/foostech>).

Secondly, I think we should discuss the mass market for a game of this nature.

Some of what you have created is unique and would be essential in any commercial implementation. Some however is going to be difficult to commercialize. For example, you have created a conventional table football table but with the table replaced by a screen. The important and unique thing is the decoupling of the tangible user interface (the rods) from the display and physics engine.

My opinion is that to mass commercialize a game like this, you need to build on what already exists. Everyone already has a screen, so I don't believe you are going to find many buyers for your massive new screen - the unit price is going to be simply too high!

So ideally, I would have a set of "handles" which are small joystick-style devices which I can place on my desk. I can play against my computer using my monitor. Crucially and interestingly, if the engine is correctly optimized, I can play against an opponent over the internet.

This builds on existing technology and uses your physics engine and tangible interfaces to create something that would genuinely have mass-market appeal.

I am a Computer Science PhD student so would be happy to help you if you think what I have written is sensible. I think I could find someone to help fund the development of a console-style game.

Best wishes,

Jonathan

--

Jonathan May

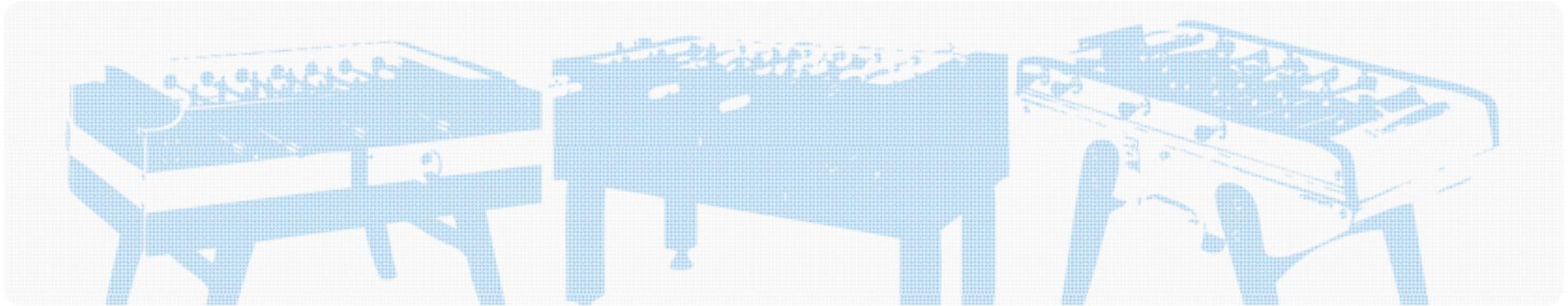
Sponsorship & Commercial Development

British Foosball Association

+44 (0)7767 847278



The British Foosball Association



Yunsil,

I'm interested in your space table football - I contacted you through Vimeoo

... the unit price is going to be simply too high!
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Virtual Foosball

The Upgrade

everyware















- ✓ Wireless
- ✓ High speed comm.
- ✓ HD sensing resolution
- ✓ Hybrid physics engine
- ✓ Multiplayer
- ✓ Mass-production Ready











Realtime shadow

Global Illumination

Vertex Shader

Pixel Shader

Normal/Parallax Map

Halo

3D Audio

Motion Blur

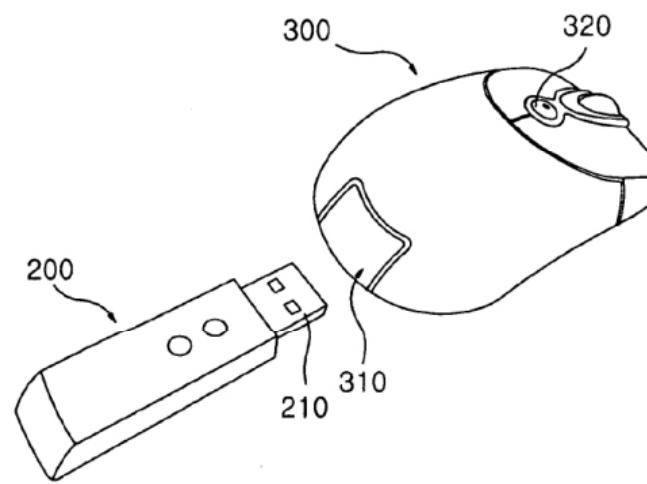
Depth of Focus

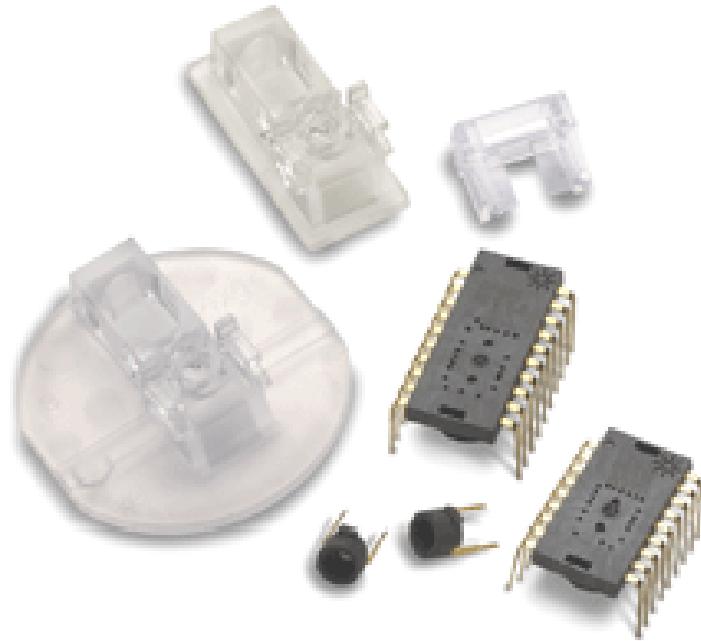
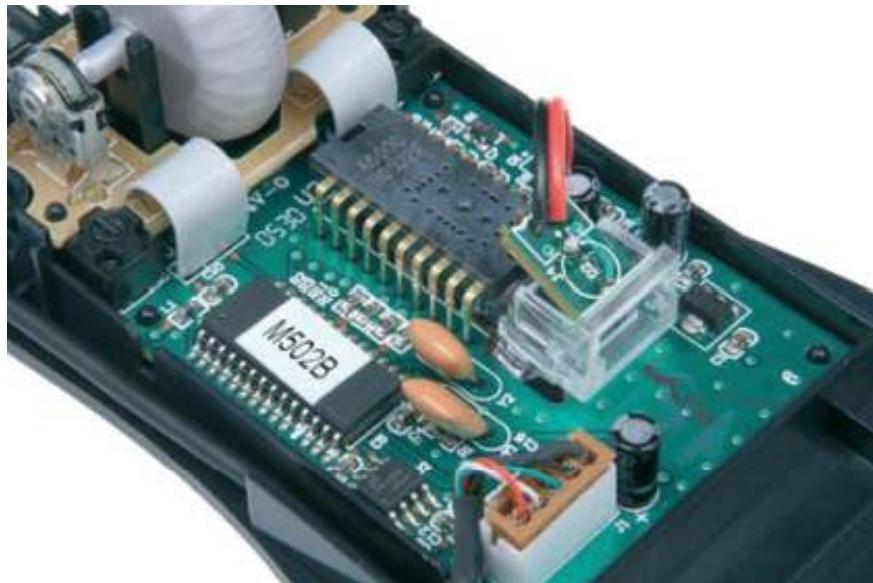
Render to texture

Virtual Foosball

Technology

everyware

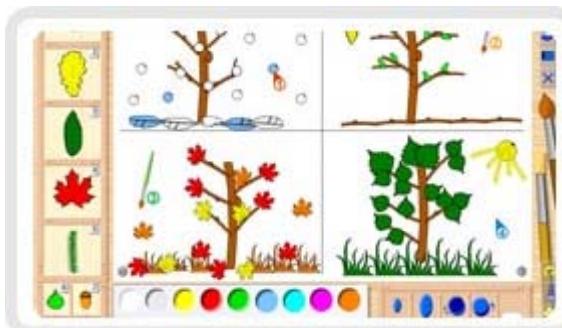




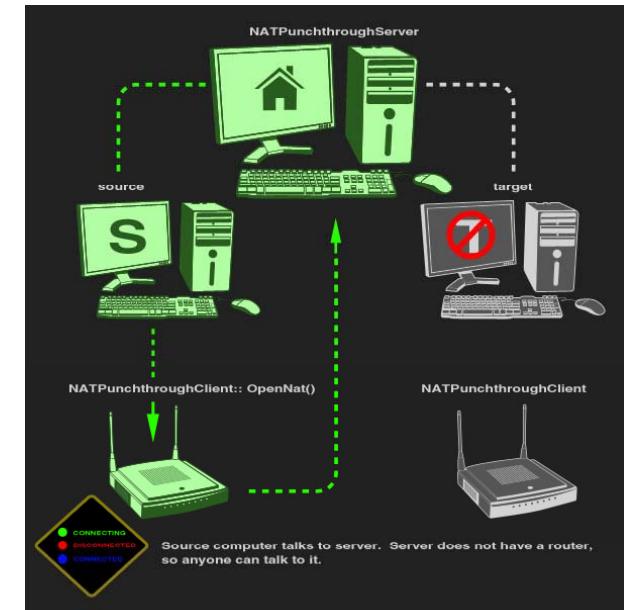
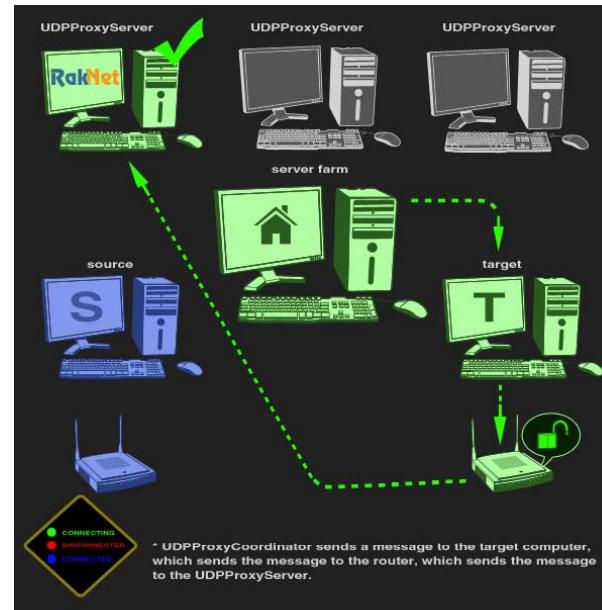
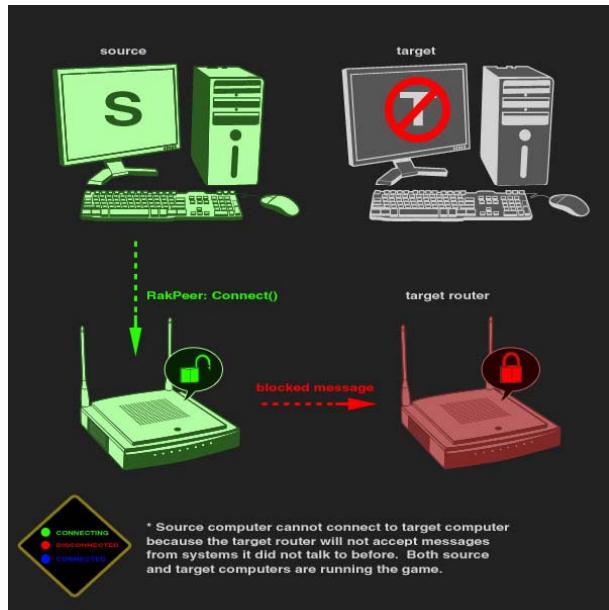
One PC, Multiple Mice, Endless Possibilities

Make your PowerPoint
presentations interactive

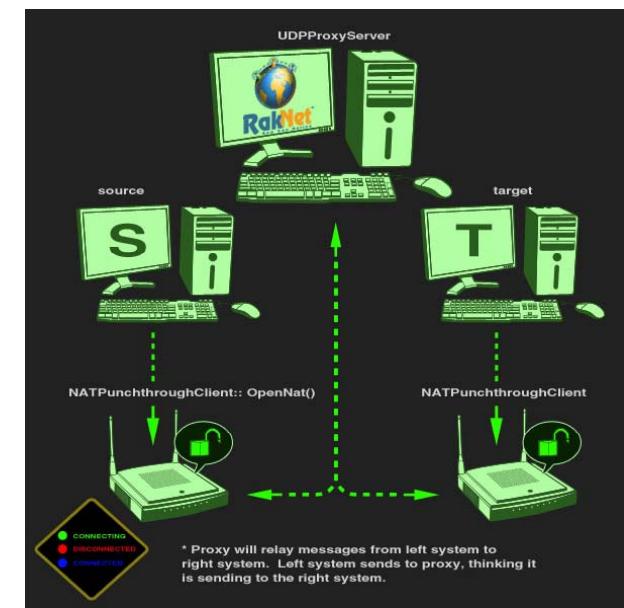
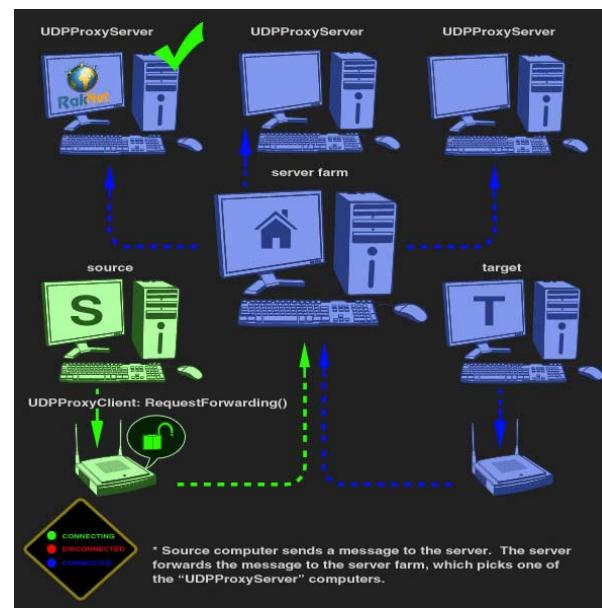
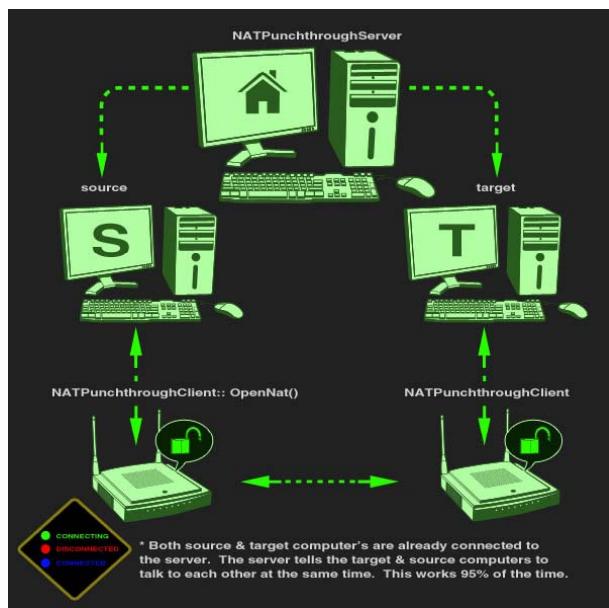
 Download Beta

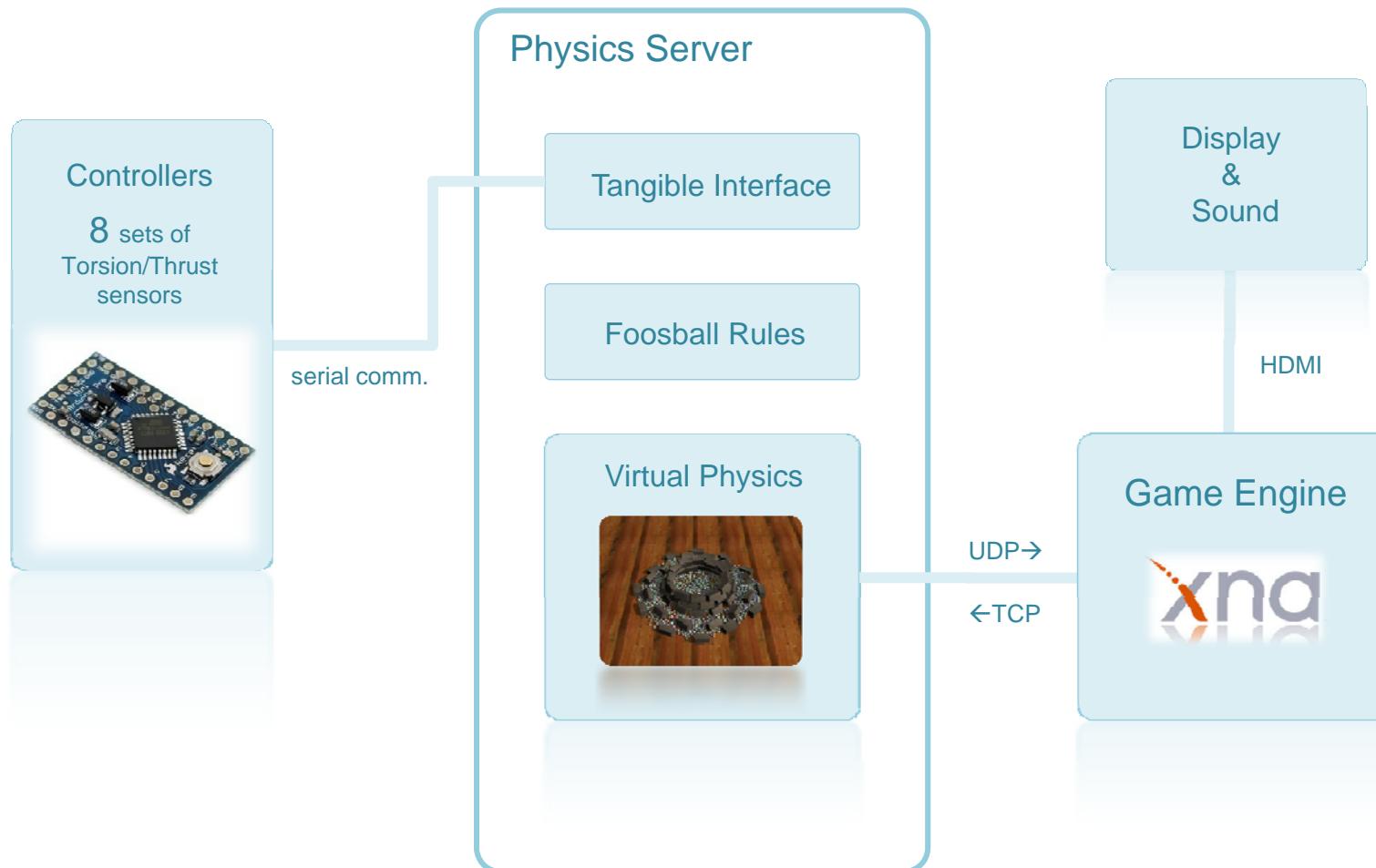






“NAT Punch-Through”





UDP : simulation objects posture refresh @ ~10000 times/s
TCP : simulation mode switching orders @ ~60 times/s

Virtual Physics



VP.net



Game Engine

VP.net





Multipoint SDK

